



22137306



MATHEMATICS
STANDARD LEVEL
PAPER 2

Friday 10 May 2013 (morning)

1 hour 30 minutes

Candidate session number

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Examination code

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INSTRUCTIONS TO CANDIDATES

- Write your session number in the boxes above.
- Do not open this examination paper until instructed to do so.
- A graphic display calculator is required for this paper.
- Section A: answer all questions in the boxes provided.
- Section B: answer all questions in the answer booklet provided. Fill in your session number on the front of the answer booklet, and attach it to this examination paper and your cover sheet using the tag provided.
- Unless otherwise stated in the question, all numerical answers should be given exactly or correct to three significant figures.
- A clean copy of the **Mathematics SL information booklet** is required for this paper.
- The maximum mark for this examination paper is [90 marks].



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2. [Maximum mark: 6]

The random variable X is normally distributed with mean 20 and standard deviation 5.

(a) Find $P(X \leq 22.9)$. [3 marks]

(b) Given that $P(X < k) = 0.55$, find the value of k . [3 marks]

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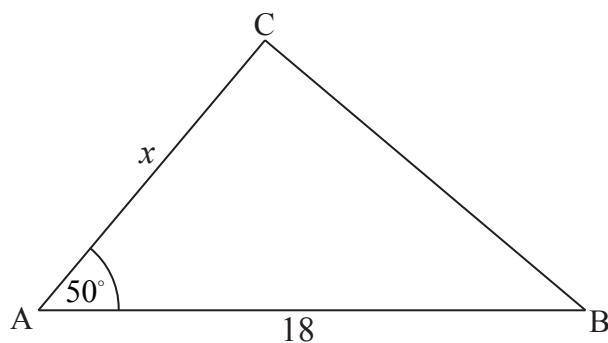
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3. [Maximum mark: 6]

The following diagram shows a triangle ABC.



*diagram
not to scale*

The area of triangle ABC is 80 cm^2 , $AB = 18 \text{ cm}$, $AC = x \text{ cm}$ and $\hat{BAC} = 50^\circ$.

(a) Find x . [3 marks]

(b) Find BC. [3 marks]

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4. [Maximum mark: 6]

Two events A and B are such that $P(A) = 0.2$ and $P(A \cup B) = 0.5$.

(a) Given that A and B are mutually exclusive, find $P(B)$. [2]

(b) Given that A and B are independent, find $P(B)$. [4]

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4. [Maximum mark: 7]

Line L_1 has equation $\mathbf{r}_1 = \begin{pmatrix} 10 \\ 6 \\ -1 \end{pmatrix} + s \begin{pmatrix} 2 \\ -5 \\ -2 \end{pmatrix}$ and line L_2 has equation $\mathbf{r}_2 = \begin{pmatrix} 2 \\ 1 \\ -3 \end{pmatrix} + t \begin{pmatrix} 3 \\ 5 \\ 2 \end{pmatrix}$.

Lines L_1 and L_2 intersect at point A. Find the coordinates of A.

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5. [Maximum mark: 6]

The sum of the first three terms of a geometric sequence is 62.755, and the sum of the infinite sequence is 440. Find the common ratio.

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6. [Maximum mark: 7]

The constant term in the expansion of $\left(\frac{x}{a} + \frac{a^2}{x}\right)^6$, where $a \in \mathbb{Z}$, is 1280. Find a .

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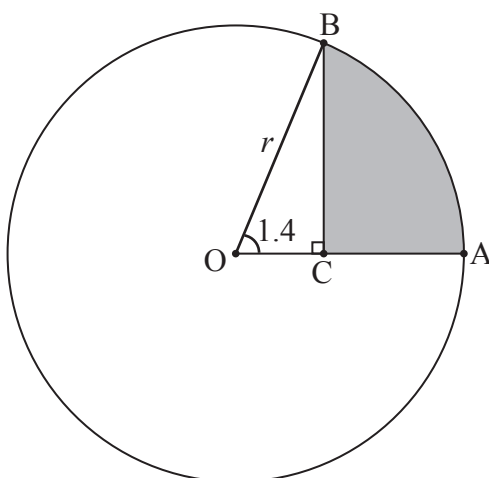
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7. [Maximum mark: 8]

The following diagram shows a circle with centre O and radius r cm.



*diagram
not to scale*

Points A and B are on the circumference of the circle and $\angle AOB = 1.4$ radians.

The point C is on $[OA]$ such that $\angle BCO = \frac{\pi}{2}$ radians.

(a) Show that $OC = r \cos 1.4$. [1 mark]

(b) The area of the shaded region is 25 cm^2 . Find the value of r . [7 marks]



Do **NOT** write solutions on this page.

SECTION B

Answer **all** questions in the answer booklet provided. Please start each question on a new page.

8. [Maximum mark: 15]

Consider the points $A(5, 2, 1)$, $B(6, 5, 3)$, and $C(7, 6, a+1)$, where $a \in \mathbb{R}$.

(a) Find

(i) \vec{AB} ;

(ii) \vec{AC} .

[3 marks]

Let α be the angle between \vec{AB} and \vec{AC} .

(b) Find the value of a for which $\alpha = \frac{\pi}{2}$.

[4 marks]

(c) (i) Show that $\cos \alpha = \frac{2a+14}{\sqrt{14a^2+280}}$.

(ii) Hence, find the value of a for which $\alpha = 1.2$.

[8 marks]



Do **NOT** write solutions on this page.

9. [Maximum mark: 15]

A bag contains four gold balls and six silver balls.

(a) Two balls are drawn at random from the bag, with replacement. Let X be the number of gold balls drawn from the bag.

(i) Find $P(X = 0)$.

(ii) Find $P(X = 1)$.

(iii) Hence, find $E(X)$.

[8 marks]

Fourteen balls are drawn from the bag, with replacement.

(b) Find the probability that exactly five of the balls are gold.

[2 marks]

(c) Find the probability that at most five of the balls are gold.

[2 marks]

(d) Given that at most five of the balls are gold, find the probability that exactly five of the balls are gold. Give the answer correct to two decimal places.

[3 marks]



Do **NOT** write solutions on this page.

10. [Maximum mark: 14]

Samantha goes to school five days a week. When it rains, the probability that she goes to school by bus is 0.5. When it does not rain, the probability that she goes to school by bus is 0.3. The probability that it rains on any given day is 0.2.

- (a) On a randomly selected school day, find the probability that Samantha goes to school by bus. [4]
 - (b) Given that Samantha went to school by bus on Monday, find the probability that it was raining. [3]
 - (c) In a randomly chosen school week, find the probability that Samantha goes to school by bus on exactly three days. [2]
 - (d) After n school days, the probability that Samantha goes to school by bus at least once is greater than 0.95. Find the smallest value of n . [5]
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