Pre-Test: Sequences & series

Name:

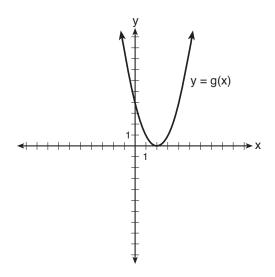
## Answer on lined paper. Show work.

- 1. In an arithmetic sequence, the first term is 15 and the second term is 9.
  - (a) Find the common difference.
  - (b) Find the sixth term.
  - (c) Find the sum of the first six terms of the sequence.
- 2. Given that for a geometric sequence  $u_1 = 54$  and  $u_4 = 16$ 
  - (a) Find the value of r.
  - (b) Given that  $u_k$  is the first term of the sequence with a value less than one, find k.
  - (c) Find the sum of the infinite series  $S_{\infty}$
- 3. The first three terms of an arithmetic sequence are  $u_1 = 7.1$ ,  $u_2 = 7.4$ , and  $u_3 = 7.7$ .
  - (a) Find the common difference.
  - (b) Given that the kth term of the sequence,  $u_k = 11$ . Find k.
- 4. Let f(x) = 3x 4 and  $g(x) = (x + 1)^2$ 
  - (a) Find  $(f \circ g)(3)$
  - (b) Find  $f^{-1}(x)$
- 5. Simplify the expression  $\sqrt{a^2} \cdot \sqrt{a^3}$
- 6.  $(x^2 5x 1)(2x + 1) 2x(x^2 + 2x 7)$
- 7. What is the inverse of the function  $y = \frac{3}{x+2}$ ?
- 8. Let  $x = \ln 3$  and  $y = \ln 7$ . Write down the following expressions in terms of x and y.
  - (a)  $\ln \frac{7}{3}$
  - (b) ln 63
  - (c) ln 9
- 9. Using the quadratic formula or otherwise, find the solution set to  $2x^2 5x 3 = 0$ .
- 10. Simplify the complex expression 3ai(3-2i).
- 11. Simplify the expression  $\left(\frac{x^{-3}}{x^5}\right)^{\frac{1}{4}}$  to one with positive integer exponents and radicals.

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- 12. The function g is defined by graph of y = g(x) below.
  - (a) Write down the equation for g(x) in factored form.
  - (b) The function h(x) is made by reflecting g across the x-axis. What is the equation for h(x)?



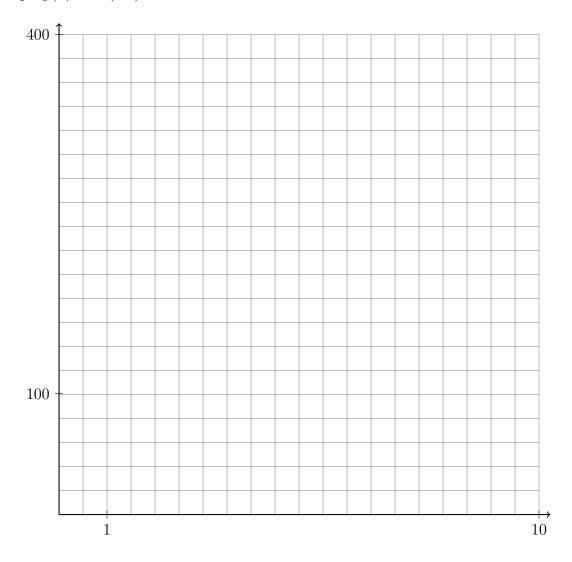
- 13. Let  $f(x) = x^2 8x + 3$ 
  - (a) Rewrite quadratic in vertex form and state the vertex as an ordered pair.
  - (b) The parabola is translated vertically by k units to make the function g(x). The equation g(x) = 0 has one solution. Find k.
- 14. Use your knowledge of the binomial expansion and combinatorics to answer the following questions.
  - (a) Write down the first 5 rows of Pascal's triangle.
  - (b) Find  ${}_{9}C_{4}$ .
  - (c) Expand the binomial  $(x+1)^5$ .
  - (d) What is the coefficient of the  $x^3$  term of the expansion of  $(x+1)^9$ ?

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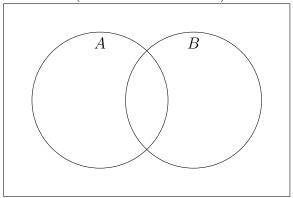
## For these last two pages, answer in the space provided

15. Graph  $g(x) = 30(1.5)^{\frac{x}{2}} - 5$  on the set of axes below.



Is the function an example of exponential growth or exponential decay? Justify your answer algebraically.

- 16. Let A and B be independent events, where P(A) = 0.5 and P(B) = 0.6.
  - (a) Find  $P(A \cap B)$
  - (b) Fill in the probability value for each area in the Venn diagram representing the situation. (there are four values)



- (c) Find  $P(A \cup B)$
- (d) Find  $P(A \cap B')$
- 17. The function  $f(x) = e^x$  is shown on the graph. Sketch g(x) = f(x-3) 1. Plot and label the asymptote(s).

