

6-9DN-analytic-proof

1. The line l has the equation $y = \frac{3}{2}x + 5$.

(a) What is the slope of the line k , given $k \parallel l$?

(b) What is the slope of the line j , given $j \perp l$?

2. Find the decimal value of each expression, rounded to the nearest thousandth.

Write your answer as given in example #1.

(a) $\tan 60^\circ = 1.7320508 \dots$ (c) $\frac{2}{3}\sqrt{11}$

≈ 1.732

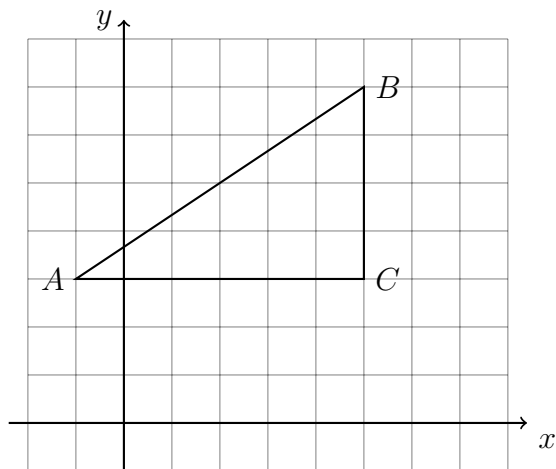
(b) $\tan 30^\circ$ (d) $\frac{(-5)^2}{7}$

3. Given $\triangle ABC$, find the lengths of its sides. $A(-1, 3)$, $B(5, 7)$, $C(5, 3)$.

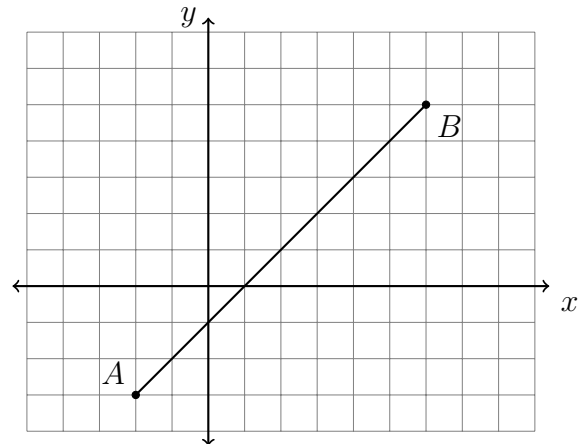
(a) $AC =$

(b) $BC =$

(c) Use the formula for distance:
 $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$
 $AB =$



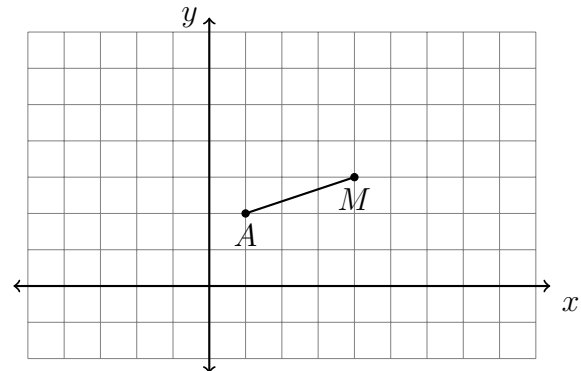
4. As shown, \overline{AB} has endpoints with coordinates $A(-2, -3)$ and $B(6, 5)$. Show the calculation for the coordinates of the midpoint M of \overline{AB} . Mark and label it on the graph.



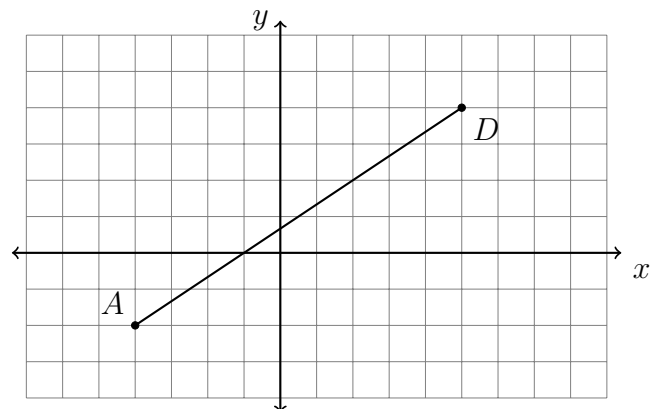
5. $A(1, 2)$ is one endpoint of \overline{AB} . The segment's midpoint is $M(4, 3)$. Find the other endpoint, B .

What translation maps

$$A(1, 2) \rightarrow M(4, 3)?$$



6. In the diagram below, \overline{AD} has endpoints with coordinates $A(-4, -2)$ and $D(5, 4)$. What points B and C trisect \overline{AD} into three congruent segments? Mark and label them on the graph. State their coordinates.



Spicy Regents problems: Using slope to prove a parallelogram

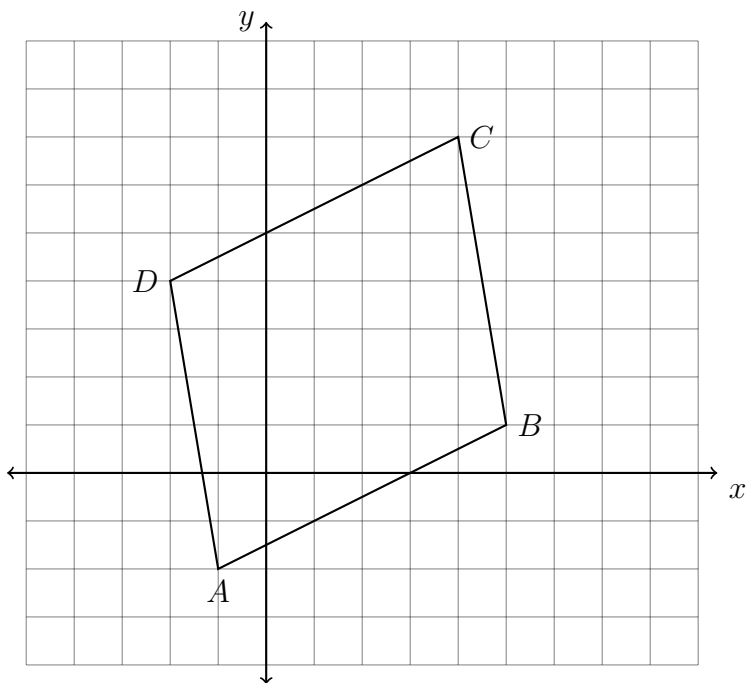
7. In this problem use the following theorem (copy it at the bottom of the page after your calculations):

A quadrilateral is a parallelogram if and only if it's opposite sides are parallel.

Shown below is quadrilateral $ABCD$, $A(-1, -2)$, $B(5, 1)$, $C(4, 7)$, and $D(-2, 4)$.

Prove it is a parallelogram by

- (a) finding the slope of each of the four sides,
- (b) stating which sides are parallel,
- (c) copying the theorem as your conclusion.



Using the distance formula to prove a parallelogram

8. In this problem use the following theorem (copy it at the bottom of the page after your calculations):

A quadrilateral is a parallelogram if and only if it's opposite sides are congruent.

Shown below is quadrilateral $ABCD$, $A(-1, -2)$, $B(5, 1)$, $C(4, 7)$, and $D(-2, 4)$.

Prove it is a parallelogram by

- (a) finding the length of each of the four sides,
- (b) stating which sides are congruent,
- (c) copying the theorem as your conclusion.

