Name:

## Unit 5 Test: Integral Calculus

You may use a calculator on these problems

[30 marks]

1. Let 
$$f(x) = x^3 - 4x^2 - 7$$
. Find  $f'(x)$ . [2]

2. Let 
$$f(x) = e^{3x-1}$$
. Find  $f'(x)$ . [2]

3. Let 
$$f(x) = x \sin x$$
. Find  $f'(x)$ . [2]

4. Let 
$$f(x) = \sqrt{x} + \ln x$$
. Find  $f'(x)$ . [2]

5. Find 
$$\int x^3 dx$$
. [2]

6. Find 
$$\int \sin x \, dx$$
.

7. Find 
$$\int e^{3x} dx$$
. [2]

8. Find 
$$\int (2x+4)(x^2+4x)^3 dx$$
. [2]

9. Find 
$$\int_0^2 x^2 e^{-x} dx$$
. [4]

10. Find 
$$\int_0^3 x - e^{0.5x} + 3 \, dx$$
. [4]

11. Let 
$$f(x) = xe^{-x}$$
 and  $g(x) = -3f(x) + 1$ . [6 marks]  
The graphs of  $f$  and  $g$  intersect at  $x = p$  and  $x = q$ , where  $p < q$ .

(a) Find the values of 
$$f$$
 and  $q$ . [3]

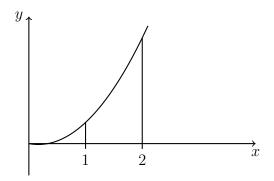
(b) Hence, find the area of the region enclosed by the graphs of f and g. [3]

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## No Calculator section

[38 marks]

12. Let  $f(x) = 3x^2 - x$ . The graph of f is shown in the following diagram. [6 marks]



(a) Find f'(x).

(b) Find the area of the region enclosed by the graph of f, the x-axis and the lines x = 1 and x = 2. [4]

13. Consider a function f(x) such that  $\int_1^6 f(x) dx = 8$ . [6 marks]

(a) Find 
$$\int_{1}^{6} 2f(x) dx$$
. [2]

(b) Find 
$$\int_1^6 (f(x) + 2) dx$$
. [4]

14. 14M.1.sl.TZ2.5 [6 marks]

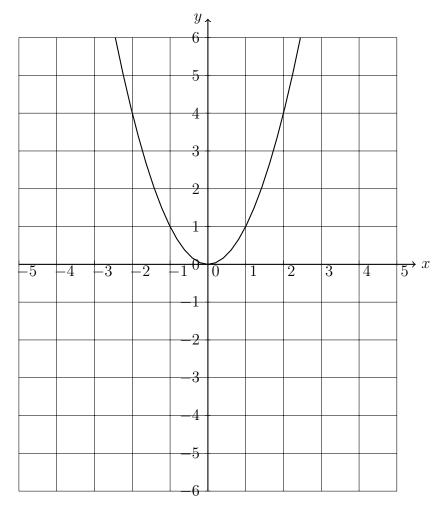
The graph of a function h passes through the point  $(\frac{\pi}{12}, 5)$ . Given that  $h'(x) = 4\cos 2x$ , find h(x).

[6]

[7 marks]

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- 15. 18M.2.sl.TZ1.4 Let  $g(x) = -(x-1)^2 + 5$ .
  - (a) Write down the coordinates of the vertex of the graph of g. [1]
  - (b) Let  $f(x) = x^2$ . The following diagram shows part of the graph of f.



The graph of g intersects the graph of f at x=-1 and x=2. On the grid above, sketch the graph of g for  $-2 \le x \le 4$ .

[3]

- (c) Find the area of the region enclosed by the graphs of f and g.
- [3]
- 16. A function f(x) has derivative  $f'(x) = 3x^2 + 18x$ . The graph of f has an x-intercept at x = -1.
  - (a) Find f(x).
  - (b) The graph of f has a point of inflexion at x = p. Find p. [4]
  - (c) Find the values of x for which the graph of f is concave-down. [3]