

**HW: Sequences and series, currency, and interest calculations**

**1a.** Only one of the following four sequences is arithmetic and only one of them is geometric.

$$a_n = 1, 2, 3, 5, \dots$$

$$b_n = 1, \frac{3}{2}, \frac{9}{4}, \frac{27}{8}, \dots$$

$$c_n = 1, \frac{1}{2}, \frac{1}{3}, \frac{1}{4}, \dots$$

$$d_n = 1, 0.95, 0.90, 0.85, \dots$$

State which sequence is

(i) arithmetic;

(ii) geometric.

[2 marks]

**1b.** For **another** geometric sequence  $e_n = -6, -3, -\frac{3}{2}, -\frac{3}{4}, \dots$

write down the common ratio;

[1 mark]

**1c.** For **another** geometric sequence  $e_n = -6, -3, -\frac{3}{2}, -\frac{3}{4}, \dots$

find the **exact** value of the tenth term. Give your answer as a fraction.

[3 marks]

1a. i) _____
ii) _____
1b. _____
1c. _____

**2a.** The second term of an arithmetic sequence is 30. The fifth term is 90.

Calculate

(i) the common difference of the sequence;

(ii) the first term of the sequence.

*[3 marks]*

**2b.** The first, second and fifth terms of this arithmetic sequence are the first three terms of a geometric sequence.

Calculate the seventh term of the **geometric** sequence.

*[3 marks]*

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**3a.** The first term,  $u_1$ , of an arithmetic sequence is **145**. The fifth term,  $u_5$ , of the sequence is **113**.

Find the common difference of the sequence.

[2 marks]

**3b.** The  $n^{\text{th}}$  term,  $u_n$ , of the sequence is  $-7$ .

Find the value of  $n$ .

[2 marks]

**3c.** Find  $S_{20}$ , the sum of the first twenty terms of the sequence.

[2 marks]

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3a. \_\_\_\_\_

3b. \_\_\_\_\_

3c. \_\_\_\_\_

**4a.** The fourth term,  $u$ , of a geometric sequence is 135. The fifth term,  $u$ , is 101.25 .

Find the common ratio of the sequence.

[2 marks]

**4b.** Find  $u$ , the first term of the sequence.

[2 marks]

**4c.** Calculate the sum of the first 10 terms of the sequence.

[2 marks]

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4a. \_\_\_\_\_

4b. \_\_\_\_\_

4c. \_\_\_\_\_

**5a.** Shiyun bought a car in 1999. The value of the car  $V$ , in USD, is depreciating according to the exponential model

$$V = 25000 \times 1.5^{-0.2t}, t \geq 0$$

where  $t$  is the time, in years, that Shiyun has owned the car.

Write down the value of the car when Shiyun bought it.

[1 mark]

**5b.** Calculate the value of the car three years after Shiyun bought it. Give your answer correct to **two decimal places**.

[2 marks]

**5c.** Calculate the time for the car to depreciate to half of its value since Shiyun bought it.

[3 marks]

5a. \_\_\_\_\_

5b. \_\_\_\_\_

5c. \_\_\_\_\_

**6a. Give your answers to parts (a) to (e) to the nearest dollar.**

On Hugh's 18th birthday his parents gave him options of how he might receive his monthly allowance for the next two years.

**Option A** \$60 each month for two years

**Option B** \$10 in the first month, \$15 in the second month, \$20 in the third month, increasing by \$5 each month for two years

**Option C** \$15 in the first month and increasing by 10% each month for two years

**Option D** Investing \$1500 at a bank at the beginning of the first year, with an interest rate of 6% per annum, **compounded monthly**.

Hugh does not spend any of his allowance during the two year period.

If Hugh chooses **Option A**, calculate the total value of his allowance at the end of the two year period. [2 marks]

**6b.** If Hugh chooses **Option B**, calculate

- (i) the amount of money he will receive in the 17th month;
- (ii) the total value of his allowance at the end of the two year period. [5 marks]

**6c.** If Hugh chooses **Option C**, calculate

- (i) the amount of money Hugh would receive in the 13th month;
- (ii) the total value of his allowance at the end of the two year period. [5 marks]

**6d.** If Hugh chooses **Option D**, calculate the total value of his allowance at the end of the two year period. [3 marks]

**6e.** State which of the options, A, B, C or D, Hugh should choose to give him the greatest total value of his allowance at the end of the two year period. [1 mark]

**6f.** Another bank guarantees Hugh an amount of \$1750 after two years of investment if he invests \$1500 at this bank. The interest is **compounded annually**.

Calculate the interest rate per annum offered by the bank. [3 marks]