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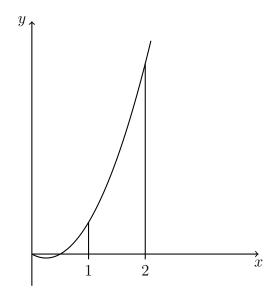
## Unit 5 Pretest: Integral Calculus

## Using the calculator for definite integrals

- 1. 16M.2.sl.TZ1.2 [6 marks] Let  $f(x) = x^2$  and  $g(x) = 3 \ln(x+1)$ , for x > -1.
  - (a) Solve f(x) = g(x)[3]
  - [3] (b) Find the area of the region enclosed by the graphs of f and q.
- 2. 16N.2.sl.TZ0.4 [6 marks] Let  $f(x) = xe^{-x}$  and g(x) = -3f(x) + 1. The graphs of f and g intersect at x = p and x = q, where p < q.
  - (a) Find the values of f and q. [3]
  - (b) Hence, find the area of the region enclosed by the graphs of f and g. [3]

## No Calculator section

3. 18M.1.sl.TZ2.2 [6 marks] Let  $f(x) = 6x^2 - 3x$ . The graph of f is shown in the following diagram.



- (a) Find f'(x). [2]
- (b) Find the area of the region enclosed by the graph of f, the x-axis and the lines x = 1 and x = 2. [4]
- 4. 15N.1.sl.TZ0.3 [6 marks] Let  $f'(x) = 6x^2 - 5$ . and f(2) = -3, find f(x). [6]

5. 13N.1.sl.TZ0.4 [6 marks]

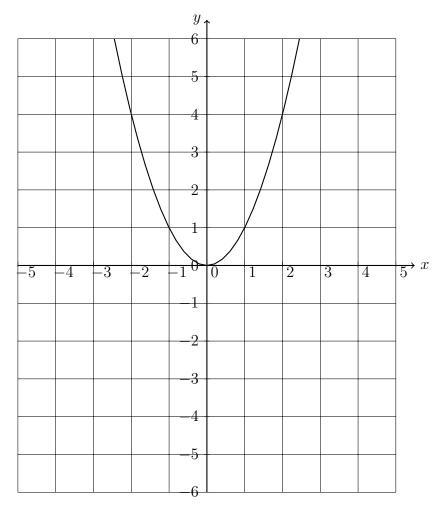
Consider a function f(x) such that  $\int_1^6 f(x) dx = 8$ .

(a) Find 
$$\int_{1}^{6} 2f(x) dx$$
. [2]

(b) Find 
$$\int_{1}^{6} (f(x) + 2) dx$$
. [4]

6. 18M.2.sl.TZ1.4 [7 marks] Let  $g(x) = -(x-1)^2 + 5$ .

- (a) Write down the coordinates of the vertex of the graph of g. [1]
- (b) Let  $f(x) = x^2$ . The following diagram shows part of the graph of f.



The graph of g intersects the graph of f at x=-1 and x=2. On the grid above, sketch the graph of g for  $-2 \le x \le 4$ .

[3]

(c) Find the area of the region enclosed by the graphs of f and g.

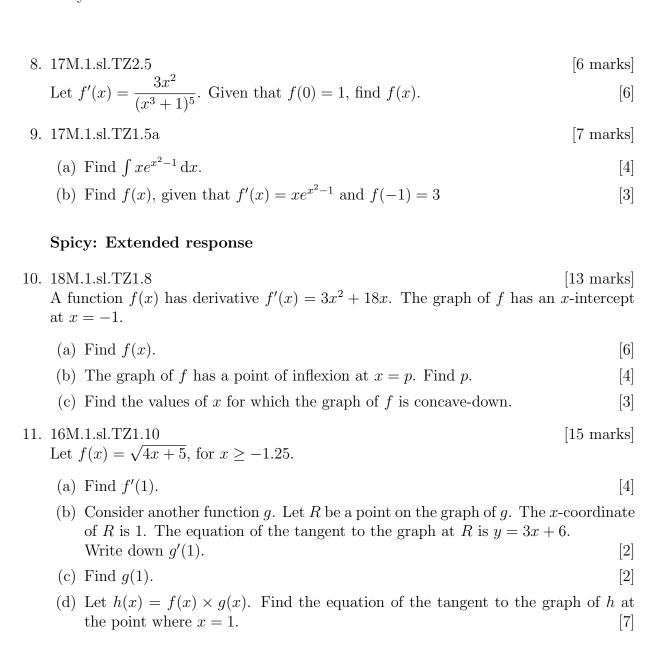
[3]

7. 14M.1.sl.TZ2.5 [6 marks]

The graph of a function h passes through the point  $(\frac{\pi}{12}, 5)$ . Given that  $h'(x) = 4\cos 2x$ , find h(x).

[6]

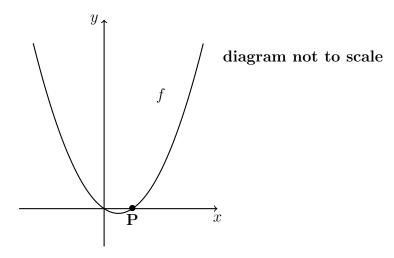
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## 12. (#19) 17N.1.sl.TZ0.8

[16 marks]

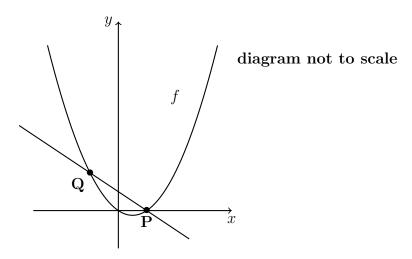
Let  $f(x) = x^2 - x$ , for  $x \in \mathbb{R}$ . The following diagram shows part of the graph of f.



The graph of f crosses the x-axis at the origin and at the point P(1,0).

(a) Show that 
$$f'(1) = 1$$
. [3]

- (b) The line L is the normal to the graph of f at P. Find the equation of L in the form y = ax + b.
- (c) The line L intersects the graph of f at another point Q, as shown in the following diagram.



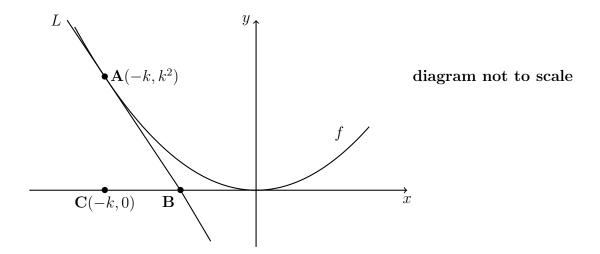
Find the x-coordinate of Q.

[4] [6]

(d) Find the area of the region enclosed by the graph of f and the line L.

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13. (#23) 17M.1.sl.TZ2.10 [17 marks] Let  $f(x) = x^2$ . The following diagram shows part of the graph of f.



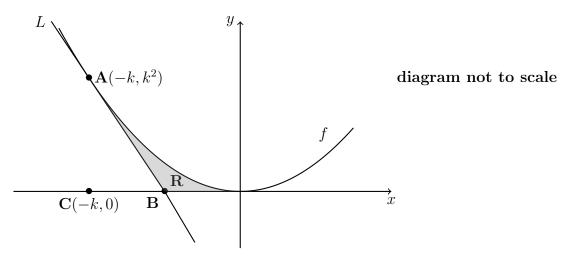
The line L is the tangent to the graph of f at the point  $A(-k, k^2)$ , and intersects the x-axis at point B. The point C is (-k, 0).

(a) Write down 
$$f'(x)$$
. [1]

(b) Find the gradient of 
$$L$$
. [2]

(c) Show that the x-coordinate of B is 
$$-\frac{k}{2}$$
. [5]

- (d) Find the area of triangle ABC, giving your answer in terms of k. [2]
- (e) The region R is enclosed by L, the graph of f, and the x-axis. This is shown in the following diagram.



Given that the area of triangle ABC is p times the area of R, find the value of p. [7]