Review: Exponents and radicals (easier)

Do these problems without a calculator. Use algebra properties to simplify each expression.

Exponent rules

1.
$$4x^2 \times x^4y^3$$

$$2. \ a^3b \div a^2$$

3.
$$(x^2y^2)^2 \times (x^3y)$$

4.
$$(\frac{1}{2}x^3)^2$$

Fractional and negative exponents

Simplify. Express as fractions or radicals

5.
$$49^{\frac{1}{2}}$$

6.
$$(xy)^{\frac{1}{2}}$$

7.
$$(ab)^{-1}$$

8.
$$(x^2y)^{-2}$$

Radicals and exponents

Simplify, leaving no negative or fractional exponents. $\,$

9.
$$\sqrt{x^4y^2}$$

$$10. \ \frac{\sqrt[3]{8x}}{4}$$

11.
$$\sqrt{\frac{x^2y^6}{z^4}}$$

Review: Exponents and radicals (challenge)

Do these problems without a calculator. Answer the first page on loose leaf paper.

Simplify, leaving no negative or fractional exponents.

1.
$$\frac{3}{4}a^{-3} \times a^3b^{-3}$$

$$2. \ \frac{2\sqrt{36x^2}}{\sqrt[3]{27x^3}}$$

3.
$$x^3y^{-2} \times (\frac{x}{y^2})^{-1}$$

4.
$$(-2x^2y)^2$$

5.
$$\frac{2}{3}(x^{-2}y)^3 \times \frac{6}{11}(x^2y^{-1})$$

6.
$$49^{\frac{1}{4}}$$

7.
$$\sqrt[3]{\frac{a^3b^{-9}}{z^{-6}}}$$

8. Let
$$f(x) = x^2 - 6x - 7$$
.

- (a) Show that the roots of f(x) are 7 and -1.
- (b) Rewrite f(x) in vertex form. (complete the square)
- (c) Hence, state the vertex as an ordered pair.
- (d) The function g(x) is made by translating f(x) right two units and up one unit. Write down the vertex of g(x).
- (e) Find the y-intercept of g(x).
- (f) Find the zeros of g(x).

9. Let
$$f(x) = (x-3)^2 - 4x$$
 and $g(x) = 2x - 5$.

(a) Find
$$q^{-1}(x)$$

(b) Find
$$(f \circ g)(x)$$

10. Let
$$f(x) = 2x^2 + kx + 2$$
.

(a) f(x) has exactly one root. Find k.

(b)
$$g(x) = -f(x) + 4$$
. Find the solution(s) to $g(x) = f(x)$

11. Let
$$f(x) = x^2 + 3x - 1$$
 and $g(x) = 2x - 3$. Find $(f \times g)(x)$

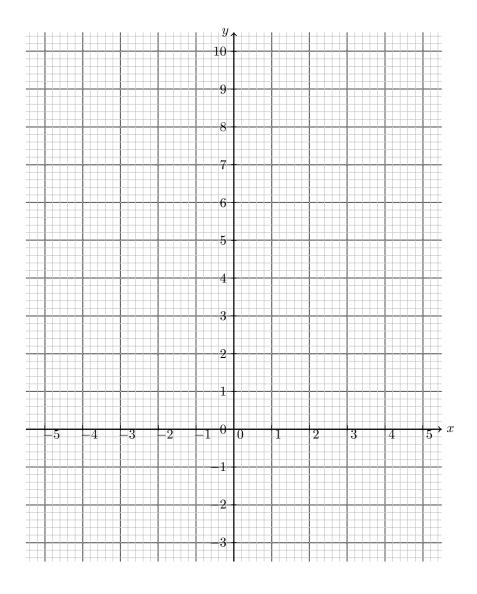
12. Let $f(x) = \frac{1}{3}(3)^x$, for $-3 \le x \le 3$.

(a) On the grid below, graph f.

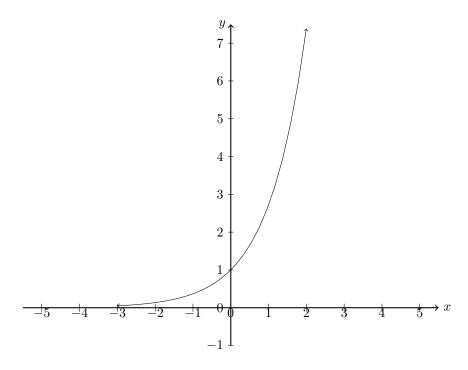
(b) Write down the value of f(0).

(c) Using the graph, solve for f(x) = 1.

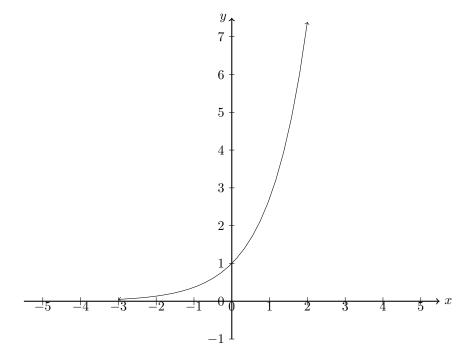
(d) What is the value of $f^{-1}(9)$?



13. The function $f(x) = e^x$ is shown on the graph. Sketch g(x) = f(x) + 1. Plot and label the asymptote.



14. The function $f(x) = e^x$ is shown on the graph. Sketch g(x) = -f(x) + 5. Plot and label the asymptote.



- 15. Graph the function $f(x) = 2^x$ on the grid below.
 - (a) Label the y-intercept as an ordered pair.
 - (b) Label the point representing the solution to the equation f(x) = 4 as an ordered pair.
 - (c) Write down the value of $f^{-1}(\frac{1}{2})$ and label the point on the graph of f.
 - (d) Graph the inverse function, $f^{-1}(x)$. Hint: plot the three points above, reversing the x and y.

