11.6 Problem set: Exact values of standard trigonometry ratios

1. A right $\triangle ABC$ is shown with side lengths 1, $\sqrt{3}$, and 2, as marked.

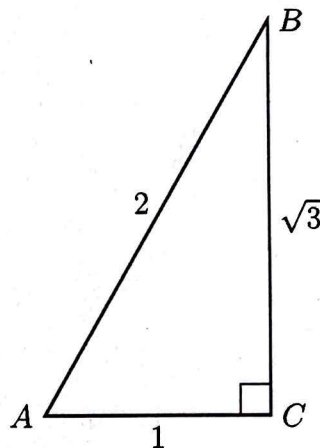   Identify each true statement

   ☑ (a) $1^2 + (\sqrt{3})^2 = 2^2$

   ☑ (b) $\cos A = \dfrac{1}{2}$

   ☐ (c) $\sin B = \dfrac{\sqrt{3}}{2}$ ✗

   ☑ (d) $m\angle A = 60°$

   ☑ (e) $\cos B = \dfrac{\sqrt{3}}{2}$

   ☑ (f) $m\angle A = 2 \times m\angle B$

2. Two similar, right isosceles triangles $\triangle HAT \sim \triangle CAB$ have a scale factor $k = 3$. Angles $\angle H$ and $\angle C$ measure 90° and $HA = HT = 1$, as shown.

   (a) Find the length of the hypotenuse TA
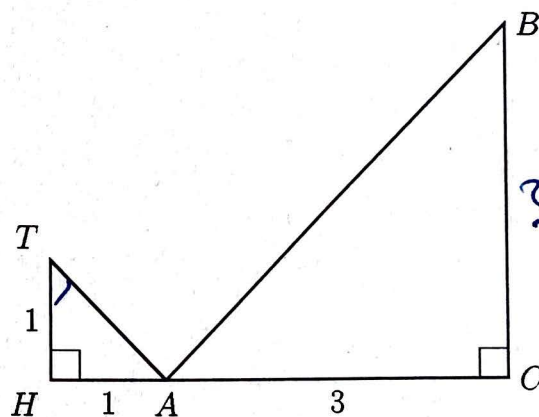
   $$TA^2 = 1^2 + 1^2 = 2$$
   $$TA = \sqrt{2}$$

   (b) Write down the measure of $\angle T$

   $$45°$$

   (c) Find the altitude of $\triangle CAB$, BC

   $$BC = AC = 3$$

3. Using a calculator, find θ and round to the *nearest whole degree*.

   (a) $\theta = \sin^{-1} 0.500$

   $$= 30°$$

   (b) $\theta = \cos^{-1}\left(\dfrac{\sqrt{3}}{2}\right)$

   $$= 30°$$

   (c) $\tan\theta = 1.000$

   $$\theta = 45°$$

   (d) $\cos\theta = 0.707$

   $$\theta = 45.00865...$$
   $$\approx 45°$$