

11.8 Problem set: Reference angles

1. Two right triangles, $\triangle ABC$ and $\triangle ADE$, are shown in the unit circle with the coordinates of B and D marked.

Identify each true statement.

☐ (a) $AC = 1$ \times

☒ (b) The altitude of $\triangle ABC$ is $\frac{\sqrt{2}}{2}$

☒ (c) $\tan \angle BAC = 1$

☒ (d) $m\angle BAC = 45^\circ$

☐ (e) $m\angle DAE = 60^\circ$ \times

☒ (f) $AD = 1$

- (g) Mark the $\angle CAD$ on the diagram.

State its measure, given its reference angle's measure, $m\angle DAE = 30^\circ$.

Justify your answer.

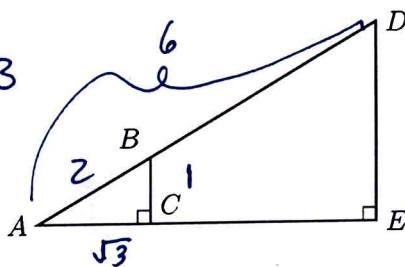
$m\angle CAD = 150^\circ$. $\angle CAD$ is an obtuse angle falling in the second quadrant. It is supplementary to $\angle DAE$. $180 - 30 = 150^\circ$

2. Given two 30-60-90 degree triangles, $\triangle ABC \sim \triangle ADE$, with $AC = 1$, $BC = \sqrt{3}$, $AB = 2$. If $AD = 6$ find the lengths of the other two sides.

(a) $DE = 3 \times 1 = 3$
 $BC \rightarrow DE$

$AB \rightarrow AD$
 $2 \rightarrow 6$
 $k = \frac{6}{2} = 3$

(b) $DF = 3\sqrt{3}$
 $AC \rightarrow AE$



3. Simplify. Rationalize denominators.

(a) $\sqrt{72}$
 $= \sqrt{36 \cdot 2}$
 $= 6\sqrt{2}$

(b) $\sqrt{50} - 4\sqrt{2}$
 $= \sqrt{25 \cdot 2} - 4\sqrt{2}$
 $= 5\sqrt{2} - 4\sqrt{2}$
 $= \sqrt{2}$

(c) $\frac{5}{\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}} = \frac{5\sqrt{5}}{5}$
 $= \sqrt{5}$