Name:

Classwork: Mixed review, short answer (57 marks). Paper 1, no calculator

Happy New Year! Take two days to complete this problem set.

1a. In an arithmetic sequence, the first term is 8 and the second term is 5.

Find the common difference.

[2 marks]

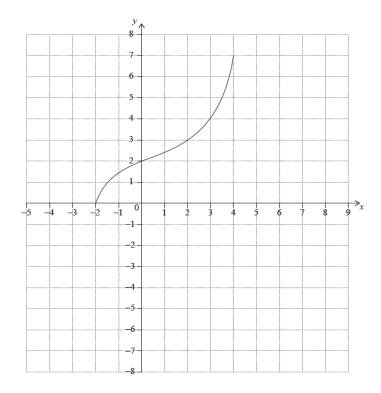
1b. Find the tenth term.

[2 marks]

1c. Find the sum of the first ten terms.

[2 marks]

2a. The following diagram shows the graph of a function f , with domain $-2\leqslant x\leqslant 4$.



The points (-2, 0) and (4, 7) lie on the graph of f.

Write down the range of f.

[1 mark]

2b. Write down f(2);

[1 mark]

2c. Write down $f^{-1}(2)$.

[1 mark]

2d. On the grid, sketch the graph of f^{-1} .

[3 marks]

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3a. [2 marks]

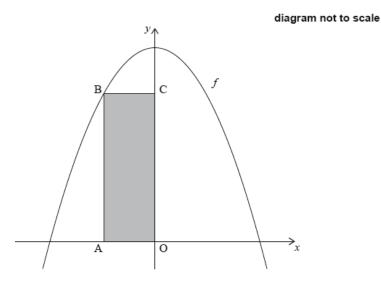
Let
$$f(x)=1+\mathrm{e}^{-x}$$
 and $g(x)=2x+b$, for $x\in\mathbb{R}$, where b is a constant. Find $(g\circ f)(x)$.

3b. [4 marks]

$$\lim_{{
m Given \ that}} (g\circ f)(x) = -3$$
 , find the value of b .

4. [7 marks]

Let $f(x)=15-x^2$, for $x\in\mathbb{R}$. The following diagram shows part of the graph of f and the rectangle OABC, where A is on the negative x-axis, B is on the graph of f, and C is on the y-axis.



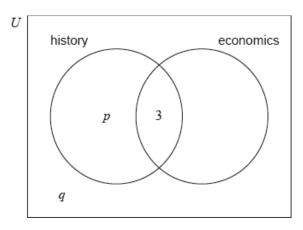
Find the x-coordinate of A that gives the maximum area of OABC.

5. [7 marks]

Consider
$$f(x) = \log k(6x - 3x^2)$$
, for $0 < x < 2$, where $k > 0$.

The equation f(x)=2 has exactly one solution. Find the value of k.

6a. In a group of 20 girls, 13 take history and 8 take economics. Three girls take both history and economics, as shown in the following Venn diagram. The values p and q represent numbers of girls.



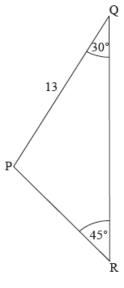
Find the value of p; [2 marks]

6b. Find the value of q. [2 marks]

6c. A girl is selected at random. Find the probability that she takes economics but not history. [2 marks]

7. The following diagram shows triangle PQR.

diagram not to scale



 $\hat{PQR} = 30^{\circ}$, $\hat{QRP} = 45^{\circ}$ and $PQ = 13 \, cm$.

Find PR. [6 marks]

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8a. [1 mark]

Jim heated a liquid until it boiled. He measured the temperature of the liquid as it cooled. The following table shows its temperature, d degrees Celsius, t minutes after it boiled.

t (min)	0	4	8	12	16	20
d (°C)	105	98.4	85.4	74.8	68.7	62.1

Write down the independent variable.

8b. Write down the boiling temperature of the liquid.

[1 mark]

8c. [2 marks]

Jim believes that the relationship between d and t can be modelled by a linear regression equation.

Jim describes the correlation as **very strong**. Circle the value below which best represents the correlation coefficient.

0.992

0.251

0

-0.251

-0.992

8d. [2 marks]

Jim's model is d=-2.24t+105, for $0\leqslant t\leqslant 20$. Use his model to predict the decrease in temperature for any 2 minute interval.