PreTest: Statistics, sequences, overall review (complete on lined paper)

(109 points, approximately 2 hours work. 1 hour's work due tomorrow)

1a. Consider the following frequency table.

x	Frequency
2	8
4	15
7	21
10	28
11	3

[1 mark]

Write down the mode.

1b. Find the value of the range. [2 marks]

1c. Find the mean. [2 marks]

1d. Find the variance. [2 marks]

2a. There are 10 items in a data set. The sum of the items is 60.

Find the mean. [2 marks]

- **2b.** The variance of this data set is 3. Each value in the set is multiplied by 4.
 - (i) Write down the value of the new mean.
 - (ii) Find the value of the new variance. [3 marks]

3a. Let
$$f(x) = e^{0.5x} - 2$$
.

For the graph of *f*:

- (i) write down the y-intercept;
- (ii) find the x-intercept;
- (iii) write down the equation of the horizontal asymptote. [4 marks]
- **3b.** On the grid on page 5, sketch the graph of f, for $-4 \leqslant x \leqslant 4$.

4a. The following box-and-whisker plot represents the examination scores of a group of students.

Examination scores



Write down the median score.

[1 mark]

The range of the scores is 47 marks, and the interquartile range is 22 marks.

- **4b.** Find the value of
 - (i) C;

(ii) d. [4 marks]

5. Three consecutive terms of a geometric sequence are x-3, 6 and x+2.

Find the possible values of x.

[6 marks]

- **6.** In a geometric sequence, the fourth term is 8 times the first term. The sum of the first 10 terms is 2557.5. Find the 10th term of this sequence. [6 marks]
- **7a.** The first three terms of an arithmetic sequence are $u_1=0.3,\ u_2=1.5,\ u_3=2.7$

Find the common difference.

[2 marks]

7b. Find the 30th term of the sequence.

[2 marks]

7c. Find the sum of the first 30 terms.

[2 marks]

8a. The sums of the terms of a sequence follow the pattern

$$S_1=1+k,\; S_2=5+3k,\; S_3=12+7k,\; S_4=22+15k,\; \ldots, \; ext{where} \; k\in \mathbb{Z}.$$

Given that $u_1 = 1 + k_1 \operatorname{find} u_2$, u_3 and u_4 .

[4 marks]

8b. Find a general expression for u_n .

[4 marks]

BECA / Huson / 11.1 IB Math SL 15 May 2019

Name:

 $g_{a. \text{ Let }} f(x) = 3 \ln x_{\text{ and }} g(x) = \ln 5x^3$

Express g(x) in the form $f(x) + \ln a$, where $a \in \mathbb{Z}^+$.

[4 marks]

9b. The graph of g is a transformation of the graph of f. Give a full geometric description of this transformation.

[3 marks]

10. Solve
$$\log_2 x + \log_2 (x-2) = 3$$
 , for $x>2$.

[7 marks]

11a. Let $f(x) = \mathrm{e}^{x+3}$

- (i) Show that $f^{-1}(x) = \ln x 3$.
- (ii) Write down the domain of f^{-1} .

[3 marks]

11b. Solve the equation $f^{-1}(x) = \ln rac{1}{x}$.

[4 marks]

 $_{\mathbf{12a.}\,\mathrm{Let}}f(x)=(x-5)^3$, for $x\in\mathbb{R}_{.}$

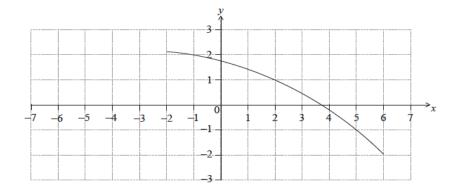
 $_{ ext{Find}} f^{-1}(x)$

[3 marks]

12b. Let g be a function so that $(f\circ g)(x)=8x^6$. Find g(x)

[3 marks]

13a. The following diagram shows the graph of a function f.



Find $f^{-1}(-1)$.

[2 marks]

13b. Find $(f \circ f)(-1)$

[3 marks]

13c. On the same diagram, sketch the graph of y=f(-x)

[2 marks]

BECA / Huson / 11.1 IB Math SL 15 May 2019

Name:

14. Let f(x) = 2x + 3 and $g(x) = x^3$.

Find $(f \circ g)(x)$

[2 marks]

15. Let $f(x)=m-\frac{1}{x}$, for $x\neq 0$. The line y=x-m intersects the graph of f in two distinct points. Find the possible values of m.

16a. Consider $f(x) = x^2 + qx + r$. The graph of f has a minimum value when x = -1.5.

The distance between the two zeros of f is 9.

Show that the two zeros are 3 and -6.

[2 marks]

16b. Find the value of q and of r.

[4 marks]

17a. Let $f(x) = x^2 + x - 6$.

Write down the y-intercept of the graph of f.

[1 mark]

17b. Solve f(x) = 0

[3 marks]

 $f(x)=p+rac{9}{x-q}$, for x
eq q . The line x=3 is a vertical asymptote to the graph of f .

Write down the value of q.

[1 mark]

18b. The graph of f has a y-intercept at $(0,\ 4)$.

Find the value of p.

[4 marks]

18c. Write down the equation of the horizontal asymptote of the graph of f.

[1 mark]

Name:

(continued from page 1)

3. Let
$$f(x) = e^{0.5x} - 2$$
.

3b. On the grid on page 5, sketch the graph of f , for $-4\leqslant x\leqslant 4$.

[3 marks]

