

**1a.** The first three terms of an arithmetic sequence are 5, 6.7, 8.4 .

Find the common difference.

[2 marks]

**1b.** Find the 28<sup>th</sup> term of the sequence.

[2 marks]

**1c.** Find the sum of the first 28 terms.

[2 marks]

**2a.** The first term of a geometric sequence is 200 and the sum of the first four terms is 324.8.

Find the common ratio.

[4 marks]

**2b.** [2 marks] Find the tenth term.

**3a.** In an arithmetic sequence,  $u_1 = 2$  and  $u_3 = 8$  .

Find  $d$  .

[2 marks]

**3b.** Find  $u_{20}$  .

[2 marks]

**3c.** Find  $S_{20}$  .

[2 marks]

**4a.** In an arithmetic sequence  $u_1 = 7$ ,  $u_{20} = 64$  and  $u_n = 3709$  .

Find the value of the common difference.

[3 marks]

**4b.** Find the value of  $n$  .

[2 marks]

**5a.** The first three terms of an infinite geometric sequence are 32, 16 and 8.

Write down the value of  $r$  .

[1 mark]

**5b.** Find  $u_6$  .

[2 marks]

**5c.** Find the sum to infinity of this sequence.

[2 marks]

**6a.** Consider the arithmetic sequence 3, 9, 15,  $\dots$ , 1353 .

Write down the common difference.

[1 mark]

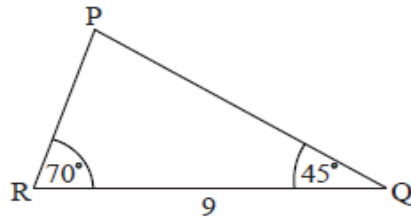
**6b.** Find the number of terms in the sequence.

[3 marks]

**6c.** Find the sum of the sequence.

[2 marks]

7a. The following diagram shows  $\triangle PQR$ , where  $RQ = 9$  cm,  $\hat{P}RQ = 70^\circ$  and  $\hat{P}QR = 45^\circ$ .



*diagram  
not to scale*

Find  $\hat{R}PQ$ .

[1 mark]

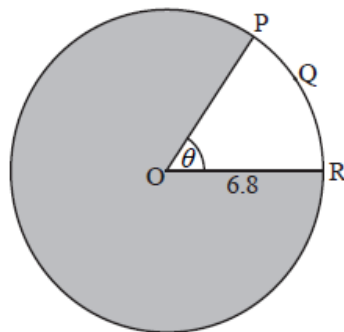
7b. Find  $PR$ .

[3 marks]

7c. Find the area of  $\triangle PQR$ .

[2 marks]

8a. Consider the following circle with centre  $O$  and radius 6.8 cm.



*diagram  
not to scale*

The length of the arc  $PQR$  is 8.5 cm.

Find the value of  $\theta$ .

[2 marks]

8b. Find the area of the shaded region.

[4 marks]

9a. Consider the triangle  $ABC$ , where  $AB = 10$ ,  $BC = 7$  and  $\hat{C}AB = 30^\circ$ .

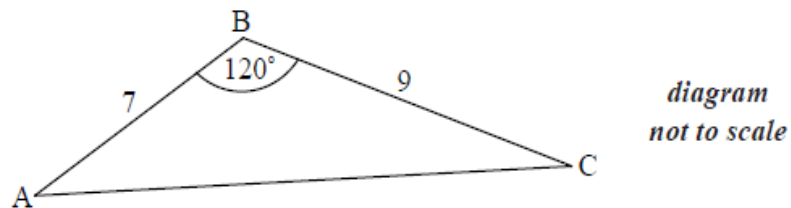
Find the two possible values of  $\hat{A}CB$ .

[4 marks]

9b. Hence, find  $\hat{A}BC$ , given that it is acute.

[2 marks]

**10a.** The following diagram shows triangle ABC .



$AB = 7$  cm,  $BC = 9$  cm and  $\widehat{ABC} = 120^\circ$  .

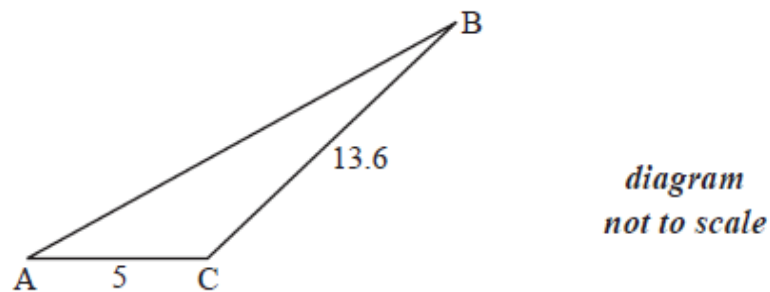
Find AC .

[3 marks]

**10b.** Find  $\widehat{BAC}$  .

[3 marks]

**11a.** The following diagram shows the triangle ABC.



The angle at C is obtuse,  $AC = 5$  cm,  $BC = 13.6$  cm and the area is  $20$  cm<sup>2</sup> .

Find  $\widehat{ACB}$  .

[4 marks]

**11b.** Find AB.

[3 marks]

**12a.** Let  $f(x) = \frac{\cos x}{\sin x}$ , for  $\sin x \neq 0$ .

Use the quotient rule to show that  $f'(x) = \frac{-1}{\sin^2 x}$ . [5 marks]

**12b.** Find  $f''(x)$ . [3 marks]

**12c.** In the following table,  $f'(\frac{\pi}{2}) = p$  and  $f''(\frac{\pi}{2}) = q$ . The table also gives approximate values of  $f'(x)$  and  $f''(x)$  near  $x = \frac{\pi}{2}$ .

$x$	$\frac{\pi}{2} - 0.1$	$\frac{\pi}{2}$	$\frac{\pi}{2} + 0.1$
$f'(x)$	-1.01	$p$	-1.01
$f''(x)$	0.203	$q$	-0.203

Find the value of  $p$  and of  $q$ . [3 marks]

**12d.** Use information from the table to explain why there is a point of inflexion on the graph of  $f$  where  $x = \frac{\pi}{2}$ . [2 marks]

**13a.** Let  $f(x) = \cos 2x$  and  $g(x) = 2x^2 - 1$ .

Find  $f(\frac{\pi}{2})$ . [2 marks]

**13b.** Find  $(g \circ f)(\frac{\pi}{2})$ . [2 marks]

**13c.** Given that  $(g \circ f)(x)$  can be written as  $\cos(kx)$ , find the value of  $k$ ,  $k \in \mathbb{Z}$ . [3 marks]