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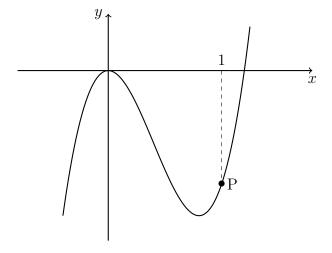
7-9 Homework: Mixed Calculus - without calculator

[58 marks]

- 1. 12M.1.sl.TZ1.3 [6 marks] Let $f(x) = e^{6x}$.
 - (a) Write down f'(x) [1]
 - (b) The tangent to the graph of f at the point P(0,b) has gradient m. [4]
 - i. Show that m = 6.
 - ii. Find b.
 - (c) Hence, write down the equation of this tangent. [1]
- 2. 09M.1.sl.TZ1.3 [6 marks] Let $f(x) = e^x \cos x$. Find the gradient of the normal to the curve of f at $x = \pi$.
- 3. 13M.1.sl.TZ1.3 [7 marks] Consider $f(x) = x^2 \sin x$.

(a) Find
$$f'(x)$$
. [4]

- (b) Find the gradient of the curve of f at $x = \frac{\pi}{2}$. [3]
- 4. 12N.1.sl.TZ0.4 [6 marks] Part of the graph of $f(x) = ax^3 6x^2$ is shown below.



The point P lies on the graph of f. At P, x=1.

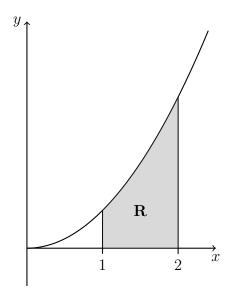
- (a) Find f'(x). [2]
- (b) The graph of f has a gradient of 3 at the point P. Find the value of a. [4]

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5. Let $f(x) = x^2$. [6 marks]

(a) Find
$$\int_{1}^{2} (f(x))^{2} dx$$
 [4]

(b) The following diagram shows part of the graph of f.



The shaded region R is enclosed by the graph of f, the x-axis, and the lines x=1 and x=2.

Find the volume of the solid formed when R is revolved 360° about the x-axis. [2]

6. 13N.1.sl.TZ0.4 [6 marks] Consider a function f(x) such that $\int_2^5 f(x) dx = 10$.

(a) Find
$$\int_{2}^{5} 3f(x) dx$$
. [2]

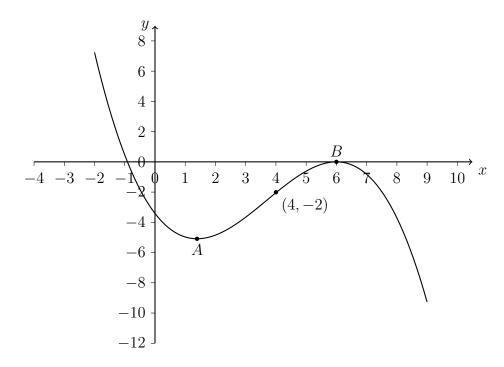
(b) Find
$$\int_2^5 (f(x) + 12) dx$$
. [4]

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7. 17M.1.sl.TZ1.6 [6 marks]

The following diagram shows the graph of f', the derivative of f.



The graph of f' has a local minimum at A, a local maximum at B and passes through (4,2). The point P(4,3) lies on the graph of the function, f.

- (a) Write down the gradient of the curve of f at P. [1]
- (b) Find the equation of the normal to the curve of f at P. [3]
- (c) Determine the concavity of the graph of f when 4 < x < 5 and justify your answer. [2]
- 8. 16M.1.sl.TZ1.10 [15 marks] Let $f(x) = \sqrt{4x+5}$, for $x \ge -1.25$.
 - (a) Find f'(1). [4]
 - (b) Consider another function g. Let R be a point on the graph of g. The x-coordinate of R is 1. The equation of the tangent to the graph at R is y = 3x + 6. Write down g'(1).
 - (c) Find g(1). [2]
 - (d) Let $h(x) = f(x) \times g(x)$. Find the equation of the tangent to the graph of h at the point where x = 1.