

Angle pairs and angle measure calculations

1. Notation and terminology
2. Complementary and supplementary calculations
3. Algebraic solutions of pair situations
 - (a) Linear pairs
 - (b) Vertical angles
4. Triangle exterior angles

Draw a linear pair with given measure

1. Given opposite rays \overrightarrow{AB} and \overrightarrow{AC} , with $\overline{AB} = 6$ cm. Draw a ray \overrightarrow{AD} such that $m\angle BAD = 60^\circ$ and $\overline{AD} = 6$ cm.



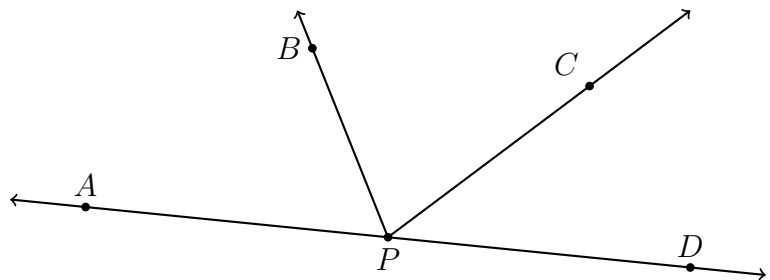
Angle pair short questions

1. The sum of the measures of two supplementary angles equals _____.
2. True or false: The angles making a linear pair are adjacent. _____.
3. The sum of the measures of two complementary angles equals _____.
4. True or false: The angles making a linear pair are complementary. _____.
5. Two vertical angles are supplementary. What are their measures? _____.
6. Sketch a linear pair.
 1. *variations*
True or false: The angles making a linear pair are supplementary. _____.
 2. The sum of the measures of two complementary angles equals _____.
 3. True or false: Vertical angles are congruent. _____.
 4. The sum of the measures of two supplementary angles equals _____.

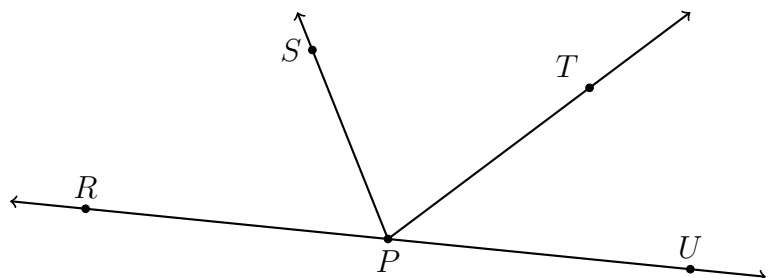
5. Two vertical angles are complementary. What are their measures? _____.
6. Sketch a pair of vertical angles.

Diagram short questions

1. Given the situation in the diagram, answer each question.



- (a) True or false: \overrightarrow{PA} and \overrightarrow{PD} are opposite rays. _____.
- (b) Name an angle adjacent to $\angle APB$. _____.
- (c) True or false: $\angle APC$ and $\angle CPD$ are supplementary angles. _____.
- (d) Name two angles that constitute a linear pair. _____.
2. (*variation*) Given the situation in the diagram, answer each question.



- (a) True or false: \overrightarrow{PR} and \overrightarrow{PT} are opposite rays. _____.
- (b) Name an angle adjacent to $\angle TPU$. _____.
- (c) True or false: $\angle RPT$ and $\angle SPU$ are supplementary angles. _____.
- (d) Name two angles that are adjacent. _____.

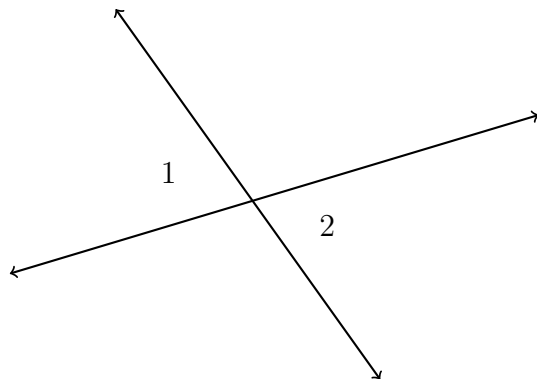
Complementary & supplementary arithmetic

- Given two supplementary angles: $m\angle 1 = 50$, $m\angle 2 = x$. Find x .
- Given two complementary angles: $m\angle 1 = x$, $m\angle 2 = 20$. Find $m\angle 1$.
- Given two supplementary angles: $m\angle 1 = 135$, $m\angle 2 = x$. Find x .
- Given two complementary angles: $m\angle 1 = x$, $m\angle 2 = 75$. Find $m\angle 1$.
- Given $m\angle A = 60$, $m\angle B = 20$, $m\angle 1 = 30$, $m\angle DEF = 150$, $m\angle FEG = 10$.

- (a) Find a pair of complementary angles. _____
- (b) Find a pair of supplementary angles. _____
- (c) Spicy: Find a different pair of supplementary angles. _____

Vertical angle algebra

- Given two vertical angles: $m\angle 1 = 3x + 10$, $m\angle 2 = 2x + 25$. Find $m\angle 1$. First label the drawing.



- (a) Write a geometric equation: _____

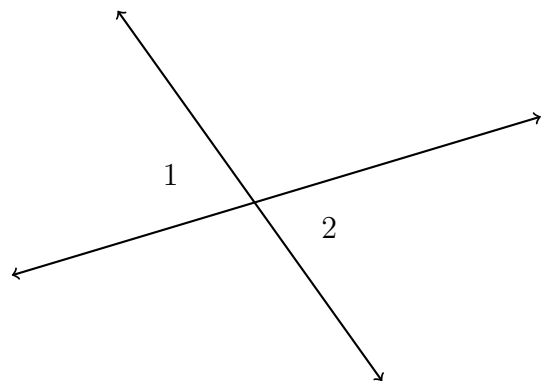
(b) Substitute algebraic values: _____

(c) Solve for x

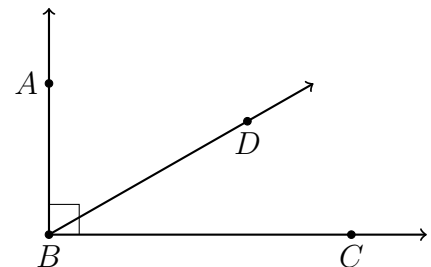
(d) Answer the question:

(e) Check your answer

2. *variation* Given two vertical angles: $m\angle 1 = 7x + 10$, $m\angle 2 = 2x + 45$. Find $m\angle 1$.
 First label the drawing.

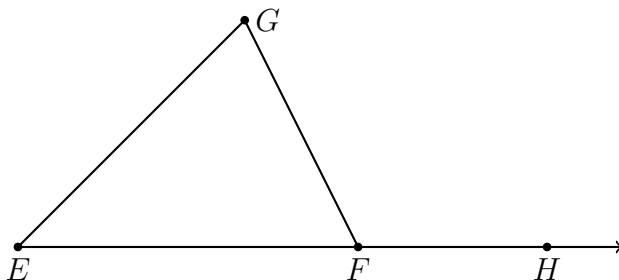


3. *variation* Given two perpendicular rays, \overrightarrow{BA} and \overrightarrow{BC} , as shown. $m\angle ABD = 2x + 10$, $m\angle DBC = x + 5$. Find $m\angle DBC$. First label the drawing.

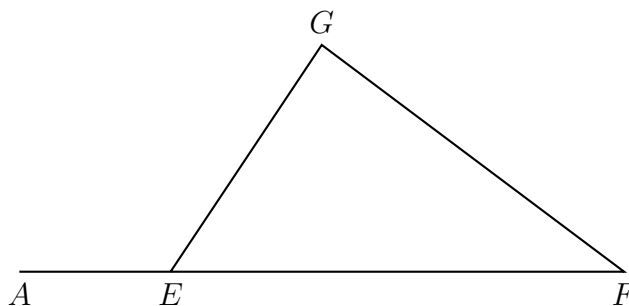


0.0.1 Triangle external angles

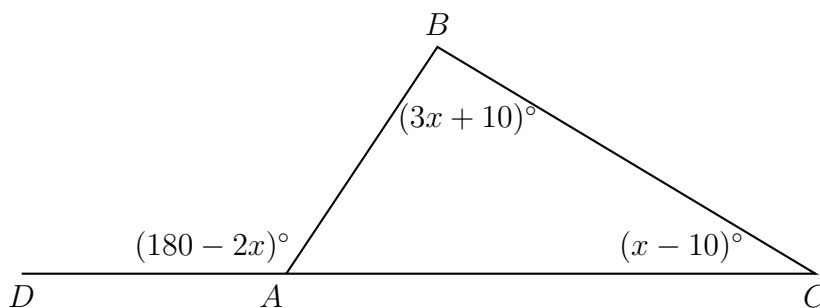
4. Given $m\angle E = 44$, and $m\angle GFH = 112$. Find $m\angle G$.



5. Given $\triangle EFG$ with \overline{EF} extended to A . If $m\angle F = 40^\circ$ and $m\angle AEG = 140^\circ$, what is $m\angle EGF$?



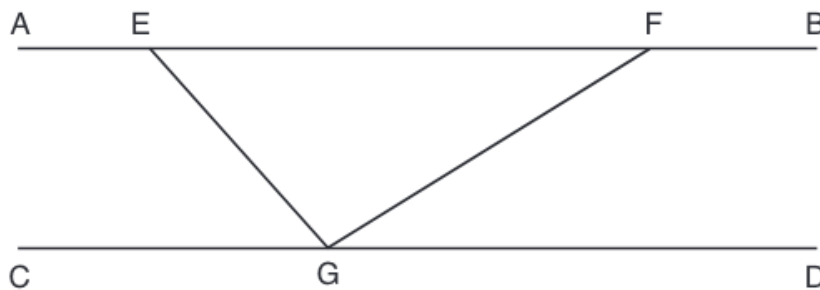
6. In $\triangle ABC$ shown below, side \overline{AC} is extended to point D with $m\angle DAB = (180 - 2x)^\circ$, $m\angle C = (x - 10)^\circ$, and $m\angle B = (3x + 10)^\circ$.



What is $m\angle BAC$?

7. Spicy: Regents problem

In the diagram below, $\overline{AEFB} \parallel \overline{CGD}$, and \overline{GE} and \overline{GF} are drawn.



If $m\angle EFG = 32^\circ$ and $m\angle AEG = 137^\circ$, what is $m\angle EGF$?

- | | |
|----------------|-----------------|
| (1) 11° | (3) 75° |
| (2) 43° | (4) 105° |