

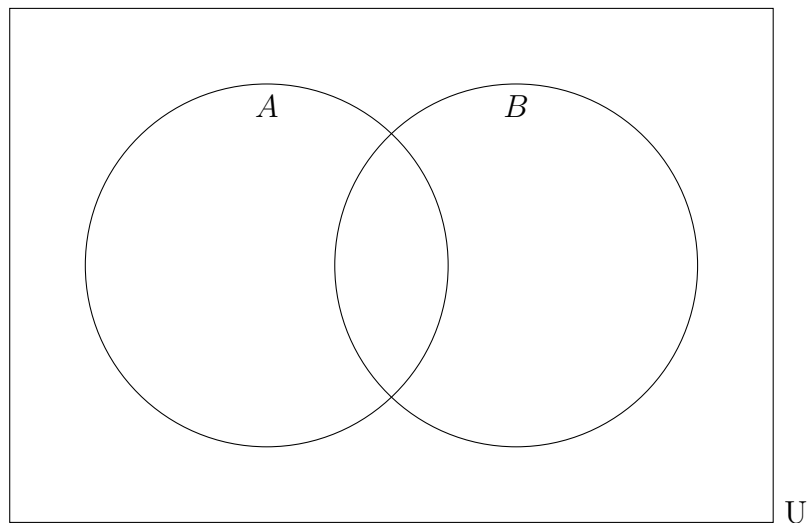
**Exam: Probability, Venn diagrams, descriptive statistics, trigonometry**

1. Given:

$$U = \{\text{the letters in the alphabet}\} \quad A = \{b, e, c, a\} \quad B = \{r, u, l, e, s\}$$

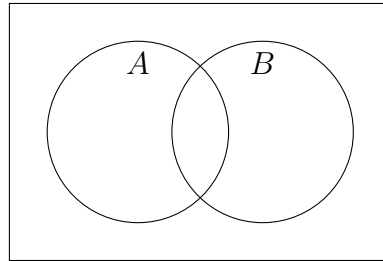
(a) List the elements of  $A \cap B$ . [1 mark](b) List the members of  $A \cup B$ . [1 mark]2. The universal set  $U$  is defined as the set of positive integers less than 10. The subsets  $A$  and  $B$  are defined as follows:

$$A = \{\text{the odd numbers}\} \quad B = \{\text{prime numbers}\}$$

(a) List the members of  $A'$ . [1 mark](b) List the members of  $(A \cup B)'$ . [1 mark](c) Place the elements of  $A$  and  $B$  in the appropriate regions in the Venn diagram below. [2 marks](d) List the items in  $A \cap B$ . [1 mark](e) If an element is selected at random, what is the probability that it is a member of both sets,  $(A \cap B)$ ? [1 mark]

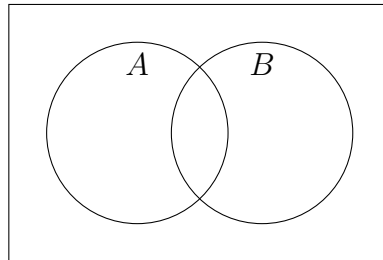
3. For each Venn diagram, shade the area representing the expression. Use pencil.

(a)  $A \cup B$



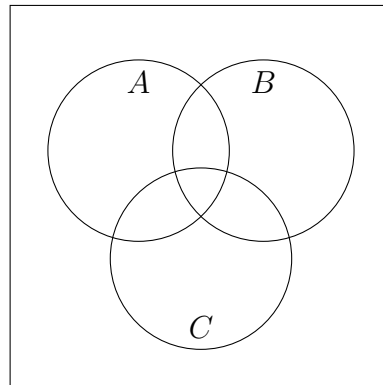
[2 marks]

(b)  $A' \cap B$



[2 marks]

(c)  $(A \cap B) \cup C$



[2 marks]

4. The events  $A$  and  $B$  are mutually exclusive with  $P(A) = 0.7$  and  $P(B) = 0.2$ .

(a) Write down  $P(A \cup B)$ .

[1 mark]

(b) Find  $P(A' \cup B)$ .

[1 mark]

5. The events  $A$  and  $B$  are independent with  $P(A) = 0.5$  and  $P(B) = 0.8$ .

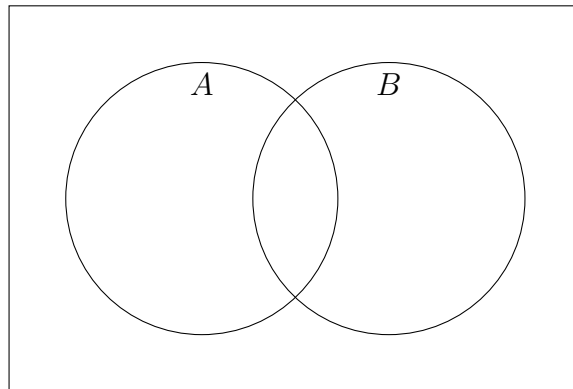
(a) Find  $P(A \cap B)$ . [2 marks]

(b) Find  $P(A \cup B)$ . [2 marks]

(c) Find  $P(B|A)$ . [2 marks]

6. Given events  $A$  and  $B$  with  $P(A) = 0.4$ ,  $P(B) = 0.5$ ,  $P(A \cap B) = 0.25$ .

(a) Completely mark the Venn diagram with probabilities for each area. [2 marks]



(b) Find  $P(A \cup B)$ . [2 marks]

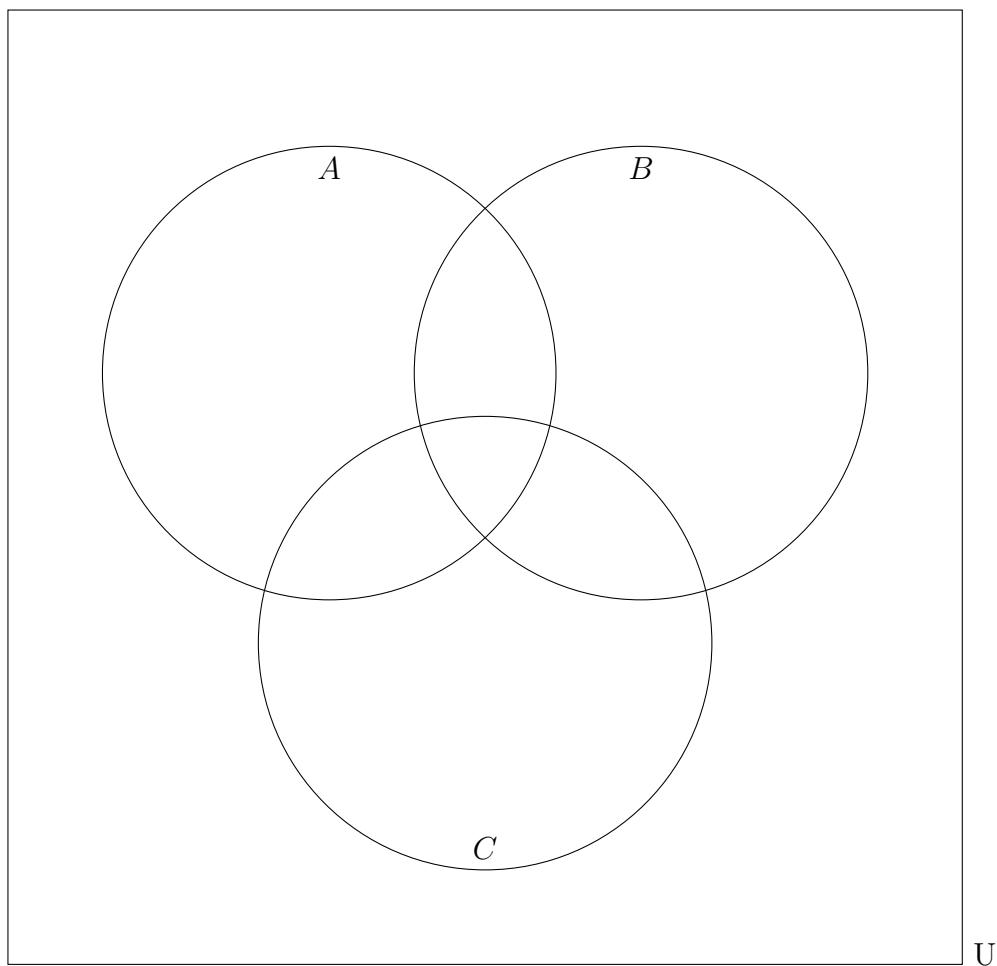
(c) State whether events  $A$  and  $B$  are independent. Justify your answer. [3 marks]

(d) Find  $P(A|B)$ . [2 marks]

7. There are 80 athletes playing the following sports:

- 35 play Archery
- 44 play Badminton
- 39 play Cricket
- 16 play Archery and Badminton
- 15 play Archery and Cricket
- 10 play Badminton and Cricket
- 3 play all three of these sports

Complete the Venn diagram below with the number of students in each region to represent the situation. [4 marks]



8. Forty IB high school students range in age from 15 to 18 years old. The following table shows the frequencies of each age.

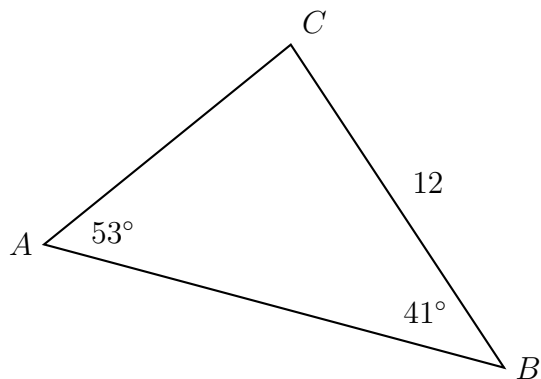
Age (years)	15	16	17	18
Frequency	5	$k$	15	7

- (a) Calculate the value of  $k$ . [1 mark]
- (b) Write down the mode. [1 mark]
- (c) Find the value of the range. [1 marks]
- (d) Find the median. [1 marks]
- (e) Find the mean. [2 marks]
- (f) Find the standard deviation. [2 marks]
9. A runner records her pace in terms of distance run ( $d$ ) in miles over time ( $t$ ) in minutes during a 4.5 mile run. She models her pace with a linear regression equation  $d = at + b$ .

minutes ( $t$ )	0	8	15	22	30
miles ( $d$ )	0	1.8	2.7	3.7	4.5

- (a) Find the values of  $a$ ,  $b$ , and the correlation  $r$ . [3 marks]
- (b) Explain what the value of  $a$  represents in the context of the situation. [2 marks]

10. The following diagram shows triangle  $ABC$  (not drawn to scale).



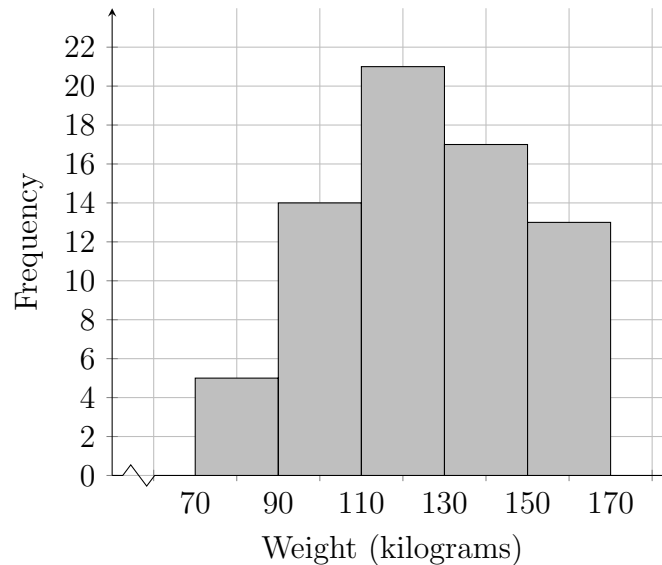
$BC = 12$ ,  $\hat{C}AB = 53^\circ$ , and  $\hat{A}BC = 41^\circ$

(a) Find the measure of  $\hat{A}CB$ . [1 mark]

(b) Find  $AC$ . [3 marks]

(c) Find the area of triangle  $ABC$ . [3 marks]

11. The histogram below shows the weight  $w$  in kilograms for 70 professional football players.

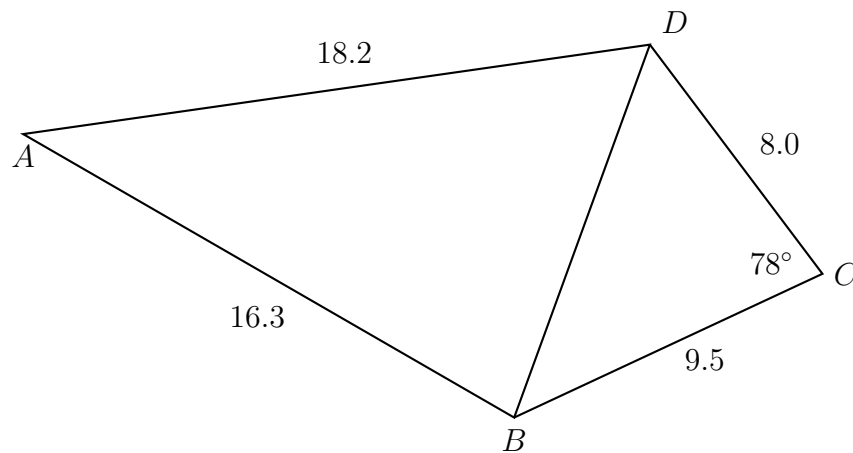


The following is the frequency table for the distribution of  $w$ .

HR ( $x$ )	$70 \leq x < 90$	$90 \leq x < 110$	$110 \leq x < 130$	$130 \leq x < 150$	$150 \leq x < 170$
Freq	5	14	21	$p$	13

- (a) Write down the value of  $p$ . [1 mark]
- (b) Write down the modal class. [2 marks]
- (c) A player is selected at random. Find the probability that the athlete weighs less than 110 kilograms. [2 marks]
- (d) Write down the mid-interval value for the class  $110 \leq x < 130$ . [1 mark]
- (e) Hence find an estimate for the
- mean; [2 marks]
  - standard deviation. [2 marks]

12. The following diagram shows quadrilateral  $ABCD$  (not drawn to scale).



$AB = 16.3$ ,  $BC = 9.5$ ,  $CD = 8.0$ ,  $AD = 18.2$ , and  $\angle BCD = 78^\circ$

(a) Find  $BD$ .

[3 marks]

(b) Find  $\angle ABD$ .

[3 marks]