

18 April 2019

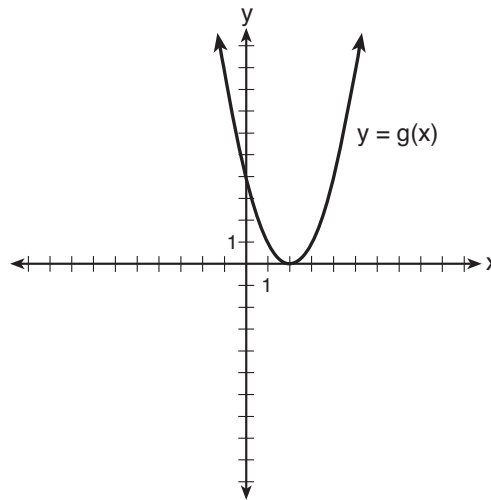
Test: Sequences & series

Name:

1. In an arithmetic sequence, the first term is 7 and the second term is 11.
 - (a) Find the common difference.
 - (b) Find the eighth term.
 - (c) Find the sum of the first eight terms of the sequence.
2. Given that for a geometric sequence $u_1 = 18$ and $u_3 = 8$
 - (a) Find the value of r .
 - (b) Given that u_k is the first term of the sequence with a value less than one, find k .
 - (c) Find the sum of the infinite series S_∞
3. The first three terms of an arithmetic sequence are $u_1 = 5.1$, $u_2 = 5.5$, and $u_3 = 5.9$.
 - (a) Find the common difference.
 - (b) Given that the k th term of the sequence, $u_k = 11.5$. Find k .
4. Let $f(x) = 2x - 3$ and $g(x) = (x - 1)^2$
 - (a) Find $(f \circ g)(4)$
 - (b) Find $f^{-1}(x)$
5. Simplify the expression $\sqrt{a} \cdot \sqrt{a^5}$
6. $(2x^2 - 2x - 5)(x + 3) - 2x(x^2 - x - 4)$
7. What is the inverse of the function $y = \frac{2}{x+3}$?
8. Let $x = \ln 2$ and $y = \ln 5$. Write down the following expressions in terms of x and y .
 - (a) $\ln \frac{2}{5}$
 - (b) $\ln 50$
 - (c) $\ln 0.1$
9. Using the quadratic formula or otherwise, find the solution set to $2x^2 - 3x - 5 = 0$.
10. Simplify the expression $2xi(4 + 3i)$.
11. Simplify the expression $\left(\frac{x^{-2}}{x^2}\right)^{\frac{1}{2}}$ to one with positive integer exponents and radicals.

12. The function g is defined by graph of $y = g(x)$ below.

- (a) Write down the equation for $g(x)$ in factored form.
- (b) The function $h(x)$ is made by reflecting g across the y -axis. What is the equation for $h(x)$?



13. Let $f(x) = x^2 - 6x + 4$

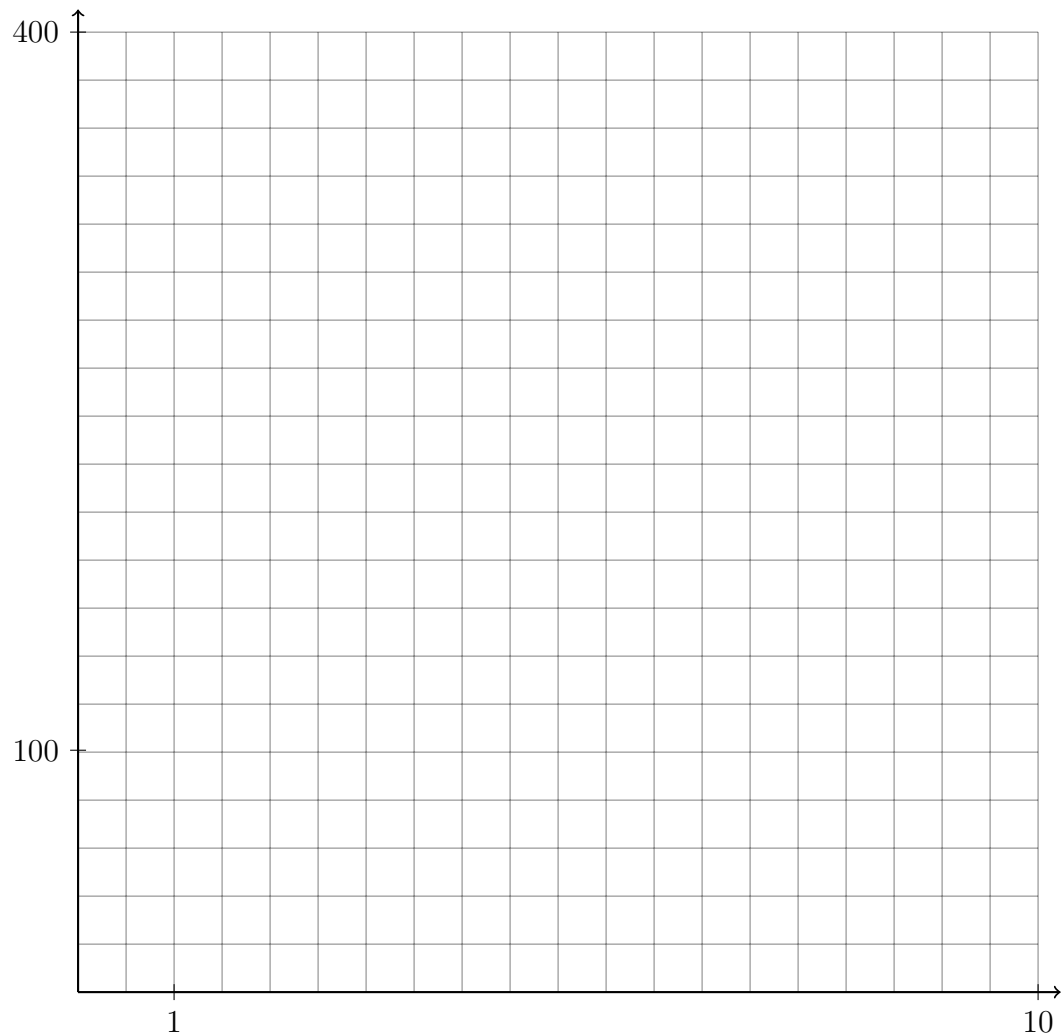
- (a) Rewrite quadratic in vertex form and state the vertex as an ordered pair.
- (b) The parabola is translated vertically by k units to make the function $g(x)$. The equation $g(x) = 0$ has one solution. Find k .

14. Use your knowledge of the binomial expansion and combinatorics to answer the following questions.

- (a) Write down the first 5 rows of Pascal's triangle.
- (b) Find 7C_3 .
- (c) Expand the binomial $(x + 1)^6$.
- (d) What is the coefficient of the x^3 term of the expansion of $(x + 1)^7$?

For these last two pages, answer in the space provided

15. Graph $f(x) = 280 \cdot 0.75^{\frac{x}{2}} + 20$ on the set of axes below.

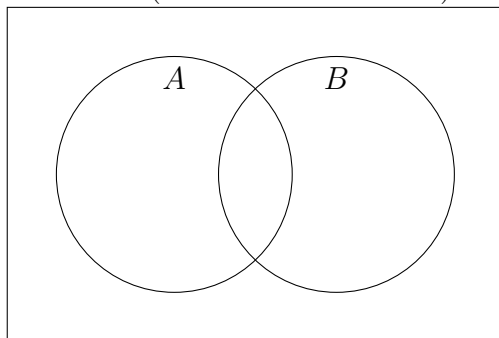


Is the function an example of exponential growth or exponential decay? Justify your answer algebraically.

16. Let A and B be independent events, where $P(A) = 0.4$ and $P(B) = 0.5$.

(a) Find $P(A \cap B)$

(b) Fill in the probability value for each area in the Venn diagram representing the situation. (there are four values)



(c) Find $P(A \cup B)$

(d) Find $P(A \cap B')$

17. The function $f(x) = e^x$ is shown on the graph. Sketch $g(x) = f(x - 2) + 1$. Plot and label the asymptote(s).

