11.17 Quiz: Function transformations

1. The standard form of a linear equation is ax + by = c, where x and y are variables and a, b, and c are parameters (fixed numbers).

The equation of a line is 5x + 3y = -7. Write down the value of each parameter.

(a)
$$a = 5$$

(b)
$$b = 3$$

(c)
$$c = -7$$

2. The slope-intercept form of a linear equation is y = mx + b. The parameter m quantifies the slope and b the y-intercept.

For the equation $y = -\frac{3}{2}x + 4$, write down the value of each parameter...

(a)
$$m = -\frac{3}{2}$$

(b)
$$b = 4$$

3. The point-slope form of a linear equation is y - k = m(x - h). The parameter m represents the slope. The parameters h the h are the coordinates of a point that the line passes through.

For the equation y-2=-9(x+5), write down the value of each parameter..

(a)
$$m = -9$$

(b)
$$h = -5$$

(c)
$$k = 7$$

- (d) Write down a point that the line passes through as a coordinate pair. (-5, 2)
- 4. Rewrite each equation in the specified form.

(a)
$$y = 2x - 5$$
 in the form $ax + by = c$ (b) $y - 2 = \frac{1}{2}(x + 6)$ in the form $y = mx + b$

$$-2x+y=-5 \qquad y=\frac{1}{2}x+5$$

(a) Find the slope m of the line 6x - 2y = 10.

$$y = 3x - 5$$

$$M = 3$$

(b) Write down the slope perpendicular to the line, m_{\perp} .

6. Write down the slope perpendicular to the given slope.

(a)
$$m = -\frac{5}{2}$$
 $m_{\perp} = \frac{2}{5}$

(b)
$$m = -1$$
 $m_{\perp} =$

$$m_{\perp} =$$
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7. Write down the equation of the line through (3, -7) with a slope of 5.

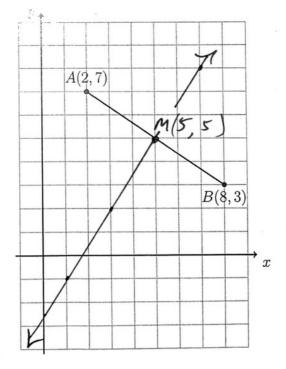
- 8. The line segment \overline{AB} , A(2,7) and B(8,3), is shown below.
 - (a) Mark the midpoint M of \overline{AB} . Label it as an ordered pair.
 - (b) Find the slope of \overline{AB} .

$$M = -\frac{4}{6} = -\frac{2}{3}$$

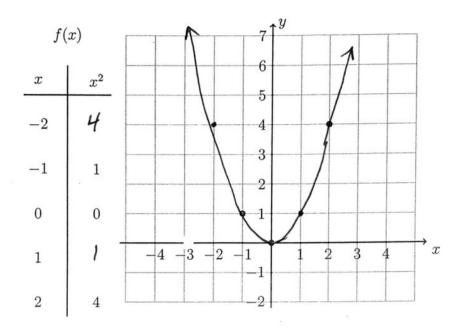
(c) Write down the slope perpendicular to \overline{AB} .

(d) Write down the equation of the perpendicular bisector of \overline{AB} .

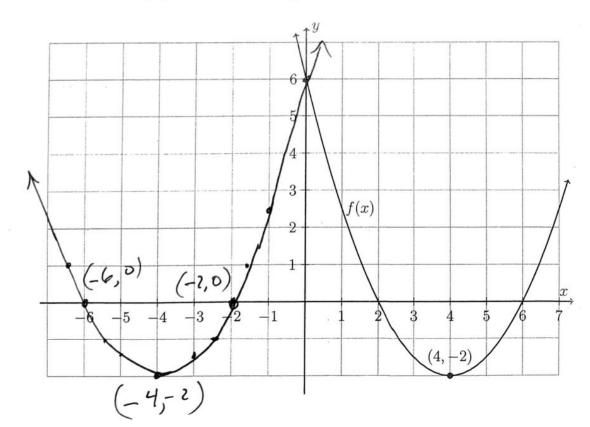
(e) Draw the perpendicular bisector on the graph using a straight edge.



9. Complete the t-table for the parent function f: $y = x^2$, plot the points, and draw f as a smooth curve.



10. The parabola $f(x) = \frac{1}{2}(x-4)^2 - 2$ graphed below. Reflect f across the y-axis. Mark and label the image parabola's x-intercepts and vertex



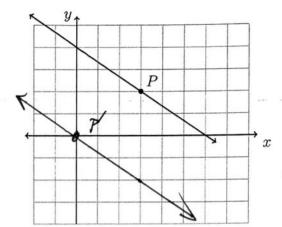
- 11. The line l having the equation $y-2=-\frac{2}{3}(x-3)$ is shown below.
 - (a) Write down coordinates of P.

(3,2)

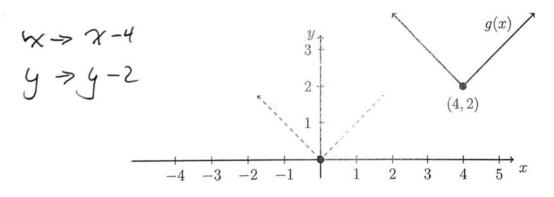
(b) Point P is mapped to the origin by $x \to x - h$ $y \to y - k$

Write down h and k.

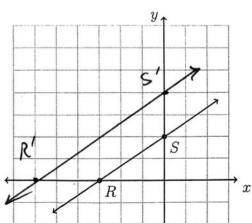
(c) Plot the image of l after the translation.



12. The function g: y = |x-4| + 2 is plotted below as a solid line. What translation would map g onto the parent function (dotted)? State your answer in the form $x \to x - h$, $y \to y - k$.

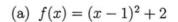


- 13. The line \overrightarrow{RS} having the equation $y = \frac{2}{3}x + 2$ is shown below.
 - (a) Write down the slope of \overrightarrow{RS} , $m = \frac{2}{3}$
 - (b) Write down the y-intercept of \overrightarrow{RS} , $b = \sum_{i=1}^{n} a_i b_i$
 - (c) Dilate \overrightarrow{RS} by a scale factor k=2 centered at the origin. Mark the images R' and S'.
 - (d) Write down the equation of $\overrightarrow{R'S'}$



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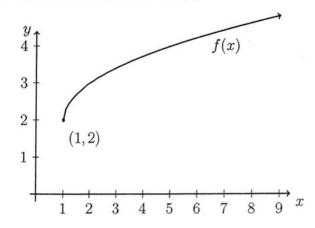
14. The function f is plotted below for $x \geq 1$. Identify the equation of f(x).



(b)
$$f(x) = |x - 1| + 2$$

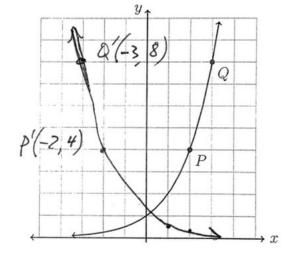
(c)
$$f(x) = \sqrt{x-1} + 2$$

(d)
$$f(x) = \sin(x-1) + 2$$



- 15. Part of the exponential function $f: y = 2^x$, is shown below.
 - (a) Reflect f across the x-axis.
 - (b) Write down the coordinates of P and

(c) Mark and label the images P' and Q' with their coordinates.



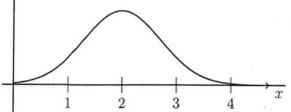
- 16. The function f is plotted below for $x \geq 0$. Identify the function represented by the graph.
 - (a) Reciprocal function $y = \frac{1}{x-2}$



(b) Principal square root $f(x) = \sqrt{x-2}$



(c) Quadratic function $y = (x-2)^2$



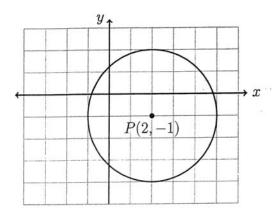
(d) Normal distribution $N(\mu, \sigma)$

17. The circle with center P shown below can be represented by an equation of the form $(x-h)^2 + (y-k)^2 = r^2$. Write down the values of the parameters.



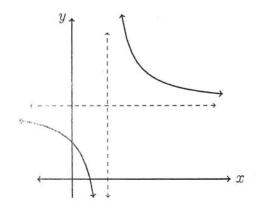
(b)
$$h = 2$$

(c)
$$k = -$$



- 18. The reciprocal function shown below has the equation $f(x) = \frac{1}{x-1} 2$. Its asymptotes are plotted as dashed lines.
 - (a) Write down the equation of the horizontal asymptote.

(b) Write down the equation of the vertical asymptote.



19. The sine function shown below has the form $f(x) = a \sin x + d$, where the coefficient a is the vertical stretch factor and the parameter d is the vertical translation. f passes through the points $(90^{\circ}, 3)$ and $(270^{\circ}, -1)$.

Write down the parameter values:

(a)
$$a = 2$$

(b)
$$d = \int_{-\infty}^{\infty} dt$$

