BECA / Huson / Precalculus: 3. Complex numbers First and last name: 11 December 2024 Section:

## 3.18 PreTest: Rational exponents and complex numbers

**A2.A.APR.6** 

#### A2-APR.1 Perform operations with polynomials

1. Find the sum in standard form:

$$(2x^2 - 3x - 5) + (x^2 - 6x + 9).$$

2. Find the difference f(x) - g(x) as a polynomial in standard form, given:

$$f(x) = 4x^4 - x^3 + 6x^2 - 2x + 3$$
 and  $g(x) = x^4 + 3x^2 - 2x - 4$ .

3. Select each correct equation.

(a) 
$$x^2 - 16 = x^2 - 4^2$$

(d) 
$$x^2 - 8x + 16 = (x - 4)^2$$

(b) 
$$x^2 - 16 = (x - 4)(x + 4)$$

(e) 
$$x^2 + 8x + 16 = (x+4)^2$$

(c) 
$$x^2 + 16 = (x - 4)(x + 4)$$

(f) 
$$x^2 - 8x - 16 = (x - 4)^2$$

4. Which equations represent correct polynomial identities?

(a) 
$$x^3 + y^3 = (x+y)^3$$

(c) 
$$x^3 - y^3 = (x+y)(x^2 - xy + y^2)$$

(b) 
$$x^3 + y^3 = (x - y)(x^2 + xy + y^2)$$
 (d)  $x^3 - y^3 = (x - y)(x^2 + xy + y^2)$ 

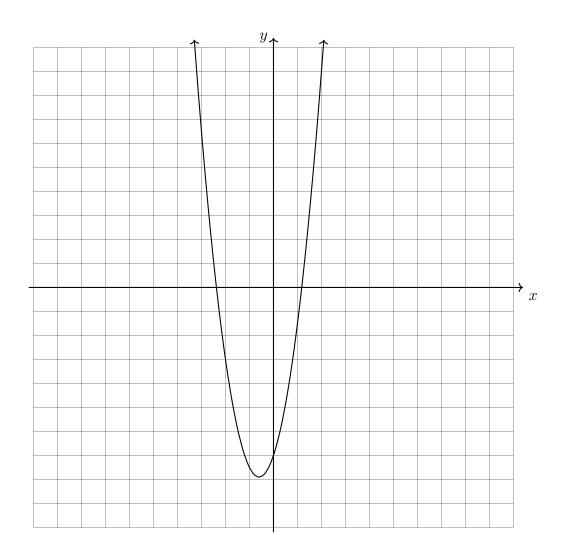
(d) 
$$x^3 - y^3 = (x - y)(x^2 + xy + y^2)$$

### A2-F.IF.7a Graph linear and quadratic functions, show key features

- 5. One equation of a system is graphed.
  - (a) Graph the second equation, labeling the intersections as ordered pairs.
  - (b) Find the value of the leading coefficient a of the quadratic equation.

$$y = ax^2 + 3x - 7$$

$$3x - y = -3$$



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#### A2-A.APR.3 Identify zeros of polynomials given suitable factorizations

- 6. Write down the solutions to the equation x(x-1)(2x+5)(x+4)=0.
- 7. The polynomial p is a function of x. The graph of p has three zeros at -5,  $\frac{3}{2}$ , and -1. Select all the expressions that could represent p.

(a) 
$$(x-5)(x-\frac{3}{2})(x+1)$$

(e) 
$$(x-5)(x+\frac{2}{3})(x-1)$$

(b) 
$$(x+5)(3x-2)(x+1)$$

(f) 
$$(x+5)(2x-3)(x+1)$$

(c) 
$$3(x+5)(x-\frac{3}{2})(x+1)$$

(g) 
$$3(x-5)(x-\frac{2}{3})(x-1)$$

(d) 
$$3x(x+5)(x+\frac{2}{3})(x-1)^2$$

(h) 
$$3x(x+5)(x-\frac{3}{2})(x+1)^2$$

8. Select the expression that is equivalent to  $\frac{3x^2 + 10x - 8}{x - 2}$  for  $x \neq 2$ .

(a) 
$$3x + 4 - \frac{16}{x - 2}$$

(b) 
$$3x + 6 - \frac{10}{x - 2}$$

(c) 
$$3x + 4 - \frac{8}{x-2}$$

(d) 
$$3x + 6 - \frac{14}{x - 2}$$

#### A2-F.BF.2 Write arithmetic and geometric sequences with recursive formulas

- 9. Write a recursive definition of the sequence  $a_1=-3,\ a_2=2,\ a_3=7,\ a_4=12,\ldots$
- 10. Write a recursive definition of the arithmetic sequence b.

n	$b_n$
1	12
2	1.2
3	0.12

#### A2-F.IF.7c Graph polynomials, identify zeros, end behavior

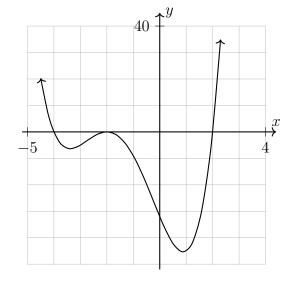
- 11. Below is a graph of the polynomial f(x).
  - (a) Is the leading coefficient positive or negative?
  - (b) Which of the following could be its equation?

i. 
$$f(x) = (x+2)(x-4)(x-2)^2$$

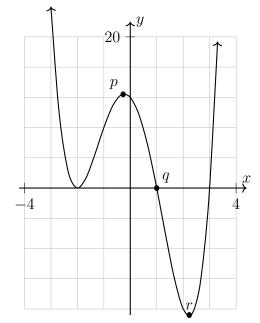
ii. 
$$f(x) = (x-2)(x-4)(x+2)^2$$

iii. 
$$f(x) = (x+2)(x+4)(x-2)^2$$

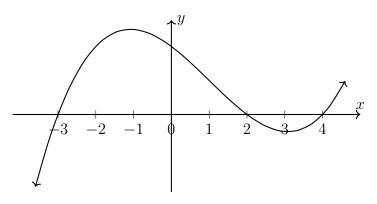
iv. 
$$f(x) = (x-2)(x+4)(x+2)^2$$



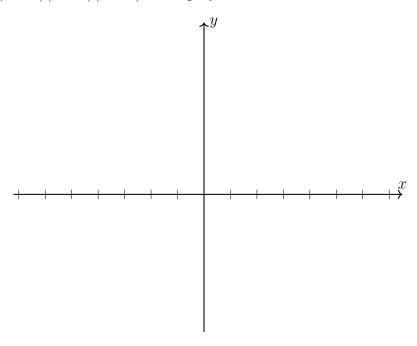
- 12. The graph of the polynomial  $f(x) = x^4 9x^2 4x + 12$  is shown.
  - (a) What is the degree of the function?
  - (b) What are the zeros of the function?
  - (c) Which factor has a multiplicity of 2?
  - (d) Write down the y-intercept as an ordered pair.
  - (e) Three points are marked on the graph, p, q, and r. Which one is a local minimum?



13. The graph of the function  $f(x) = x^3 - 3x^2 - 10x + 24$  is shown. Write the function in factored form.



14. Let  $j(x) = (x+4)(x+1)(x-4)^2$  be a polynomial function.



- (a) Sketch a graph of the function. Label the x-intercepts.
- (b) Find the value of the y-intercept and mark it on the graph.
- (c) Identify the end behavior of the function.

i. As 
$$x \to +\infty$$
,  $y \to +\infty$ ;  
as  $x \to -\infty$ ,  $y \to -\infty$ 

iii. As 
$$x \to +\infty$$
,  $y \to +\infty$ ; as  $x \to -\infty$ ,  $y \to +\infty$ 

ii. As 
$$x \to +\infty$$
,  $y \to -\infty$ ; as  $x \to -\infty$ ,  $y \to +\infty$ 

iv. As 
$$x \to +\infty$$
,  $y \to -\infty$ ;  
as  $x \to -\infty$ ,  $y \to -\infty$ 

#### HSN.RN.2 Expressions with radicals and rational exponents

- 15. Simplify each radical expression.
  - (a)  $\sqrt{49} =$

(c)  $\sqrt{-45} =$ 

(b)  $\sqrt{32} =$ 

(d)  $\frac{\sqrt{-12}}{\sqrt{3}} =$ 

- 16. Simplify each expression.
  - (a)  $8^{\frac{2}{3}} =$

(b)  $\left(\sqrt{\frac{4}{9}}\right)^3 =$ 

- 17. Rewrite each expression as a fractional exponent in simplest terms.
  - (a)  $\sqrt[3]{3} =$

(c)  $\sqrt[4]{x^3} =$ 

(b)  $\frac{1}{\sqrt[2]{3}} =$ 

- (d)  $\frac{1}{(\sqrt[4]{x})^2} =$
- 18. Rewrite each expression with fractional exponent as a radical.
  - (a)  $3^{\frac{1}{2}} =$

(c)  $x^{\frac{1}{3}} =$ 

(b)  $3^{-\frac{2}{3}} =$ 

(d)  $x^{-\frac{2}{3}} =$ 

# A2-A.SSE.3c Apply the properties of exponents

19. Identify the expressions that are equal to  $\frac{3^3}{3^5}$ 



20. Identify the expressions that are equal to  $5^{-2}$ 

(a)	$\frac{1}{5^2}$	(d)	$\frac{1}{25}$
(b)	5.5	(e)	0.04
(c)	$\sqrt{5}$	(f)	10

21. Identify the expressions that are equal to  $16^{\frac{1}{4}}$ 

(a) 2	(d) $\sqrt[4]{16}$
(b) 4	(e) 16.25
(c) $\sqrt{4}$	(f) 256

### 6.EE.b Reason about and solve one-variable equations and inequalities

- 22. Use the function  $f(x) = \frac{1}{2}x + 11$  to answer the questions.
  - (a) Find the value of f(4).

(b) Solve for x if f(x) = 2.

23. Solve each equation for x.

(a) 
$$x^2 + 5x + 6 = 0$$

(b) 
$$x^3 - 7x^2 + 6x = 0$$

24. The expression  $2 - \frac{x-1}{x+2}$  is equivalent to

(a) 
$$1 - \frac{3}{x+2}$$

(c) 
$$1 - \frac{1}{x+2}$$

(b) 
$$1 + \frac{3}{x+2}$$

(d) 
$$1 + \frac{1}{x+2}$$

25. Find all of the values of x that make the equation true.

$$\frac{3}{x-4} = \frac{x-5}{x}$$

- 26. Given the rational function  $r(x) = 3 \frac{x-1}{x+2}$ .
  - (a) Sketch a graph of the function.
  - (b) Mark the vertical asymptote as dotted line and label it with its equation.
  - (c) Explain why the asymptote is located there.

