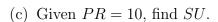
7.12 Similarity transformations

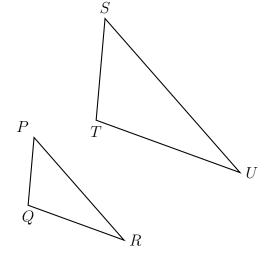
 ${\bf CCSS.HSG.SRT.B.5}$

1. A dilation maps triangle PQR onto triangle STU with QR=7 and TU=14.

(a) $\overline{PR} \rightarrow \underline{\hspace{1cm}}$

(b) What scale factor maps $\triangle PQR \rightarrow \triangle STU$?

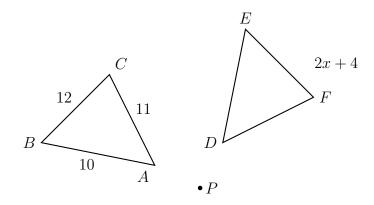




(d) Given
$$ST = 6$$
, find PQ .

2. After a dilation with center (0,0), the image of \overline{MN} is $\overline{M'N'}$. If MN=7.2 and M'N'=36, find the scale factor of this dilation.

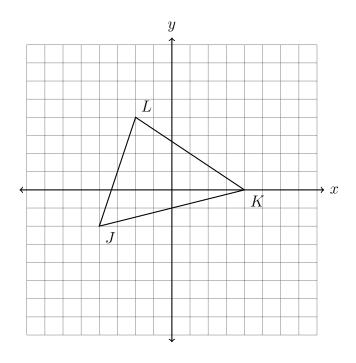
3. In the diagram below, $\triangle ABC$ with sides of 10, 12, and 11, is mapped onto $\triangle DEF$ after a clockwise rotation of 90° about point P.



If EF = 2x + 4, what is the value of x?

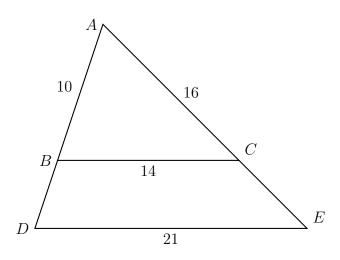
4. The vertices of $\triangle JKL$ have the coordinates $J(-4,-2),\ K(4,0),\ {\rm and}\ L(-2,4),\ {\rm as}$ shown.

Apply a dilation to $\triangle JKL \to \triangle J'K'L'$, centered on the origin and with a scale factor k=1.5. Draw the image $\triangle J'K'L'$ on the set of axes below, labeling the vertices, and make a table showing the correspondence of both triangles' coordinate pairs.

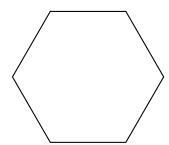


5. Triangle ABC is dilated with a scale factor of k centered at A, yielding $\triangle ADE$, as shown. Given AB = 10, BC = 14, AC = 16, and DE = 21.

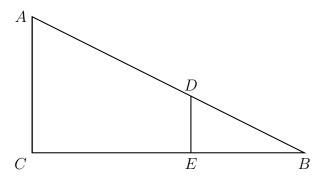
Find BD, AE, and k (the scale factor).



- 6. Circle YES or NO to indicate whether the given transformation maps the hexagon onto itself.
 - (a) Yes No A rotation of 120° counterclockwise around point D.
 - (b) Yes No A reflection over \overrightarrow{AE}
 - (c) Yes No A reflection over a line through the midpoints of \overline{BC} and \overline{EF} .
 - (d) Yes No A rotation of 60° clockwise around the hexagon's center.

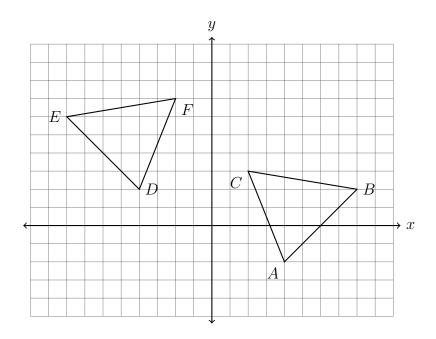


7. In right triangle ABC shown below, point D is on \overline{AB} and point E is on \overline{BC} such that $\overline{AC} \parallel \overline{DE}$



If AB = 20, BC = 15, and AD = 12, what is the length of \overline{BE} ?

8. What series of transformations map $\triangle ABC$ onto $\triangle DEF$, shown below? Fully specify the transformations.



9. What is the length of the segment A(-2,1), B(3,13)?

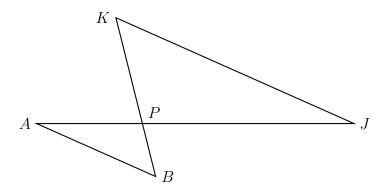
- 10. What is the equation of a line through the point A(5,-1) and parallel to the line $y=\frac{2}{3}x-2$? (hint: use the point-slope formula, $y-y_A=m(x-x_A)$)
- 11. The line l has the equation $y = -\frac{3}{5}x + 4$. To each line below, circle whether l is parallel, perpendicular, or neither.
 - (a) parallel perpendicular neither $y = \frac{3}{5}x 2$
 - (b) parallel perpendicular neither $y = \frac{5}{3}x + 9$
 - (c) parallel perpendicular neither 3x 5y = -15
 - (d) parallel perpendicular neither 5x 3y = 6
- 12. Simplify each expression. (Leave it in radical form if necessary, not a decimal.)
 - (a) $\sqrt{20}$

(c) $\sqrt{300}$

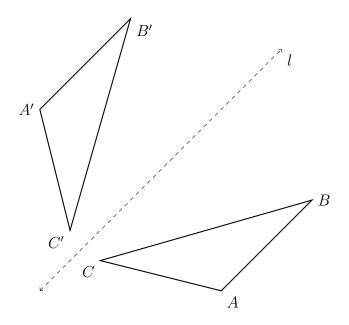
(b) $\sqrt{75}$

(d) $\sqrt{\frac{36}{49}}$

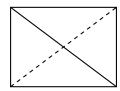
13. Given $\triangle ABP$ and $\triangle JKP$ as shown below. $\overline{AB} \parallel \overline{JK}$. $AP=5,\ JP=12,$ and JK=18. Find AB.



14. The $\triangle ABC$ is reflected across l to yield $\triangle A'B'C'$. AB = 3x + 4, A'B' = 5x - 10, and BC = 4x + 12. Find the length B'C'.



15. The figure shows a rectangle (not a square).



Which transformations carries the rectangle onto itself? Mark each True or False.

(a) A reflection over the solid diagonal

True False

(b) A reflection over the dashed diagonal

True False

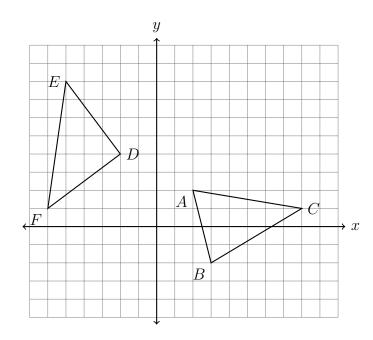
(c) A clockwise rotation of 90° about the intersection of the diagonals True

True False

(d) A clockwise rotation of 180° about the intersection of the diagonals True

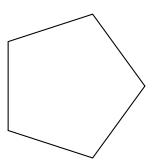
False

16. The grid shows $\triangle ABC$ and $\triangle DEF$.



Let $\triangle A'B'C'$ be the image of $\triangle ABC$ after a rotation about point A. Determine and state the location of B' if the location of point C' is (3,8). Explain your answer, supported by stating the transformation applied.

17. What is the smallest non-zero angle of rotation about its center that would map the pentagon onto itself?

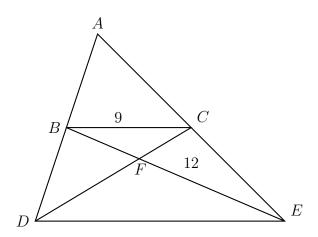


18. Triangle ADE and its midline \overline{BC} are drawn, with B the midpoint of \overline{AD} and C the midpoint of \overline{AE} . The two medians \overline{BE} and \overline{CD} are drawn, as shown, intersecting in point F, the centroid.

 $\triangle FCB \sim \triangle FDE$ with scale factor k=2.

Given BC = 9, find DE.

Given FE = 12, find BF.

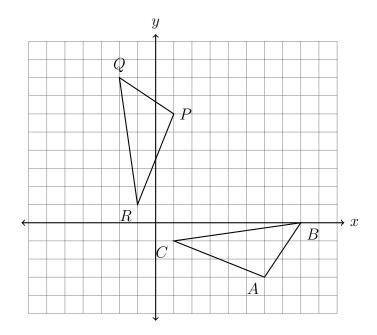


19. Write down the center and radius of each circle.

(a)
$$(x+1)^2 + (y-1)^2 = 16$$

(b)
$$(x-2)^2 + (y-7)^2 = 25$$

20. Determine and state the transformation or sequence of transformations applied to $\triangle ABC$, mapping it onto $\triangle PQR$, as shown.



21. The diagram below shows $\triangle ABC$, with \overline{AEB} , \overline{ADC} , and $\angle ACB \cong \angle AED$. AB = 14, AD = 8, and DE = 4.

(a) $AE \rightarrow \underline{\hspace{1cm}}$	(a)	$\overline{AE} \rightarrow$	
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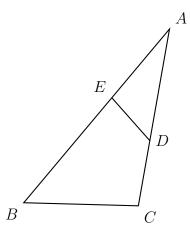
(b)
$$\overline{AD} \rightarrow \underline{\hspace{1cm}}$$

(c)
$$\triangle ADE \sim$$

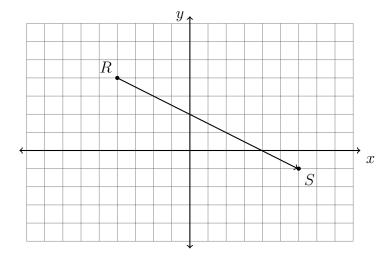
(d) What is the scale factor?

$$k = \underline{\hspace{1cm}}$$

(e) What is the length of \overline{BC} ?



- 22. Given $\triangle JKL \sim \triangle MNO$. $m\angle J=43^\circ$ and $m\angle L=92^\circ$. Find the measure of $\angle N$.
- 23. A translation maps $A(3,5) \to A'(-2,7)$. What is the image of B(-4,1) under the same translation?
- 24. As shown below, what is the translation that maps the point R(-4,4) onto the point S(6,-1)?



If two fifths of that translation was performed, what coordinates would R be mapped to?

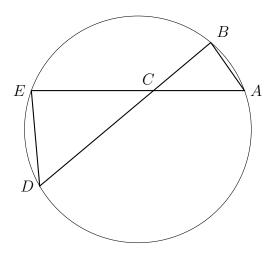
25. Given A(-3,5) and B(0,-1), find the length of \overline{AB} . Leave the result in simplified radical form (not a decimal).

Name:

11

Early finishers

26. In the diagram below, the chords \overline{AE} and \overline{BD} intersect at C, with $\triangle ABC \sim \triangle DEC$, BC=3, AC=4, and AE=11. Determine the length of \overline{CD} .



27. In the diagram below, $\triangle ABC \sim \triangle DEF$, DE=6, AB=x, AC=2x, and DF=2x+4. Determine the length of \overline{AB} .

