

3.18 PreQuiz: Solving quadratics, complex numbers, radicals and exponents

Do Not Use a Calculator

A2.REI.4 Solve quadratic equations

1. Solve by factoring.

$$\begin{aligned}x^2 - 5x + 6 &= 0 \\(x-2)(x-3) &= 0 \\x &= 2, 3\end{aligned}$$

2. Solve by completing the square.

$$\begin{aligned}x^2 + 10x + 20 &= 0 \\x^2 + 10x + 25 &= 5 \\(x+5)^2 &= 5 \\x+5 &= \pm\sqrt{5} \\x &= -5 \pm \sqrt{5}\end{aligned}$$

$\frac{10}{2} = 5$
 $5^2 = 25$

3. Solve by using the quadratic formula.

$$\begin{aligned}2x^2 - 5x + 7 &= 0 \\x &= \frac{-(-5) \pm \sqrt{(-5)^2 - 4(2)(7)}}{2(2)} \\&= \frac{5 \pm \sqrt{25 - 56}}{4} \\&= \frac{5 \pm \sqrt{31}}{4}\end{aligned}$$

$$4 \pm \sqrt{7}$$

4. Select all of the solutions to $(x - 4)^2 = 7$. (HSN.CN.A Complex numbers)

(a) $x = 4 + 7i$

(d) $x = 4 - 7 = -3$

(b) $x = 4 - 7i$

(e) $x = 4 + 7 = 11$

(c) $x = 4 - \sqrt{7}$

(f) $x = 4 + \sqrt{7}$

5. Write each expression in the form $a + bi$ with a, b real numbers.

Given $s = -4 - i$ and $t = 5 + 3i$.

(a) $s + t = (-4 + 5) + (-1i + 3i)$
 $= 1 + 2i$

(b) $s - t = (-4 - i) - (5 + 3i)$
 $= -9 - 4i$

(c) $st = (-4 - i)(5 + 3i)$
 $= -20 - 12i - 5i - 3i^2$
 $= -17 - 17i$

6. Simplify each expression.

(HSN.RN.A Rational exponents)

(a) $27^{\frac{2}{3}} = 9$

(b) $(\sqrt{\frac{1}{4}})^{-3} = 8$

7. Simplify each radical expression.

(a) $\sqrt{81} = 9$

(c) $\sqrt{-50} = i\sqrt{25}\sqrt{2} = 5i\sqrt{2}$

(b) $\sqrt{18} = \sqrt{9}\sqrt{2}$
 $= 3\sqrt{2}$

(d) $\frac{\sqrt{-8}}{\sqrt{2}} = \frac{i\sqrt{4}\sqrt{2}}{\sqrt{2}} = 2i$