

Prep #24 Exponential regression

Casio instructions: <https://www.youtube.com/watch?v=jcX93Grn8o8>

Menu > Stat > enter data in List 1 and List 2

> Calc (F2) > REG (F3) > (F6) > EXP (F2) > ab^X (F2)

1. Consider the data in the table below.

x	1	2	3	4	5	6
y	3.9	6	11	18.1	28	40.3

State an exponential regression equation to model these data, rounding all values to the *nearest thousandth*.

2. A cup of coffee is left out on a countertop to cool. The table below represents the temperature, $F(t)$, in degrees Fahrenheit, of the coffee after it is left out for t minutes.

t	0	5	10	15	20	25
$F(t)$	180	144	120	104	93.3	86.2

Based on these data, write an exponential regression equation, $F(t)$, to model the temperature of the coffee. Round all values to the *nearest thousandth*.

3. Kelly-Ann has \$20,000 to invest. She puts half of the money into an account that grows at an annual rate of 0.9%. At the same time, she puts the other half of the money into an account that grows continuously at an annual rate of 0.8%. Write an equation that represents the value of Kelly-Ann's investments after t years.

4. An investment of \$5000 grows at an annual rate of 3.5% compounded monthly.

$$P(t) = 5000\left(1 + \frac{0.035}{12}\right)^{12t}$$

- (a) Find the investment value after 10 years.

- (b) Determine the time for the investment value to double, to the *nearest month*.

5. The table below gives air pressures in kPa at selected altitudes above sea level measured in kilometers.

x	Altitude (km)	0	1	2	3	4	5
y	Air Pressure (kPa)	101	90	79	70	62	54

Write an exponential regression equation that models these data rounding all values to the *nearest thousandth*.

Use this equation to algebraically determine the altitude, to the *nearest hundredth* of a kilometer, when the air pressure is 29 kPa.

6. Expand and simplify each complex expression.

(a) $6xi^3(-4xi + 5)$

(b) $(x + 3i)^2 - (2x - 3i)^2$

7. Solve each equation. Express the answer in $a + bi$ form.

(a) $2x^2 + 5x + 8 = 0$

(b) $5x^2 - 2x + 13 = 9$

8. Find the solution set of each equation (round to the *nearest tenth*).

(a) $\frac{2}{3x+1} = \frac{1}{x} - \frac{6x}{3x+1}$

(b) $\frac{1}{1-x^2} = -|3x-2| + 5$

9. Over the set of integers, factor completely $x^4 - 5x^2 + 4$.

10. Determine which expressions are equivalent to $\frac{x^4 - 5x^2 + 4x + 14}{x + 2}$.

(hint: substitute $x = 0$ and $x = 1$)

(a) $x^3 - 2x^2 - x + 6 + \frac{2}{x + 2}$

(c) $x^3 + 2x^2 - x + 2 + \frac{18}{x + 2}$

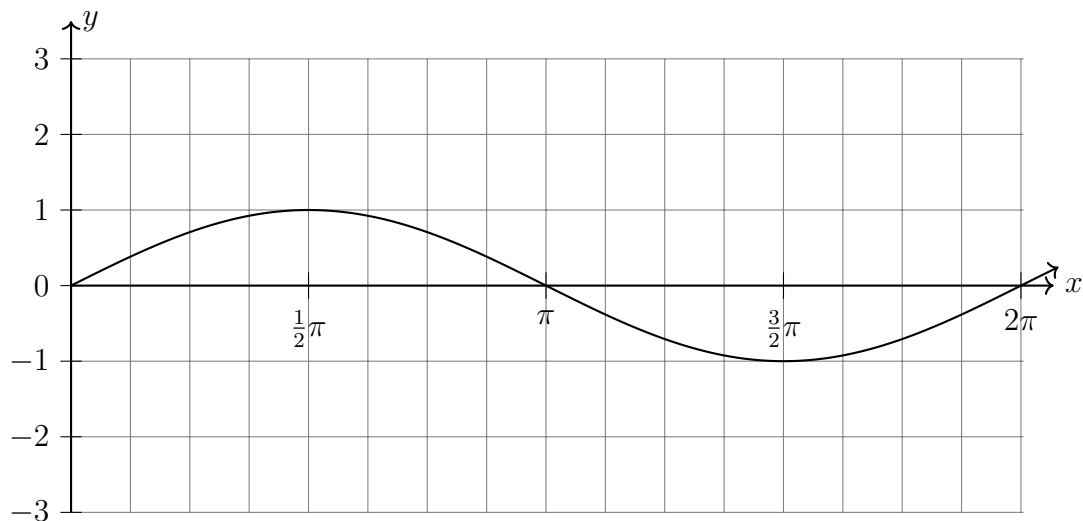
(b) $x^3 - 5x + 4 - \frac{14}{x + 2}$

(d) $x^3 + 2x^2 - 9x + 22 - \frac{30}{x + 2}$

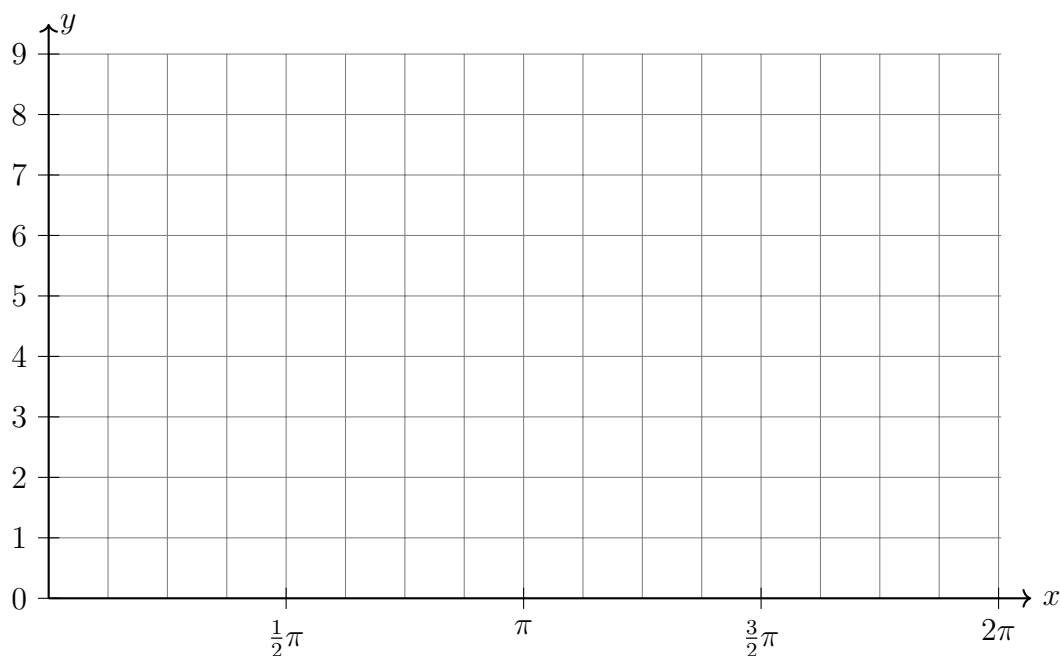
11. Given $a > 0$, solve the equation $a^{x+1} = \sqrt[3]{a^2}$ for x algebraically.

Prep #24 Periodic functions

12. The function $f(x) = \sin x$ is shown on the graph below.

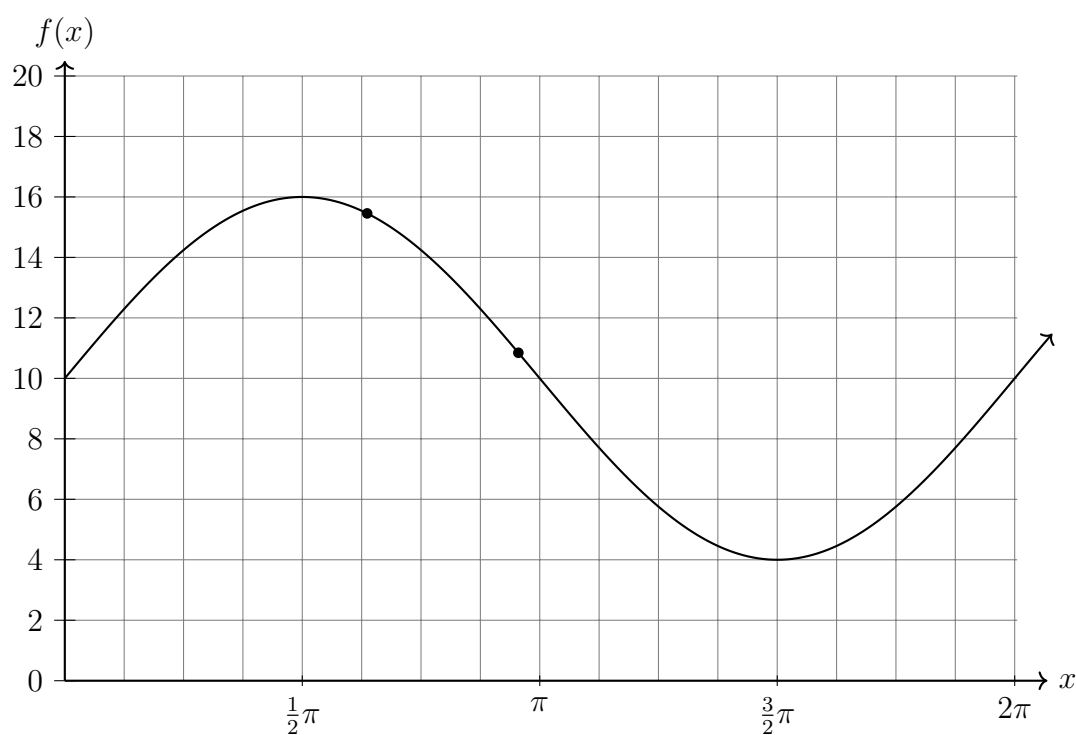


- (a) A second periodic function $g(x)$ has an amplitude of 2. Graph $g(x) = 2 \sin x$ on the same set of axes as $f(x)$.
- (b) Find $g(\frac{3}{4}\pi)$ as an exact value. Mark the point on the graph and label it as an ordered pair.
13. Graph the function $f(x) = 3 \sin x + 5$. Draw and label the midline of f , $y = 5$.



14. A periodic function $f(x)$ is shown on the graph below.

- (a) Draw and label as an equation the midline of f .
- (b) Mark the maximum and minimum points of f over the graphed domain, and label them as ordered pairs.
- (c) Write down an equation for the function in the form $f(x) = A \sin x + D$.



- (d) Find the average rate of change of $f(x)$ over the interval $2 < x < 3$ rounded to the nearest hundredth.