BECA / Huson / Precalculus: 3. Complex numbers First and last name: 16 January 2025 Section:

4.9 Test: Cumulative year-to-date standards

A1-APR.1 Perform operations with polynomials

1. Find the difference f(x) - g(x) as a polynomial in standard form, given:

$$f(x) = x^4 - 3x^3 - 3x^2 - 2x + 5$$
 and $g(x) = 2x^4 - x^3 + 2x + 5$.

2. Select each correct equation.

(a)
$$x^2 + 14 = x^2 + 7^2$$

(e)
$$x^2 - 14x + 49 = (x+7)^2$$

(b)
$$x^2 + 49 = (x - 7)(x + 7)$$

(f)
$$x^2 - 14x + 49 = (x - 7)^2$$

(c)
$$x^2 - 49 = (x - 7)(x + 7)$$

(g)
$$x^3 + y^3 = (x+y)(x^2 - xy + y^2)$$

(d)
$$x^2 + 14x + 49 = (x - 7)^2$$

(h)
$$x^3 + y^3 = (x - y)(x^2 - xy + y^2)$$

A2-A.APR.3 Identify zeros of polynomials given suitable factorizations

3. Write down the solutions to the equation (x-7)(4x+3)(x-2)=0.

A2-A.REI.2 Solve rational and radical equations, identify extraneous solutions

4. Square both sides of the equation and solve for x.

(a)
$$\sqrt{x+9} = 4$$

(b) Check your solution.

5. Solve for x and check.

(a)
$$\sqrt{5x+16}+5=14$$

(b) Check your solution.

6. Solve for x. $\frac{8}{x+3} = \frac{x+1}{x}$

A2-F.BF.2 Write arithmetic and geometric sequences with recursive formulas

- 7. Write a recursive definition of the sequence $a_1=0.25,\,a_2=0.75,\,a_3=1.25,\,a_4=1.75,\dots$
- 8. Write a recursive definition of the geometric sequence b.

n	b_n
1	-1
2	5
3	-25

A2.N.CN.2 Apply the properties of complex numbers

9. Write each expression in the form a + bi with a, b real numbers.

Given s = 2 - 5i and t = 9 - 3i.

- (a) s + t =
- (b) s t =
- (c) st =

10. Simplify each expression, using complex numbers as necessary.

(a)
$$\sqrt{-49} =$$

(b)
$$\frac{1}{2}\sqrt{-12} =$$

11. Does the equation $x^2 + 3x + 7 = 0$ have real or imaginary solutions? Justify your answer.

A2.HSN.RN.2 Expressions with radicals and rational exponents

- 12. Simplify each radical expression, using complex numbers as necessary.
 - (a) $\sqrt{64} =$

(c) $\sqrt{-9} =$

(b) $\sqrt{27} =$

(d) $\frac{\sqrt{-50}}{\sqrt{2}} =$

- 13. Simplify each expression.
 - (a) $125^{\frac{2}{3}} =$

(b) $\left(\sqrt[3]{\frac{8}{27}}\right)^2 =$

- 14. Rewrite each expression as a fractional exponent in simplest terms. x > 0
 - (a) $\sqrt[3]{7} =$

(c) $\sqrt[2]{x^4} =$

(b)
$$\frac{1}{\sqrt[3]{5}} =$$

(d)
$$\frac{1}{(\sqrt[3]{x})^2} =$$

- 15. Rewrite each expression with fractional exponent as a radical.
 - (a) $5^{\frac{1}{4}} =$

(c) $x^{\frac{2}{5}} =$

(b) $5^{-\frac{1}{3}} =$

(d) $x^{-\frac{1}{3}} =$