Mathematics Class Slides Bronx Early College Academy

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13-22 September 2021

- BECA / Dr. Huson / Geometry Unit 1
- 1.1 1st day of Geometry, Segment addition, 13-14 Sept
- 1.3 Segment addition, midpoint, 17 Sept
- 1.4 Number line situations, 20 Sept
- 1.5 Midpoint calculations; Isosceles triangles, 21 Sept
- 1.6 Angles and their measures, 22 September
- 1.7 Angles and their measures, 23 September
- 1.8 Angles addition problems, 24 September
- 1.9 Angles addition problems, 27 September
- 1.10 Angles addition problems, 28 September
- 414 Seating chart 10.1 420 Seating chart 10.3

Learning Target: I can measure and diagram my world

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.1 Tuesday 13-14 Sept

Welcome back to school

Do Now: Measurement

- 1. Notebook first page: Name / Course / Instructor
- 2. Diagram people closest to you and their distance
- 3. Early finishers: Calculate diagonal distances

Supply list: Composition book, looseleaf, pencils & pens, compass and ruler, calculator; Optional: folder

Lesson: Points, line segments, length; Segment addition postulate

Homework: Diagram your bedroom (with measurements), or another room

Take class notes in a composition book

Use this notebook format (required)

- 1. In the front, write your name, my contact info, your passwords
- 2. Each page in the top left corner:

First+Last Name

14 September 2021

Learning Target: I can measure and diagram my world

- 3. Copy definitions using your own words
- 4. Write down example diagrams and problems

Point: a location, a dot, has no size; label with capital letter, P

Line segment: two points and all the points between them; label with *end points* and a bar, \overline{AB}

Example: Points and line segments

Shown points P, A, B, C, line segments \overline{AB} , \overline{BC}



Given AB = 3, BC = 4.

Notation: the length of a line segment is written as the two end points without a bar over them, AB.

Example: Points and line segments

Segment Addition Postulate

Shown collinear points A, B, C. Given AB = 3, BC = 4.

Find *AC*.



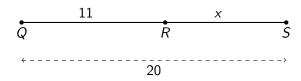
Definition: Points are collinear when they lie on a straight line.

Example 2: Points and line segments

Segment Addition Postulate

Given collinear points Q, R, S, with QR = 11, QS = 20.

Find RS.



- 1. How would you check your answer?
- 2. Which equation represents the situation?

$$11 + x = 20$$

$$x = 20 - 11$$

Example 3: Segment addition postulate

Given \overline{JKL} , JK = 2x + 3, KL = 5, JL = 12. Find x.



1. Write down an equation to represent the situation.

2. Solve for *x*.

3. Check your answer.

Example 4 (challenge): Segment addition postulate

Given
$$\overline{ABC}$$
, $AB = 3x - 7$, $BC = x + 5$, $AC = 14$. Find AB .

Learning Target: I can solve for segment lengths

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.3 Friday 17 Sept

Do Now: Given collinear points A, B, C, with AB = 7, AC = 13.

$$7 + x = 13$$
 $x = 13 - 7$

2. Find BC.

Classwork: Handout (pre-quiz for 6th period)

Lesson: Point, line segment, end point, collinear, distance or length; line, ray, plane, coplanar, *congruent* line segments Midpoints, bisectors, practice segment addition situations

1. Which equation most simply represents the situation?

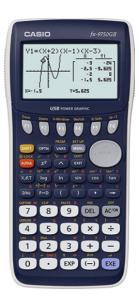
Casio fx-9750GII calculator - due Friday 1 October

In the high school at BECA we use the Casio fx-9750GII.

It is allowed on the Regents exams, SAT tests, and International Baccalaureate exams.

You may use a different calculator in Geometry if you prefer, but I recommend buying the Casio fx-9750GII.

(see me if buying a calculator is a hardship for your family)



Review: points, segments, length

Give an example of each geometric object. Use proper notation.

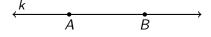
- 1. point
- 2. line segment
- 3. end point
- 4. three collinear points



5. Given TQ = 1.4, QU = 0.6. Find TU.

More definitions: lines, rays, planes

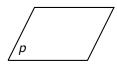
A *line* extends infinitely in both directions, \overrightarrow{AB} . (sometimes labeled with a small letter, for example, line k)



A ray has one end point and extends infinitely in one direction, \overrightarrow{CD} .

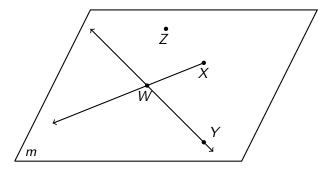
$$C$$
 D

A *plane* is flat and extends infinitely in two directions, *p*.



Several objects are shown in a plane

- 1. T F The name of the plane is m
- 2. T F The line \overrightarrow{WY} is in the plane
- 3. T F The ray \overrightarrow{WX} is shown in the plane
 - 4. T F Points W, X, and Z are collinear

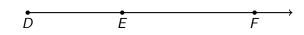


Solve for length using the Segment Addition postulate

Given
$$\overrightarrow{DEF}$$
, $DE = x + 1$, $EF = 9$, $DF = 3x$. Find DE .

Solve for length using the Segment Addition postulate

Given \overrightarrow{DEF} , DE = x + 1, EF = 9, DF = 3x. Find DE.



- 1. Sketch and label the situation
- 2. Write a geometric equation
- 3. Substitute algebraic values
- 4. Solve for x
- 5. Answer the question
- 6. Check your answer

The midpoint of a line segment

Also called the bisector

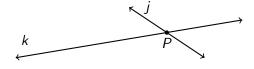
Given
$$\overline{ABC}$$
, with $AB = 2x + 2$, $AC = 20$. $AB = BC$

Find x.

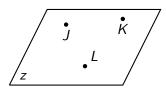
Definition: the *midpoint* or *bisector* of a line segment divides it exactly in half.

More definitions: intersections, coplanar

Two lines *intersect* if they cross. Their common point is the *intersection*. (shown here, lines j and k intersect at point P)



Coplanar means to lie in the same plane. Three points are always coplanar, but four points may not be.

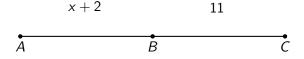


Learning Target: I can work with a number line

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.4 Monday 20 Sept

Do Now: Midpoint calculations

Given point B is the midpoint of \overline{AC} , with AB = x + 2, BC = 11. Find x.



1.3 Segments scores in Jumprope. Make up if absent Lesson: Number lines, distance and length, absolute value Practice midpoints and segment addition situations

A bisector creates two line segments with the same length Congruent line segments are the same length

Given point *B* is the midpoint of \overline{AC} , with AB = x + 2, BC = 11. Find x.

$$X+2$$
 11

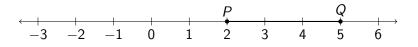
 A B C

Definition: Congruent means equal in length. $\overline{AB}\cong \overline{BC}$ We mark congruent segments in diagrams with cross hatch marks.

A number line is useful for calculating length or distance

Take the difference in the points' values

Given \overline{PQ} as shown on the number line.



What is the distance on the number line between the points P and Q?

Absolute value: the distance from a point to the origin Always a positive number (or zero)

The absolute value of 5 is 5. |5| = 5

The absolute value of -3 is 3. |-3|=3

Negative number practice on a number line

Take the difference in the points' values. Check by counting the marks.

Given MN with M(-1) and N(3), as shown on the number line.

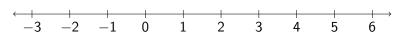
What is the length of the segment MN? Show your work as an equation.

Can a length be a negative number?

Decimal practice on a number line

Mark the points then take the difference in the points' values.

Given \overline{GH} with G(1) and H(4.5).

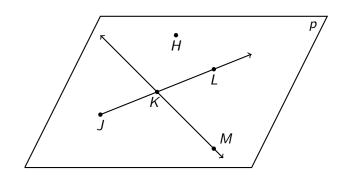


- 1. Mark and label the points and segment on the number line.
- 2. What is the length of the segment \overline{GH} ? Show your work as an equation.

Identifying objects in a plane

Identify each item

- 1. The point *H*
- 2. The ray \overrightarrow{JL}
- 3. The name of the plane shown



Formal meanings of sketch, draw, and construct

- Sketch is to make a freehand diagram of important features.
 Use a pencil to write carefully in your notebook or on paper.
- Draw is to depict with accurate measures using ruler, protractor, and compass.
 - For example, draw a diagram of your room.
- 3. *Construct* is a formal, logical process to create geometric figures using only a straightedge and compass.
- Drawn to scale means that all of the lengths are proportional.
 (e.g. a "scale model")
 - Tests will often warn that diagrams are "not drawn to scale"

Learning Target: I can work with congruent segments

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.5 Tuesday 21 Sept

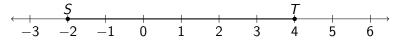
What is the length of the segment ST? Show your work as an equation.

Lesson: Perimeter, congruent line segments in rectangles & isosceles triangles

Negative number practice on a number line

Take the difference in the points' values. Check by counting the marks.

Given \overline{ST} with S(-2) and T(4), as shown on the number line.

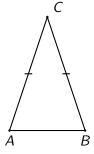


What is the length of the segment \overline{ST} ? Show your work as an equation.

Why is "minus a negative" the same as add a positive?

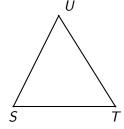
Use proper notation (including the bar over the letters)

Given $\triangle ABC$ write down two congruent line segments using proper notation.



On the diagram mark the congruent line segments with tick marks.

Given $\triangle STU$ with $\overline{ST} \cong \overline{TU}$.



Sketch an isosceles triangle

 $\label{eq:marks} \mbox{Mark the congruent sides with tick marks.}$

Draw a ray. (careful! which direction does it go?)

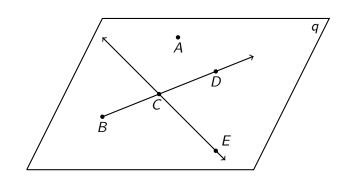
Given the points X and Y, draw \overrightarrow{YX} .



γ

Identify each item.

- 1. The point A
- 2. The ray \overrightarrow{BD}
- 3. The name of the plane

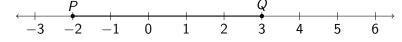


Apply the Segment Addition Postulate Show your work by marking the diagram and writing an equation.

Given \overline{DEF} , DE = 8.5, and EF = 2.5. Find DF.

Find the length of the line segment \overline{PQ} .

Given P(-2) and Q(3), as shown on the number line.



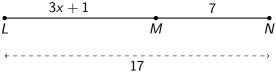
State an equation and the solution. Check your work by counting the distance. Leave marks to show your work.

Learning Target: I can measure angles

CCSS: HSG.CO.A.1 Know precise geometric definitions

1.6 Wednesday 22 Sept

Do Now: Given \overline{LMN} , LM = 3x + 1, MN = 7, LN = 17. Find x.



- 1. Write down an equation to represent the situation.
- 2. Solve for x.
- 3. Check your answer.

Lesson: Angle measures, internal, external, acute, obtuse, right

Solve for *x* using the segment addition postulate

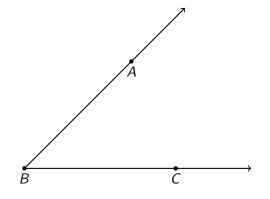
Given LMN, LM = 3x + 1, MN = 7, LN = 17. Find x.

- 1. Write down an equation to represent the situation.
- 2. Solve for *x*.

3. Check your answer.

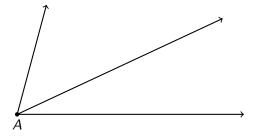
Angle: two rays with a common endpoint or vertex

Rays \overrightarrow{BA} and \overrightarrow{BC} . Vertex B. Written notation is $\angle ABC$ or $\angle B$.



Angle measures: the Babylonian system of 360° in a circle

- ▶ A full rotation is 360° (a full "turn").
- ightharpoonup A half turn (straight line) is 180° .
- ▶ 90° is a quarter turn or a *right* angle.
- ► Acute angles measure less than 90° . Obtuse angles measure more than 90° .
- Adjacent angles ("next to" each other) share a common ray and are external to each other.



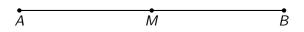
Learning Target: I can measure angles

CCSS: HSG.CO.A.1 Know precise geometric definitions

1.7 Thursday 23 Sept

Do Now: Given M bisects \overline{AB} , AM = 5x + 2, MB = 20.

- 1. Mark the diagram with the values and tick marks
- 2. Write an equation and solve for x
- 3. Check your result

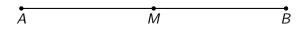


Lesson: Angle measures, angle addition postulate

Solve for x given a bisector

Given M is the midpoint of \overline{AB} , AM = 5x + 2, MB = 20.

- 1. Mark the diagram with the values and tick marks
- 2. Write an equation and solve for x
- 3. Check your result



Angle addition postulate

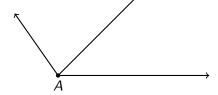
For adjacent angles, the sum of their measures is the measure of their combined angle.

A *linear pair* are two angles that make a straight line.

Opposite rays have a common endpoint and make a line. (They form an angle measuring 180°).

Angles whose measures sum to 180° are supplementary.

Angles whose measures sum to 90° are $\emph{complementary}.$



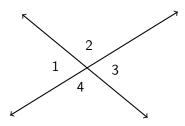
Learning Target: I can identify vertical angles

CCSS: HSG.CO.A.1 Know precise geometric definitions

1.8 Friday 24 Sept

Do Now: Given \overline{RST} , $RS = 3\frac{2}{3}$, and $RT = 9\frac{1}{3}$. Find ST.

Definition: Vertical angles are angles opposite each other when two lines intersect. $\angle 1$ and $\angle 3$ are vertical angles, as are $\angle 2$ and $\angle 4$.



Lesson: Angle addition problems, vertical angles

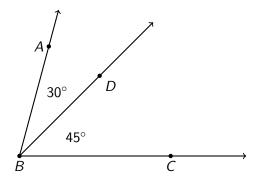
Mark the diagram and state your answer as a fraction

Given
$$\overline{RST}$$
, $RS=3\frac{2}{3}$, and $RT=9\frac{1}{3}$. Find ST .

Learning Target: I can solve for angle measures

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.9 Monday 27 Sept

Do Now: $m\angle ABD = 30^{\circ}$, $m\angle DBC = 45^{\circ}$. Find $m\angle ABC$.



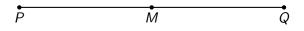
Lesson: Angle addition problems, vertical angles

Learning Target: I can solve for angle measures

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.10 Tuesday 28 Sept

Do Now: Given M bisects \overline{PQ} , PM = x + 7, PQ = 23.

- 1. Mark the diagram with the values and tick marks
- 2. Write an equation and solve for x
- 3. Check your result

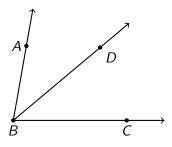


Lesson: Angle bisectors

Definition of angle bisector

Angle bisector: a ray dividing an angle into two congruent angles.

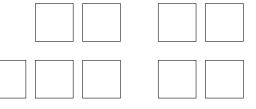
As shown, \overrightarrow{BD} bisects $\angle ABC$ if and only if $\angle ABD \cong \angle CBD$.



Open Middle problem (fun)

Use digits from 0 to 9. Using a digit no more than once.

The first two angle measures are complementary. The second two angles supplementary. (degrees)



414 Seating chart 10.1

| Front of room Video Screen | | | | | | | | |
|----------------------------|-----------|-----------|-------------|-----------|------------|--|--|--|
| Ebenezer | Sadia Z. | Jose L | Christian V | Muhamed K | Abigail M. | | | |
| Nathalia P | Alex R. | Ebrima G | Jonathan R | Joshua S. | Alexis N. | | | |
| Jeremy D. | Isaias A. | Edwin S. | Tyler S. | Robert C. | Jada C. | | | |
| Andrew U. | Ivana T. | Angel M. | Juan R. | Yuliana G | Andrian A. | | | |
| Emmanuel W | | Steven L. | Aiden P. | | | | | |

420 Seating chart 10.3

| Room 420 | 10.3 | F | ont (screen) | | |
|--------------------------------------|--------------------------|-------------------------------|----------------------------|----------------|------------------------|
| Chasidy S Matphew S Jonathan S | | 5 Oprah M | Jada M Jefferson M | 1 Flora A | Lessly A Jason R |
| 8 Jonathan | Ashley R Lisbeth E | 6 Taniah G | Zinaira D Fariha S | 2 Aminata B | Catalina M Kelvin A |
| 9 Ashley 0 | Richard A Cristhian A | 7 Maryelis T | Christopher S Annette M | 3 Juan P | Xiomara A Manny B |
| Back door | 1 Yaeli | 0 <i>Leslie</i> M Jarryw B | | 4 David A | Jose M Anaylis 0 |