

Geometry Unit 4: Volume

Bronx Early College Academy

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31 October - 18 November 2022

4.1 Nets

31 October

4.2 Rectangular prisms

1 November

4.3 Solve for a side

3 November

4.4 Surface area

4 November

Learning Target: I can fold nets into 3-dimensional solids

HSG.CO.C.9 Prove theorems about lines and angles

4.1 Monday 31 October

Do Now

1. Review your Deltamath assignments
2. Check your Jump rope scores
3. Set a study goal
4. Answer survey in Google Classroom, "Mark as Done"

Lesson: Nets, Deltamath classwork practice

Homework: Area formulas review problem set

Learning Target: I can calculate the volume of a *rectangular prism*

HSG.CO.C.9 Prove theorems about lines and angles

4.2 Tuesday 1 November

Do Now

1. Find the area of a rectangle 4 inches by 6 inches
2. Find the length of a rectangle 7 inches wide with an area of 63 square inches

Lesson: Prism definitions, volume formula

Homework: Deltamath practice

A prism is a polyhedron, a 3-dimensional shape

Solid A 3-dimensional object

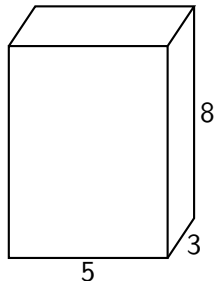
Face A flat surface of a geometric solid

Edge A line segment where two faces meet

Vertex A point where edges meet

Prism A solid with two identical, parallel, bases and uniform cross section

Base Flat shapes that form the top and bottom or ends of a prism



Lateral face The sides of a prism, which are parallelograms

Cross section The shape of a plane's intersection with a solid

Common types of prisms, named by their base

Rectangular Bases are rectangles (or squares)

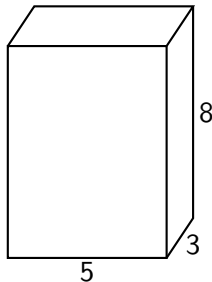
Triangular Triangular base

Hexagonal Six-sided base, a hexagon

Cylinder Solid with two parallel circles as bases

Right Lateral faces are a right angles to the base

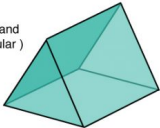
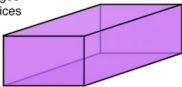
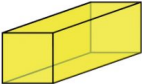
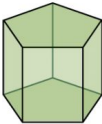
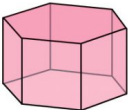
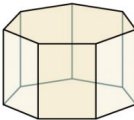
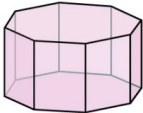

Oblique Slanted



Math Monks prisms page

Prism Shapes



<p>Triangular</p> <ul style="list-style-type: none"> • 5 faces (2 triangular and 3 rectangular) • 9 edges • 6 vertices 	<p>Rectangular</p> <ul style="list-style-type: none"> • 6 faces (all rectangular) • 12 edges • 8 vertices 
<p>Square</p> <ul style="list-style-type: none"> • 6 faces (2 squares and 4 rectangular) • 12 edges • 8 vertices 	<p>Pentagonal</p> <ul style="list-style-type: none"> • 7 faces (2 pentagonal and 5 rectangular) • 15 edges • 10 vertices 
<p>Hexagonal</p> <ul style="list-style-type: none"> • 8 faces (2 hexagonal and 6 rectangular) • 18 edges • 12 vertices 	<p>Heptagonal</p> <ul style="list-style-type: none"> • 9 faces (2 Heptagonal and 7 rectangular) • 19 edges • 14 vertices 
<p>Octagonal</p> <ul style="list-style-type: none"> • 10 faces (2 octagonal and 8 rectangular) • 24 edges • 16 vertices 	<p>Trapezoidal</p> <ul style="list-style-type: none"> • 6 faces (2 trapezoidal and 4 rectangular) • 12 edges • 8 vertices 

Volume is a measure of space, the number of unit cubes a solid contains

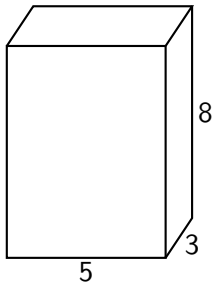
Given the area of the base B and height h ,
the volume of a prism is $V = B \times h$

Rectangular $V = l \times w \times h$

Square $V = s^2 \times h$

Triangular $V = \frac{1}{2}(l \times w \times h)$

Cylinder $V = \pi r^2 \times h$



Learning Target: I can solve for a missing parameter

HSG.CO.C.9 Prove theorems about lines and angles

4.3 Thursday 3 November

Do Now

1. Find the area of a circle with radius $r = 10$, in terms of π
2. Find the radius of a circle with area $A = 49\pi$

Lesson: Using algebra to solve problems, Deltamath practice

Homework: Handout practice with volume calculations

Muhammad ibn Musa al-Khwarizmi - the “father” of algebra

Persian 780 - 847 AD worked in Baghdad during the “Islamic golden age”

Algebra Mathematics with symbols (named after al-Khwarizmi’s book, al-jabra)

Algorithm Logical steps to solve a problem (comes from his name)

Unknown A symbol or letter representing a number, x , y , a , π , θ

“reduction” Cancellation of like terms on opposite sides of the equation



“Solve for x ” or “isolate the variable”

The algorithm developed by al-Khwarizmi

Operation Combine two numbers (multiplication or addition, for example)

Identity 0 for addition, 1 for multiplication.

$$a + 0 = a \text{ and } a \times 1 = a$$

Inverse Two values that make the identity for an operation.

$$a + (-a) = 0 \text{ and } a \times \frac{1}{a} = 1$$

$$a = b \iff a + c = b + c$$

Multiplying and dividing fractions

Rational numbers those that can be expressed as fractions, $\frac{p}{q} \in \mathbb{Q}$

Numerator The top number in a fraction, *dividend*, p

Denominator *Divisor*, bottom number in a fraction, q

Reciprocal The multiplicative inverse

Division Means to multiply by the reciprocal. $a \div b = \frac{a}{b} = a \times \frac{1}{b}$

To multiply fractions, multiply the numerators and denominators

$$\frac{a}{b} \times \frac{c}{d} = \frac{a \times c}{b \times d}$$

To divide fractions, multiply by the reciprocal

$$\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \times \frac{d}{c} = \frac{a \times d}{b \times c}$$

Learning Target: I can calculate the surface area of a rectangular prism

HSG.CO.C.9 Prove theorems about lines and angles

4.4 Friday 4 November

Do Now: Lumber used in construction called a “two-by-four” is actually $3\frac{1}{2}$ inches by $1\frac{1}{2}$ inches by 8 feet long.

1. Find the area of the rectangular cross section, $3\frac{1}{2}$ inches by $1\frac{1}{2}$ inches
2. Find the area of a triangular wedge cut from a two-by-four that is $3\frac{1}{2}$ inches by one foot long.

Lesson: Surface area definition, formula; adding fractions

Homework: Deltamath practice

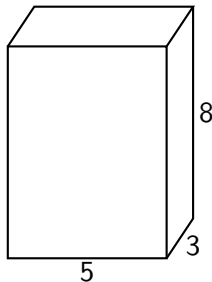
Extension: Deltamath absolute value, percent error

Surface area is the combined total area of the faces of a polyhedron

Surface area The total area of the outside of a solid

Given a rectangular prism with dimensions l , w , and h the surface area is the sum of the six faces:

$$\begin{aligned} S.A. &= 2lw + 2lh + 2wh \\ &= 2(5 \times 3) + 2(5 \times 8) + 2(3 \times 8) \\ &= 158 \text{ square units} \end{aligned}$$



Adding and subtracting fractions

To add fractions with the same denominator, add the numerators.

$$\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$$

Equivalent fractions Fractions that are equal.

$$\frac{a}{b} = \frac{a}{b} \times \frac{c}{c} = \frac{ac}{bc}$$

LCM Lowest Common Multiple, for two fractions, multiples of the denominators that are equal.

Mixed fraction A whole number and a fraction. e.g. $3\frac{1}{2}$

Adding fractions with different denominators

First convert to equivalent fractions with a common denominator. e.g. find

$$\frac{1}{3} + \frac{1}{2}$$

Convert to sixths

$$\frac{1}{3} \times \frac{2}{2} = \frac{2}{6} \text{ and } \frac{1}{2} \times \frac{3}{3} = \frac{3}{6}$$

Add these equivalent fractions instead:

$$\frac{2}{6} + \frac{3}{6} = \frac{5}{6}$$