

11.14 Exit note: Perpendicular bisectors

1. The line l has the equation $y = -3x - 2$.

(a) What is the slope of line l ?

-3

(b) Rewrite the equation of l in the form $ax + by = c$.

$3x + y = -2$

2. (a) Find the slope m of the line $3x - y = 12$.

$y = 3x - 12$
 $m = 3$

(b) Write down the slope perpendicular to the line, m_{\perp} .

$-\frac{1}{3}$

3. Write down the slope perpendicular to the given slope.

(a) $m = -\frac{3}{2}$

$m_{\perp} =$

$\frac{2}{3}$

(b) $m = 2$

$m_{\perp} = -\frac{1}{2}$

4. The line segment \overline{AB} , $A(1, 7)$ and $B(9, 3)$, is shown below.

(a) Mark the midpoint M of \overline{AB} . Label it as an ordered pair.

(b) Find the slope of \overline{AB} .

$m = \frac{3-7}{9-1} = -\frac{1}{2}$

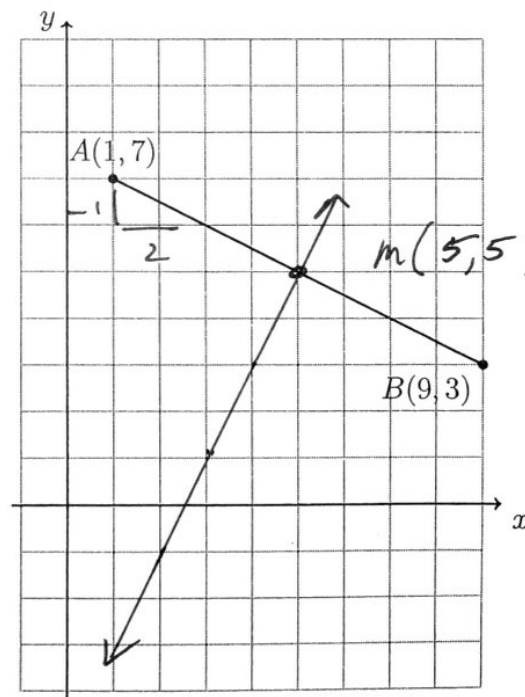
(c) Write down the slope perpendicular to \overline{AB} .

$+2$

(d) Write down the equation of the perpendicular bisector of \overline{AB} .

$y - 5 = 2(x - 5)$

(e) Draw the perpendicular bisector on the graph.



5. Write down the equation of the line through $(2, 3)$ with a slope of -2 .

$$y - 3 = -2(x - 2)$$

6. The line l has the equation $y - 5 = -3(x - 2)$. Rewrite the equation in slope-intercept form, $y = mx + b$.

$$y = -3x + 6 + 5$$

$$y = -3x + 11$$

7. Quadrilateral $ABCD$ is shown on the graph below with $A(-1, -2)$, $B(5, 2)$, $C(2, 6)$, and $D(-4, 2)$. Calculate the slopes of the four sides and show that $ABCD$ is a parallelogram but not a rectangle.

Slopes

$$m_{\overline{AB}} = \frac{2}{3}$$

$$m_{\overline{BC}} = -\frac{4}{3}$$

$$m_{\overline{CD}} = \frac{2}{3}$$

$$m_{\overline{AD}} = -\frac{4}{3}$$

$$m_{\overline{AB}} = m_{\overline{CD}}$$

$$m_{\overline{BC}} = m_{\overline{AD}}$$

Slopes equal \Rightarrow sides parallel

$$\overline{AB} \parallel \overline{CD}, \overline{BC} \parallel \overline{AD}$$

\Rightarrow $ABCD$ parallelogram

But

$$(m_{\overline{AB}})(m_{\overline{BC}}) = \left(\frac{2}{3}\right)\left(-\frac{4}{3}\right) \neq -1 \Rightarrow \text{Not perpendicular}$$

$$\Rightarrow \text{Not rectangle}$$

