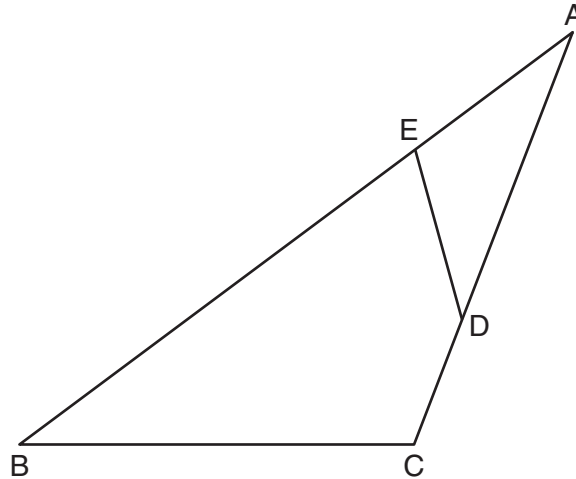


Challenge: Similar triangles

1.

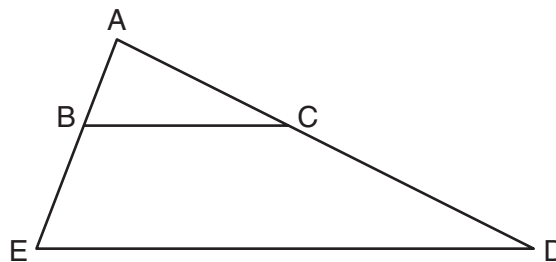
The diagram below shows $\triangle ABC$, with \overline{AEB} , \overline{ADC} , and $\angle ACB \cong \angle AED$.

Write down what triangles are similar. How would you prove it? Try to write a proof.



2.

In the diagram below of $\triangle ADE$, B is a point on \overline{AE} and C is a point on \overline{AD} such that $\overline{BC} \parallel \overline{ED}$, $AC = x - 3$, $BE = 20$, $AB = 16$, and $AD = 2x + 2$. Find the length of \overline{AC} .

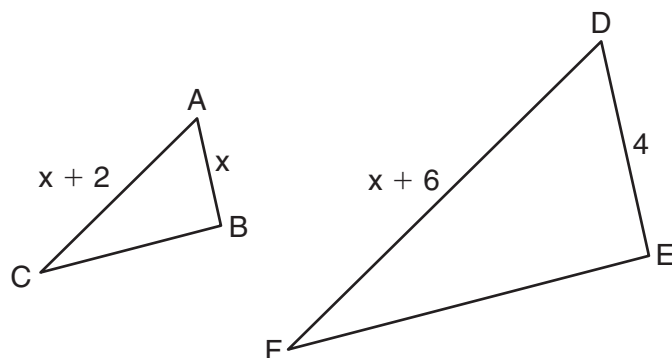


3. Explain this mathematics using words and algebraic symbols:

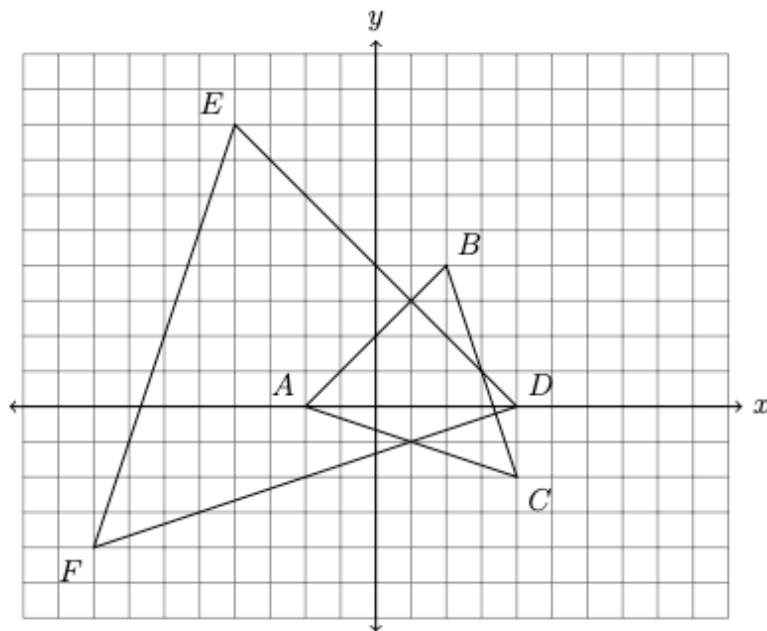
The father's will bequeaths his 17 camels to his sons in the following proportions: $\frac{1}{2}$ to the oldest, $\frac{1}{3}$ to the middle, $\frac{1}{9}$ to the youngest. To enact the division, a passerby temporarily donates his one camel, making 18. They are allocated 9, 6, & 2 camels, with one remaining for this stranger.

4.

In the diagram below, $\triangle ABC \sim \triangle DEF$, $DE = 4$, $AB = x$, $AC = x + 2$, and $DF = x + 6$. Determine the length of \overline{AB} . [Only an algebraic solution can receive full credit.]



5. *Spicy* On the set of axes below, $\triangle ABC$ has vertices at $A(-2, 0)$, $B(2, 4)$, $C(4, -2)$, and $\triangle DEF$ has vertices at $D(4, 0)$, $E(-4, 8)$, $F(-8, -4)$.



Which transformations map $\triangle ABC \rightarrow \triangle DEF$? Mark each statement True or False

- | | | |
|--|------|-------|
| (a) A dilation with a scale factor of -2 centered at the origin | True | False |
| (b) A dilation with a scale factor of $\frac{1}{2}$ centered at point A | True | False |
| (c) A dilation with a scale factor of 2 centered at the origin, followed by a rotation of 180° about the origin | True | False |
| (d) A dilation with a scale factor of 2 centered at the origin, followed by a reflection across the y -axis | True | False |