Name:

Unit 5 Exam Part 1: Integral Calculus - with calculator

You may use a calculator on these problems

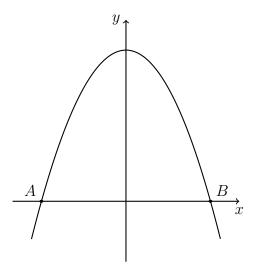
[34 marks]

1. Let $f(x) = x^2$ and $g(x) = \sin(x+1)$.

(a) Solve for
$$f(x) = g(x)$$
. [3]

(b) Find the area of the region enclosed by the graphs of f and g. [3]

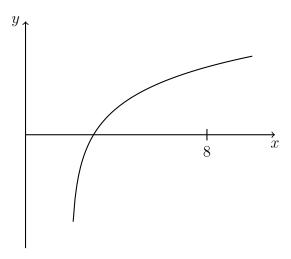
2. Let $f(x) = 6 - x^2$. Part of the graph of f is shown in the following diagram.



(a) The graph crosses the x-axis at the points A and B.Find the x-coordinate of A and of B.[3]

(b) The region enclosed by the graph of f and the x-axis is rotated 360° about the x-axis. Find the volume of the solid formed. [3]

3. Let $f(x) = 3\ln(x-2)$, for x > 2. The following diagram shows part of the graph of f.



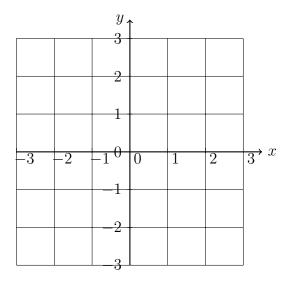
- (a) Find the equation of the vertical asymptote to the graph of f. [2]
- (b) Find the x-intercept of the graph of f. [2]
- (c) The region enclosed by the graph of f, the x-axis, and the line x=8 is rotated 360° about the x-axis. Find the volume of the solid formed. [3]

[3]

[2]

4. Let
$$f(x) = -x^4 + 2x^3 - \frac{1}{2}$$
, for $0 \le x \le 2$.

(a) Sketch the graph of
$$f$$
.

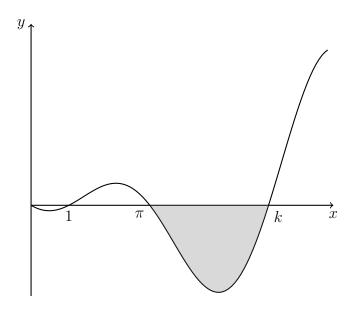


(b) Solve for
$$f(x) = 0$$
.

(c) The region enclosed by the graph of f and the x-axis is rotated 360° about the x-axis. Find the volume of the solid formed. [3]

[2]

5. The graph of $y = (x - 1)\sin x$, for $0 \le x \le \frac{5\pi}{2}$, is shown below.



- (a) The graph has x-intercepts at $0, 1, \pi$, and k. Find k.
- (b) The shaded region is rotated 360° about the x-axis. Let V be the volume of the solid formed.

Write down an expression for V. [3]

(c) Find V. [2]

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Unit 5 Exam Part 2: Integral Calculus - without calculator

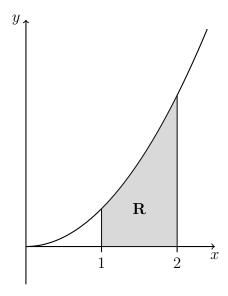
No Calculator section

[38 marks]

6. Let $f(x) = x^2$.

(a) Find
$$\int_{1}^{2} (f(x))^{2} dx$$
 [4]

(b) The following diagram shows part of the graph of f.



The shaded region R is enclosed by the graph of f, the x-axis, and the lines x=1 and x=2.

Find the volume of the solid formed when R is revolved 360° about the x-axis. [2]