

9.2 Geometry: Sectors and Trigonometry functions

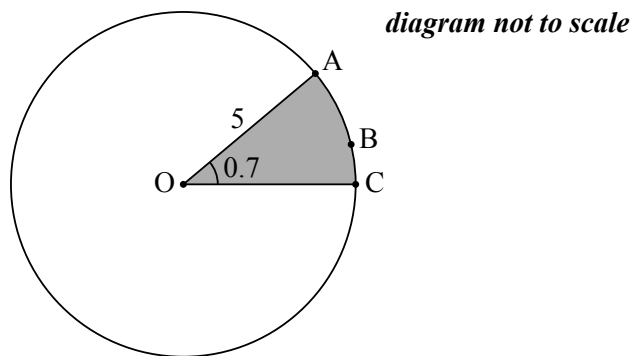
Full marks are not necessarily awarded for a correct answer with no working. Answers must be supported by working and/or explanations. In particular, solutions found from a graphic display calculator should be supported by suitable working, for example if graphs are used to find a solution, you should sketch these as part of your answer. Where an answer is incorrect, some marks may be given for a correct method, provided this is shown by written working. You are therefore advised to show all working.

SECTION A

Answer **all** questions in the boxes provided. Working may be continued below the lines if necessary.

1. [Maximum mark: 6]

The following diagram shows a circle with centre O and radius 5 cm.



The points A, B and C lie on the circumference of the circle, and $\angle AOC = 0.7$ radians.

(a) (i) Find the length of the arc ABC.

(ii) Find the perimeter of the shaded sector.

[4]

(b) Find the area of the shaded sector.

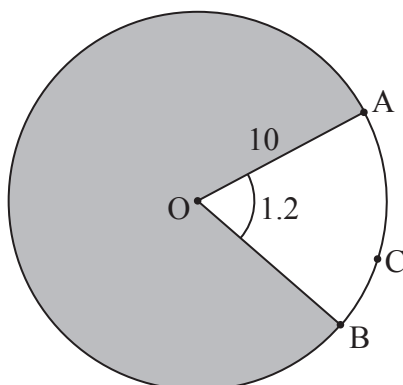
[2]

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2. [Maximum mark: 5]

The following diagram shows a circle with centre O and a radius of 10 cm. Points A , B and C lie on the circle.



Angle AOB is 1.2 radians.

- (a) Find the length of arc ACB . [2]
- (b) Find the perimeter of the shaded region. [3]

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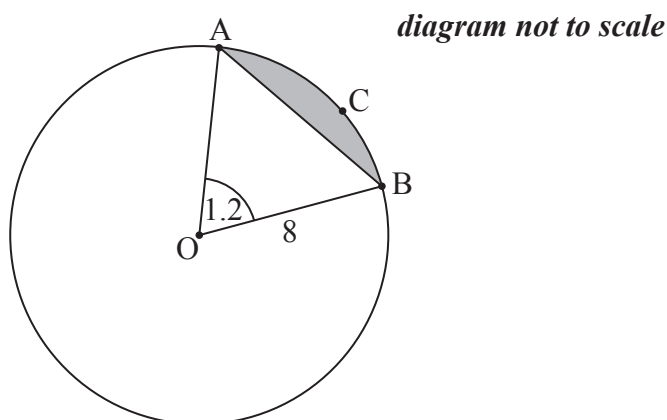
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3. *[Maximum mark: 7]*

The following diagram shows a circle with centre O and radius 8 cm.



The points A, B and C are on the circumference of the circle, and $\widehat{AOB} = 1.2$ radians.

- (a) Find the length of arc ACB. [2]
- (b) Find AB. [3]
- (c) Hence, find the perimeter of the shaded segment ABC. [2]

[illegible]

5. [Maximum mark: 7]

In triangle ABC, $AB = 6\text{ cm}$ and $AC = 8\text{ cm}$. The area of the triangle is 16 cm^2 .

(a) Find the two possible values for \hat{A} . [4]

(b) Given that \hat{A} is obtuse, find BC. [3]

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5. [Maximum mark: 7]

Given that $\sin x = \frac{3}{4}$, where x is an obtuse angle, find the value of

(a) $\cos x$; [4]

(b) $\cos 2x$. [3]

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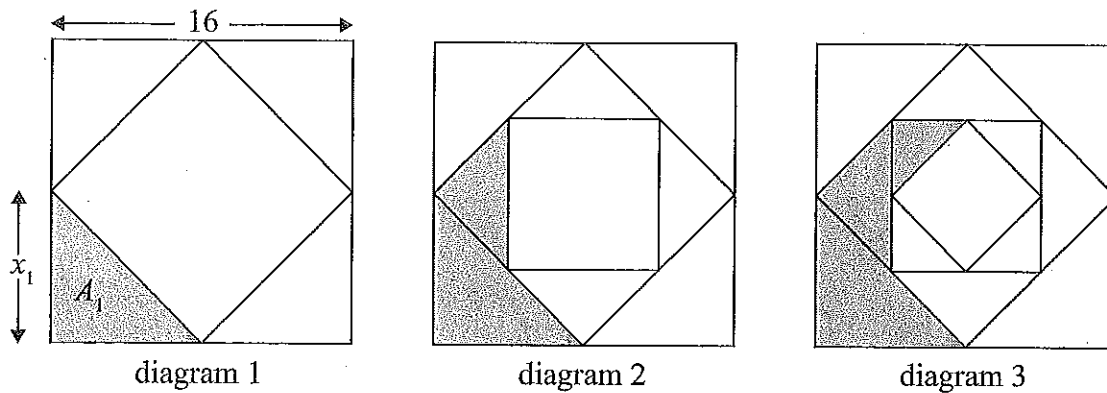
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10. [Maximum mark: 15]

The sides of a square are 16 cm in length. The midpoints of the sides of this square are joined to form a new square and four triangles (diagram 1). The process is repeated twice, as shown in diagrams 2 and 3.



Let x_n denote the length of one of the equal sides of each new triangle.
Let A_n denote the area of each new triangle.

- (a) The following table gives the values of x_n and A_n , for $1 \leq n \leq 3$. **Copy** and complete the table. (Do **not** write on this page.)

[4]

n	1	2	3
x_n	8		4
A_n	32	16	

- (b) The process described above is repeated. Find A_6 .
- (c) Consider an initial square of side length k cm. The process described above is repeated indefinitely. The total area of the shaded regions is k cm². Find the value of k .

[4]

[7]