

**Practice Regents problems #9**

All-F.BF.6 Represent and evaluate the sum of a finite arithmetic or finite geometric series, using summation (sigma) notation. For geometric series:

$$\sum_{k=1}^n a_k = a_1 + a_2 + \dots + a_n = a_1 \left( \frac{1-r^n}{1-r} \right)$$

1. Given the geometric sequence 55, 77, 107.8, 150.92, ...

(a) Find the common ratio  $r$ .

$$r = \frac{77}{55} = \frac{107.8}{77} = \dots = 1.4$$

(b) Write a recursive formula for the sequence.

$$a_1 = 55$$

$$a_n = 1.4 \cdot a_{n-1}$$

(c) Write an explicit formula for the sequence.

$$a_n = 55 \cdot 1.4^{(n-1)}$$

(d) Find the sum of the first seven terms the sequence rounded to the *nearest tenth*.

$$S_7 = 55 \left( \frac{1 - 1.4^7}{1 - 1.4} \right) = \cancel{1311.53568} \approx 1311.9$$

2. Express each of the following using rational or integer exponents.

(a)  $\sqrt[3]{8x^4}$

$$= 2x^{\frac{4}{3}}$$

(b)  $\sqrt[5]{x^{10}} \sqrt[3]{x^{-2}}$

$$= \frac{x^2}{x^{2/3}} = x^{\frac{4}{3}}$$

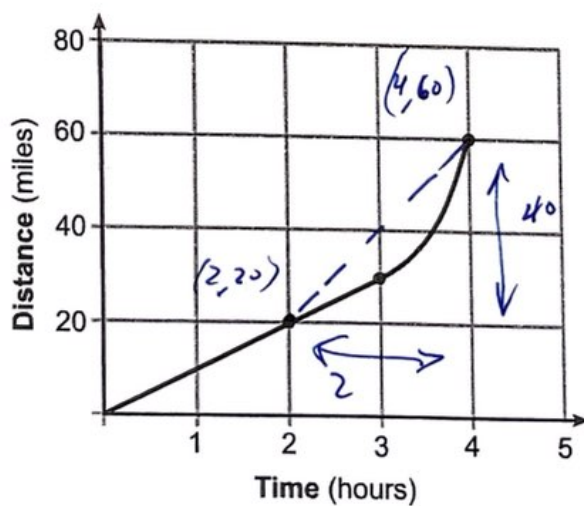
3. Determine algebraically how long it would take an investment to double, to the *nearest tenth of a year*, given 4.25% interest rate, compounded continuously.

$$1e^{0.0425t} = 2$$

$$0.0425t = \ln 2$$

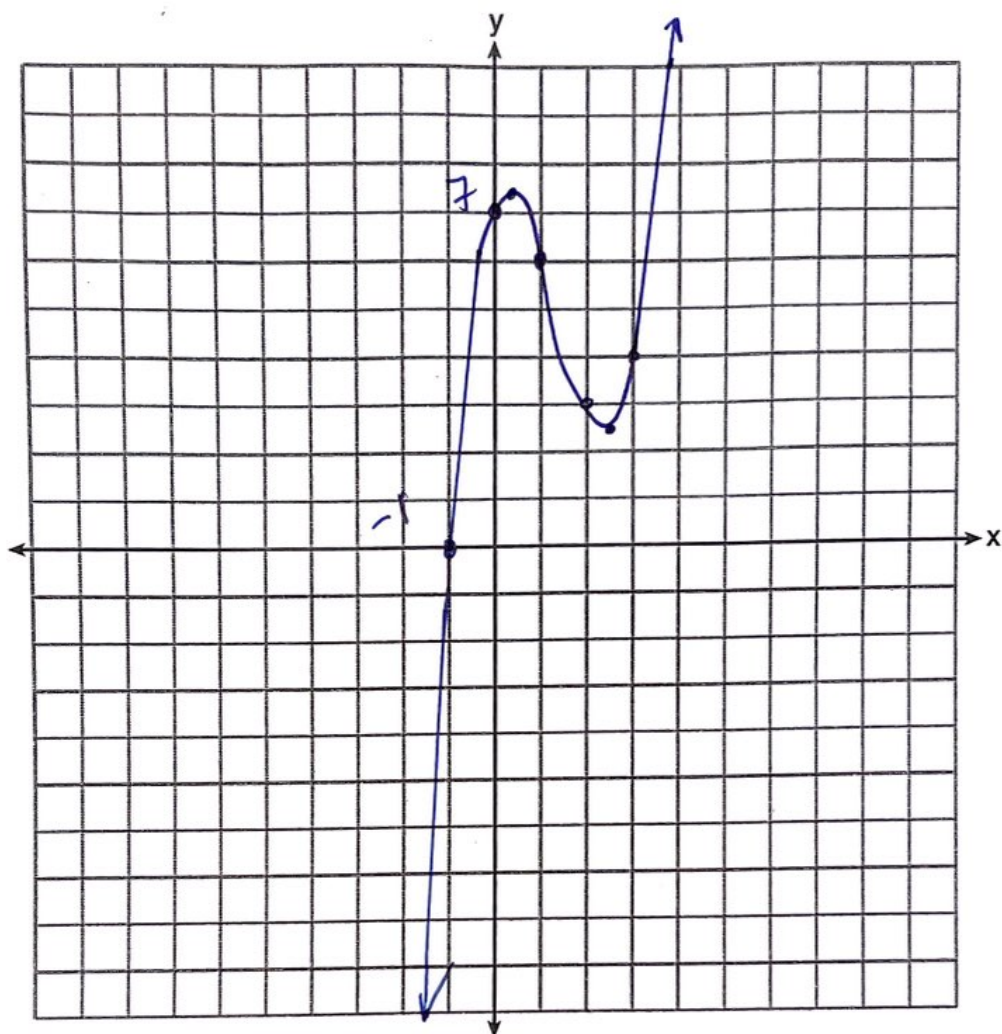
$$t = \frac{\ln 2}{0.0425} = 16.30934... \approx 16.3$$

- 25 Determine the average rate of change, in mph, from 2 to 4 hours on the graph shown below.



$$\bar{m} = \frac{40}{2} = 20 \text{ mph}$$

32 Graph  $y = x^3 - 4x^2 + 2x + 7$  on the set of axes below.



- 26 The zeros of a quartic polynomial function are 2, -2, 4, and -4. Use the zeros to construct a possible sketch of the function, on the set of axes below.

