Geometry Unit 1: Segments, Length, and Area Bronx Early College Academy

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8-23 September 2022

1.1 Segment addition	8 September
1.2 Solve for length	9 September
1.3 Terminology and notation	12 September
1.4 Midpoint and bisector	13 September
1.5 Equilateral and isosceles triangles, perimeter	14 September
1.6 Roundtable review	15 September
1.7 Unit conversion, Exit note quiz	16 September

Learning Target: I can measure my world

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.1 Thursday 8 Sept

Do Now: Make simple measurements on paper

- 1. Diagram the desks adjacent to yours and their distances
- 2. Early finishers: Calculate diagonal distances

ToDo: add classroom desk image, diagram

Lesson: Points, line segments, length; Segment addition postulate

Homework: Write for me your "math autobiography" on looseleaf (due tomorrow)

Optional homework: spicy absolute value worksheet

A diagram is a simplied image representing a situation

This is an example diagram of a desk arrangement

When making diagrams

Include common elements: labels, titles, distances

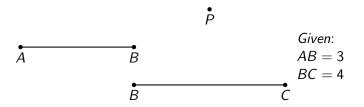
Conventions Standard ways of doing things to make it easier to work with other people

Adjacent Positioned next to each other

Write down vocabulary and terminology in your notebook with definitions and examples. (I write new terms in *italics*)

Line segments and their endpoints

Points P, A, B, C, and line segments \overline{AB} , \overline{BC} are shown.

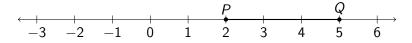


The *length* of a line segment is the distance between the two endpoints. The length of segment \overline{AB} is written AB (no bar over).

A *number line* is useful for calculating length or distance

Take the difference in the points' values

Given \overline{PQ} as shown on the number line.

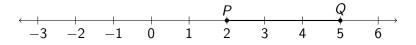


Find the distance on the number line between the points P and Q.

A *number line* is useful for calculating length or distance

Take the difference in the points' values

Given \overline{PQ} as shown on the number line.



Find the distance on the number line between the points P and Q.

$$PQ = 5 - 2 = 3$$

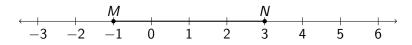
Can a length be a negative number?

Most of the lengths on our problem sets are in centimeters.

Negative number practice on a number line

Take the difference in the points' values. Check by counting the marks.

Given \overline{MN} with M(-1) and N(3), as shown on the number line.

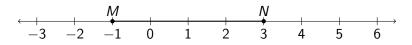


What is the length of the segment \overline{MN} ? Show your work as an equation.

Negative number practice on a number line

Take the difference in the points' values. Check by counting the marks.

Given \overline{MN} with M(-1) and N(3), as shown on the number line.



What is the length of the segment MN? Show your work as an equation.

$$MN = 3 - (-1) = 4$$

Why is "minus a negative" like adding a positive?

Decimal practice on a number line

Mark the points then take the difference in the points' values.

Given \overline{GH} with G(1) and H(4.5).

- 1. Mark and label the points and segment on the number line.
- 2. What is the length of the segment \overline{GH} ? Show your work as an equation.

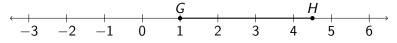


Decimal practice on a number line

Mark the points then take the difference in the points' values.

Given \overline{GH} with G(1) and H(4.5).

- 1. Mark and label the points and segment on the number line.
- 2. What is the length of the segment \overline{GH} ? Show your work as an equation.



$$GH = 4.5 - 1 = 3.5$$

Take class notes in a composition book

Copy definitions using your own words. Write down example diagrams and problems

Terminology:

Point A location, has no size; label with capital letter, P

Endpoint A point at the end of a line segment

Line segment Two points and all the points between them; label with *endpoints* and a bar, e.g. \overline{AB}

Distance The positive difference between two points on a number line (length is the same thing). AB = 3 inches

Number line A line with lengths marked on it

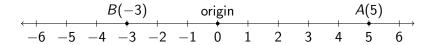
Conventions Standard ways of doing things to make it easier to work with other people

Diagram Simplified image of a situation

Adjacent Positioned next to each other

Spicy: Absolute value is the distance from a point to zero

"Spicy", or extension topics, must be written in your notebook, but homework and tests are optional.



The absolute value of 5 is 5. |5| = 5

The absolute value of -3 is 3. |-3| = 3

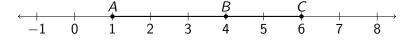
The absolute value of a number is always a positive number, or zero Write the absolute value of a number x using vertical bars |x| or abs(x)

Learning Target: I can solve for segment lengths

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.2 Friday 9 September

Do Now: Given A(1), B(4), C(6).

Write down AB, BC, and AC.



Lesson: Segment addition, solving algebraic models

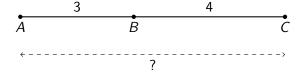
Homework: Problem set 1.2 (plus optional spicy worksheet)

1.2 Solve for length

Lengths add up on a straight line

Segment Addition Postulate

Shown *collinear* points A, B, C. Given AB=3, BC=4. Find AC.

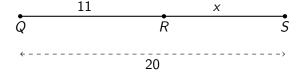


Definitions:

Collinear Points that lie on the same straight line Postulate A rule that we assume is true

Use a variable (x) to represent an unknown value An equation is a *model* of a situation

Given collinear points Q, R, S, with QR=11, QS=20. Find RS.

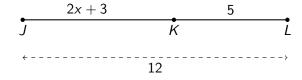


- 1. How would you check your answer?
- 2. Which equation represents the situation?

$$11 + x = 20$$
 $x = 20 - 11$

Step-by-step modeling

Given \overline{JKL} , JK = 2x + 3, KL = 5, JL = 12. Find x.

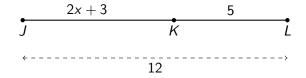


- 1. Write down an equation to represent the situation.
- 2. Solve for *x*.
- 3. Check your answer.

The diagram may be given, or you may have to sketch it

Write the steps in your notebook

Given
$$\overline{JKL}$$
, $JK = 2x + 3$, $KL = 5$, $JL = 12$. Find x .



$$JK + KL = JL$$

$$(2x+3)+5=12$$

$$2x + 8 = 12$$

$$2x = 4$$

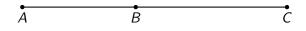
$$x = 2$$

$$2(2) + 3 + 5 = 12$$
?

- 2. Write a geometric equation
- 3. Substitute algebraic values
- 4. Solve for *x*
- 5. Answer the question
- 6. Check your answer

Mark the diagram, find x, answer AB = ?

Given
$$\overline{ABC}$$
, $AB = 3x - 7$, $BC = x + 5$, $AC = 14$.



Find AB.

More practice: Solve an equation with x on both sides

Given
$$\overrightarrow{DEF}$$
, $DE = x + 1$, $EF = 9$, $DF = 3x$. Find DE .

9 September

Check your notebook for completeness

Segment Addition Postulate

Mathematics is constructed of fundamental rules or postulates, and basic objects like points, lines, and numbers.

Vocabulary:

Collinear Points that lie on the same straight line

Postulate A rule that we assume is true (also called axioms)

Modeling Using an equation (algebra) to represent a situation in a simplified way

Check Substitute the value of x into the equation to test whether it is correct

Spicy: Fractional coefficients

Given
$$\overline{ABC}$$
, $AB = \frac{1}{2}x$, $BC = x$, $AC = 21$. Find x .



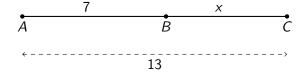
Term An expression representing a number, for example $\frac{1}{2}x$ Variable The unknown value represented by a letter (x)

Coefficient The fixed number in front of the variable. (e.g. $\frac{1}{2}$)

Learning Target: I can use geometric conventions

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.3 Monday 12 Sept

Do Now: Given collinear points A, B, C, with AB = 7, AC = 13.



1. Circle the equation that most simply represents the situation.

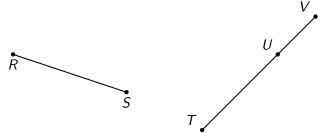
$$7 + x = 13$$
 $x = 13 - 7$

2. Find *BC*.

Write down an example of each geometric object.

Use proper notation.

- 1. point
- 2. line segment
- endpoint
- 4. three collinear points



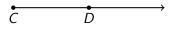
5. Given TU = 1.4, UV = 0.6. Find TV. (label the diagram first)

More definitions: lines, rays, planes

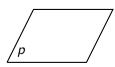
A line extends infinitely in both directions, \overrightarrow{AB} . (sometimes labeled with a small letter, for example, line k)



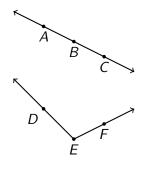
A ray has one endpoint and extends infinitely in one direction, \overrightarrow{CD} .



A plane is flat and extends infinitely in two directions, p.

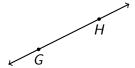


Opposite rays are collinear rays with a common endpoint.



 \overrightarrow{BA} and \overrightarrow{BC} are opposite rays.

These rays do not make a straight line.

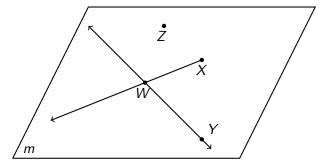


The rays \overrightarrow{GH} and \overrightarrow{HG} do not share a common endpoint.

Several objects are shown in a plane

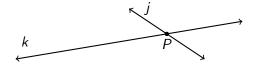
Circle true or false

- 1. T F The name of the plane is m.
- 2. T F The line \overrightarrow{WY} is in the plane.
- 3. T F The ray \overrightarrow{WX} is shown in the plane.
- 4. T F Points W, X, and Z are collinear.
- 5. T F \overrightarrow{WY} and \overrightarrow{YW} are the same line.

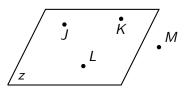


More definitions: intersections, coplanar

Two lines *intersect* if they cross. Their common point is the *intersection*. (shown here, lines j and k intersect at point P)



Coplanar means to lie in the same plane. Three points are always coplanar, but four points may not be.



Learn and practice using formal language and notation

- Line An infinite collection of points extending straight in both directions indefinitely, \overrightarrow{AB} or I
- Ray An endpoint and half of a straight line extending away from the endpoint, \overrightarrow{JK}
- Plane A flat surface extending infinitely in two dimensions, p
- Opposite rays Collinear rays with a common endpoint.
 - Coplanar Points or objects all in the same plane Intersection Where two lines cross, the common point

$$\frac{2}{3}(x+5)=4$$

$$\frac{2}{3}(x+5)=4$$

Distribute Multiply both terms in parentheses by the coefficient Numerator. The top of a fraction (i.e. n in $\frac{p}{2}$)

Numerator The top of a fraction (i.e. p in $\frac{p}{q}$)

Denominator The bottom of a fraction (i.e. q in $\frac{p}{q}$)

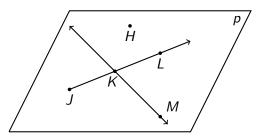
LCD Converting to the *Lowest Common Denominator* is the most efficient way to add fractions

Learning Target: I can bisect a length

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.4 Tuesday 13 Sept

Do Now: Circle or mark each object in the plane

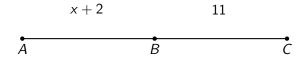
- 1. The point H
- 2. The ray \overrightarrow{JL}
- 3. The name of the plane shown



Lesson: Midpoint, congruence, bisection

The point *B* bisects the segment \overline{AC}

Point B is in the exact middle between A and C Given AB = x + 2, BC = 11. Find x.



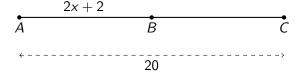
Hint: The line segment is split into two equal lengths.

1.4 Midpoint and bisector

The *midpoint* of a line segment

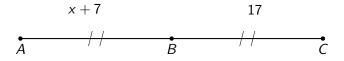
Given
$$\overline{ABC}$$
, with $AB = 2x + 2$, $AC = 20$. $AB = BC$

Find x.



A *bisector* creates two line segments with the same length *Congruent* line segments are the same length

Given point *B* is the midpoint of \overline{AC} , with AB = x + 7, BC = 17. Find x.

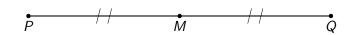


The *midpoint* or *bisector* of a line segment divides it exactly in half.

Congruent means equal in length, $\overline{AB} \cong \overline{BC}$ (also AB = BC) Mark congruent segments in diagrams with cross "hash" marks.

Check your notes

M bisects \overline{PQ}



Bisect Divide exactly in half

Midpoint The point in the exact middle of a line segment

Congruent Equal in length or measure. $\overline{AB} \cong \overline{BC}$ Hash marks Mark congruent segments with small crossways lines (also called "tick" marks)

Spicy: *Trisect* a segment into three congruent parts

Points B and C trisect segment \overline{AD} with segment lengths as shown. Find x.

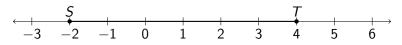
Trisect Divide exactly in three equal parts
Partition Cut into parts (not necessarily evenly)

Learning Target: I can work with objects having congruent parts

CCSS: HSG.CO.A.1 Know precise geometric definitions

1.5 Wednesday 14 Sept

Do Now: Given \overline{ST} with S(-2) and T(4)



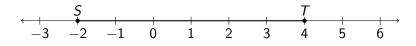
What is the length of the segment \overline{ST} ? Show your work as an equation.

Lesson: Perimeter, congruent line segments in rectangles & isosceles triangles

Negative number practice on a number line

Take the difference in the points' values. Check by counting the marks.

Given ST with S(-2) and T(4), as shown on the number line.



What is the length of the segment \overline{ST} ? Show your work as an equation.

Solution

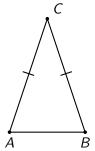
$$ST = 4 - (-2) = 6$$

Why is "minus a negative" the same as add a positive?

An isosceles triangle has two congruent sides

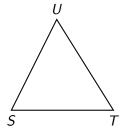
Given isosceles $\triangle ABC$. Which two sides are congruent?

Write your answer using symbols (i.e. two segments and \cong)



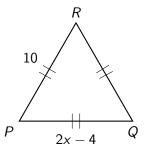
On the diagram mark the congruent line segments with tick marks.

Given isosceles $\triangle STU$ with $\overline{ST} \cong \overline{TU}$.



An equilateral triangle has all three sides congruent

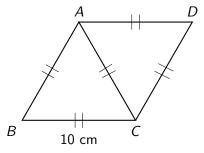
Given equilateral $\triangle PQR$ with PQ = 2x - 4, PR = 10. Find x.



The perimeter is the distance around the triangle. Find the perimeter of $\triangle PQR$.

A *quadrilateral* has four sides

Given two adjacent equilateral \triangle s, $\triangle ABC$ and $\triangle ACD$. All sides measure 10 cm.



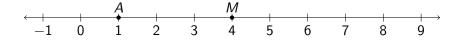
Find the perimeter of the quadrilateral ABCD.

Check your notes

Equilateral Triangle with all three sides congruent
Isosceles Triangle having two sides of the same length
Scalene Triangle without any sides of matching lengths
Quadrilateral A four-sided figure (examples: square, rectangle, parallelogram, rhombus, kite)
Perimeter The total length around a figure (all sides added)
Adjacent "next to", two things that are side by side

Spicy: Given the midpoint, find an end point

Points A(1), M(4), and B lie on a numberline. M bisects \overline{AB} . Find B.



Learning Target: I can collaborate in review

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.6 Thursday 15 September

Do Now: Given the points X and Y, draw \overrightarrow{YX} .

(careful! which direction does it go?)





Lesson: Roundtable quiz review

Groupwork review for quiz tomorrow

"Roundtable" of four students, with four topics assigned

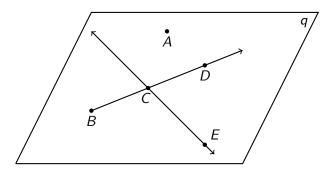
Geometry skills to study / teach

- 1. Conventions: terminology, notation, diagramming
- 2. Perimeter and special shapes:
 - ► Scalene, isosceles, and equilateral △s
 - Squares, rectangles, rhombuses, kites
- 3. Modeling situations with algebra
- 4. Solving algebraic equations for one variable

Identify each item.

Example of Topic 1: Conventions: terminology, notation, diagramming

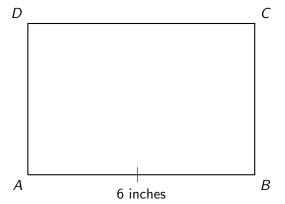
- 1. The point A
- 2. The ray \overrightarrow{BD}
- 3. The name of the plane



Find the perimeter of the rectangle ABCD finish

Example of Topic 2: Perimeter and special triangles and quadrilaterals

Given AB = 6 inches, BC = 4 inches.

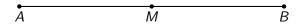


Write down an equation to represent the situation

Example of Topic 3: Modeling situations with algebra

Given M is the midpoint of \overline{AB} , AM = 4x + 2, AB = 20.

First mark the diagram with hash marks and values.



Sometimes you will not be asked to solve the equation.

Solve for *x*

Example of Topic 4: Solving algebraic equations for one variable

Given
$$\overline{LMN}$$
, $LM = 3x + 1$, $MN = 7$, $LN = 17$.

$$3x + 7 = 17$$

You must check the solution.

Learning Target: I can change units of length

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.7 Friday 16 September

Do Now: Mike is six feet tall. How many inches is that?

Conversion ratio: 1 foot = 12 inches

Exit note quiz today

Formal meanings of sketch, draw, and construct

- Sketch is to make a freehand diagram of important features.
 Use a pencil to write carefully in your notebook or on paper.
- Draw is to depict with accurate measures using ruler, protractor, and compass.
 For example, draw a diagram of your room.
- 3. *Construct* is a formal, logical process to create geometric figures using only a straightedge and compass.
- Drawn to scale means that all of the lengths are proportional.
 (e.g. a "scale model")
 - Tests will often warn that diagrams are "not drawn to scale"