Unit 1: Segments, length, and area

23 Sept 2022

## Name:

## 1.13 Extra problems

1. Draw the ray  $\overrightarrow{WV}$  with a straight edge (or ruler). Measure VW in centimeters.



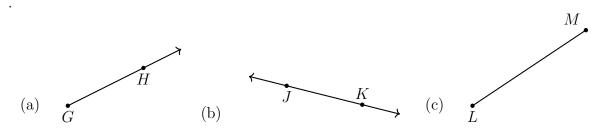


2. Draw the ray  $\overrightarrow{ST}$  with a straight edge (or ruler). Measure ST in centimeters.

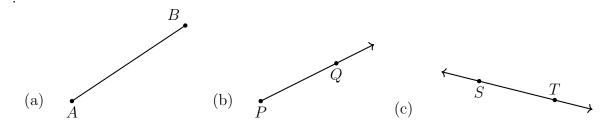


 $\overset{\bullet}{T}$ 

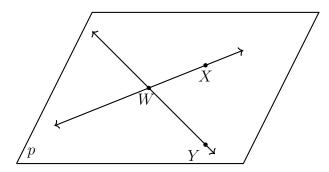
- 3. A flat surface is a(n) \_\_\_\_\_
- 4. Two line segments or angles of equal measure are \_\_\_\_\_\_.
- 5. Use conventional notation to write the names of the ray, line, and segment shown.



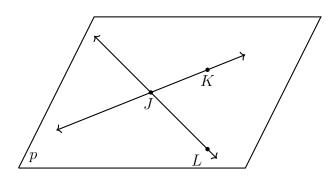
- 6. Points that are all located on the same plane are \_\_\_\_\_
- 7. Two rays with a common vertex compose a(n) \_\_\_\_\_\_.
- 8. Points that are all located on the same line are \_\_\_\_\_\_.
- 9. Use conventional notation to write the names of the ray, line, and segment shown.



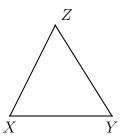
- 10. Two line segments or angles of equal measure are \_\_\_\_\_
- 11. Identify three points in the given plane.



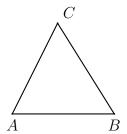
12. Identify two line segments in the given plane.



13. Given isosceles  $\triangle XYZ$  with  $\overline{XY}\cong \overline{XZ}$ . On the diagram mark the congruent line segments with tick marks.



14. Given isosceles  $\triangle ABC$  with  $\overline{AB}\cong \overline{AC}$ . On the diagram mark the congruent line segments with tick marks.



15. Given  $\overline{ABC}$ , AB = 29, and BC = 63. Find AC.



16. Given  $\overline{ABC}$ , AB = 84, and AC = 116. Find BC.



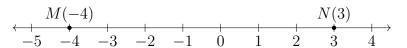
17. Given  $\overline{DEF}$ ,  $DE = 7\frac{1}{3}$ , and  $EF = 3\frac{1}{6}$ . Find DF.



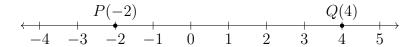
18. Given  $\overline{DEF}$ ,  $DE = 5\frac{1}{14}$ , and  $DF = 9\frac{4}{7}$ . Find EF. State as a fraction.



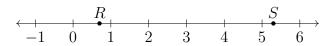
19. Find the distance between M and N.



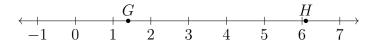
20. Find the distance between P and Q.



21. Find RS, given R = 0.7 and S = 5.3.



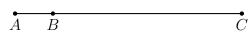
22. Find GH, given G = 1.4 and H = 6.1.



23. Given  $\overline{ABC}$ ,  $AB = \frac{2}{3}$ , and  $AC = 3\frac{1}{3}$ .

Find BC.

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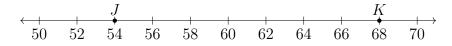
24. Given  $\overline{DEFG}$ ,  $DE = 3\frac{1}{4}$ ,  $EF = 6\frac{1}{4}$ , and  $FG = 1\frac{3}{4}$ . (diagram not to scale) Find DG, expressed as a fraction, not a decimal.



25. Given  $\overline{FGHI}$ ,  $FG=8\frac{1}{6}$ ,  $GH=12\frac{1}{3}$ , and  $HI=5\frac{1}{2}$ . (diagram not to scale) Find FI.



26. Given  $\overrightarrow{JK}$  as shown on the number line.

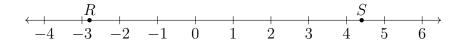


What is the midpoint between the points J and K?

27. The point M(2.3) is the midpoint of segment  $\overline{AB}$ . Given A(-1.5), find the value of B. Mark and label it below.

$$A(-1.5)$$
  $M(2.3)$   $\leftarrow$   $-2$   $-1$   $0$   $1$   $2$   $3$   $4$   $5$   $6$   $7$   $8$ 

28. Given  $\overrightarrow{RS}$  as shown on the number line, with R = -2.8 and S = 4.4.

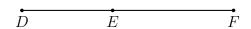


The points T and U trisect  $\overline{RS}$ . Find their values, and mark and label them on the number line.

29. Given  $\overline{ABC}$ , AB = 84, AC = 116. Find BC.



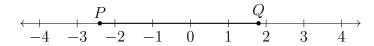
30. Given  $\overline{DEF}$ ,  $DE = 3\frac{1}{3}$ , and  $EF = 4\frac{1}{6}$ . Find DF.



31. Given  $\overline{DEFG}$ ,  $DE = 3\frac{1}{4}$ ,  $EF = 6\frac{1}{4}$ , and  $FG = 1\frac{3}{4}$ . (diagram not to scale) Find DG, expressed as a fraction, not a decimal.

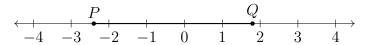


- 32. Given  $\overline{DEFG}$ ,  $DE = 3\frac{1}{4}$ ,  $EF = 6\frac{1}{4}$ , and  $FG = 1\frac{3}{4}$ . (diagram not to scale) Find DG, expressed as a fraction, not a decimal.
- 33. Given P(-2.4) and Q(1.8), as shown on the number line. Find the length of the line segment  $\overline{PQ}$ . State an equation for full credit.



34. Given P(-2.4) and Q(1.8), as shown on the number line.

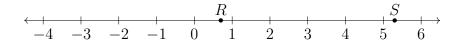
Find the length of the line segment  $\overline{PQ}$ . State an equation for full credit.



35. Given  $\overrightarrow{PQ}$  as shown on the number line. Find PQ.



36. Given  $\overrightarrow{RS}$ , with R = 0.7 and S = 5.3. Find RS, showing the formula.

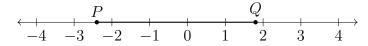


37. Given  $\overline{DEFG}$ ,  $DE = 3\frac{1}{4}$ ,  $EF = 6\frac{1}{4}$ , and  $FG = 1\frac{3}{4}$ . (diagram not to scale) Find DG, expressed as a fraction, not a decimal.



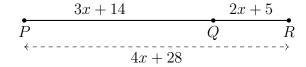
38. Given P(-2.4) and Q(1.8), as shown on the number line.

Find the length of the line segment  $\overline{PQ}$ . State an equation for full credit.



39. Given  $\overline{PQR}$ , PQ = 3x + 14, QR = 2x + 5, PR = 4x + 28.

Write down an equation to represent the situation.



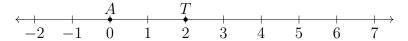
40. Given  $\overline{PQRS}$ . Q is the midpoint of  $\overline{PS}$ , and R bisects  $\overline{QS}$ .

If  $PR = 4\frac{1}{2}$  find PS. Justify your answer.



41. Given A(0) and T(2), as shown on the number line. T is one of the points that trisects  $\overline{AB}$ .

Find B. For full credit, find both solutions.

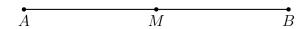


42. Given  $\overline{DEFG}$ ,  $DE = 1\frac{2}{5}$ ,  $EF = 2\frac{3}{10}$ , and  $FG = \frac{4}{5}$ . (diagram not to scale)

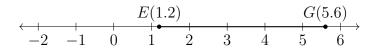
Find DG, expressed as a fraction, not a decimal.



- 43. Given M is the midpoint of  $\overline{AB}$ , AM = 7x + 1, MB = 33 x.
  - (a) Mark the diagram with the values and tick marks
  - (b) Write an equation that could be solved for x

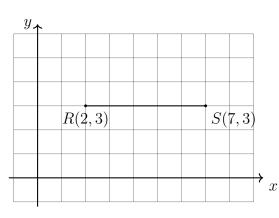


44. Given points on the number line E(1.2) and G(5.6) as shown. Find the midpoint F of  $\overline{EG}$ . Mark it on the number line and label it as an ordered pair.



45. The horizontal line segment  $\overline{RS}$  is plotted on the coordinate plane with R(2,3) and S(7,3).

Find length RS, showing the calculation.

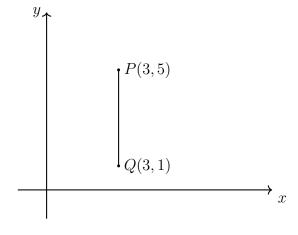


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46. The vertical line segment  $\overline{PQ}$  is plotted on the coordinate plane with P(3,5) and Q(3,1).

Find the length PQ.

Show the calculation, including the absolute value bars.



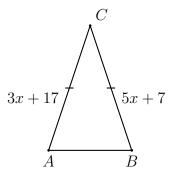
Do Not Solve! Make a drawing on the right, an equation to the left, and circle where it states what to find.

- 47. The point Q is the midpoint of  $\overline{PR}$ , PQ = 11, and QR = 2x + 1. Find x.
- 48. Given  $\overline{PQR}$ , with PQ = 3x 7, QR = x + 3, and PR = 12. Find x.
- 49. Given that Q bisects  $\overline{PR}$ . PQ = 2x 5, PR = 42. Find x.
- 50. The points P, Q, and R are collinear, with PQ = x + 4 and PR = 27.  $\overline{QR}$  is twice the length of  $\overline{PQ}$ . Find x.

Do Not Solve! Draw and label the situation on the right, model with an equation to the left, and circle where it states what to find.

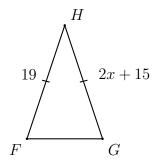
- 51. Given  $\overline{ABC}$ , with AB = 2x 7, BC = 3x 3, and AC = 15. Find AB.
- 52. Given that K bisects  $\overline{JL}$ . JK = 3x + 8, KL = 17. Find x.
- 53. The point M is the midpoint of  $\overline{UV}$ , UM = x + 7, and MV = 2x + 1. Find UV.
- 54. The points P, Q, and R are collinear, with PQ = 6x + 16 and PR = 42.  $\overline{QR}$  is half the length of  $\overline{PQ}$ . Find x.

55. Given isosceles  $\triangle ABC$  with  $\overline{AC} \cong \overline{BC}$ . AC = 5x + 7 and BC = 3x + 17. Find AC.



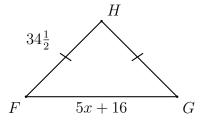
56. The isosceles  $\triangle FGH$  is shown with  $\overline{FH} \cong \overline{GH}$ . Given GH = 2x + 15 and FH = 19.

Write an equation that could be used to find x.

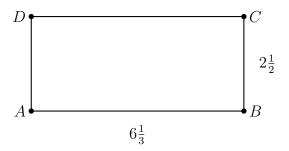


57. The perimeter of the isosceles  $\triangle FGH$  is 115 and  $\overline{FH}\cong \overline{GH}$ . Given FG=5x+16 and  $FH=34\frac{1}{2}$ .

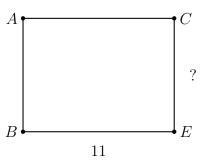
Write an equation that could be used to find x.



58. Given the rectangle ABCD shown below, with  $AB = 6\frac{1}{3}$  and  $BC = 2\frac{1}{2}$ . Find the area of the rectangle, expressing your result as a fraction.

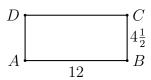


- 59. A triangle has an area of 68 square centimeters. Its height is 16 centimeters. Find the length of its base.
- 60. A triangle has an area of 75 square centimeters. Its height is 12 centimeters. Find the length of its base.
- 61. The rectangle BECA has an area of 77, with length BE = 11.
  - (a) Write an equation with the unknown w as the width of the rectangle.
  - (b) Solve.



62. Find the area of rectangle ABCD having length l=12 and width  $w=4\frac{1}{2}$ . Start with a formula of this form, substituting the given values:

$$A = l \times w$$



63. Rectangle ABCD has area A=15 and base b=6 but unknown height. Write an equation then solve. Start with this form (for the unknown, use h, x, or BC) and state your answer as a fraction:

 $A = b \times h = 15$ 

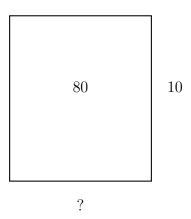
$D \vdash$		$\neg C$
	A = 15	?
$_A$ $lacksquare$		$\exists B$
A	6	· D

64. Find the base of a rectangle with area A = 16.8 and height h = 4.8, expressed as a decimal. First write an equation substituting the given values in the area formula.

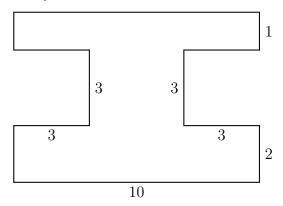
$$A = 16.8 = 4.8$$

65. Find the length of the base of a rectangle with area A=80 and height h=10. Start with the form (use b or x):

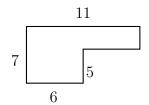
$$A = b \times h = 80$$



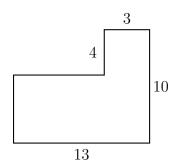
66. The shape shown below is composed of straight lines and right angles, with some lengths as marked. Find the perimeter of the figure. Show your work.



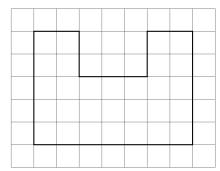
67. Find the area and perimeter of the shape shown below. Mark the missing side lengths



68. Find the area and perimeter of the shape shown below. Mark the missing side lengths first. All angles are 90°. (not drawn to scale)



69. Find the area A of the shape shown below in terms of unit squares.

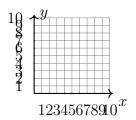


70. On the grid below, accurately draw and label two adjacent squares, one with a side length of 4 cm, the other with a side length of 3 cm. The grid is in centimeters.

Find the area A and perimeter P of combined shape.

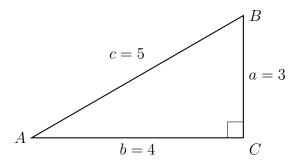


71. On the graph, draw polygon ABCDEF with vertices A(1, 1), B(1, 4), C(3, 4), D(3, 7), E(8, 7), and F(8, 1). Find the perimeter and the area of the polygon.

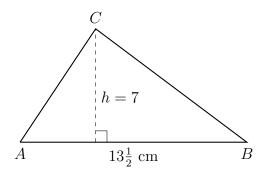


72. Draw and label a triangle  $\triangle ABC$  with base  $\overline{AB}$  8 centimeters long and altitude of 5 centimeters. (show the altitude as a dotted line, and make sure it is perpendicular to the base)

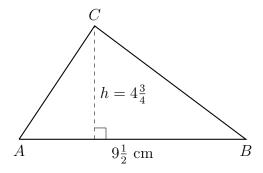
73. Find the area of  $\triangle ABC$  shown below (not actual size) with  $m \angle C = 90^{\circ}$  and the lengths of the triangle's sides as a = 3, b = 4, and c = 5.



74. Find the area of  $\triangle ABC$ . The altitude h of the triangle is 7 centimeters and the base  $AB=13\frac{1}{2}$  cm. (diagram not to scale)



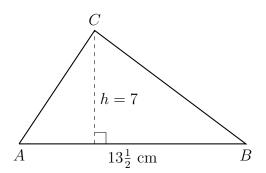
75. Find the area of  $\triangle ABC$ . The altitude h of the triangle is  $4\frac{3}{4}$  centimeters and the base  $AB = 9\frac{1}{2}$  cm. (diagram not to scale)



76. Find the area of  $\triangle ABC$ . The altitude h of the triangle is 7 centimeters and the base  $AB=13\frac{1}{2}$  cm. (diagram not to scale)

Unit 1: Segments, length, and area

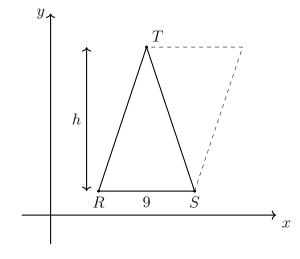
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77. Find the height of the  $\triangle RST$ , having an area of A=117 and base RS=9.

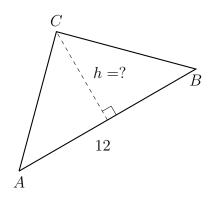
Start by substituting values in the area formula:

$$A = \frac{1}{2}bh = 117$$

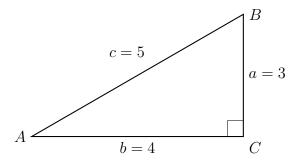


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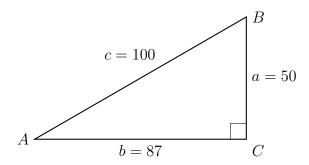
78. One side of the  $\triangle ABC$  has a length AB=12. The triangle's area is 60. Find the length of the altitude h of the triangle to vertex C and perpendicular to side  $\overline{AB}$ .



79. Find the area of  $\triangle ABC$  shown below (not actual size) with  $m \angle C = 90^{\circ}$  and the lengths of the triangle's sides as a = 3, b = 4, and c = 5.

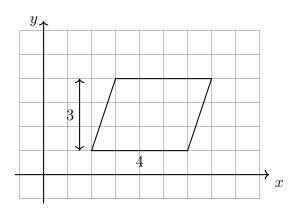


80. Find the area of  $\triangle ABC$  shown below (not actual size) with  $m \angle C = 90^{\circ}$  and the lengths of the triangle's sides as a = 50, b = 87, and c = 100.



81. A parallelogram is shown on the x-y plane having a base b=4 and height h=3.

Find its area, showing the calculation.



Name:

82. The  $\triangle ABC$  is shown below with A(3,1), B(7,1), and C(1,5). The length of the base of the triangle is AB = 4.

(a) Find the height h.

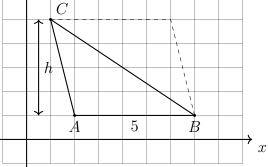
CA4 В  $\boldsymbol{x}$ 

(b) Find the triangle's area, showing the calculation.

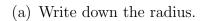
83. The  $\triangle ABC$  is shown below with A(2,1), B(7,1), and C(1,5). The length of the base of the triangle is AB = 5.

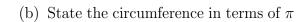
(a) Find the height h.

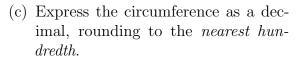
(b) Find its area, showing the calculation.

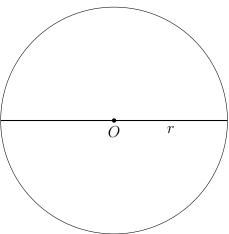


84. Find the radius and circumference of circle O with diameter D=15 centimeters.



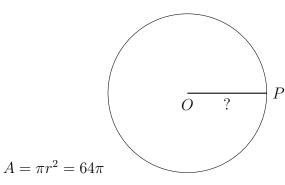






85. Given circle O with area  $A=64\pi$  square centimeters.

Find the radius of circle, OP. Start with the formula

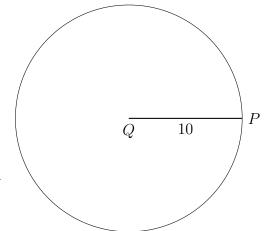


86. Find the area of the given circle Q with radius r=10 centimeters.

Start with the formula

$$A = \pi r^2$$

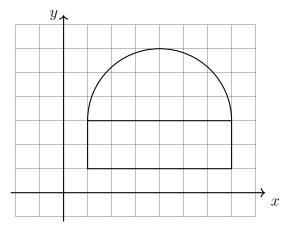
(a) State the area in terms of  $\pi$ 



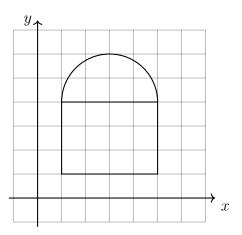
(b) Now round to the nearest hundredth

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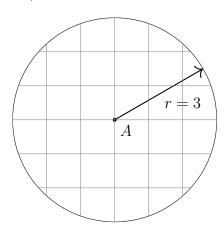
87. Find the area of the shape shown below composed of a rectangle and circular cap. Leave your answer as an exact value in terms of  $\pi$ .



88. Find the *perimeter* of the shape shown below composed of a rectangle and circular cap. Leave your answer as an exact value in terms of  $\pi$ .



- 89. Given the circle A with radius r=3. Leave exact answers, in terms of  $\pi$ .
  - (a) Find the circumference of circle A.
  - (b) Find the area of the circle.



## Challenge problems

90. A square is partitioned into rectangles is 36. Find the area	~	The sum of the perimeters of the two