

Section A

1. [Maximum mark: 5]

(a) Find the coordinates of M. [2]

(b) Find the gradient of L . [2]

(c) Hence, write down the equation of L . [1]

[illegible]

Full marks are not necessarily awarded for a correct answer with no working. Answers must be supported by working and/or explanations. Where an answer is incorrect, some marks may be given for a correct method, provided this is shown by written working. You are therefore advised to show all working.

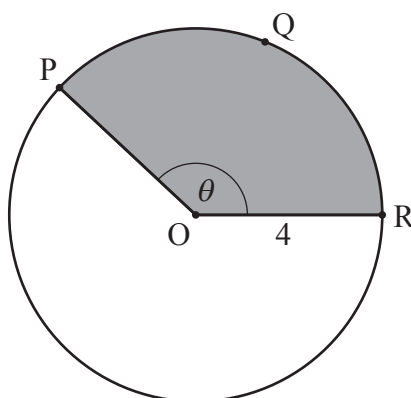
Section A

Answer **all** questions. Answers must be written within the answer boxes provided. Working may be continued below the lines, if necessary.

1. [Maximum mark: 6]

The following diagram shows a circle with centre O and radius 4 cm .

diagram not to scale



The points P , Q and R lie on the circumference of the circle and $\angle POR = \theta$, where θ is measured in radians.

The length of arc PQR is 10 cm .

- (a) Find the perimeter of the shaded sector. [2]
- (b) Find θ . [2]
- (c) Find the area of the shaded sector. [2]

(This question continues on the following page)



(Question 1 continued)

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3. [Maximum mark: 5]

A function f is defined by $f(x) = 1 - \frac{1}{x-2}$, where $x \in \mathbb{R}$, $x \neq 2$.

- (a) The graph of $y = f(x)$ has a vertical asymptote and a horizontal asymptote.

Write down the equation of

- (i) the vertical asymptote;
- (ii) the horizontal asymptote.

[2]

- (b) Find the coordinates of the point where the graph of $y = f(x)$ intersects

- (i) the y -axis;
- (ii) the x -axis.

[2]

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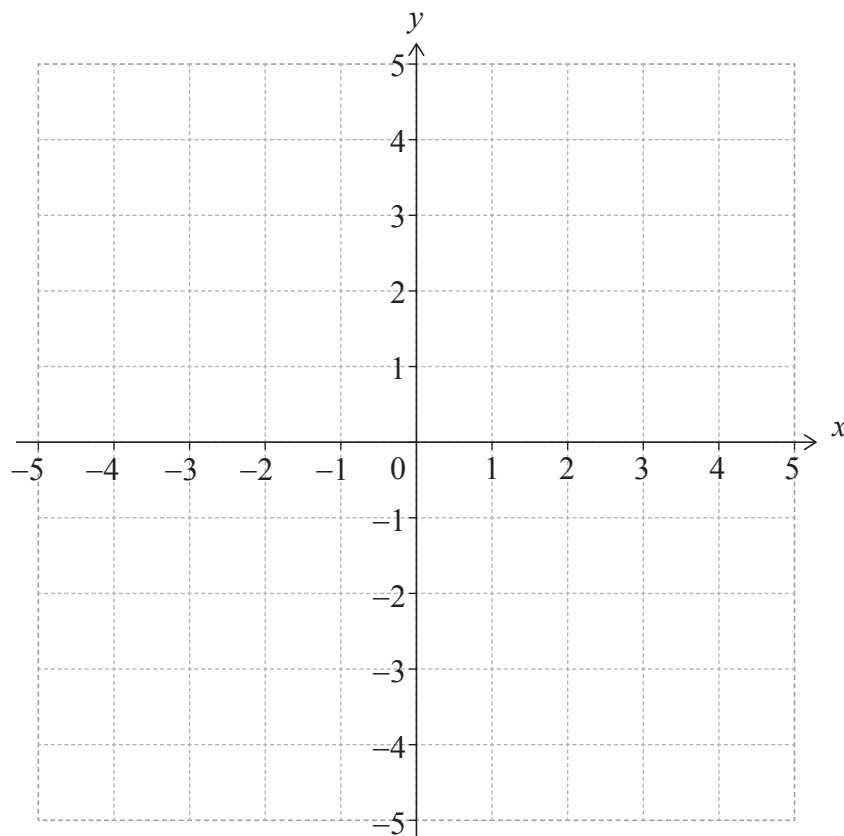
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(Question 3 continued)

- (c) On the following set of axes, sketch the graph of $y = f(x)$, showing all the features found in parts (a) and (b).

[1]



2. [Maximum mark: 7]

The function f is defined by $f(x) = \frac{7x+7}{2x-4}$ for $x \in \mathbb{R}$, $x \neq 2$.

(a) Find the zero of $f(x)$. [2]

(b) For the graph of $y = f(x)$, write down the equation of

(i) the vertical asymptote;

(ii) the horizontal asymptote. [2]

(c) Find $f^{-1}(x)$, the inverse function of $f(x)$. [3]

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3. [Maximum mark: 6]

On a Monday at an amusement park, a sample of 40 visitors was randomly selected as they were leaving the park. They were asked how many times that day they had been on a ride called *The Dragon*. This information is summarized in the following frequency table.

Number of times on <i>The Dragon</i>	Frequency
0	6
1	16
2	13
3	2
4	3

It can be assumed that this sample is representative of all visitors to the park for the following day.

(a) For the following day, Tuesday, estimate

(i) the probability that a randomly selected visitor will ride *The Dragon*;

(ii) the expected number of times a visitor will ride *The Dragon*. [4]

It is known that 1000 visitors will attend the amusement park on Tuesday. *The Dragon* can carry a maximum of 10 people each time it runs.

(b) Estimate the minimum number of times *The Dragon* must run to satisfy demand. [2]

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5. [Maximum mark: 6]

Find the range of possible values of k such that $e^{2x} + \ln k = 3e^x$ has at least one real solution.

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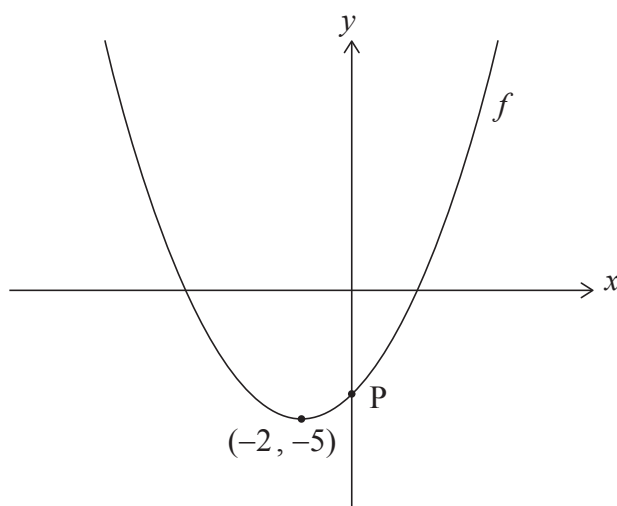
Section B

Answer **all** questions in the answer booklet provided. Please start each question on a new page.

7. [Maximum mark: 17]

The following diagram shows part of the graph of a quadratic function f .

The vertex of the parabola is $(-2, -5)$ and the y -intercept is at point P.



(a) Write down the equation of the axis of symmetry.

[1]

The function can be written in the form $f(x) = \frac{1}{4}(x-h)^2 + k$, where $h, k \in \mathbb{Z}$.

(b) Write down the values of h and k .

[2]

(c) Find the y -coordinate of P.

[2]

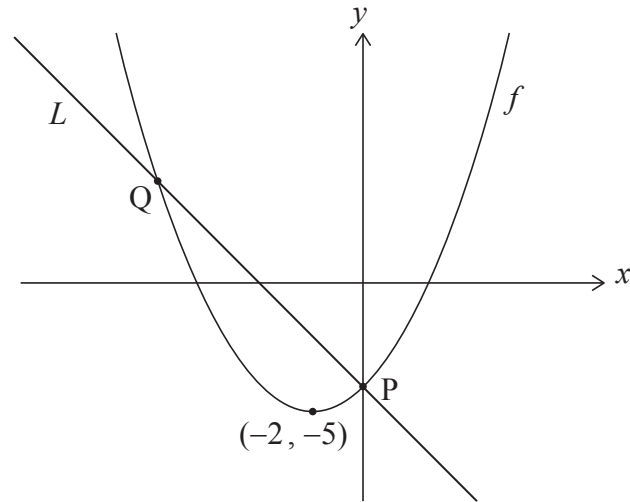
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(Question 7 continued)

In the following diagram, the line L is normal to the graph of f at point P .



- (d) Find the equation of the line L , in the form $y = ax + b$. [4]

The line L intersects the graph of f at a second point, Q , as shown above.

- (e) Calculate the distance between P and Q . [8]



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8. [Maximum mark: 14]

Consider the arithmetic sequence u_1, u_2, u_3, \dots

The sum of the first n terms of this sequence is given by $S_n = n^2 + 4n$.

- (a) (i) Find the sum of the first five terms. [4]
- (ii) Given that $S_6 = 60$, find u_6 . [2]
- (b) Find u_1 . [3]
- (c) Hence or otherwise, write an expression for u_n in terms of n . [3]

Consider a geometric sequence, v_n , where $v_2 = u_1$ and $v_4 = u_6$.

- (d) Find the possible values of the common ratio, r . [3]
- (e) Given that $v_{99} < 0$, find v_5 . [2]

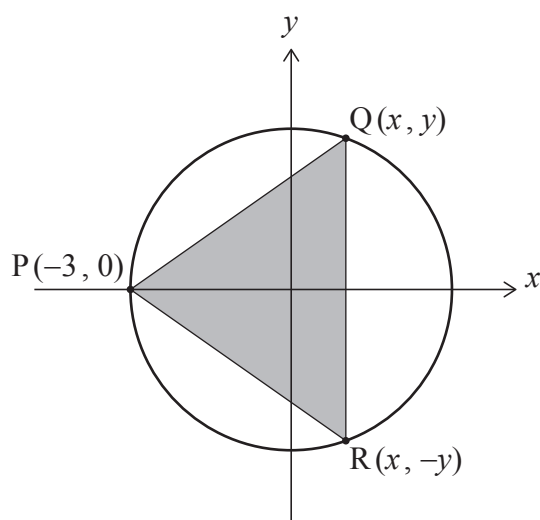


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9. [Maximum mark: 14]

A circle with equation $x^2 + y^2 = 9$ has centre $(0, 0)$ and radius 3.

A triangle, PQR, is inscribed in the circle with its vertices at $P(-3, 0)$, $Q(x, y)$ and $R(x, -y)$, where Q and R are variable points in the first and fourth quadrants respectively. This is shown in the following diagram.



- (a) For point Q, show that $y = \sqrt{9 - x^2}$. [1]
- (b) Hence, find an expression for A , the area of triangle PQR, in terms of x . [3]
- (c) Show that $\frac{dA}{dx} = \frac{9 - 3x - 2x^2}{\sqrt{9 - x^2}}$. [4]
- (d) Hence or otherwise, find the y -coordinate of R such that A is a maximum. [6]

References:

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