3.5 Trimester Final Exam

A2.A.APR.6

A2-APR.1 Perform operations with polynomials

1. Find the sum in standard form $(x^2 - 4x - 7) + (2x^2 - 2x + 11)$.

2. Find the difference f(x) - g(x) as a polynomial in standard form, given $f(x) = 3x^4 - 2x^3 + 5x^2 - 3x + 4$ and $g(x) = 2x^4 + 2x^2 + x - 1$.

3. Select each correct equation.

(a)
$$x^2 - 25 = x^2 - 5^2$$

(d)
$$x^2 - 10x + 25 = (x - 5)^2$$

(b)
$$x^2 - 25 = (x - 5)(x + 5)$$

(e)
$$x^2 + 10x + 25 = (x+5)^2$$

(c)
$$x^2 + 25 = (x - 5)(x + 5)$$

(f)
$$x^2 - 10x - 25 = (x - 5)^2$$

4. Which equations represent correct polynomial identities?

(a)
$$x^3 - y^3 = (x - y)^3$$

(c)
$$x^3 + y^3 = (x+y)(x^2 - xy + y^2)$$

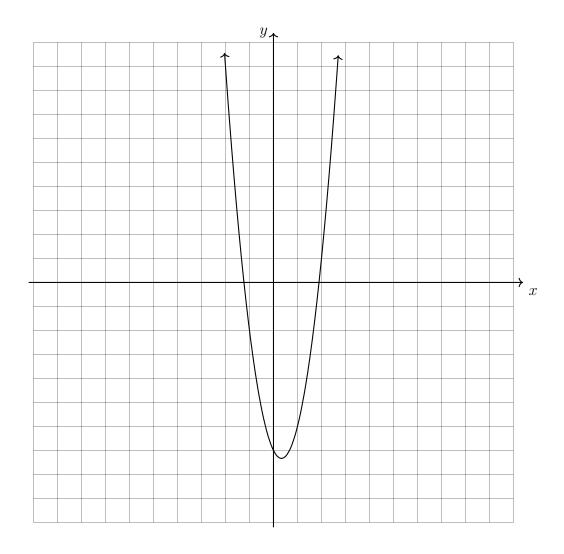
(b)
$$x^3 - y^3 = (x - y)(x^2 + xy + y^2)$$
 (d) $x^3 + y^3 = (x - y)(x^2 + xy + y^2)$

(d)
$$x^3 + y^3 = (x - y)(x^2 + xy + y^2)$$

A2-F.IF.7a Graph linear and quadratic functions, show key features

- 5. One equation of a system is graphed.
 - (a) Graph the second equation, labeling the intersections as ordered pairs.
 - (b) Find the value of the leading coefficient a of the quadratic equation.

$$y = ax^2 - 2x - 7 \qquad \qquad x - y = 1$$



A2-A.APR.3 Identify zeros of polynomials given suitable factorizations

- 6. Write down the solutions to the equation x(3x-1)(x+5)(x-1)=0.
- 7. The polynomial p is a function of x. The graph of p has three zeros at 7, $\frac{2}{3}$, and -1. Select all the expressions that could represent p.

(a)
$$(x-7)(x-\frac{2}{3})(x+1)$$

(e)
$$(x-7)(x+\frac{2}{3})(x-1)$$

(b)
$$(x-7)(3x-2)(x-1)$$

(f)
$$(x-7)(3x-2)(x+1)$$

(c)
$$3(x-7)(x-\frac{2}{3})(x+1)$$

(g)
$$3(x-7)(x-\frac{2}{3})(x-1)$$

(d)
$$3x(x+7)(x+\frac{2}{3})(x-1)^2$$

(h)
$$3x(x+7)(x-\frac{2}{3})(x+1)^2$$

A2-A.APR.6 Rewrite rational expressions in different forms

8. Select the expression that is equivalent to $\frac{2x^2 + 11x - 21}{x+3}$ for $x \neq -3$.

(a)
$$2x + 5 - \frac{6}{x+3}$$

(b)
$$2x + 17 - \frac{20}{x+3}$$

(c)
$$2x + 17 - \frac{36}{x+3}$$

(d)
$$2x + 5 - \frac{36}{x+3}$$

A2-A.SSE.3c Apply the properties of exponents

9. Identify the expressions that are equal to $\frac{3^3}{3^5}$

(a) 3^{-2}

(d) 3^8

(b) $\frac{1}{9}$

(e) $\frac{1}{3^2}$

(c) 3^3

(f) 0.111

10. Identify the expressions that are equal to 5^{-2}

(a) $\frac{1}{5^2}$

(d) $\frac{1}{25}$

(b) 5.5

(e) 0.04

(c) $\sqrt{5}$

(f) 10

11. Identify the expressions that are equal to $16^{\frac{1}{4}}$

(a) 2

(d) $\sqrt[4]{16}$

(b) 4

(e) 16.25

(c) $\sqrt{4}$

(f) 256

A2-F.BF.2 Write arithmetic and geometric sequences with recursive formulas

12. Write a recursive definition of the sequence $a_1=8,\,a_2=4,\,a_3=2,\,a_4=1,\ldots$

13. Write a recursive definition of the arithmetic sequence b.

n	b_n
1	-2
2	-0.5
3	1

A2-F.IF.7c Graph polynomials, identify zeros, end behavior

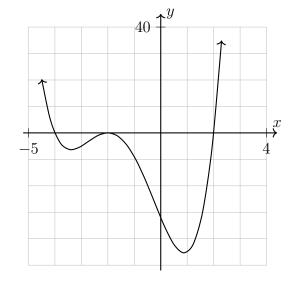
- 14. Below is a graph of the polynomial f(x).
 - (a) Is the leading coefficient positive or negative?
 - (b) Which of the following could be its equation?

i.
$$f(x) = (x+2)(x-4)(x-2)^2$$

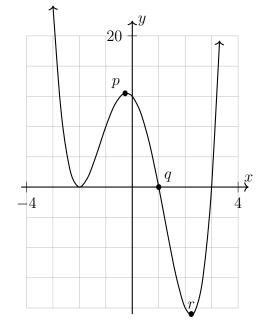
ii.
$$f(x) = (x-2)(x-4)(x+2)^2$$

iii.
$$f(x) = (x+2)(x+4)(x-2)^2$$

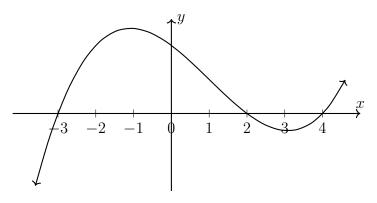
iv.
$$f(x) = (x-2)(x+4)(x+2)^2$$



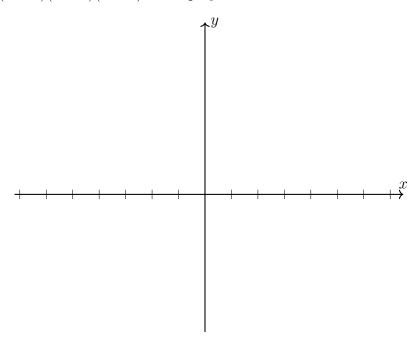
- 15. The graph of the polynomial $f(x) = x^4 9x^2 4x + 12$ is shown.
 - (a) What is the degree of the function?
 - (b) What are the zeros of the function?
 - (c) Which factor has a multiplicity of 2?
 - (d) Write down the y-intercept as an ordered pair.
 - (e) Three points are marked on the graph, p, q, and r. Which one is a local minimum?



16. The graph of the function $f(x) = x^3 - 3x^2 - 10x + 24$ is shown. Write the function in factored form.



17. Let $j(x) = (x+4)(x+1)(x-4)^2$ be a polynomial function.



- (a) Sketch a graph of the function. Label the x-intercepts.
- (b) Find the value of the y-intercept and mark it on the graph.
- (c) Identify the end behavior of the function.

i. As
$$x \to +\infty$$
, $y \to +\infty$;
as $x \to -\infty$, $y \to -\infty$

iii. As
$$x \to +\infty$$
, $y \to +\infty$; as $x \to -\infty$, $y \to +\infty$

ii. As
$$x \to +\infty$$
, $y \to -\infty$; as $x \to -\infty$, $y \to +\infty$

iv. As
$$x \to +\infty$$
, $y \to -\infty$;
as $x \to -\infty$, $y \to -\infty$

6.EE.b Reason about and solve one-variable equations and inequalities

- 18. Use the function $f(x) = \frac{1}{2}x + 11$ to answer the questions.
 - (a) Find the value of f(4).

(b) Solve for x if f(x) = 2.

19. Solve each equation for x.

(a)
$$x^2 + 5x + 6 = 0$$

(b)
$$x^3 - 7x^2 + 6x = 0$$

20. The expression $2 - \frac{x-1}{x+2}$ is equivalent to

(a)
$$1 - \frac{3}{x+2}$$

(c)
$$1 - \frac{1}{x+2}$$

(b)
$$1 + \frac{3}{x+2}$$

(d)
$$1 + \frac{1}{x+2}$$

21. Find all of the values of x that make the equation true.

$$\frac{3}{x-4} = \frac{x-5}{x}$$

- 22. Given the rational function $r(x) = 3 \frac{x-1}{x+2}$.
 - (a) Sketch a graph of the function.
 - (b) Mark the vertical asymptote as dotted line and label it with its equation.
 - (c) Explain why the asymptote is located there.

