

Solutions

## Lesson 4 Practice Problems

1. Evaluate  $8^{\frac{5}{3}}$ .  $= (\sqrt[3]{8})^5 = 2^5 = 32$

2. Select all expressions that are equal to  $64^{\frac{3}{2}}$ .  $= (\sqrt[2]{64})^3 = 8^3 = 512$

A. 96

☒ B.  $8^3$

☒ C. 512

D.  $4^2$

☒ E.  $\sqrt{64^3}$

F.  $\sqrt[3]{64^2}$

3. Write the expression  $17^{\frac{4}{3}}$  using radicals.

$$\sqrt[3]{17^4}$$

4. An arithmetic sequence  $k$  starts 4, 13, ... Explain how you would calculate the value of the 5,000th term.

+9

$$a_1 = 4$$

$$d = 9$$

$$k_{5000} = 4 + 9(5000 - 1)$$

(From Unit 1, Lesson 8.)

5. Select **all** items equivalent to  $\sqrt{24}$ .

- A. the area of a square with side length 24 units ✗
- ☒ B. the side length of a square with area 24 square units
- ☒ C. the positive number  $x$ , where  $x \cdot x = 24$
- D. the positive number  $y$ , where  $y = 24 \cdot 24$  ✗
- E. the edge length of a cube with volume 24 cubic units ✗
- F. the volume of a cube with edge length 24 units ✗

(From Unit 3, Lesson 2.)

6. Which expression is equivalent to  $23^{\frac{1}{2}}$ ?

- A.  $\frac{1}{23}$
- B.  $\frac{1}{\sqrt{23}}$
- C. 11.5
- ☒ D.  $\sqrt{23}$

(From Unit 3, Lesson 3.)

## Lesson 5 Practice Problems

1. Write each expression in the form  $a^b$ , without using any radicals.

a.  $\sqrt{5^9} = 5^{\frac{9}{2}}$

b.  $\frac{1}{\sqrt[3]{12}} = 12^{-\frac{1}{3}}$

2. Write  $32^{-\frac{2}{5}}$  without using exponents or radicals.

$$= \frac{1}{(\sqrt[5]{32})^2} = \frac{1}{2^2} = \frac{1}{4}$$

3. Match the equivalent expressions.

A. $8^{\frac{1}{3}}$	5. $2^{\frac{1}{2}}$	①. $\frac{1}{8}$
B. $8^{-\frac{1}{3}}$	3. $\frac{1}{2}$	②. $\frac{1}{4}$
C. $8^{-1}$	1. $\frac{1}{8}$	③. $\frac{1}{2}$
D. $16^{\frac{1}{2}}$	6. 4	④. 1
E. $16^{-\frac{1}{2}}$	2. $\frac{1}{4}$	⑤. 2
F. $16^0$	4. 1	⑥. 4

4. Complete the table. Use powers of 27 in the top row and radicals or rational numbers in the bottom row.

$27^1$	$27^{\frac{1}{2}}$	$27^{\frac{1}{3}}$	$27^0$	$27^{-\frac{1}{2}}$	$27^{-\frac{1}{3}}$
27	$\sqrt{27}$	$\sqrt[3]{27}$ = 3	1	$\frac{1}{\sqrt{27}}$	$\frac{1}{3}$

(From Unit 3, Lesson 3.)

5. What are the solutions to the equation  $(x - 1)(x + 2) = -2$ ?

$$\begin{aligned} x^2 + x - 2 &= -2 \\ x^2 + x &= 0 \\ x(x+1) &= 0 \\ x &= 0, x = -1 \end{aligned}$$

$$\begin{aligned} (0-1)(0+2) &= -2 \\ (-1-1)(-1+2) &= -2 \\ (-2)(1) &= -2 \end{aligned}$$

(From Unit 2, Lesson 11.)

6. Use exponent rules to explain why  $(\sqrt{5})^3 = \sqrt{5^3}$ .

(From Unit 3, Lesson 4.)

$$(\sqrt{5})^3 = 5^{\frac{3}{2}} = (5^3)^{\frac{1}{2}} = \sqrt{5^3}$$