# Mathematics Class Slides Bronx Early College Academy

Christopher J. Huson PhD

13-22 September 2021

1.1 1st day of Geometry, Segment addition, 13-14 Sept

1.3 Segment addition, midpoint, 17 Sept

1.4 Number line situations, 20 Sept

1.5 Midpoint calculations; Isosceles triangles, 21 Sept

1.6 Angles and their measures, 22 September

## Learning Target: I can measure and diagram my world

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.1 Tuesday 13-14 Sept

Welcome back to school

Do Now: Measurement

- 1. Notebook first page: Name / Course / Instructor
- 2. Diagram people closest to you and their distance
- 3. Early finishers: Calculate diagonal distances

Supply list: Composition book, looseleaf, pencils & pens, compass and ruler, calculator; Optional: folder

Lesson: Points, line segments, length; Segment addition postulate

Homework: Diagram your bedroom (with measurements), or another room

## Take class notes in a composition book

### Use this notebook format (required)

- 1. In the front, write your name, my contact info, your passwords
- 2. Each page in the top left corner:

First+Last Name

14 September 2021

Learning Target: I can measure and diagram my world

- 3. Copy definitions using your own words
- 4. Write down example diagrams and problems

Point: a location, a dot, has no size; label with capital letter, P

Line segment: two points and all the points between them; label with *end points* and a bar,  $\overline{AB}$ 

## Example: Points and line segments

Shown points P, A, B, C, line segments  $\overline{AB}$ ,  $\overline{BC}$ 



Given AB = 3, BC = 4.

Notation: the length of a line segment is written as the two end points without a bar over them, AB.

## Example: Points and line segments

Segment Addition Postulate

Shown collinear points A, B, C. Given AB = 3, BC = 4.

Find *AC*.



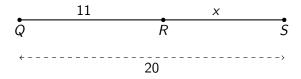
Definition: Points are collinear when they lie on a straight line.

## Example 2: Points and line segments

Segment Addition Postulate

Given collinear points Q, R, S, with QR = 11, QS = 20.

Find RS.



- 1. How would you check your answer?
- 2. Which equation represents the situation?

$$11 + x = 20$$

$$x = 20 - 11$$

## Example 3: Segment addition postulate

Given  $\overline{JKL}$ , JK = 2x + 3, KL = 5, JL = 12. Find x.



1. Write down an equation to represent the situation.

2. Solve for *x*.

3. Check your answer.

## Example 4 (challenge): Segment addition postulate

Given 
$$\overline{ABC}$$
,  $AB = 3x - 7$ ,  $BC = x + 5$ ,  $AC = 14$ . Find  $AB$ .

## Learning Target: I can solve for segment lengths

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.3 Friday 17 Sept Do Now: Given collinear points A, B, C, with AB = 7, AC = 13.

x = 13 - 7

1. Which equation most simply represents the situation?

7 + x = 13

Classwork: Handout (pre-quiz for 6th period)

Lesson: Point, line segment, end point, collinear, distance or length; line, ray, plane, coplanar, *congruent* line segments

Midpoints, bisectors, practice segment addition situations

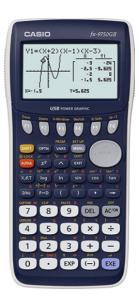
## Casio fx-9750GII calculator - due Friday 1 October

In the high school at BECA we use the Casio fx-9750GII.

It is allowed on the Regents exams, SAT tests, and International Baccalaureate exams.

You may use a different calculator in Geometry if you prefer, but I recommend buying the Casio fx-9750GII.

(see me if buying a calculator is a hardship for your family)



### Review: points, segments, length

Give an example of each geometric object. Use proper notation.

- 1. point
- 2. line segment
- 3. end point
- 4. three collinear points



5. Given TQ = 1.4, QU = 0.6. Find TU.

## More definitions: lines, rays, planes

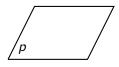
A *line* extends infinitely in both directions,  $\overrightarrow{AB}$ . (sometimes labeled with a small letter, for example, line k)

$$\stackrel{\kappa}{\stackrel{\bullet}{A}} \stackrel{\bullet}{\stackrel{B}{\longrightarrow}}$$

A ray has one end point and extends infinitely in one direction,  $\overrightarrow{CD}$ .

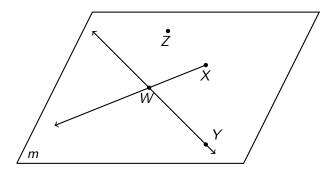
$$C \longrightarrow D$$

A *plane* is flat and extends infinitely in two directions, *p*.



### Several objects are shown in a plane

- 1. T F The name of the plane is m
- 2. T F The line  $\overrightarrow{WY}$  is in the plane
- 3. T F The ray  $\overrightarrow{WX}$  is shown in the plane
- 4. T F Points W, X, and Z are collinear



## Solve for length using the Segment Addition postulate

Given 
$$\overrightarrow{DEF}$$
,  $DE = x + 1$ ,  $EF = 9$ ,  $DF = 3x$ . Find  $DE$ .

## Solve for length using the Segment Addition postulate

Given  $\overrightarrow{DEF}$ , DE = x + 1, EF = 9, DF = 3x. Find DE.



- 1. Sketch and label the situation
- 2. Write a geometric equation
- 3. Substitute algebraic values
- 4. Solve for x
- 5. Answer the question
- 6. Check your answer

## The midpoint of a line segment

Also called the bisector

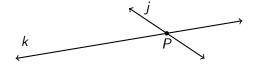
Given 
$$\overline{ABC}$$
, with  $AB = 2x + 2$ ,  $AC = 20$ .  $AB = BC$ 

Find x.

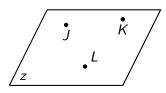
Definition: the *midpoint* or *bisector* of a line segment divides it exactly in half.

### More definitions: intersections, coplanar

Two lines *intersect* if they cross. Their common point is the *intersection*. (shown here, lines j and k intersect at point P)



Coplanar means to lie in the same plane. Three points are always coplanar, but four points may not be.



## Learning Target: I can work with a number line

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.4 Monday 20 Sept

### Do Now: Midpoint calculations

Given point B is the midpoint of  $\overline{AC}$ , with AB = x + 2, BC = 11. Find x.

1.3 Segments scores in Jumprope. Make up if absent Lesson: Number lines, distance and length, absolute value Practice midpoints and segment addition situations

## A bisector creates two line segments with the same length Congruent line segments are the same length

Given point *B* is the midpoint of  $\overline{AC}$ , with AB = x + 2, BC = 11. Find x.

$$X+2$$
 11

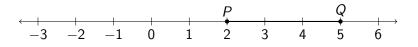
 $A$   $B$   $C$ 

Definition: Congruent means equal in length.  $\overline{AB}\cong \overline{BC}$ We mark congruent segments in diagrams with cross hatch marks.

### A number line is useful for calculating length or distance

Take the difference in the points' values

Given  $\overline{PQ}$  as shown on the number line.



What is the distance on the number line between the points P and Q?

## Absolute value: the distance from a point to the origin Always a positive number (or zero)

The absolute value of 5 is 5. |5| = 5

The absolute value of -3 is 3. |-3|=3

#### Negative number practice on a number line

Take the difference in the points' values. Check by counting the marks.

Given MN with M(-1) and N(3), as shown on the number line.

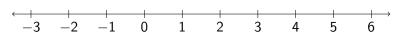
What is the length of the segment MN? Show your work as an equation.

Can a length be a negative number?

### Decimal practice on a number line

Mark the points then take the difference in the points' values.

Given  $\overline{GH}$  with G(1) and H(4.5).

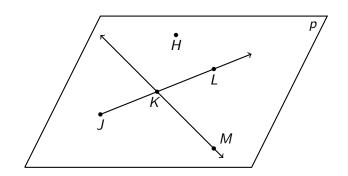


- 1. Mark and label the points and segment on the number line.
- 2. What is the length of the segment  $\overline{GH}$ ? Show your work as an equation.

## Identifying objects in a plane

Identify each item

- 1. The point *H*
- 2. The ray  $\overrightarrow{JL}$
- 3. The name of the plane shown



### Formal meanings of sketch, draw, and construct

- Sketch is to make a freehand diagram of important features.
   Use a pencil to write carefully in your notebook or on paper.
- Draw is to depict with accurate measures using ruler, protractor, and compass.
  - For example, draw a diagram of your room.
- Construct is a formal, logical process to create geometric figures using only a straightedge and compass.
- Drawn to scale means that all of the lengths are proportional.
   (e.g. a "scale model")
  - Tests will often warn that diagrams are "not drawn to scale"

## Learning Target: I can work with congruent segments

CCSS: HSG.CO.A.1 Know precise geometric definitions 1.5 Tuesday 21 Sept

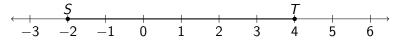
What is the length of the segment ST? Show your work as an equation.

Lesson: Perimeter, congruent line segments in rectangles & isosceles triangles

#### Negative number practice on a number line

Take the difference in the points' values. Check by counting the marks.

Given  $\overline{ST}$  with S(-2) and T(4), as shown on the number line.

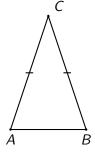


What is the length of the segment  $\overline{ST}$ ? Show your work as an equation.

Why is "minus a negative" the same as add a positive?

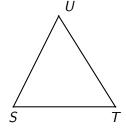
## Use proper notation (including the bar over the letters)

Given  $\triangle ABC$  write down two congruent line segments using proper notation.



On the diagram mark the congruent line segments with tick marks.

Given  $\triangle STU$  with  $\overline{ST} \cong \overline{TU}$ .



## Sketch an isosceles triangle

 $\label{eq:marks} \mbox{Mark the congruent sides with tick marks.}$ 

Draw a ray. (careful! which direction does it go?)

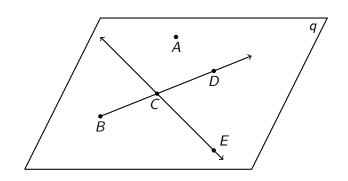
Given the points X and Y, draw  $\overrightarrow{YX}$ .



)

## Identify each item.

- 1. The point A
- 2. The ray  $\overrightarrow{BD}$
- 3. The name of the plane

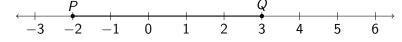


Apply the Segment Addition Postulate Show your work by marking the diagram and writing an equation.

Given 
$$\overline{DEF}$$
,  $DE = 8.5$ , and  $EF = 2.5$ . Find  $DF$ .

## Find the length of the line segment $\overline{PQ}$ .

Given P(-2) and Q(3), as shown on the number line.



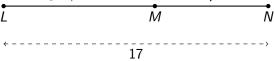
State an equation and the solution. Check your work by counting the distance. Leave marks to show your work.

## Learning Target: I can measure angles

CCSS: HSG.CO.A.1 Know precise geometric definitions

1.6 Wednesday 22 Sept

Do Now: Given  $\overline{LMN}$ , LM = 3x + 1, MN = 7, LN = 17. Find x.

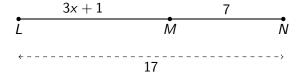


- 1. Write down an equation to represent the situation.
- 2. Solve for x.
- 3. Check your answer.

Lesson: Angle measures; Practice segment addition & congruence

## Solve for *x* using the segment addition postulate

Given LMN, LM = 3x + 1, MN = 7, LN = 17. Find x.



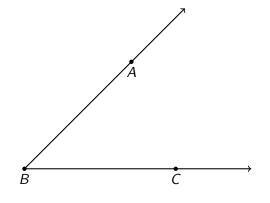
- 1. Write down an equation to represent the situation.
- 2. Solve for *x*.

3. Check your answer.

### Angle: two rays with a common endpoint or vertex

Rays  $\overrightarrow{BA}$  and  $\overrightarrow{BC}$ . Vertex B.

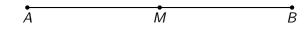
Called  $\angle ABC$  or  $\angle B$ .



### Solve for x given a bisector

Given M is the midpoint of  $\overline{AB}$ , AM = 5x + 2, MB = 20.

- 1. Mark the diagram with the values and tick marks
- 2. Write an equation and solve for x
- 3. Check your result



## Mark the diagram and state your answer as a fraction

Given 
$$\overline{RST}$$
,  $RS=3\frac{2}{3}$ , and  $RT=9\frac{1}{3}$ . Find  $ST$ .