Geometry Unit 3: Transversals

Bronx Early College Academy

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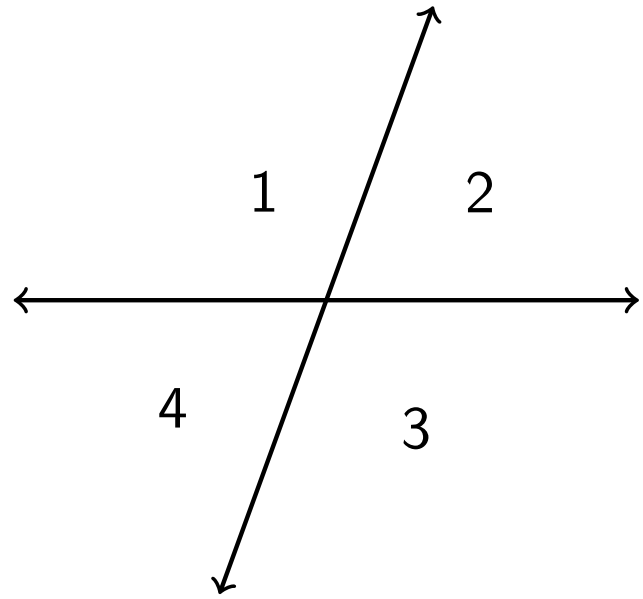
11 October - 21 October 2022

Learning Target: I can name parallel lines transversal angles

HSG.CO.C.9 Prove theorems about lines and angles 3.1 Tuesday 11 October

Do Now: Identify the true statements

1. $\angle 1 \cong \angle 2$
2. $\angle 2 \cong \angle 4$
3. $m\angle 1 + m\angle 4 = 180^\circ$
4. $m\angle 2 + m\angle 3 = 90^\circ$

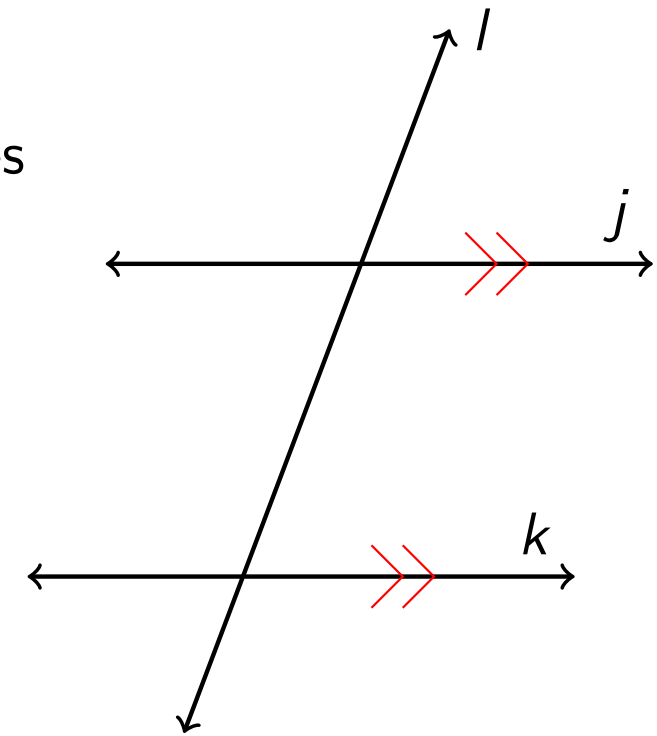


Lesson: Parallel lines crossed by a transverse line, horizontal and vertical directions

New terminology for parallel lines

Parallel lines are in the same plane and never intersect

Parallel lines	$j \parallel k$, mark with arrows
Transversal	Line l, crosses parallel lines
Interior	Inside ($\angle$s)
Exterior	Outside ($\angle$s)
Same-side	On the left or right of l
Alternate	Across l from each other
Horizontal	Sideways direction
Vertical	Up and down direction



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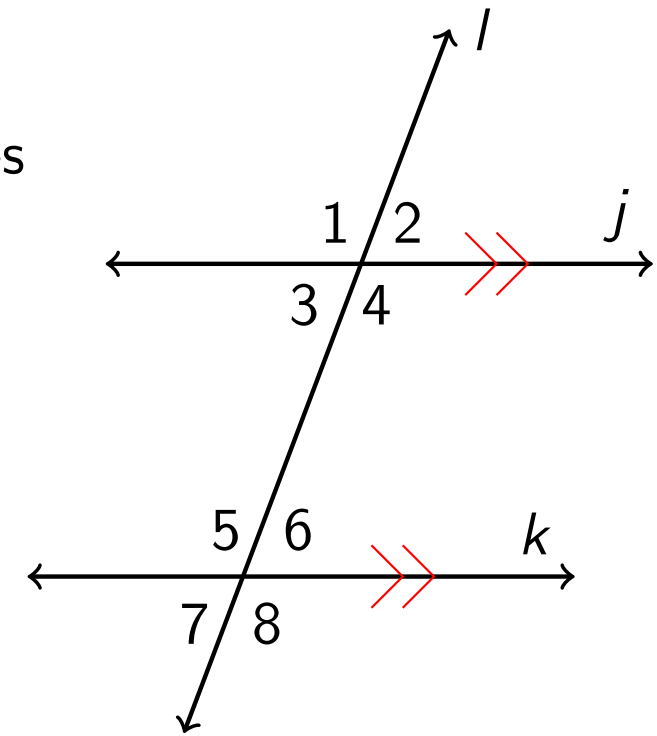


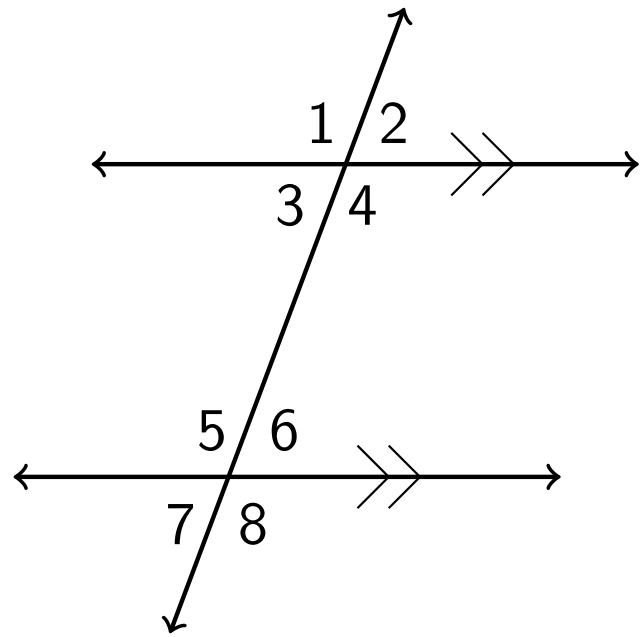
We often number the angles this way.

New theorems for parallel lines

Corresponding Having the same position. e.g. $\angle 2$ and $\angle 6$

Postulate Corresponding $\angle$s of $\parallel$ lines are congruent, $\angle 2 \cong \angle 6$

1. Alternate interior $\angle$s are $\cong$
   $\angle 4 \cong \angle 5$
2. Same-side interior $\angle$s are supplementary
   $m\angle 3 + m\angle 5 = 180$
3. Alternate exterior $\angle$s are $\cong$
   $\angle 1 \cong \angle 8$

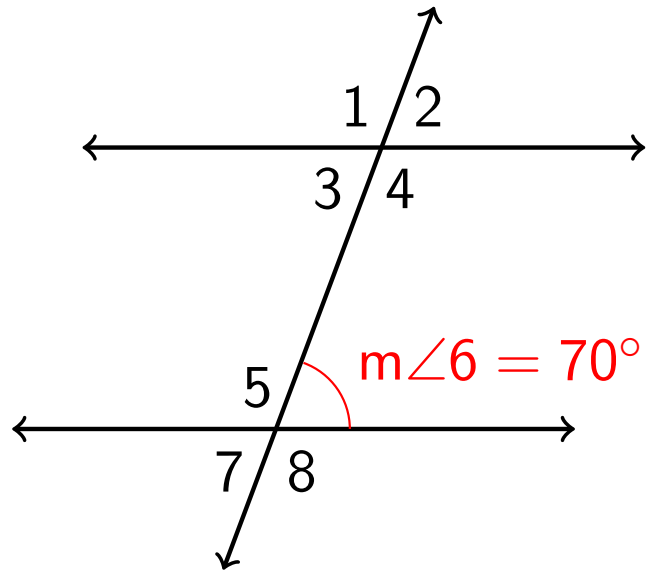


There are only two angle measures, the acute $\angle$s and the obtuse $\angle$s
And they add to 180°, i.e. supplementary

Apply the theorems of parallel lines with a transversal

Given two parallel lines and a transversal, with $m\angle 6 = 70°$. Write down the value of each angle measure.

1. $m\angle 1 =$
2. $m\angle 2 =$
3. $m\angle 3 =$
4. $m\angle 4 =$
5. $m\angle 5 =$
6. $m\angle 6 = 70°$
7. $m\angle 7 =$
8. $m\angle 8 =$



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7. $m\angle 7 =$
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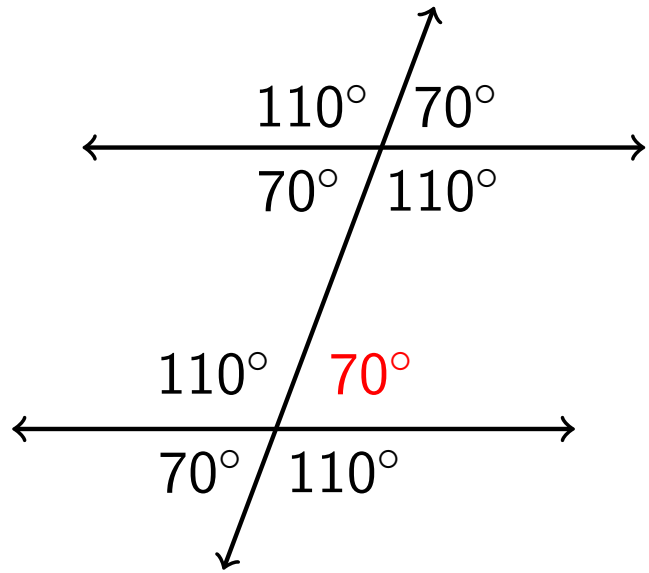


Solution

Extension: Ratios are fractions

We often state proportions as ratios

Example: Divide a distance into equal parts, i.e.

$$1 : 1$$

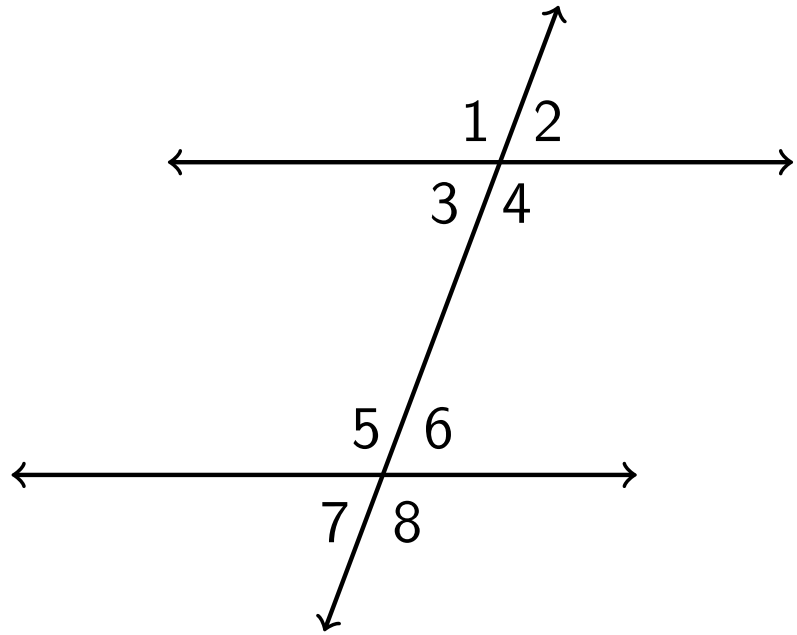
We say "one to one", or "in a one to one ratio."
A rectangle's length to width ratio is two to one. $2 : 1$

Learning Target: I can calculate transversal angles

HSG.CO.C.9 Prove theorems about lines and angles 3.2 Wednesday 12 October

Do Now: Identify each angle

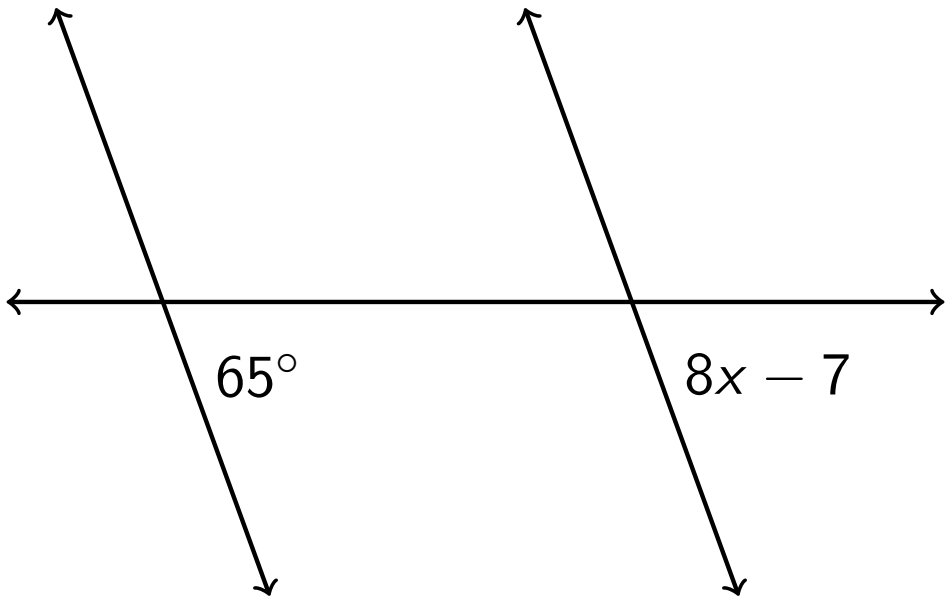
1. Opposite $\angle 4$
2. Corresponding to $\angle 3$
3. Alternate exterior to $\angle 8$
4. Same side interior to $\angle 5$
5. Alternate interior to $\angle 4$



Lesson: Triangle sum theorem

Parallel lines intersected by a transversal. Find x.

Parallel lines do not have to be horizontal.



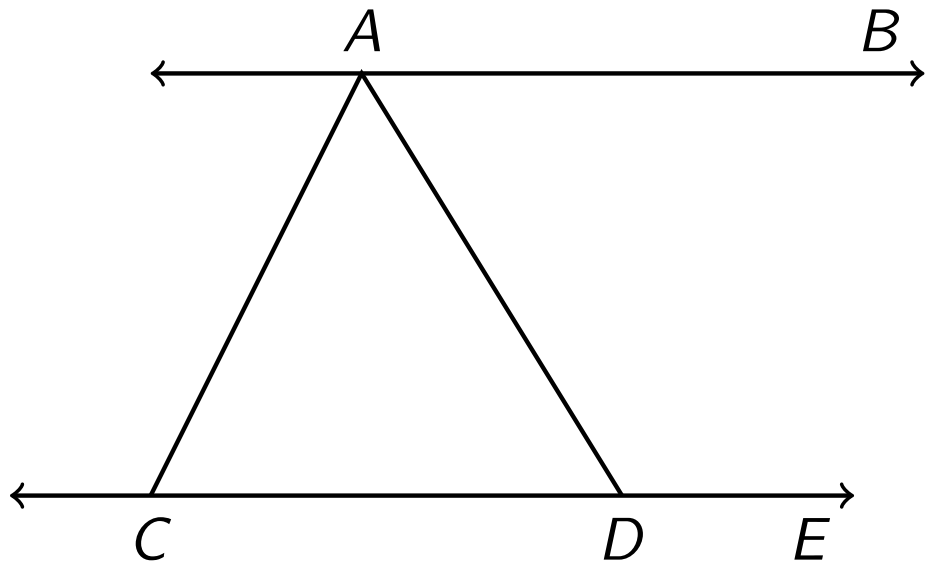
State the postulate or theorem you are employing.

Learning Target: I can calculate triangle angles

HSG.CO.C.9 Prove theorems about lines and angles 3.3 Thursday 13 October

Lesson: Sum of a triangle's interior angles is 180°

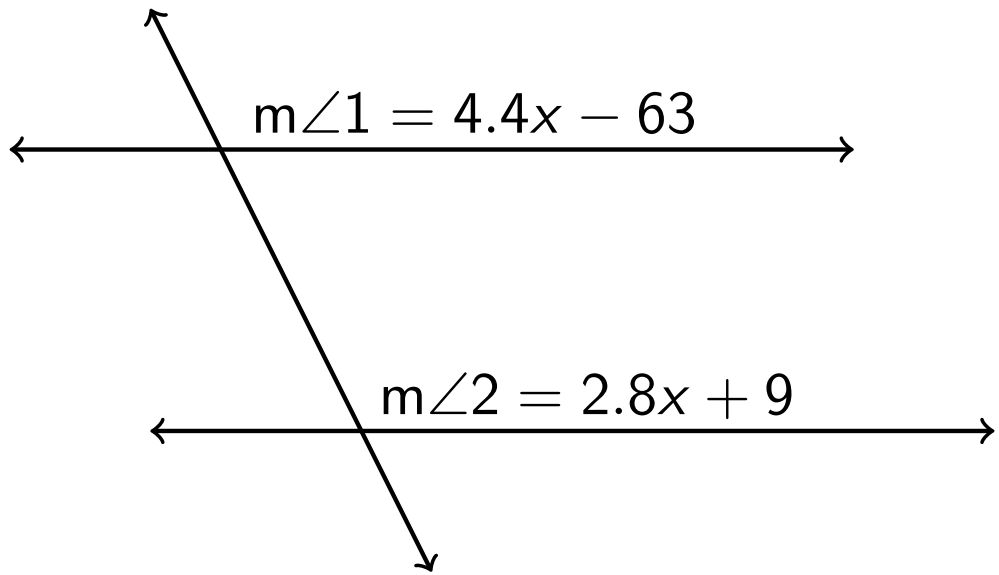
Given parallel lines $\overleftrightarrow{AB} \parallel \overleftrightarrow{CDE}$ with $\overline{AC} \cong \overline{CD}$. If $m\angle BAD = 80$ find $m\angle ACD$.



Learning Target: I can define a parallelogram

HSG.CO.C.9 Prove theorems about lines and angles 3.4 Friday 14 October

Two parallel lines intersect a transversal. Given corresponding angles $m\angle 1 = 4.4x - 63$ and $m\angle 2 = 2.8x + 9$, find the measure of $\angle 1$.

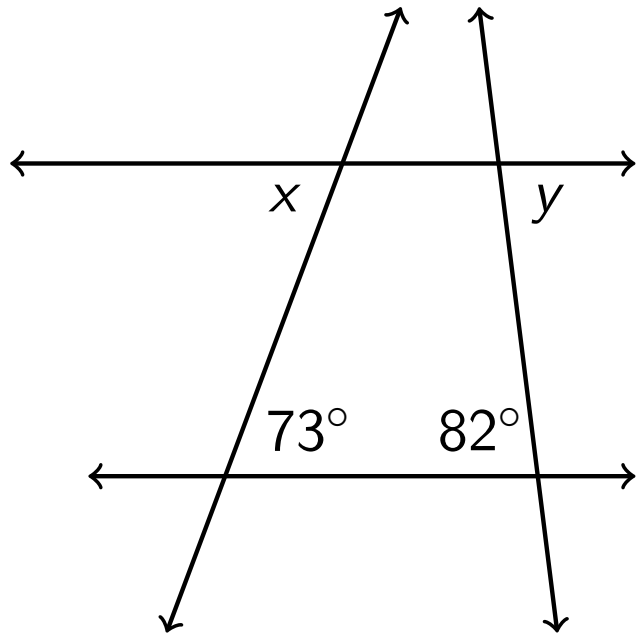


Learning Target: I can calculate external triangle angles

HSG.CO.C.9 Prove theorems about lines and angles 3.5 Monday 17 October

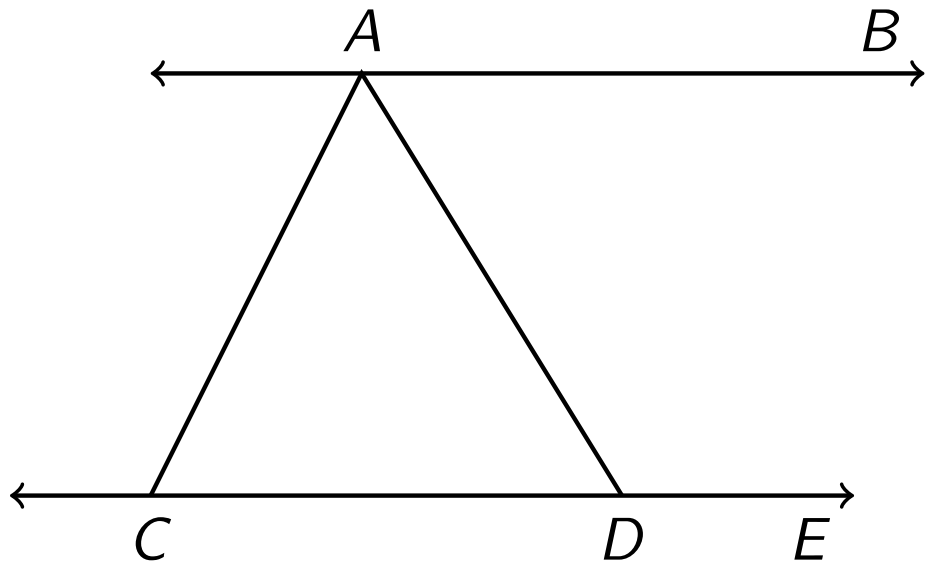
Do Now:

1. Given two parallel lines, two transversals
2. Find x, y
3. What relationship are you using? (e.g. vertical angles, same-side exterior angles, alternate interior angles, etc.)



Lesson: Triangle external angle theorem

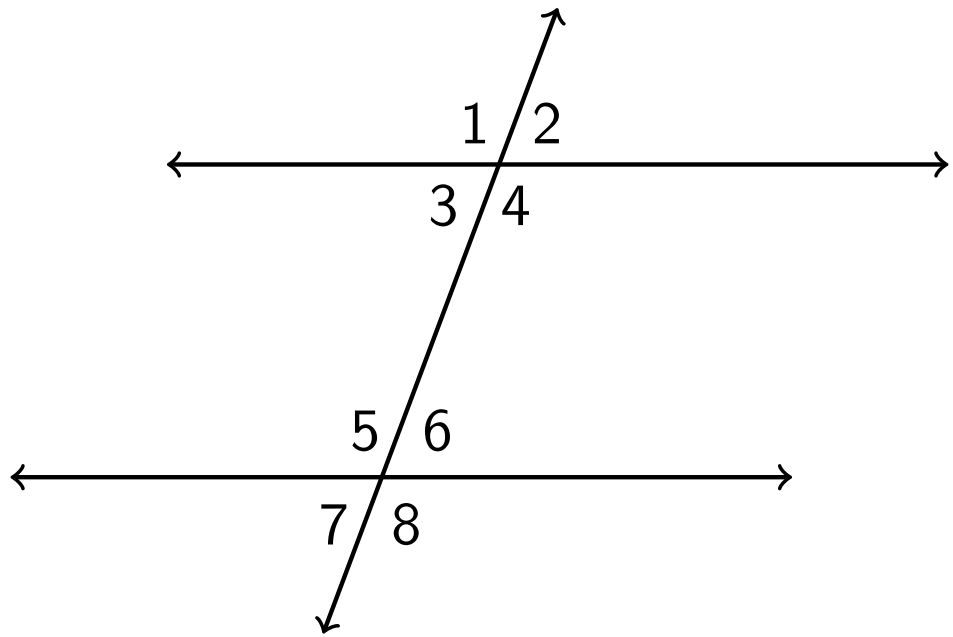
Given parallel lines $\overleftrightarrow{AB} \parallel \overleftrightarrow{CDE}$ with $\overline{AC} \cong \overline{CD}$. If $m\angle BAD = 80$ find $m\angle ACD$.



Learning Target: I can calculate transversal angles

HSG.CO.C.9 Prove theorems about lines and angles 3.6 Tuesday 18 October

Given two parallel lines and a transversal, with $m\angle 4 = 3x$ and $m\angle 5 = x + 70$.
Write an equation, then solve for x.

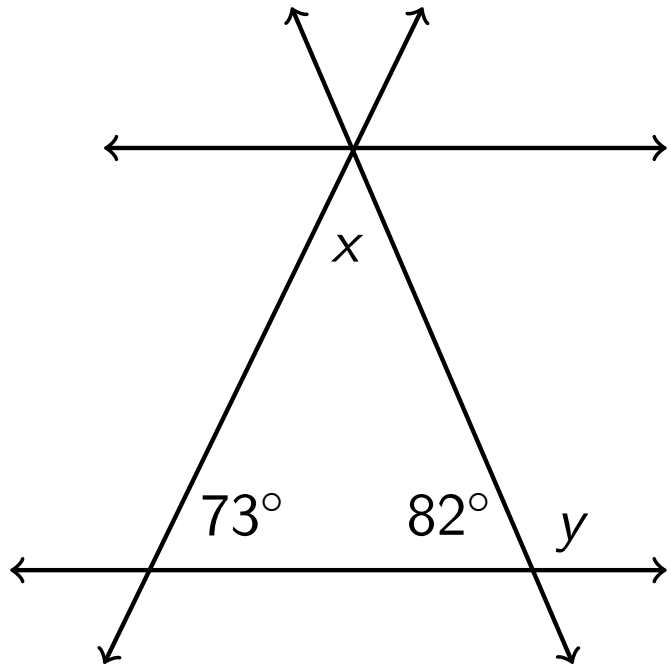


Learning Target: I can calculate angles in parallelograms

HSG.CO.C.9 Prove theorems about lines and angles 3.7 Wednesday 19 October

Do Now:

1. Given a triangle, shown
2. Find x, y
3. What relationships are you using? (e.g. vertical angles, same-side exterior angles, alternate interior angles, etc.)

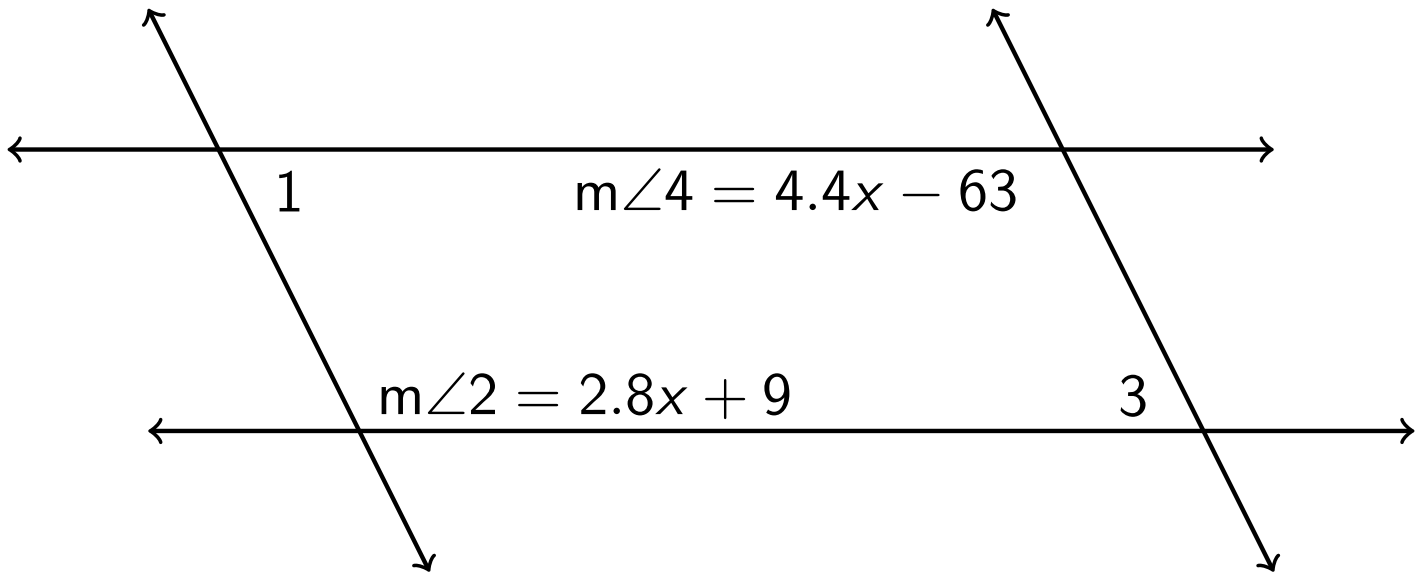


Lesson: Triangle's exterior angles

Learning Target: I can review with my classmates

HSG.CO.C.9 Prove theorems about lines and angles 3.8 Thursday 20 October

Two parallel lines intersect a second set of parallel lines. Given $m\angle 2 = 2.8x + 9$ and $m\angle 4 = 4.4x - 63$, find the measure of $\angle 1$.



Learning Target: I can review with my classmates

HSG.CO.C.9 Prove theorems about lines and angles 3.9 Friday 21 October