# Introduction

Korean morphological analysis is the process of determining parts of speech by identifying morphemes, which are the smallest units of linguistic expression with independent meanings in a sentence. In an isolating language, such as English, this identification can be achieved relatively easily by tagging parts of speech sequentially. However, in Korean, the nature of the agglutinative language requires separating endings or postpositions and restoring inflections to their original form. In addition, because the basic input of other Korean analysis tasks is often a separate morpheme, the accuracy of the morphological analysis significantly affects the performance of Korean analysis. Modern high-performance deep learning methods in natural language processing (NLP) use a tokenization process that breaks the text into smaller units and converts each token into a vector as an input to the computational model. Here, the token unit is mainly a subword unit, and to reflect the characteristics of a Korean subword, tokenization with separate morphemes is attempted in advance. Using the results of the morphological analysis for this tokenization process improves the overall performance of the analysis by reflecting the semantic units of Korean. This requires a highly accurate and fast morphological analyzer.

Various approaches have been proposed for morphological analysis, which is crucial in Korean language analysis. In general, when people understand speech or written text, they attempt to make sense of it using vocabulary and concepts that they are familiar with. While there are approaches to use rules or dictionaries to reflect this understanding, it becomes difficult to build and maintain a dictionary for the vocabulary that appears in each text. Therefore, methods for tagging syllable units without a dictionary have been proposed and studies have been conducted to improve them . From a mechanical perspective, syllable-by-syllable morphological analysis can be performed either by tagging syllable-by-syllable and then applying a base-form restoration dictionary, or by tagging syllable-by-syllable with the base form already restored. However, syllable-by-syllable morphological analysis has limitations, in that it is difficult to accurately identify morpheme boundaries and learn long-term contextual information as the length of the sequence increases. In this study, the former is referred to as dictionary-based morphological analysis and the latter as syllable-unit morphological analysis. Both methods are trained on a manually labeled corpus and cannot accurately analyze new syllable combinations or morphemes that do not appear in the training corpus. Recently, with the development of the Internet and the spread of open sources as well as open data, web texts, corpora, language resources, and knowledge shared by different people have accumulated significantly. The reduced cost of building and maintaining a dictionary provides a significant opportunity to overcome the limitations of dictionary-based methods.

Against this background, this study considers how the dictionary-based morphological analysis method used by MeCab, an open software for Korean and Japanese morphological analysis in tokenizers, which is an essential preprocessing tool for deep learning, can be effectively improved, and a method is proposed. The dictionary-based morphological analysis method trained by the CRF (Conditional Random Fields) method lists the candidate morphemes in the dictionary from a given sentence to form a lattice structure connected by a directed graph and determines the optimal morphological analysis path within it. The process of determining the optimal path in the lattice uses the Viterbi algorithm, which determines the path that minimizes the cost of each morpheme node and the sum of the neighborhood costs of two consecutive morphemes. The main types of errors in these dictionary-based morphological analysis methods occur when new words that are not in the dictionary are used in a sentence, or when the optimal path calculation selects the incorrect result owing to bias. For example, it may be cost-effective to select one long morpheme than several short morphemes, but this may often lead to an incorrect analysis. The main motivation for this study was that the path that minimizes the costs for the nodes and links may not be the optimal path.

To identify cases in which a suboptimal solution is actually the best solution according to the best path calculation, we modified the best path calculation method to generate suboptimal analysis results and verified the extent to which they are correct. Although there are numerous different approaches to select the next-best path, we used the method of replacing a morpheme node on the optimal path with a lower-ranked node. As shown in Table [tab:maximum-performance], we confirm the extent to which the analysis performance can be improved by replacing the optimal path with a lower-ranked node. We can consider the problem of finding the correct answer among the generated sub-optimals, similar to the problem of re-ranking search results in information retrieval. In , the N-best analysis results generated by the seq2seq model were re-ranked based on a convolutional neural network to improve the performance. In this study, re-ranking was performed using two BERT models of different types and forms, as proposed in . Experimental results show that first-stage re-ranking improves the performance by over 20% over existing written and spoken models, and second-stage re-ranking with a different type of input and a different type of pre-trained model further improves the performance by more than 30% over existing written and spoken models.

With this method, the performance of the dictionary-based morphological analysis method could be further improved; however, the overall analysis time increased when the morphological analysis system was configured, including the re-ranking model itself. However, it is feasible to use the results of multiple reranked morpheme analyses to update the connection costs between morphemes in a dictionary, similar to the backpropagation process in a typical neural network. It is also expected that the morphological analysis system with improved connection costs will be able to generate better re-ranking candidates, which will further improve performance by doing so iteratively. Further research is needed on this, and this study was limited to performance improvements with two-stage reranking.

The main contributions of this study are as follows.

1. **Further improvement of dictionary-based morphological analysis method using suboptimal analysis results**: We explore the possibility of performance improvement by introducing a method to replace the optimal path with a suboptimal node and propose a method to effectively improve the dictionary-based morphological analysis method through deep learning.
2. **Extending the performance improvement by introducing a two-stage re-ranking model**: To improve the performance of dictionary-based analysis by re-ranking the morphological analysis results, we propose extending the performance improvement using different BERT models to perform two rounds of re-ranking.
3. **A method for updating connection costs in the dictionary and suggestions for future research**: We propose a new method for updating dictionary connection costs based on re-ranked morphological analysis results. We also outline directions for future research, suggesting potential improvements.

These contributions provide important insights into the performance improvement of Korean morphological analysis and the direction of future research, and will serve as a useful reference for future researchers.

The remainder of this paper is organized as follows. In Section 2, we discuss configuring and training a dictionary-based morphological analysis system. In Section 3, we discuss the generation of secondary results of morphological analysis, produce re-ranking data, and propose a method for training a two-stage re-ranking model. In Section 4, we discuss the results of the performance improvement using the morphological analysis and re-ranking models. In Section 5, we introduce previous research cases related to this study. Finally, in Section 6, we conclude the study and discuss its limitations and directions for future research.

# Morphological Analysis Model

## Korean Morphological Analysis Corpora

In this study, we used three major corpora to train and evaluate Korean morphological analysis models, each of which has unique characteristics and serves different research purposes.

**Sejong Corpus**: Originating from the 21st Century Sejong Project, this corpus consists of a total of 15 million eojeols, including the raw untagged corpus, and forms the backbone of Korean morphological analysis research. It provides a wide variety of linguistic patterns and structures that are important for baseline training and validation of morphological analysis models, and has been used for performance comparisons with other studies. In most of the previous studies, only a part of the Sejong corpus was used for experiments, and in this study, we used the dataset provided by the researchers in .

**UCorpus (University of Ulsan Corpus)**: This is an extension of the Sejong corpus, which is constantly being maintained and added to by the University of Ulsan, significantly increasing its volume to 63 million eojeols and testing the adaptability and accuracy of the model to a wider range of data. The expansion includes corrections to previously raised errors and a number of annotation outputs for new data, providing a substantial basis for comprehensive linguistic analysis.

**Everyone’s Corpus**: Launched by the National Institute of the Korean Language in 2020, the Everybody’s Corpus enriches the data landscape with web texts and spoken language materials that reflect contemporary language use. This modern corpus reflects the dynamic evolution of the Korean language and is playing a pivotal role in improving models for capturing the nuances of current Korean usage.

Table [tab:data-statistics] details the specific number of sentences and words in each corpus, and the data subsets extracted for model training and evaluation. During the training data conversion process, we first removed duplicate sentences and excluded sentences with annotation errors or other problems. We can see that many duplicate sentences occur, especially in spoken language.

## Training Example Transformation

To train a dictionary-based morpheme analysis model effectively, the morpheme-tagged corpus, typically represented in lemma form, must be transformed to include the boundary information between morphemes in its surface form. Crucial to this transformation is string alignment, a process that accounts for the discrepancies between lemma forms and surface forms in the Korean morphological analysis corpus.

In this study, string alignment was performed using the Smith-Waterman algorithm, which uses a scoring matrix based on the similarity of the grapheme unit of Korean letters for each word pair (as shown in Figure [fig:sample]). Each aligned sentence containing a morpheme tag was converted into a training sample tailored for dictionary-based morphological analysis.

The resulting table in Figure [fig:sample] illustrates this process. Each row acts as a lexical unit. The first four columns contribute to feature generation, whereas the last four columns facilitate post-lemmatization. Using the morphological corpus above, a large number of training samples can be generated according to the process shown in Figure [fig:sample]. With the exception of the evaluation samples, the remaining sentences were used to train the dictionary-based morphological analysis model using the CRF algorithm. The output of this training allowed the calculation of the costs associated with each morpheme node and the linking of two consecutive morphemes. This, in turn, allowed the discovery of an optimal path using the Viterbi algorithm.

## Lattice Construction and Decoding

Figure [fig:lattice] presents a snapshot of the lattice structure, which is an integral part of the morphological analysis. (1) shows a fragment of the lattice structure formed when the example sentence in Figure [fig:sample] is entered. (2) shows the optimal path determined using the Viterbi algorithm.

However, the path inferred by the trained model may differ from the correct solution constructed by humans. The nodes marked with stars in (1) represent correct nodes. The upper-left number of each node indicates the ranking of the nodes accessible at each decoding point. The choices made at certain moments deviate from the correct solution. To improve analytical performance, mechanisms to correct these discrepancies must developed.

# Re-ranking Model

Although dictionary-based morphological analysis offers significant advances, its optimal paths occasionally diverge from the correct solutions that humans understand. This divergence underscores the need for a model that reevaluates these primary results and reorients them to achieve higher accuracy. This method, called re-ranking, involves generating multiple analyses of an input and then reordering them based on a new set of criteria or models, thereby improving the overall quality of the results.

## Secondary Path Generation

Before reranking begins, multiple analyses, typically referred to as the N-best paths, of the input sentence are generated. This involves extracting the top N atoms from the lattice structure. In this study, a novel approach is introduced to generate secondary paths, as shown in (3) of Figure [fig:lattice], by selecting the second-best node rather than each best node constituting the path from the best-path result. Some of these secondary paths provided alternatives that reconciled incorrect with correct answers. Similarly, paths modified by favoring the third-best node were called tertiary paths, and this naming convention was continued for subsequent paths. In our preliminary test, the secondary paths, including the optimal and suboptimal paths, were shown to cover the majority of the correct morphological analyses as measured through human evaluations. (Refer to Table [tab:maximum-performance]).

## BERT-based Re-ranking

Bidirectional Encoder Representations from Transformers (BERT) models have revolutionized many natural language processing tasks by understanding the context in which words appear in text. In this study, we attempt to leverage the power of BERT to reorder the generated secondary paths. We labeled the generated secondary paths with scores related to the morphological analysis performance to fine-tune a pre-trained BERT model specialized for Koreans with excess amount Korean text. After pre-testing several scoring methods on a modest scale, we found that using scores based on the degree of error rather than scores based on accuracy by widen the gap between correct and incorrect answers is effective for learning.

Once the BERT model is fine-tuned and trained for the re-ranking task, it can predict a re-ranking score for each path in the secondary path list. This implies that considering the context, morphological organization, and other essential linguistic features of the path, the model assigns a score to each path. The paths were then re-ranked according to this score, and the path with the highest score was selected for the best morphological analysis.

## Two-stage Re-ranking

Given the complexity of the Korean language, a single re-ranking step does not constantly yield accurate results. Therefore, we propose a two-step re-ranking approach as described in .

In the first step, we re-rank the secondary paths generated using the BERT model, as described in Section 3.2. In the second step, we introduced another BERT variant that was optimized for a different set of linguistic features or trained on a different dataset. This allowed us to perform a fine-grained re-evaluation, further refine the list, and push more contextually accurate paths to the top.

As shown in Figure [fig:ranking], for a two-stage reranking model, the first stage performs the first re-ranking, taking as input a secondary path in morphologically tagged lemma form. It then performs a second re-ranking, again taking as input the path re-ranked in stage 1 and the original input sentence. This was conducted to improve effectiveness, as it was ineffective given the same type of input.

In summary, the re-ranking model represents a significant advancement in our approach to Korean morphological analysis. By leveraging BERT-based models, we anticipate a marked improvement in accuracy, especially in complex linguistic scenarios. The next section will present our experimental setup and results, providing crucial empirical evidence for the efficacy of the re-ranking model in practical applications.

# Experimental Results

Having developed the re-ranking model as a theoretical framework for enhancing Korean morphological analysis, we now turn to empirical validation. This section outlines our experimental setup, designed meticulously to test the performance of our model. Through these experiments, we aim to demonstrate not just the model’s accuracy but also its practical applicability in handling the nuances of Korean language processing.

We evaluated the performance of the proposed deep learning-integrated dictionary-based morphological analysis method. This section presents the results of the experimental evaluation considering the improvements over conventional methods and the effectiveness of our re-ranking model.

## Setup and Data

For our experiments, we used the Sejong corpus (versions used in ), UCorpus, and Everyone’s Corpus. For comparison with previous studies, the Sejong corpus was trained using a single model without separation. The UCorpus and Everyone’s Corpus provided a separate spoken corpus with drama scripts and broadcast dialogues, while UCorpus separated documents that were considered to be close to spoken language and further organized them into a semi-spoken corpus. Because UCorpus and Everyone’s Corpus have synergistic effects when trained concurrently, we trained the models separately for written and spoken language rather than separating them by source. The statistics of the full data for the three types of models are presented in Table [tab:data-statistics]. Because of the large volume of UCorpus, we randomly selected some of them to train the actual model.

We transformed this organized morphological corpus using the training-example transformation process described in Section 2.2 to generate samples for training the dictionary-based morphological analysis model.

## Evaluation Metrics

To measure the accuracy of the morphological analysis model, correctness of the N-best path, and ranking accuracy of the reranking model, we used the eojeol accuracy and morpheme F1 scores as evaluation metrics. To verify that they produced the correct morphological analysis results, we measured the degree of agreement with human annotations on the corpus. However, owing to the slightly different criteria and styles of the annotators who labeled the different types of corpora, including the comparison with the MeCab-ko system, the following adjustments were made:

* Sentences containing unanalyzable tags (NF, NA, and NV) were excluded from both training and evaluation.
* As for the tagsets, we excluded three unanalyzable tags from the 45 Sejong tagsets and used 42 tagsets.
* Each tag output by the MeCab-ko system was converted to the corresponding tag in the Sejong tagset.
* Chinese characters were converted to Chinese character tags (SH) even if they were semantically used as nouns, and consecutive Chinese characters were converted to a single morpheme.
* Similarly, symbol, numeral, ending, and postposition in the same tag were converted to a single morpheme, and decimal expressions were treated as a single morpheme, including the midpoint and the numbers before and after.
* If the first lemma letter of the ending is ‘[eo]’, ‘[yeo]’, or ‘[ah]’, it is unified as ‘[eo]’, and if it is ‘[eot]’, ‘[yeot]’, or ‘[ass]’, it is unified as ‘[eot]’.
* Root tags (XR) used alone without affixes were replaced with common nouns (NNG) because they are mainly used in the Sejong corpus only.
* As mentioned in , connective endings (EC) and sentence-closing endings (EF) are not clearly defined in the tagging guidelines, and there are cases where they are used interchangeably in the corpus, to ensure that we evaluated them without distinguishing them.
* The distinction between ‘[geot]’ and ‘[geo]’ is unclear in the tagging guidelines, and there are cases where they are used interchangeably in the corpus, hence, we did not distinguish between them.
* Compound words can be interpreted as a single morpheme or as a combination of two or more morphemes or affixes, hence, we evaluated them without distinguishing between them.
* Proper nouns can also be interpreted as common nouns depending on the point of view or perspective. Human annotators have slightly different standards, and thus they were also evaluated without distinguishing the nouns.

## Basic Performance

First, we compared the initial results of the dictionary-based morphological analysis model trained using the method described in Section 2 with those of MeCab and syllable-based morphological analysis systems (refer to Table [tab:performance-without-reranking]). The results show that the dictionary-based method implemented is superior to the existing MeCab system, but it differs from human evaluations owing to the limitations mentioned above, and it does not reach the performance of existing syllable-based morphological analysis systems. We also found that the compatibility between the Sejong corpus and other corpora is poor, as the model trained on the Sejong corpus has guaranteed performance when evaluated on the Sejong corpus, and some performance degradation occurs on other corpora.

## Re-ranking Performance

Upon integrating the BERT-based re-ranking model, we observed substantial performance enhancement. Table [tab:performance-with-reranking] shows that the re-ranking model identified a better path in a significant proportion of cases. The first-stage re-ranking exhibited a performance improvement of over 20% compared with traditional models. The subsequent re-ranking, leveraging a distinct type of input and a different pre-trained model, further augmented the performance by more than 30%.

Next, we performed the BERT-based re-ranking described in Section 3 and compared its performances. Three pre-trained language models, KPF-BERT, ETRI-ELECTRA, and ETRI-RoBERTa, which are known to perform well in other Korean language understanding tasks, were used to fine-tune the re-ranking model. KPF-BERT received Korean sentences as input, ETRI-ELECTRA received morphologically tagged sentences as input, and ETRI-RoBERTa receives morpheme-separated sentences as input. For KPF-BERT and ETRI-RoBERTa, there may be problems with model learning because of the separation of morpheme tags into letter units during the tokenization process when the morpheme analysis results were received as input and re-ranked, hence, the morpheme tags of the mid-level classification unit were added as new tokens, and then training was performed. As shown in Figure [fig:ranking], for these three types of pre-trained language models, we first performed training with a re-ranking model using only the morphological analysis results and then performed training with a second re-ranking model using the top five morphological analysis results from the first re-ranking results along with the input sentences for other types of pre-trained language models. Preliminary tests indicate that using the same type of model or input results in a nearly identical retrained model, with no further improvement in performance.

The sentences used for training the re-ranking model were selected from those used for training the dictionary-based morphological analysis model: 190,000 sentences from the Sejong corpus, 240,000 sentences from the written language of the combined UCorpus and Everyone’s corpus, and 360,000 sentences from the spoken language of the combined UCorpus and Everyone’s corpus. For a large number of sentences, we adopted a floating-point 16-bit technique while using four GPUs for distributed training and significantly reduced the time required for training. In addition, the minibatch size was 120 with a maximum sequence length of 384 because the first re-ranking uses only the morphological analysis results as input. The minibatch size was 40 with a maximum sequence length of 512 because the original input sentences were given as input along with the first morphological analysis results. See Table 1 for information on other training options and software tools used in the implementation of re-ranking models.

Table [tab:performance-with-reranking] shows that incorporating the re-ranking model significantly improves the performance compared with no re-ranking. The error reduction rate (ERR) of the performance change from the existing model on eojeol accuracy is shown as 29%, 27%, and 20% for the Sejong corpus, combined written corpus, and combined spoken corpus, respectively, with the first round of re-ranking, and the second round of re-ranking improved the performance by increasing the rate to 34%, 34%, and 32%, respectively. These performance improvements demonstrate that the dictionary-based morphological analysis model outperforms traditional syllable-based morphological analysis systems, including numerous pre- and post-processing rules and dictionaries.

## Comparison to Other Studies

We found that the proposed transformer-based re-ranking technique consistently improved the results of the existing morphological analysis models. These results confirm that it opens up new possibilities by further improving the results of existing traditional machine-learning models in the field of Korean morphological analysis. Finally, because the major related studies proposed in the literature were mostly conducted on the Sejong corpus, we compared the performance improvement of the Sejong corpus with the results of previous studies. Although it is difficult to make a direct comparison because of slight differences in implementation conditions and evaluation criteria. The proposed dictionary-based morphological analysis model is not up to the latest research results; however, by incorporating a re-ranking model, it can secure a performance that is comparable to existing research.

The entire morphological analysis model, including the re-ranking model, is not suitable for real-time processing. However, it is expected that by reflecting the cases whose ranks are changed through the re-ranking model as feedback to the dictionary-based morphological analysis model, it will be feasible to obtain near-improved morphological analysis performance. The improved dictionary-based morphological analysis model can then be used as input to the re-ranking model; therefore, it is expected that a gradually improvement in morphological analysis model can be obtained through this iterative feedback loop.

# Related Work

Korean morphological analyses have seen an influx of various methodologies in recent years. The nature of the Korean language, being agglutinative, introduces challenges that have propelled researchers to develop inventive solutions, many of which have laid the groundwork for future research. Table 2 provides a concise comparison of the methodologies and key concepts of key studies that are directly or indirectly related to this research, giving a brief overview of the different methods of morphological analysis.

## Traditional Dictionary-based Approaches

The earliest attempts at Korean morphological analysis relied heavily on rule- and dictionary-based methods. These methodologies employ predefined sets of linguistic rules or large dictionaries to detect morphemes and determine parts of speech. One of the most significant advantages of this approach is its deterministic nature, which can lead to high accuracy when the input text closely adheres to the rules or dictionaries used. However, it is challenging to scale and update them, particularly with the constant evolution of language and the emergence of new words. The dynamic nature of language, particularly in the Internet age, has made the maintenance of comprehensive dictionaries labor-intensive.

## Syllable-unit Morphological Analysis

To overcome the limitations of dictionary dependence, syllable-by-syllable morphological analysis has emerged as an alternative. This method either tags each syllable and then applies a base-form restoration dictionary or tags the syllable with the base form already restored. One notable drawback is the challenge of accurately pinpointing morpheme boundaries. Furthermore, as the sequences increase in length, the system finds it increasingly challenging to understand long-term contextual data.

## Recent Deep Learning Approaches

The incorporation of deep learning into Korean morphological analysis has brought significant advancements to the field. Existing deep learning methods typically employ architectures like Bidirectional Long Short-Term Memory (Bi-LSTM) networks, Convolutional Neural Networks (CNNs), and Transformer-based models. These approaches focus on understanding language context and sequence, utilizing the ability of these models to capture long-range dependencies and intricate patterns in text data. For example, Bi-LSTM-CRF models, extensively used for sequence labeling in morphological analysis, leverage LSTM’s capacity to remember long-term dependencies and CRF’s proficiency in sequence prediction.

In contrast, our method innovatively integrates the re-ranking concept with BERT-based models for Korean morphological analysis. Unlike traditional deep learning methods that primarily use sequence-to-sequence or sequence labeling approaches, our method generates suboptimal paths using dictionary-based techniques, which are then re-ranked by BERT models. This dual approach, leveraging BERT’s contextual understanding, allows for a more detailed and accurate morphological analysis. The distinction of our approach lies in its ability to address the complexities of the Korean language. By generating and re-ranking suboptimal paths, our method can identify and rectify anomalies that standard deep learning models may miss. This innovative strategy combines the precision of dictionary-based methods with the contextual comprehension of BERT models, marking a significant advancement in the field, especially for languages with intricate morphological structures like Korean.

## Integrating Dictionary-based and Deep Learning Approaches

Tokenisation, a fundamental process in NLP deep learning models, involves breaking down text into smaller units and converting these tokens into vectors for computational processing. For Korean, with its complex morphological characteristics, tokenisation that respects morpheme boundaries is crucial. This is because it can not only accurately capture the linguistic nuances of Korean, but also improve the overall performance of deep learning models. This is especially important given the agglutinative nature of Korean, where words are formed by combining morphemes with different semantic and syntactic information.

In this respect, the combination of dictionary-based morphological analysis methods and deep learning approaches used by MeCab, a fast and lightweight morphological analyser used for tokenisation of Korean and Japanese, is quite useful. The dictionary-based morphological analysis used here uses a model trained with CRFs to form a lattice structure as in to identify the optimal path for morphological analysis. While this method provides a degree of accuracy and speed, it does not achieve the high accuracy achieved by modern deep learning.

Our research sought to bridge this gap by effectively combining these dictionary-based morphological analysis methods with the contextual understanding capabilities of deep learning. Future research should continue to refine these hybrid methods to explore the possibility of end-to-end models that seamlessly combine the strengths of traditional dictionary-based analysis with the adaptive capabilities of deep learning. This direction promises significant advances in morphological analysis and will further push the boundaries of Korean language processing.

# Conclusion

This study signifies a progressive stride in Korean morphological analysis by seamlessly merging conventional dictionary-based techniques with advanced deep learning methodologies. Our findings indicate that while relying solely on dictionary-based morphological analysis does not surpass the efficacy of some existing models, the integration of a BERT-based re-ranking system notably enhances accuracy, establishing a new standard in this domain.

While the performance improvement increases computational demand, the introduced methodology provides a promising avenue for continuous enhancement. This innovative amalgamation of classical dictionary approaches and cutting-edge machine-learning methodologies paves the way for groundbreaking advancements in the intricate and multifaceted domains of Korean linguistic processing.

Future endeavors in this domain should emphasize the refinement of this harmonious integration to achieve even higher precision in morphological analysis while optimizing computational efficiency. Moreover, our observations indicate the potential for employing a probabilistic model to discern areas where inaccuracies are likely to arise, thus enabling the retrieval of more accurate interpretations from a narrower candidate pool. The parallels between this initiative and the challenges of translation quality estimation suggest that insights from the latter can bolster the efficacy of our approach.