

carnd_t2_p2_unscented_kalman_filter

Carnd - term 2 - project 2 - unscented kalman filter

Overview

The goal of this project is to build an unscented Kalman Filter (UKF) model to process a series of sensor data provided by radar and lidar. Similar to Porject 1, Extended Kalman Filter (EKF) model, same source of radar and lidar data is used. The UKF model is conected to the same simulator via uWebSocketIO.

Project Repository

All resource are located in Udacity's project repository [CarND-Unscented-Kalman-Filter-Project](https://github.com/udacity/CarND-Unscented-Kalman-Filter-Project) (<https://github.com/udacity/CarND-Unscented-Kalman-Filter-Project>).

Project Submission

All modified code including results are committed to my personal github page [carnd-t2-p2-unscented-kalman-filter](https://github.com/chriskcheung/carnd_t2_p2_unscented_kalman_filter) (https://github.com/chriskcheung/carnd_t2_p2_unscented_kalman_filter).

Key Files

main.cpp

establishes communication between simulator and UKF model using uWebSocketIO, and reads in data during set time interval and send sensor measurements to UKF::ProcessMeasurement() in ukp.cpp for processing

ukf.cpp

contains 4 main functions: UKF::ProcessMeasurement(), UKF::Prediction(), UKF::UpdateLidarUKF(), UKF::UpdataRadar().

UKF::ProcessMeasurement() initializes state x *and process covariance matrix* P based on sensor data stypes: radar vs lidar. After initalization, delta time and meas_package will be fed to UKF::Prediction() for corresponding sigma point generation.

UKF::Prediction() generates sigma points X *base on* x and P_{-} . Then follow by generating augmented sigma points X_{sig_aug} withing adding acceleration noise $stda$ and radial acceleration noise $stdyawdd$ to existing process covariance matrix, becoming $P_{_aug}$. Then, using function $h(s, noise)$ to transform X_{sig_aug} predicted sigma points, X_{sig_pred} . Form $X_{sigpred}$, *we applied weighted summation to its sigma points to calcalate the predicted mean* $x, (x_{k+1|k})$, and predicted covariance matrix $P_{-}, (P_{k+1|k})$.

UKF::UpdateRadar() uses state transition function $h(x)$ to transform X_{sig_pred} into predicted measurement points Z_{sig} . From Z_{sig} , applies weighted summation to extract predicted measurement mean, z_pred . With the weighted summation of different between Z_{sig_pred} and z_pred , and the noise of radar equipment, we calculate measurement covariance matrix, S . Then using S , we determine cross-correlation matrix, T , and calculate Kalman gain matrix, Kag . With T and Kag , state x and process covariance $P_$ is updated with the new state and covariance. At the end, Normalized Innovation Square, NIS, is calculated to verify consistence.

UKF::UpdateLidarUKF() uses the same method as UpdateRadar, but instead of using the state transition function $h(x)$ that composes of a 3-dimensional function for ρ , ϕ , and $\dot{\rho}$, the $h(x)$ is replaced with a 2-dimensional function for p_x and p_y .

tools.cpp

includes CalculateRMSE() for calculating the root means square of the predicted result versus real groundtruth measurement

Implementation Challenge

Initialization

If radar measurement input is received, use the ρ , ϕ , and $\dot{\rho}$ measurement to update state vector x . Otherwise, lidar measurement is straightforward to use p_x and p_y directly.

```
float px      = cos(phi)*rho;    // calculate position of x from ra
dian metric phi and rho
float py      = sin(phi)*rho;    // calculate position of y from ra
dian metric phi and rho
```

The last, update the `timeus` variable with the timestamp from measurement input as all measured sensor data are processed at this time.

Prediction

Prediction applies to both Radar and Lidar the same way as so each other. No different thread is needed to decide. One thing to look for is DO NOT attempt to normalized angles at sigma point creation. Will discuss more in later parallel.

```

// Prepare x augmented by adding noise to x vector, then calculate X augmented sigma points
VectorXd x_aug(n_aug_); // 7
x_aug.head(n_x_) = x_; // fill the first 5 element with x
x_aug(5) = 0;
x_aug(6) = 0;
MatrixXd P_aug(n_aug_, n_aug_); // P_aug size is 7x7
P_aug.fill(0.0);
P_aug.topLeftCorner(n_x_, n_x_) << P_;
P_aug(5,5) = std_a_ * std_a_;
P_aug(6,6) = std_yawdd_*std_yawdd_;
MatrixXd Xsig_aug(n_aug_, 2*n_aug_+1); //Xsig_aug size is 7x15
MatrixXd A_aug = P_aug.llt().matrixL(); // P_aug transpose
Xsig_aug.col(0) = x_aug;
for (int i=0; i<n_aug_; i++){
    Xsig_aug.col(i+1) = x_aug + sqrt(lambda_*n_aug_)*A_aug.col(i);

    // a mistake of normalizing angle at sigma point generations. notice that the first angle gets
    // normalized started at 1 instead of 0. So ends up some angles get normalized while some doesn't.
    // Leaving this here as commented code for example of bad normalization practice.
    // normalized angle
    while(Xsig_aug(3,i+1) > M_PI) { Xsig_aug(3,i+1) -= 2*M_PI; }
    while(Xsig_aug(3,i+1) < -M_PI) { Xsig_aug(3,i+1) += 2*M_PI; }*/

    Xsig_aug.col(i+n_aug_+1) = x_aug - sqrt(lambda_*n_aug_)*A_aug.col(i);

    // normalized angle
    // while(Xsig_aug(3,i+n_aug_+1) > M_PI) { Xsig_aug(3,i+n_aug_+1) -
    = 2*M_PI; }
    // while(Xsig_aug(3,i+n_aug_+1) < -M_PI) { Xsig_aug(3,i+n_aug_+1) +
    = 2*M_PI; }*/
}

```

Update

Update for radar and lidar are different. Kalman filter update() for Lidar is quite straight forward by using state x directly.

```

    for(int i=0; i<2*n_aug+1; i++){
        MatrixXd Xx  = Xsig_pred_.col(i) - x_;

        // normalize angle
        while(Xx(3) >  M_PI) { Xx(3) -= 2*M_PI; }
        while(Xx(3) < -M_PI) { Xx(3) += 2*M_PI; }

        P_ += weights_(i) * Xx * Xx.transpose();
    }
    cout << "inside prediction(223)\n";
    cout << "predicted x_=\n" << x_ << endl;
    cout << "predicted P_=\n" << P_ << endl;

```

Normalizing Phi Angle

It is crucial to normalize phi angle in the range between pi and -pi. The explanation had been discussed previously in Project 1. Here for unscented Kalman Filter, phi angle is normalized every time there is a subtraction on the angle, normalization should take place to ensure the range of turning can only go from 90 degree from the center (straight) to the left(-) and to the right(+). [Here](https://discussions.udacity.com/t/ekf-gets-off-track/276122/19?u=drivewell) (https://discussions.udacity.com/t/ekf-gets-off-track/276122/19?u=drivewell).

Overly done at prediction and sigma point generation can cause incorrect results on state *x* and covariance matrix *P*.

```

// normalize phi, y(1) in this case to be within -pi to pi
while(y(1) >  M_PI){ y(1) -= 2.*M_PI; }
while(y(1) < -M_PI){ y(1) += 2.*M_PI; }

```

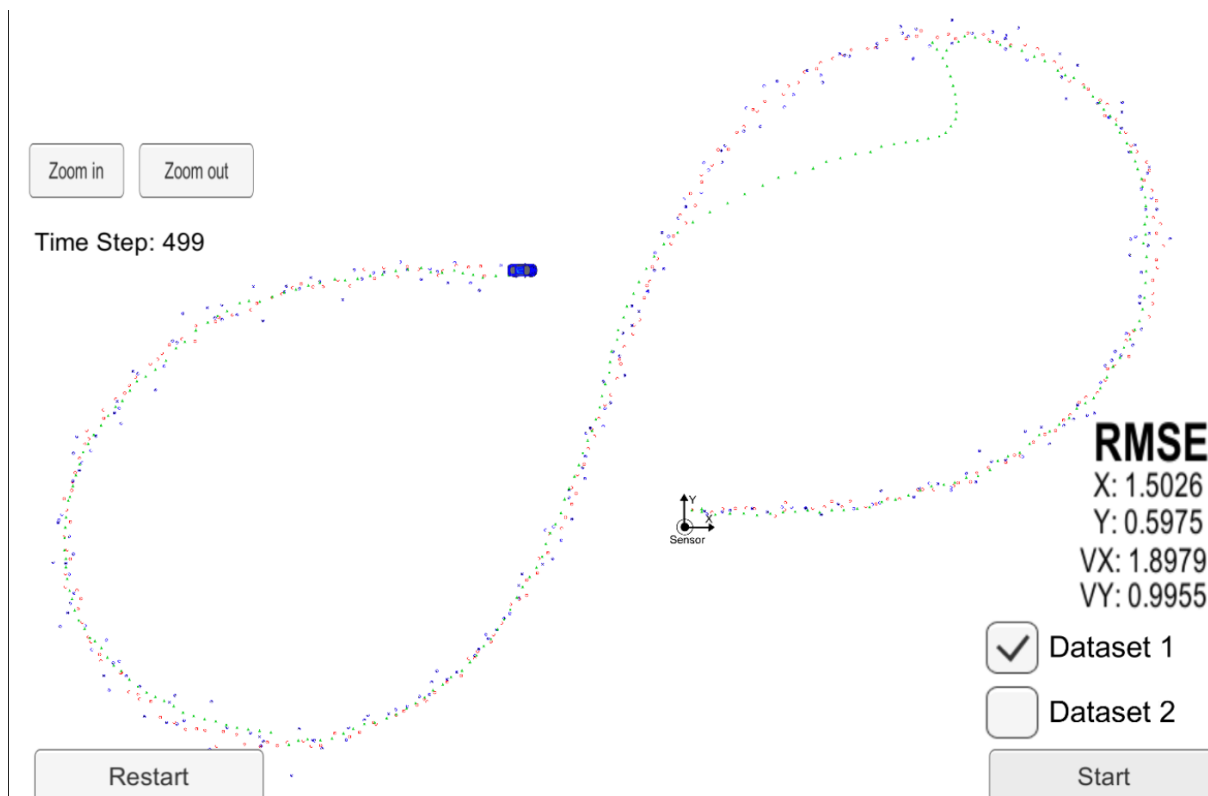
Result

Initial bring up of the code is short as I am using the old code structure from project 1. At the beginning, I got green tracker faulty mapped the estimation and prediction with bumps (off tracked) around 160 and 350 time stamps. As I observed, the calculated state *x* and covariance state matrix were increasing exponentially as raw measurement data was being processed. The problem was normalizing phi angles at sigma points generations and predicting *Xaug_pred*. It was a coding bug that normalization was not applied to the first sigma point phi but the rest of the sigma points, and causing an inconsistency in phi angles.

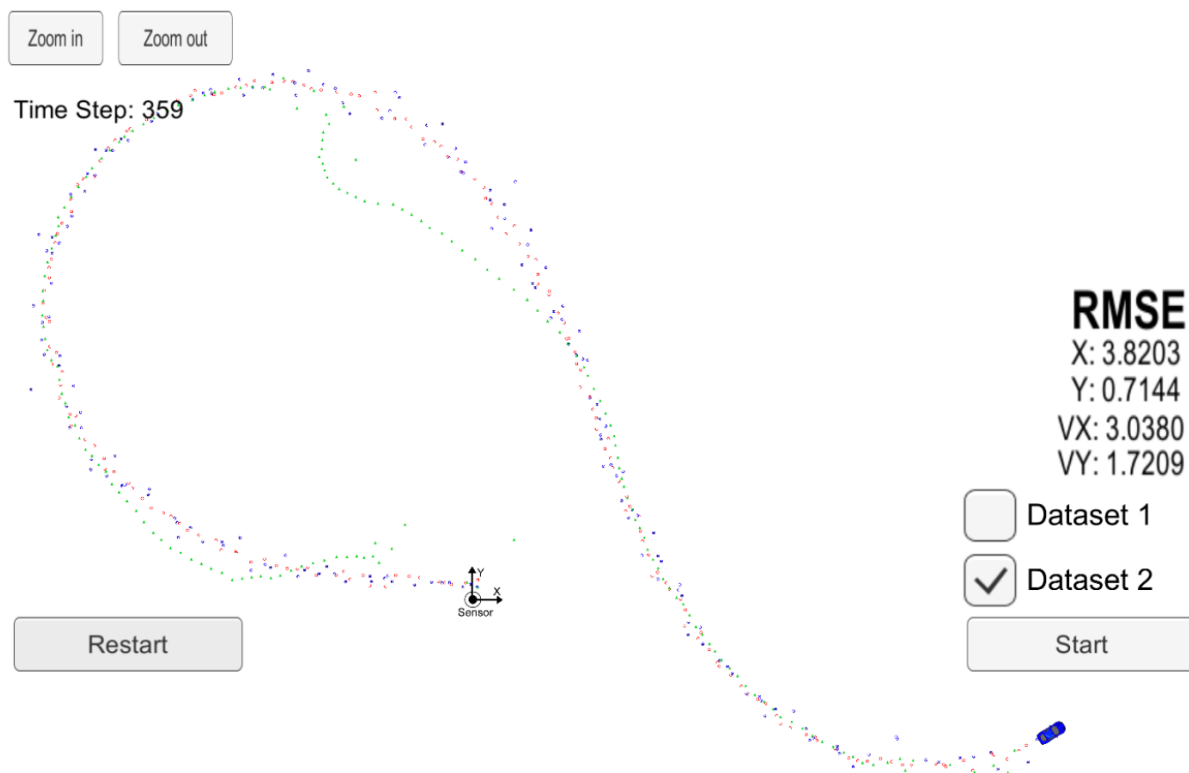
Failed attempts

Radar measurement only

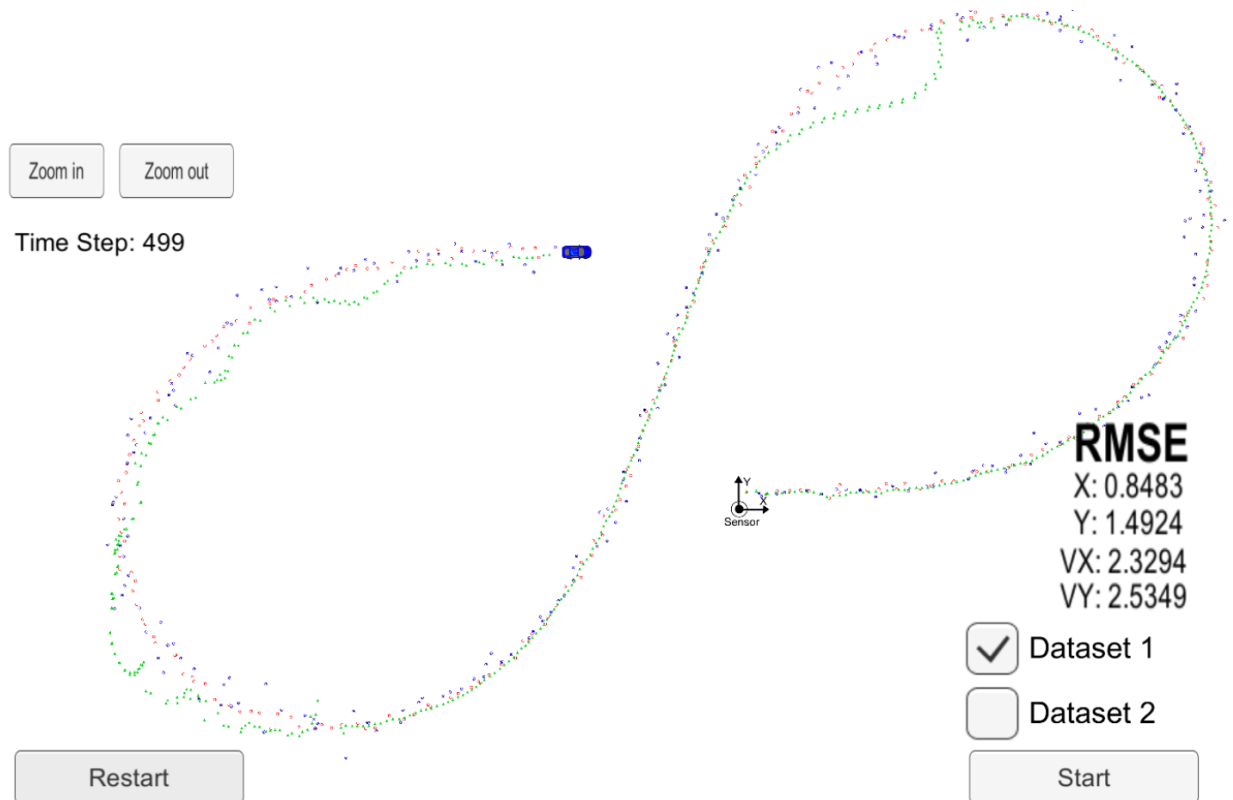
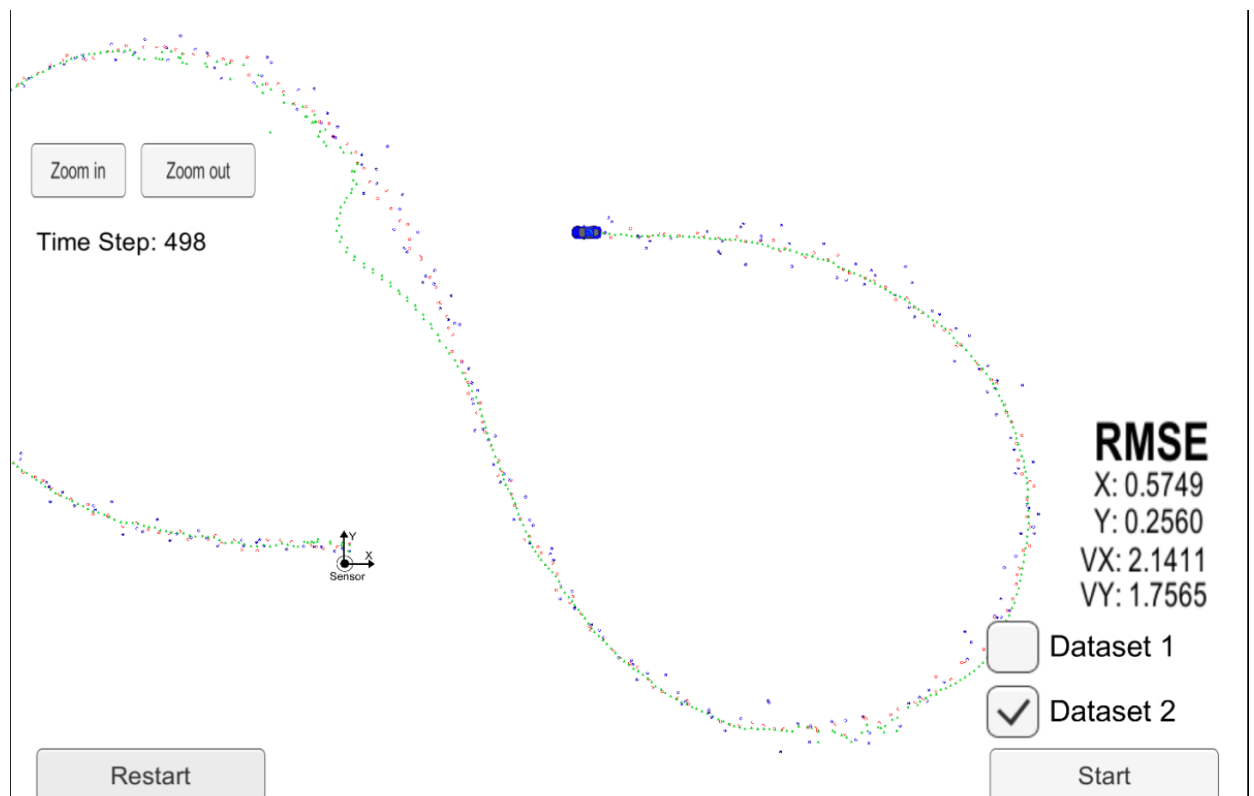
dataset 1



dataset 2



Radar and Lidar measurement

dataset 1**dataset 2**

After removing the unnecessary phi normalization, the estimation (green tracker) was able to follow the tail of the car properly. Another bug discovered was caused by `std_a` and `std_yawdd` being too larger for bicycle database. After multiple attempts to adjust the noise, I settled to the following. I

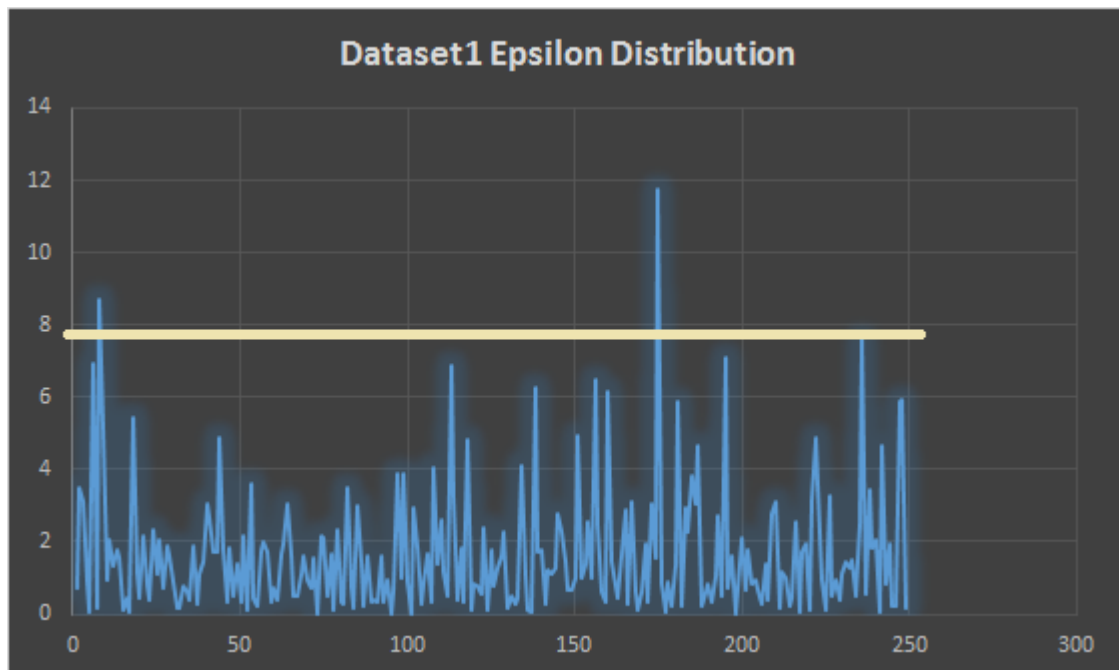
also chose to initialize P _ matrix to zero except $P_{(0,0)}=1$ and $P_{(1,1)}=1$. This gave me a better result on RMSE. But sure there is room to improve.

```
std_a_ = 5.0; // .11, .10, .65, .34
std_yawdd_ = 0.7;
```

The best RMSE is close to the required rubric guideline:

```
for dataset1, (px, py, vx, vy)=(0.11, 0.10, 0.59, 0.25)
for dataset2, (px, py, vx, vy)=(0.09, 0.08, 0.48, 0.26)
```

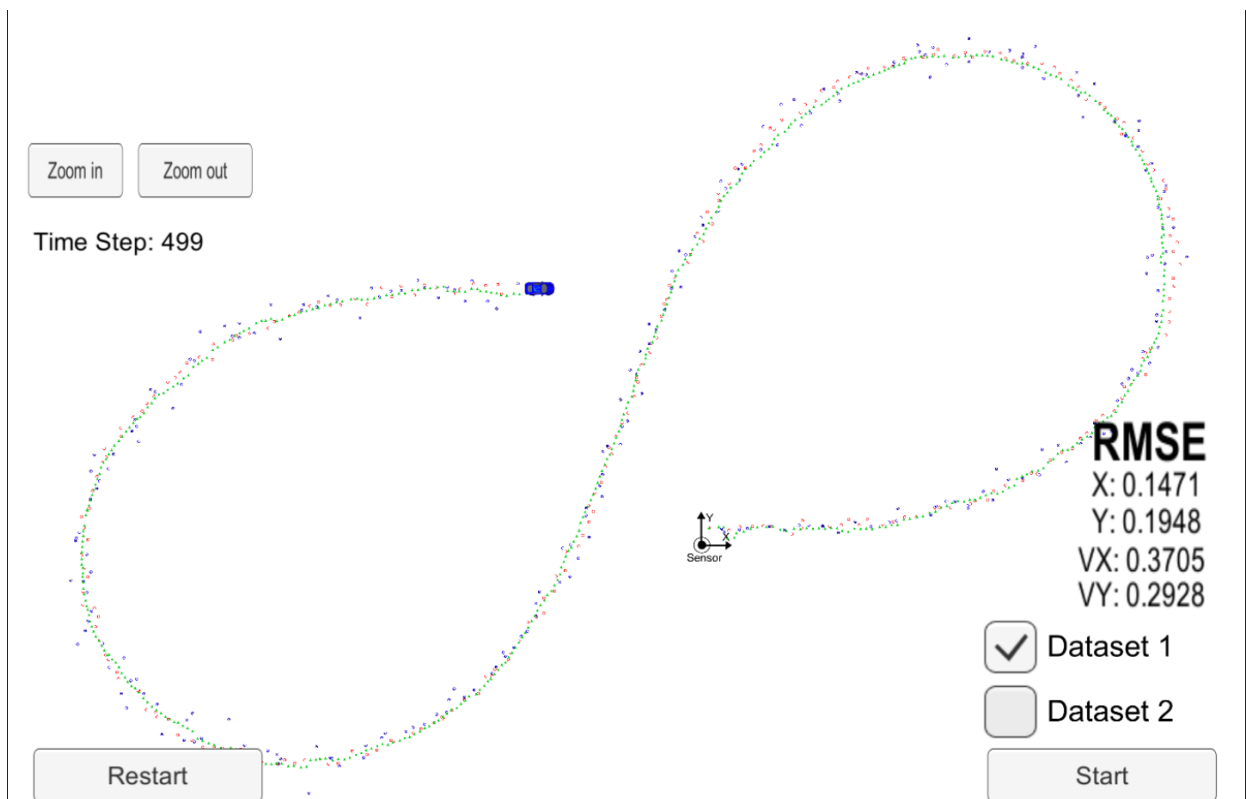
The epsilon value seems within the expectation as suggested from the lection. 95% of epsilon value are below 7.8 (shown as yellow line in chart) according to a 3 degree of freedom.



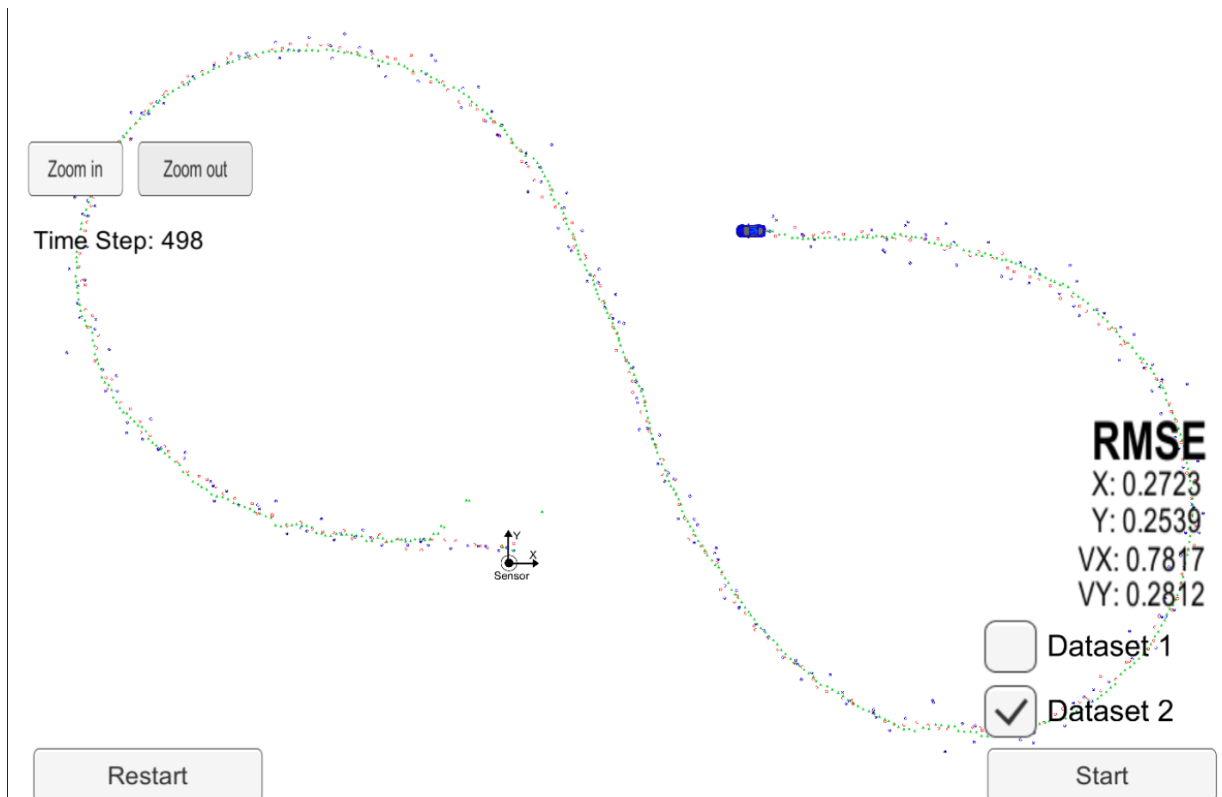
Passing cases after fixing bug

Radar measurement only

dataset 1

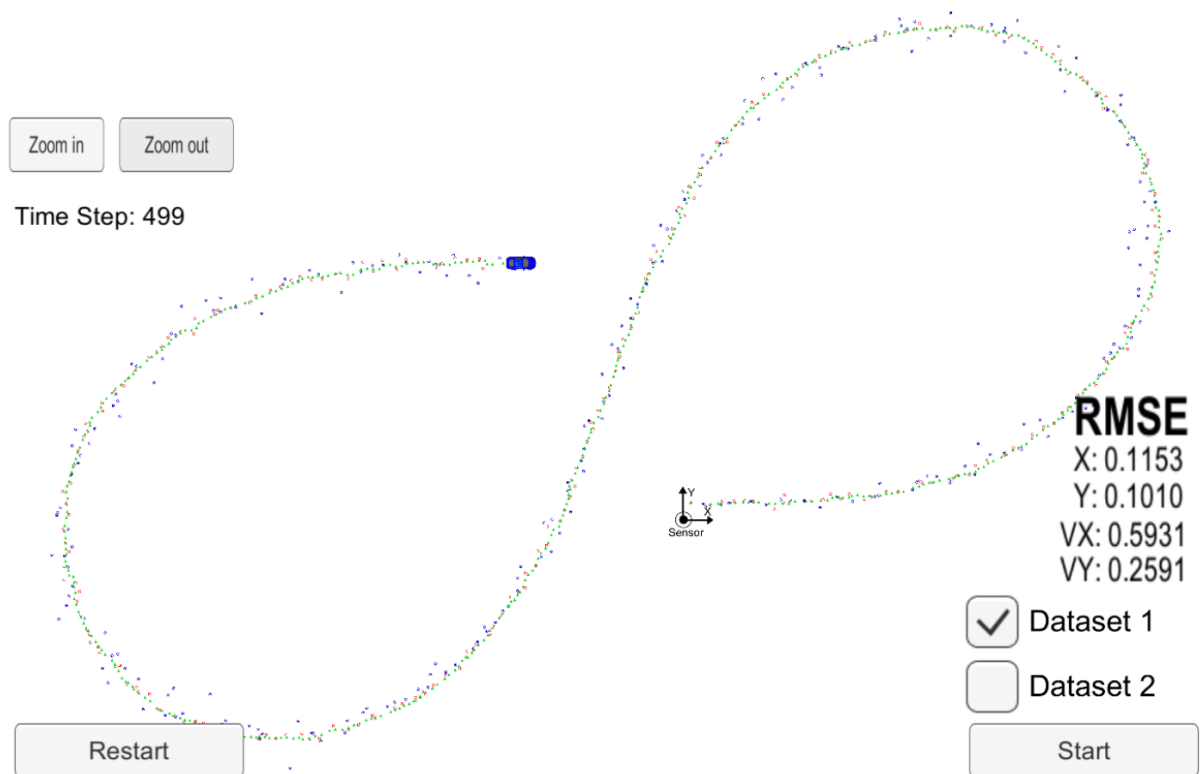


dataset 2

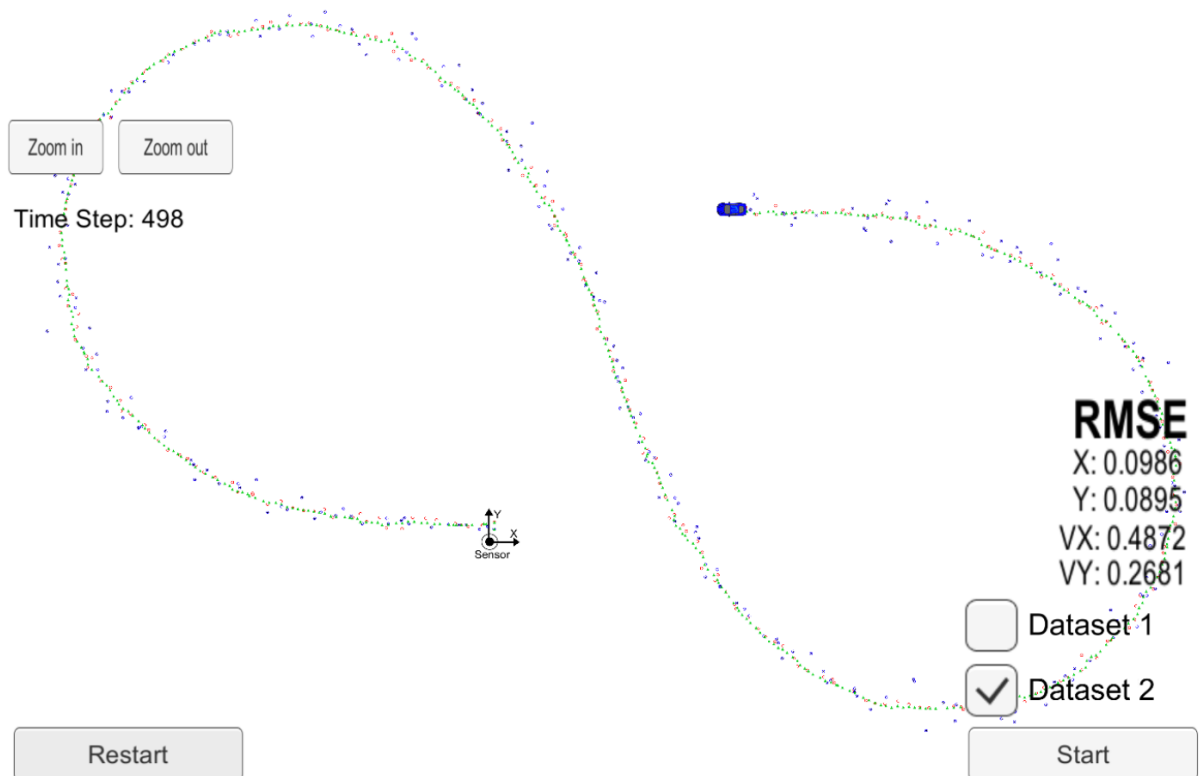


Radar and Lidar measurement

dataset 1



dataset 2



Overall, initialize bring up of this project is not difficult as all instruction had been provided, it does require a lot time to debug the issue and tuning the acceleration and radial acceleration noises to get minimize the RMSE.

In []: