

## LAWS AND THEOREMS OF BOOLEAN ALGEBRA \_\_\_\_\_

Operations with 0 and 1:

1. 
$$X + 0 = X$$

1D. 
$$X \cdot 1 = X$$

2, 
$$X + 1 = 1$$

**2D.** 
$$X \cdot 0 = 0$$

Idempotent laws:

3. 
$$X + X = X$$

3D. 
$$X \cdot X = X$$

Involution law:

4. 
$$(X')' = X$$

Laws of complementarity:

5. 
$$X + X' = 1$$

5D. 
$$X \cdot X' = 0$$

Commutative laws:

6. 
$$X + Y = Y + X$$

6D. 
$$XY = YX$$

Associative laws:

7. 
$$(X + Y) + Z = X + (Y + Z)$$

7D. 
$$(XY)Z = X(YZ) = XYZ$$

$$= X + Y + Z$$

Distributive laws:

8. 
$$X(Y+Z)=XY+XZ$$

8D. 
$$X + YZ = (X + Y)(X + Z)$$

Simplification theorems:

9. 
$$XY + XY' = X$$

**9D.** 
$$(X + Y)(X + Y') = X$$

10. 
$$X + XY = X$$

10D. 
$$X(X + Y) = X$$

11. 
$$(X + Y')Y = XY$$

11D. 
$$XY' + Y = X + Y$$

DeMorgan's laws:

12. 
$$(X + Y + Z + \cdots)' = X'Y'Z' \cdots$$

12. 
$$(X + Y + Z + \cdots)' = X'Y'Z'\cdots$$
 12D.  $(XYZ\cdots)' = X' + Y' + Z' + \cdots$ 

13. 
$$[f(X_1, X_2, \ldots, X_n, 0, 1, +, \cdot)]' = f(X'_1, X'_2, \ldots, X'_n, 1, 0, \cdot, +)$$

Duality.

14 
$$(X \perp Y \perp Z \perp \cdots)^D = XYZ \cdots$$

14. 
$$(X + Y + Z + \cdots)^D = XYZ \cdots$$
 14D.  $(XYZ \cdots)^D = X + Y + Z + \cdots$ 

**15.** 
$$[f(X_1, X_2, \ldots, X_n, 0, 1, +, \cdot)]^D = f(X_1, X_2, \ldots, X_n, 1, 0, \cdot, +)$$

Theorem for multiplying out and factoring:

16. 
$$(X + Y)(X' + Z) = XZ + X'Y$$

**16D.** 
$$XY + X'Z = (X + Z)(X' + Y)$$

Consensus theorem:

17. 
$$XY + YZ + X^2Z = XY + X^2Z$$

17D. 
$$(X + Y)(Y + Z)(X^{T} + Z)$$
  
=  $(X + Y)(X' + Z)$