

## Report for Lab 2

In this report creation of parametric functions is described with respect to the attached files consisting of circle, ellipse, spiral, helix among others.

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## Description of files

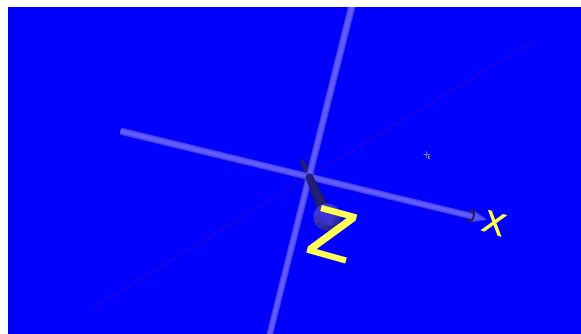
In this lab I have created 8 parametric functions. These are

- Line
- Sin
- Circle and arc
- Ellipse and arc
- 2D Spiral
- Helix

To see the code for each function see the file for the corresponding section.

### Line

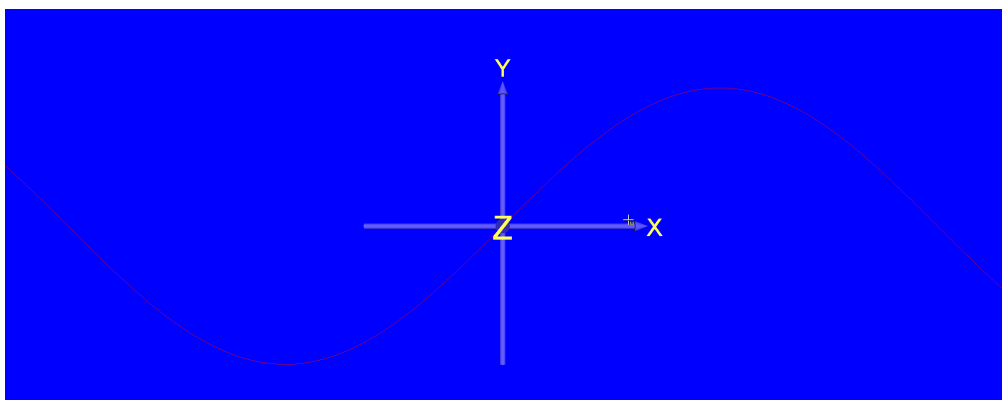
The parametric representation of a line can be as simple as  $x = u$ ,  $y = u$  with  $u$  having a limited domain as it is sufficient for the observing window.



*A picture of the line*

### Sin

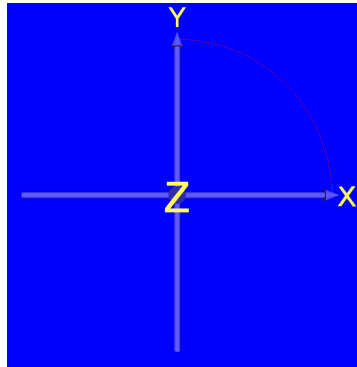
To represent  $y = \sin(x)$  as a parametric function the substitution  $u = x$  was done which resulted in  $y = \sin(u)$ ,  $x = u$ . Since this function is trigonometric  $u$  serves as the angle which implies that the domain of  $u$  is expressed in radians.



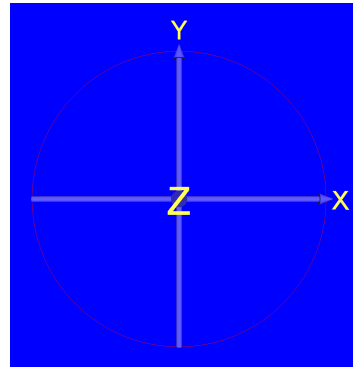
*The sin function with domain  $[-2\pi, 2\pi]$  on  $u$*

## Circle and arc

One parametric representation of a circle is  $x = \sin(u)$ ,  $y = \cos(u)$ . To represent an arc we simply limit the domain of the circle from  $[0, 2\pi]$  to  $[0, \pi/2]$ .



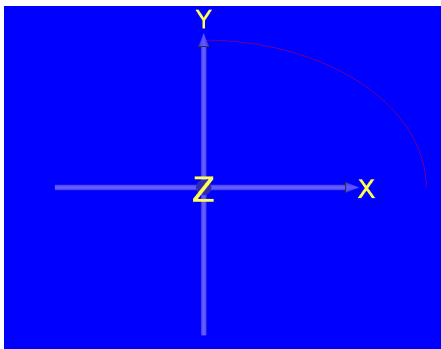
*Arc of circle with domain  $[0, \pi/2]$*



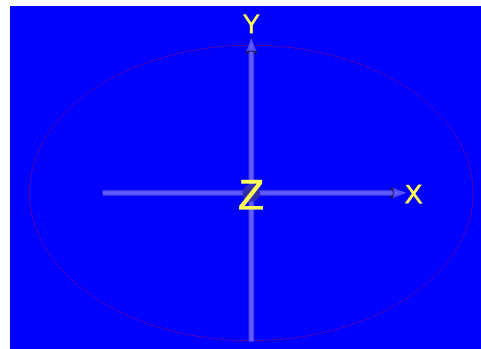
*Circle*

## Ellipse and arc

The parametric representation of an ellipse can be very similar to a circle except that it has a coefficient, it is expressed as  $x = a \sin(u)$ ,  $y = b \sin(u)$  where  $a, b \in \mathbb{R}$  and  $a, b \neq 0$  with  $u$  having a limited domain similar to the previous section.



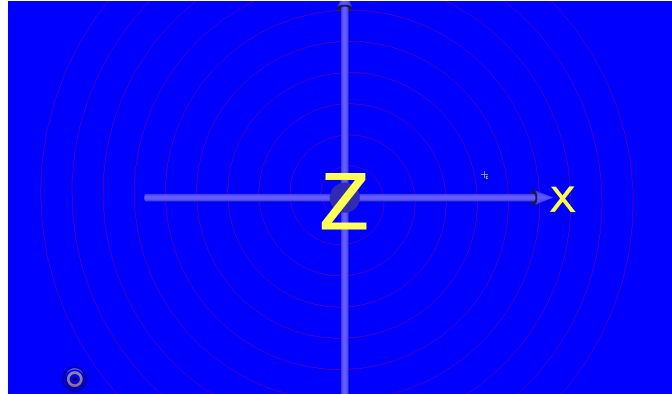
*Arc of ellipse with domain  $[0, \pi/2]$*



*Ellipse*

## 2D Spiral

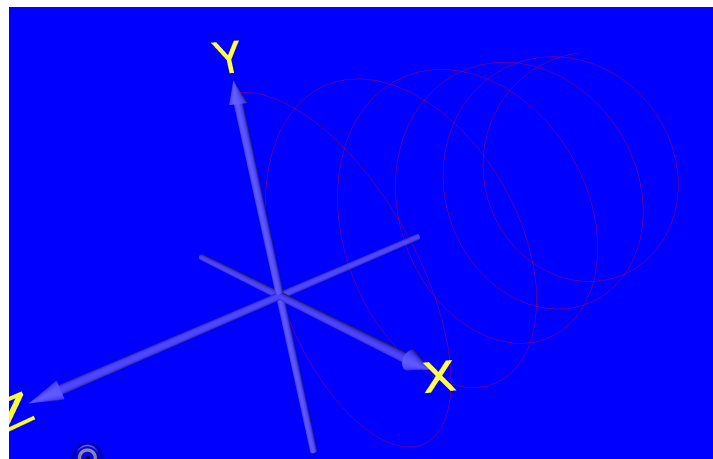
The parametric representation of a 2D spiral can be similar to an ellipse except that it has an additional coefficient  $u$  this results in  $x = ua \sin(u)$ ,  $y = ub \sin(u)$  where in this case  $a = b$ . To allow the spiral to form the domain of  $u$  should be a rather high multiple of  $2\pi$  where the multiple indicates how many turns the spiral will make. To make the spiral display properly an increase of resolution was needed.



*The spiral with a domain of  $[0, 20\pi]$  on the angle and  $a = b = 1/40$  and resolution 600*

## Helix

The parametric representation of a helix can be very similar to a circle. Up until now we have only showed functions which move through the  $xy$ -plane which was achieved by setting  $z = 0$ . In this case we need to use  $z$  to express the helix properly. For these reasons one parametric representation of a helix is  $x = \sin(u)$ ,  $y = \cos(u)$ ,  $z = au$  where  $a \in \mathbb{R}$  and  $a \neq 0$ . In this case  $a$  is used to control the derivative of the helix in the  $z$ -axis.



*A picture of the helix with domain  $[0, 10\pi]$  on the angle and  $a = -0.1$*