Raketentreibstoffe I+II - Cheat Sheet

Basics

Most chemical equations are not valid at high temperatures because of dissociation effects. More dissociation will result in a less released heat during the reaction since energy is needed to break the molecules apart. In general, the following statements are valid during combustion reactions.

Higher pressures lead to less dissociation. Higher temperatures lead to more dissociation.

| Thrust | F | N |
|----------------------|-------|------------------|
| Chamber pressure | p_c | Pa |
| Nozzle exit pressure | p_e | Pa |
| Ambient pressure | p_0 | Pa |
| Oxidizer fuel ratio | ROF | - |
| Initial mass | m_0 | kg |
| Burnout mass | m_b | $_{\mathrm{kg}}$ |

Ziolkowski equation $\Delta v = I_{\rm sp} \cdot g_0 \cdot \ln(\frac{m_0}{m_b})$

Total impulse
$$I_T = \int_0^{t_e} F dt$$

Specific vacuum impulse $I_{\rm sp} = \frac{F}{ma}$

Thrust equation
$$F = \dot{m} \cdot c_e + A_e \cdot (p_e - p_0)$$

Thrust coefficient $c_F = \frac{F}{A_t p_c}$

Characteristic length
$$L^* = V_c/A_t$$

Characteristic speed $c^* = \frac{p_c A_t}{\dot{m}}$
Efficiency of combustion $\eta_{c^*} = \frac{c_{\rm real}^*}{c_{\rm real}^*}$

Tank stress
$$S = \frac{p \cdot r}{2 \cdot t}$$

Thermodynamics

Degrees of Molecular Freedom f -

Ideal gas equation
$$pV = mRT$$

Isentropic Coefficient
$$\kappa = \frac{f+2}{f}$$

Isentropic (adiabatic) expansion
$$\frac{T_1}{T_0} = (\frac{p_1}{p_0})^{\frac{\kappa-1}{\kappa}}$$

Ideal gas constant $R_m = 8.314 \frac{\text{kg m}^2}{\text{s mol K}} = R \cdot M$

Chemical Equations

$$\begin{array}{l} \text{Massfraction } \mu_i = \frac{m_i}{m} \\ \text{Molefraction } \nu_i = \frac{n_i}{n} \\ \text{Molemass } M_i = \frac{m_i}{n_i} \\ \text{Average mole mass } \bar{M} = \frac{m}{n} = \sum M_i \cdot \nu_i \\ \text{Mole to Mass fraction } \mu_i = \frac{M_i}{M} \nu_i \end{array}$$

Assumptions of NASA CEA

Adiabatic combustion chamber.

Isentropic Expansion.

Homogenous mixing.

Thermochemical Equilibrium.

The **frozen** option of CEA will freeze all reaction products after the freezing point, allowing no further reactions in the mixture.

Geometrics

Sphere volume $V = \frac{4}{3}\pi R^3$ Sphere surface $A = 4\pi R^2$ Cylinder Side $A = 2\pi R \cdot h$

Calculating solid/hybrid rocket fuels

| Pressure Exponent | n | - |
|--------------------------------|--------------------|--------------------------------|
| Fuel Surface | A_b | m^2 |
| Port Area | A_p | m^2 |
| Fuel Density | $ ho_b$ | $\frac{\text{kg}}{\text{m}^3}$ |
| Temperature Sensitivity Factor | $\Pi_{\dot{r}}$ | - |
| Constants | a_{ref}, T_{ref} | - |
| Effective Burn Duration | Δt_{AD} | \mathbf{s} |

Regression rate
$$\dot{r} = a \cdot p_{c,0}^n = \frac{\dot{m}}{A_b \rho_b}$$

with $a = a_{ref} \cdot e^{\Pi_{\dot{r}}(T - T_{ref})}$
Temp. Sensitivity $\Pi_{\dot{r}} = \frac{1}{\dot{r}} (\frac{d\dot{r}}{dT})_p$

Regression
rate hybrid
$$\dot{r} = \frac{dR}{dt} = a \cdot G_{ox}^n = a \cdot (\frac{\dot{m}_{ox}}{A_p})^n$$

If the pressure exponent n is greater 1, the combustion chamber is sensible to pressure disturbances and can become in-stable. This leads to a destruction of the motor.

Combustion pressure
$$p_c = (c^* \rho_b a \frac{A_b}{A_t})^{\frac{1}{1-n}}$$
 with $K = \frac{A_b}{A_t}$ as "clamping".

Charact. Speed
$$c^* = \frac{\sqrt{\frac{R_m}{M}T_c}}{\Gamma}$$

Gamma Function
$$\Gamma = \sqrt{\kappa \cdot (\frac{2}{\kappa+1})^{\frac{\kappa+1}{\kappa-1}}}$$

Expansion Ratio
$$\epsilon = \frac{A_e}{A_t} = \Gamma \sqrt{\frac{\kappa - 1}{2\kappa}} \frac{(\frac{p_e}{p_c})^{-\frac{1}{\kappa}}}{\sqrt{1 - (\frac{p_e}{p_c})^{\frac{\kappa - 1}{\kappa}}}}$$

Mole to Mass fraction
$$\mu_i = \frac{M_i}{M} \nu_i$$

Oxygen balance $W_{ox} = -1600(2x + y/2 - z)/M$ with $C_x H_y O_z$

$$I_{sp} = \frac{1}{g} \left[\sqrt{\frac{2\kappa}{\kappa - 1}} \frac{R_m}{M} T_c \left[1 - \left(\frac{p_e}{p_c} \right)^{\frac{\kappa - 1}{\kappa}} \right] + \frac{(p_e - p_a) A_e}{\dot{m}} \right]$$

Effective Thrust $F_{\text{eff}} = \int_{t_A}^{t_D} F \cdot dt / \Delta t_{AD}$

Solid

- Good: High thrust density, storable, low structure mass, no pumps, cheap
- Bad: Short burn times, no reignition, moderate specific impulses, sensible to impacts, not throttable

Liquid

- Good: High specific impulses, reignitable, variable mass flow
- Bad: Movement of fuel in tanks, leakage, complex turbo pumps, big temperature range, zero-g fuel supply

Gel

Gel propellants are mixtures containing at least two phases. A base fluid and a gelator to solidify the base fluid.

- Good: easy to store like solids, can handle metal additives without sedimentation, in use similar to liquid propellants due to shear-thinning behaviour
- Bad: lower density and thrustdensity, lower specific impulses, higher operating pressures to transport the gel are necessary

Hybrid

Hybrid propellants are diffusion limited, which means that the regression rate is not pressure dependent.

- Good: Inherently safe because no oxidizer contained in the fuel, can be throttled and reignited
- Bad: low regression rates, oxidizer-fuel shift in some fuels during operation, not much experience

It has been shown that Paraffin cores have a higher regression rate (3-5 times) than the classical HTPB cores.

Green Propellants

- Good: Lower toxicity, less environmental hazards, lower costs
- Bad: medium specific impulses, not much experience

Editorial

Created by Christian Mollière. Last updated August 11, 2019. Feel free to share and edit!