Clear Cut: Algorithm Design

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1 Input data

The input data is an image of arbitrary size, $M \times N$, where M is the horizontal dimension and N is the vertical dimension of the image. Most images have three channels (RGB = "Red-Green-Blue"), this means an array with three $M \times N$ arrays. Images with exif data are checked and modified so that the image is imported in the intended orientation, e.g. in case the image is a photo taken from a phone camera.

1.1 Image size reduction

To improve the efficiency of the edge detection algorithm, the image size is reduced to that the average image dimension is less than 500 pixels in length. The final image size to be thrown into the algorithm is $M_{\text{eff}} \times N_{\text{eff}}$, where

$$\frac{M_{\text{eff}} N_{\text{eff}}}{2} < 500 \text{ pxl.} \tag{1}$$

The image is currently reduced slowly by max pooling. This relies on calculating the smallest kernel size and repeating the max pooling process until the condition in Equation 1 is satisfied. This can be implemented more effectively by calculating the smallest kernel that would satisfy the condition in Equation 1 after just one implementation of max pooling.

As it currently exists, the process consists of determining the smallest number that divides the height (width) of the image to return an integer. If there is no such factor, i.e. the height (width) is a prime number, the image is cropped by removing the single pixel row (column) at the M_{eff}^{th} (N_{eff}^{th}) index. By definition this would result in that image dimension being divisible by 2, which is then the number of pixels of the smallest kernel in that dimension. Throughout the image reduction process, the values (M_{eff}, N_{eff}, M_{kernel}, N_{kernel}) are stored in a Python dictionary to keep a record of the image reduction history.

2 Edge detection procedure

2.1 The gradient image

For Python code, refer to the **traceObjectsInImage()** function in edgeUtility.py

In order to determine the edges of an image, we must choose a criteria to distinguishing a single pixel located at (i_0, j_0) as being part of "an edge". We would refer to such pixels as "edge pixels" or "non-edge pixels" in future. This is achieved by mathematically comparing its value to those of its surrounding pixels. The simplest method to adopt is to consider only the pixels neighbouring pixels (i, j), i.e. any combination of pixels that satisfy

$$i_0 - 1 \leq i \leq i_0 + 1, \text{ and } j_0 - 1 \leq j \leq j_0 + 1. \tag{2}$$

A more advanced technique could extend the range of neighbouring pixels. For a pixel not located on the perimeter of the image, it would have 8 neighbouring pixels.

The mathematical quantity we are interested in is the difference in value between a selected pixel and it's neighbouring pixels. For the simple case, an edge pixel would be identified as having a large difference in value between any adjacent neighbouring pixel and itself. This simplest case works well for an image with sharp edges, but not so well for an image with blurry edges. With eight neighbouring pixels, we would have to calculate eight gradients per pixel. It turns out that we can more efficient in calculating the gradients and only count four instead. This is because when the neighbouring pixel has the gradient

calculated, it would be the same magnitude but a different sign. The sign is irrelevant for determining the "sharpness" between pixels. This means that the eight gradient per pixel method would double-count the number of gradients; therefore we need only calculate four gradients per pixel instead.

Thus for a generic pixel at (i, j), the difference in value between pixels $(i-1, j-1)$, $(i+1, j)$, $(i, j+1)$, and $(i+1, j+1)$ is calculated. These four directions are a choice and are not expected to make a difference in the final result. Note that not all gradients can be calculated if the pixel under consideration sits along the perimeter of the image. That each pixel in the "image space" has four unique gradients calculated, means that we will obtain a "gradient space" of size $2M_{\text{eff}} \times 2N_{\text{eff}}$.

2.2   Dealing with image channels

2.2.1   Obtaining gradient images

For Python code, refer to the **traceObjectsInImage()** function in edgeUtility.py

Each of the RGB channels have the edge detection algorithm specified in Section 2.1 applied to them. This is achieved by writing out the results to a single array of size $6M_{\text{eff}} \times 2N_{\text{eff}}$, where each channel's gradient image is offset as follows:

- the Red channel gradient array exists in the domain $(0,\ 2M_{\text{eff}} - 1)$,

- the Green channel gradient array exists in the domain $(2M_{\text{eff}},\ 4M_{\text{eff}} - 1)$, and

- the Blue channel gradient array exists in the domain $(4M_{\text{eff}},\ 6M_{\text{eff}} - 1)$.

Recall that we could only reduce the number of gradients per pixel if we ignore the gradients sign. Therefore, we must take care to only add up the gradient images element-wise AFTER taking the magnitude of each element first. The initial step in edge detection is to determine whether an (rgb) pixel in the reduced image is, or is not, part of an edge; this turns each pixel into a "yes" or "no" (boolean) answer. We therefore set a numerical upper and lower limit on what is an edge pixel, and what is not. We implement this through a variable parameter called `imCut`, whereby an edge pixel is one in which the gradient lives between:

$$255 \times \texttt{imCut} < \text{Gradient}_{\text{edge pixel}} < 255 \times (1 - \texttt{imCut}). \tag{3}$$

We have found $\texttt{imCut} = 0.07 \pm 0.02$ to work effectively. We have found both the upper limit and lower limit are necessary to extract clear edge pixels for any image. The lower limit is understandable because it determines adjacent pixels with too similar a colour as not being an edge pixel, however, the upper limit is less trivial. We believe the upper limit is necessary to remove random fluctuations in light/darkness within an image. These may be the result of tiny defective regions of photographical film that cannot be seen by the human eye when the image view at a larger scale that the size of the defect.

2.2.2   Returning detected edges in reduced image size

For Python code, refer to the **mergeChannelsTracedImage()** function in edgeUtility.py

We now have three gradient space arrays. However, we only want one gradient space array to say whether a single (rgb) pixel in the reduced image is an edge or not. This means we that we need to merge each of the gradient arrays into a single gradient array, and then reduce this gradient array to be the same size as the reduced image. The idea behind the merge is that **the more channels that detect an edge, the**

more likely it is to be an edge. This is in agreement with human perception that an orange boat on a blue sea is far more distinct object than a blue boat on a blue sea. We therefore simply add up each gradient image element-wise to form our final gradient image.

This final gradient image is still roughly double the width and double the height of the reduced image. We reduce the gradient image to the same size as the reduced image using max pooling of (2×2)-sized kernels. Therefore the final "edge value" of each (rgb) pixel of the reduced image is determined by the largest gradient of that pixel and its neighbouring pixel. This in turn determines whether it is an edge pixel or not.

2.3   Cleaning the edge data

Now that we have two arrays of the same size, we can mask the edge image on top of the reduced image to view our current results. In doing so for a number of unique images, we observe two main features:

1. There exist spurious regions of edge pixels with a size of the order of a few pixels. **Solution: remove tiny regions of edge data.**

2. There are edge pixels around the perimeter of objects in the reduced image, but with the occasional break, whereby no edge pixels exist. **Solution: extrapolate long regions of edge data.**

2.3.1   Removing small scale edge data

For Python code, refer to the **edgeKiller()** function in edgeUtility.py

To accomplish this task, we first need to decide what a small scale is. This is necessary for object recognition because many complicated objects are made of smaller, perhaps even more complicated objects. Fundamentally, if an object is identified as being surrounded by a continuous border of edge pixels, then the smallest object would be three pixels in size. This because the border must be at least one pixel thick and the central pixel must not be recognised as an edge (two pixels either side of a non-edge pixel in the x and y direction), i.e. a square drawn around the perimeter of a 3×3 pixel grid.

2.3.2   Expand large-length edge data

For Python code, refer to the **edgeFiller()** function in edgeUtility.py