CS 106B Section 8 (Week 9) Solutions

1. Depth-First Search (DFS)

Graph 1:

A to B: {A, B}
A to C: {A, B, E, F, C}
A to D: {A, B, E, D}
A to E: {A, B, E}
A to F: {A, B, E, F}
A to G: {A, B, E, D, G}
A to H: {A, B, E, D, G, H}

Graph 6:

A to B: {A, C, B} A to C: {A, C} A to D: {A, C, D} A to E: {A, C, B, F, E} A to F: {A, C, B, F} A to G: {A, C, G}

2. Breadth-First Search (BFS) – shorter paths underlined

Graph 1:

A to I: no path

A to B: {A, B}
A to C: {A, B, E, F, C}
A to D: {A, D}
A to E: {A, B, E}
A to F: {A, B, E, F}
A to G: {A, D, G}
A to H: {A, D, G, H}
A to I: no path

Graph 6:

A to B: {A, C, B} A to C: {A, C} A to D: {A, C, D} A to E: {A, E} A to F: {A, E, F} A to G: {A, C, G}

3. Minimum weight paths – *lower weight paths underlined*

A to B: {A, E, F, B}, weight=5

A to C: {A, E, F, B, C}, weight=6

A to D: {A, E, F, B, C, G, D}, weight=12

A to E: $\{A, E\}$, weight=1

A to F: $\{A, E, F\}$, weight=3

A to G: {A, E, F, B, C, G}, weight=11

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4. isReachable

```
DFS solution:
bool_isReachable(BasicGraph& graph, Vertex* v1, Vertex* v2) {
      Set<Vertex*>`visited;
      return isReachable(graph, v1, v2, visited);
bool isReachable(BasicGraph& graph, Vertex* v1, Vertex* v2,
                          Set<Vertex*> visited) {
      if (v1 == v2)
            return tŕuè;
      visited += v1;
for (Edge* edge : graph.getEdgeSet(v1)) {
    Vertex* neighbor = edge->finish;
    if (!visited.contains(neighbor)
                        && isReachable(graph, neighbor, v2, visited)) {
                  return true;
      return false;
}
BFS solution:
bool isReachable(BasicGraph& graph, Vertex* v1, Vertex* v2) {
   Queue<Vertex*> toExplore;
   Set<Vertex*> visited;
     visited += v1;
visited += v1;
toExplore.enqueue(v1);
while (!toExplore.isEmpty()) {
    Vertex* next = toExplore.dequeue();
    if (next == v2) {
        return true:
                  return true;
            for (Vertex* neighbor : graph.getNeighbors(next)) {
   if (!visited.contains(neighbor)) {
                         visited += neighbor;
                        toExplore.enqueue(neighbor);
      return false;
}
```

5. isConnected

```
bool isConnected(BasicGraph& graph) {
    for (Vertex* v1 : graph.getVertexSet()) {
        for (Vertex* v2 : graph.getVertexSet()) {
            if (v1 != v2 && !isReachable(graph, v1, v2)) {
                return false;
            }
        }
        return true;
}
```

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6. findMinimumVertexCover

```
Set<Vertex*> best = graph.getVertexSet();
Set<Vertex*> chosen;
    Set<Edge*> coveredEdges
    Vector<Vertex*> allVertices;
for (Vertex* v : graph.getVertexSet()) {
    allVertices += v;
    coverHelper(graph, chosen, coveredEdges, allVertices, 0, best);
}
return;
} else if (coveredEdges.size() == graph.getEdgeSet().size()) {
    // base case: found a new smaller cover that uses all edges;
    // remember it
         best = chosen;
    return;
} else if (index == graph.getVertexSet().size()) {
   // base case: exhausted all vertices to explore
         return;
    } else {
    // recursive case: explore whether or not to include the current vertex
    // recursive case: explore whether or not to include the current vertex
         // choose not to include this vertex; explore
         coverHelper(graph, chosen, coveredEdges, allVertices, index + 1, best);
          / choose to include this vertex; explore
         chosen += allVertices[index];
         Edge* inverse = graph.getEdge(e->finish, e->start);
newEdges += e, inverse;
coveredEdges += e, inverse;
         coverHelper(graph, chosen, coveredEdges, allVertices, index + 1, best);
         // unchoose
         chosen -= allVertices[index];
         coveredEdges -= newEdges;
}
```