## On a Class of Permutation Polynomials

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## Abstract

A polynomial f(x) defined over a set A is called a **permutation polynomial** if f(x) acts as a permutation over the elements of A. This is, if  $f:A\to A$  is 1-1 and onto. We study the coefficients a and b that make polynomials of the form  $F_{a,b}(x)=x^{\frac{p+1}{2}}+ax^{\frac{p+5}{6}}+bx$  permutation polynomials over the finite field  $\mathbb{F}_q$ ,  $a,b\in\mathbb{F}_q^\times$ . We show that this family of polynomials is rich in permutations, and that the amount of permutation polynomials for any q is divisible by 6. Our approach in studying  $F_{a,b}(x)$  is to use the division algorithm to consider  $x=\alpha^n$  where n=6k+r, r=0,...,5. If  $F_{a,b}(x)$  is a permutation, this partitions  $\mathbb{F}_q^\times$  into 6 classes:  $F_{a,b}(\alpha^{6k+r})$  for r=0,...,5.