On a Class of Permutation Polynomials over Finite Fields

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Abstract

1 Results

Definition 1.1. Sea $a=\alpha^i,b=\alpha^j$ y \sim la relacion definida por $(a,b)\sim(a',b')$ $<=>a'=\alpha^{i+h(\frac{p-1}{d_1}-\frac{p-1}{d_2})},b'=\alpha^{j+h(\frac{p-1}{d_1})}$

Proposition 1.2. \sim definida arriba es una relación de equivalencia.

Proof. Pendiente

Proposition 1.3. Sea [a,b] la clase de equivalencia de (a,b). Si $(a',b') \in [a,b]$, entonces $|V_{a',b'}| = |V_{a,b}|$

Proposition 1.4. Si $d_2 = d_1 \cdot h$, entonces $|[a, b]| = d_2$

Proof. Sea α la raiz primitiva del cuerpo finito.

$$F_{a',b'}(\alpha^{k+1}) = \alpha^{k+1} ((\alpha^{k+1})^{\frac{p-1}{d_1}} + \alpha^{i + \frac{p-1}{d_1} - \frac{p-1}{d_2}} (\alpha^{k+1})^{\frac{p-1}{d_2}} + \alpha^{j + \frac{p-1}{d_1}})$$

$$= \alpha^{k+1} ((\alpha^k)^{\frac{p-1}{d_1}} \cdot \alpha^{\frac{p-1}{d_1}} + \alpha^i \cdot \frac{\alpha^{\frac{p-1}{d_1}}}{\alpha^{\frac{p-1}{d_2}}} (\alpha^k)^{\frac{p-1}{d_2}} \cdot \alpha^{\frac{p-1}{d_2}} + \alpha^j \cdot \alpha^{\frac{p-1}{d_1}})$$

$$= \alpha^{\frac{p-1}{d_1}+1} \cdot \alpha^k ((\alpha^k)^{\frac{p-1}{d_1}} + \alpha^i (\alpha^k)^{\frac{p-1}{d_2}} + \alpha^j)$$

$$= C \cdot F_{a,b}(\alpha^k), \text{ donde } C = \alpha^{\frac{p-1}{d_1}+1}$$

Proposition 1.5. Suponga que $d_2=d_1\cdot h+r,\, 1\leq r\geq d_1.$ Entonces, $|[a,b]|=\frac{d_1\cdot d_2}{?}$

Proposition 1.6. El número de polinomios $F_{a',b'}(x)$ con $|V_{a,b}|$ es un múltiplo de |[a,b]|

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