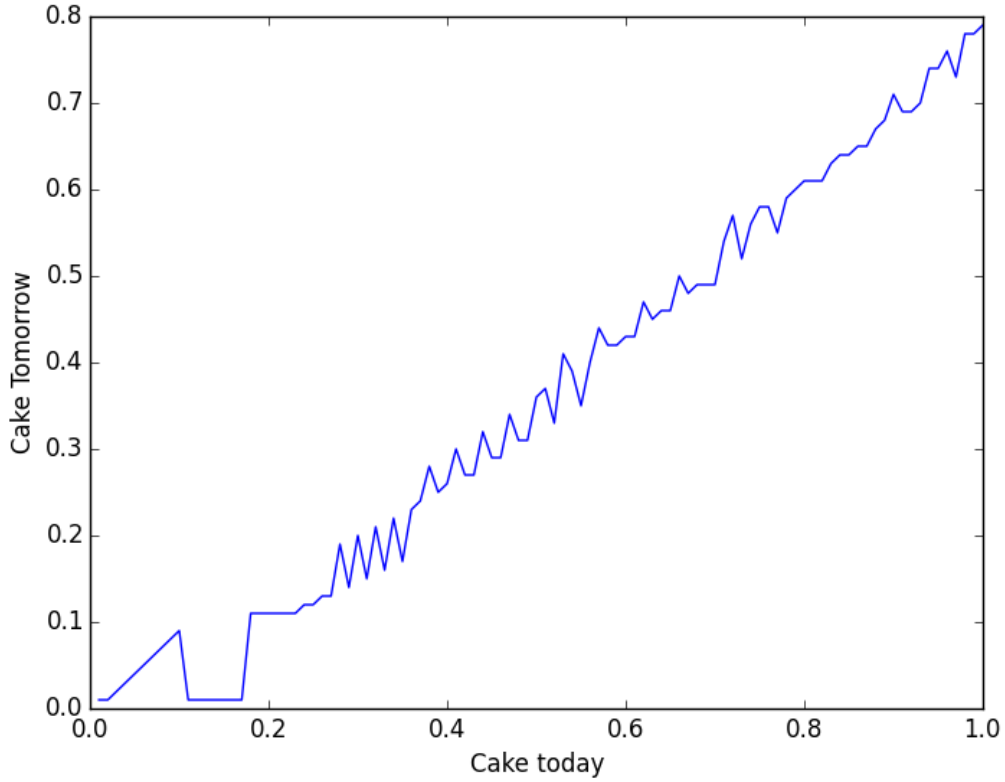


# 1 First Section

## 1.1 5.31



The policy function takes 17 iterations to converges to within the error tolerance. This is much quicker than the 134 iterations it took in 5.14

## 1.2 6.1

$$\begin{aligned}
 \frac{1}{e^{z_t} K_t^\alpha - K_{t+1}} &= \beta E_t \frac{\alpha e^{z_t+1} K_{t+1}^{\alpha-1}}{e^{z_t+1} K_{t+1}^\alpha - K_{t+2}} \\
 &= \beta E_t \frac{\alpha e^{\rho z_t + \sigma \epsilon_t} K_{t+1}^{\alpha-1}}{e^{\rho z_t + \sigma \epsilon_t} K_{t+1}^\alpha - A e^{\rho z_t + \sigma \epsilon_t} K_{t+1}^\alpha} \\
 &= \beta E_t \frac{\alpha}{K_{t+1}(1-A)} \\
 &= \beta \frac{\alpha}{K_{t+1}(1-A)} \\
 &= \frac{1}{K_{t+1}(\frac{1-A}{A})} = \beta \frac{\alpha}{K_{t+1}(1-A)} \\
 &\implies A = \beta \alpha
 \end{aligned}$$

### 1.3 6.2

$$\begin{aligned}
R_t &= \alpha e_t^z K_t^{\alpha-1} L_t^{1-\alpha} \\
L_t &= (1-\alpha) e_t^z K_t^\alpha L_t^{-\alpha} \\
\frac{1}{c_t} &= \beta E_t \left[ \frac{1}{c_{t+1}} [(r_{t+1} - \delta)(1-\tau) + 1] \right] \\
\frac{a}{1-l_t} &= \frac{1}{c_t} w_t (1-\tau)
\end{aligned}$$

### 1.4 6.3

$$\begin{aligned}
R_t &= \alpha e_t^z K_t^{\alpha-1} L_t^{1-\alpha} \\
L_t &= (1-\alpha) e_t^z K_t^\alpha L_t^{-\alpha} \\
\frac{1}{c_t^\gamma} &= \beta E_t \left[ \frac{1}{c_{t+1}^\gamma} [(r_{t+1} - \delta)(1-\tau) + 1] \right] \\
\frac{a}{1-l_t} &= \frac{1}{c_t^\gamma} w_t (1-\tau)
\end{aligned}$$

### 1.5 6.4

$$\begin{aligned}
R_t &= \alpha e^{z_t} K_t^{\eta-1} [\alpha K_t^\eta + (1-\alpha) L_t^\eta]^{\frac{1-\eta}{\eta}} \\
L_t &= (1-\alpha) \eta L_t^{\eta-1} e^{z_t} [\alpha K_t^\eta + (1-\alpha) L_t^\eta]^{\frac{1-\eta}{\eta}} \\
\frac{1}{c_t^\gamma} &= \beta E_t \left[ \frac{1}{c_{t+1}^\gamma} [(r_{t+1} - \delta)(1-\tau) + 1] \right] \\
\frac{-a}{(1-l_t)^\xi} &= \frac{1}{c_t^\gamma} w_t (1-\tau)
\end{aligned}$$

### 1.6 6.5

Characterizing equations:

$$\begin{aligned}
R_t &= \alpha K_t^{\alpha-1} (e^{z_t} L_t)^{1-\alpha} \\
L_t &= (1-\alpha) (e^{z_t})^{1-\alpha} K_t^\alpha L_t^{-\alpha} \\
\frac{1}{c_t} &= \beta E_t \left[ \frac{1}{c_{t+1}} [(r_{t+1} - \delta)(1-\tau) + 1] \right]
\end{aligned}$$

Steady-state versions of equations:

$$\bar{R} = \alpha \bar{K}^{\alpha-1} (e^{\bar{z}} \bar{L})^{1-\alpha}$$

$$\bar{L} = (1 - \alpha)(e^{\bar{z}})^{1-\alpha} \bar{K}^\alpha \bar{L}^{-\alpha}$$

$$\frac{1}{\bar{c}^\gamma} = \beta \bar{E} \left[ \frac{1}{\bar{c}^\gamma} [(\bar{r} - \delta)(1 - \tau) + 1] \right]$$

Steady-state value of K:

$$\bar{K} = \left( \left( \frac{1 - \beta}{\beta(1 - \tau)} + \delta \right) \frac{1}{\alpha(e^{\bar{z}})^{1-\alpha}} \right)^{\frac{1}{(1-\alpha)}}$$

Steady-state values of variables:

$$\begin{aligned} k &= 7.28749795 \\ y &= 2.21325461 \\ i &= 0.7287498 \\ c &= 1.48450482 \\ r &= 0.12148228 \\ w &= 1.32795277 \\ T &= 0.07422524 \end{aligned}$$

## 1.7 6.6

Characterizing equations:

$$\begin{aligned} R_t &= \alpha K_t^{\alpha-1} (e^{z_t} L_t)^{1-\alpha} \\ L_t &= (1 - \alpha)(e^{z_t})^{1-\alpha} K_t^\alpha L_t^{-\alpha} \\ \frac{1}{c_t^\gamma} &= \beta E_t \left[ \frac{1}{c_{t+1}^\gamma} [(r_{t+1} - \delta)(1 - \tau) + 1] \right] \\ a(1 - L_t)^{-\xi} &= c^{-\gamma} w(1 - \tau) \end{aligned}$$

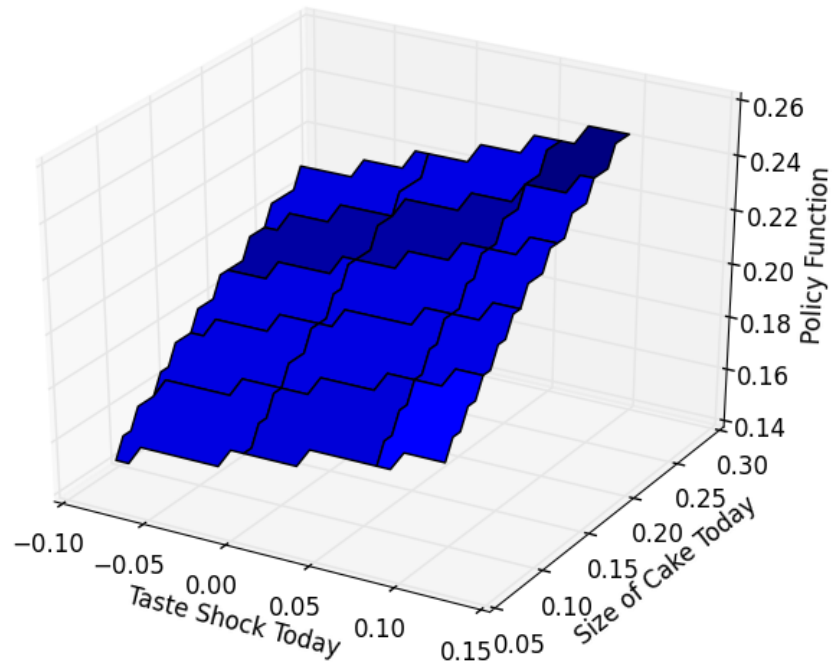
Steady State versions:

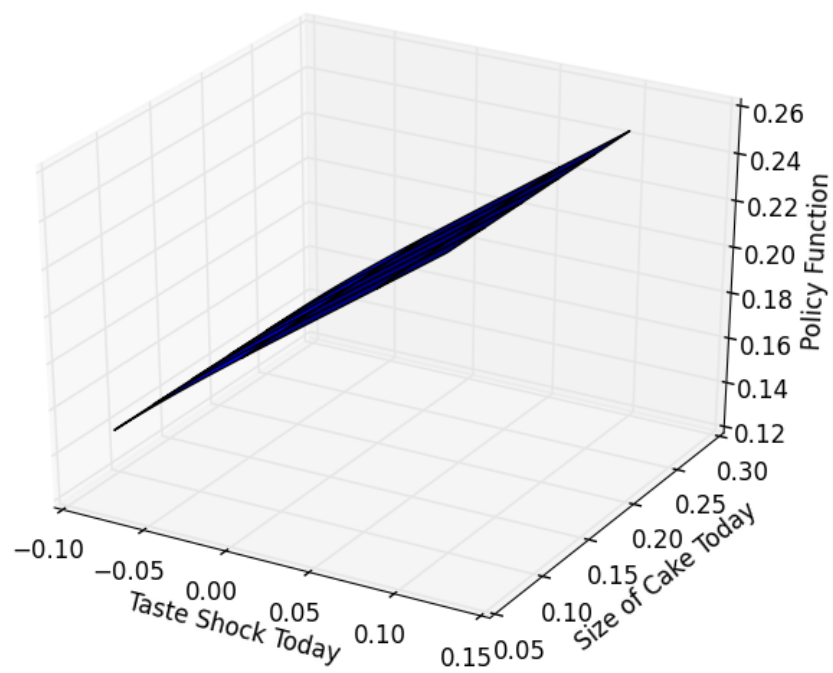
$$\bar{K} = \left( \left( \frac{1 - \beta}{\beta(1 - \tau)} + \delta \right) \frac{1}{\alpha(e^{\bar{z}})^{1-\alpha}} \right)^{\frac{1}{(1-\alpha)}}$$

Steady-state values of variables:

$$\begin{aligned} k &= 4.22522902678 \\ l &= 0.579791453167 \\ y &= 1.28322610883 \\ i &= 0.422522902678 \\ c &= 0.860703206154 \\ r &= 0.121482277121 \\ w &= 1.32795276835 \\ T &= 0.0430351603077 \end{aligned}$$

1.8 6.8





1.9 6.9

