Assignment 3 - Depletion assumptions

Christian Carson

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Leslie Depletion Model Base

$$N_t = N_0 - K_t$$

Where: - N_t is the number of fish at time t - N_0 is the initial number of fish - K_t is the cumulative catch up to the last time period

K t is calculated as:

$$K_t = \sum_{t=0}^{t-1} C_t$$

So, in period 1, $K_1 = C_0$, in period 2, $K_2 = C_0 + C_1$, and so on.

If we assume catch rate is proportional to abundance (i.e. $C_t/E_t = qN_t$), then we can substitute this into the Leslie Depletion Model to get:

$$C_t/E_t = qN_0 - qK_t$$

Where: - q is the catchability constant, the proportion of the population caught per unit of fishing effort. If effor is constant, E_t is constant, and C_t/E_t is the catch rate, then q is the catch rate per unit of effort.

So, if we assume that the catch rate is proportional to abundance, then the Leslie Depletion Model becomes: $C_t = pN_0 - pK_t$

Where: -p = is the probability of capture

The main assumptions of the Leslie Depletion Model are: 1. equal capture probability between successive depletion events; 2. all animals are equally catchable; 3. the population is closed.

This markdown explores where or not these assumptions 'hold water', pun intended.

First, we adapt the code from class of the threepass code from class to evaluate how changes in capture probability and abundance affect the estimated abundance at time 0.

```
```r
"Base" <- function(N_0 = 100, p = 0.5) {
C t <- vector()
N_t <- vector()
K t <- vector()</pre>
K_t[1] <- 0
N_t[1] <- N_0
for(t in 1:5){
 C_t[t] \leftarrow rbinom(n = 1, size = N_t[t], prob = p)
 K_t[t+1] \leftarrow K_t[t] + C_t[t]
 N_t[t+1] <- N_t[t] - C_t[t]
lin_est \leftarrow lm(C_t \sim K_t[1:5])
N_0_hat <- lin_est$coef[1]/-lin_est$coef[2]</pre>
return(N_0_hat)
}
. . .
```

Then, we modify the capture probability and abundance in several different ways: (1) proportional change in capture probability of +5% per time step

```
"P_Pos" <- function(N_0 = 100, p = 0.5, delta_p = 0.05) {
 C t <- vector()
 N_t <- vector()
 K t <- vector()</pre>
 K_t[1] <- 0
 N t[1] <- N 0
 for(t in 1:5){
 C_t[t] \leftarrow rbinom(n = 1, size = N_t[t], prob = p)
 K_t[t+1] \leftarrow K_t[t] + C_t[t]
 N_t[t+1] <- N_t[t] - C_t[t]
 p \leftarrow p * (1 + delta_p)
 }
 lin_est <- lm(C_t~K_t[1:5])</pre>
 N_0_hat <- lin_est$coef[1]/-lin_est$coef[2]</pre>
 return(N_0_hat)
}
```

2. proportional change in capture probability of -5% per time step

```
"P_Neg" <- function(N_0 = 100, p = 0.5, delta_p = -0.05) {
 C_t <- vector()
 N_t <- vector()
 K_t[1] <- 0
 N_t[1] <- N_0
 for(t in 1:5){
 C_t[t] <- rbinom(n = 1, size = N_t[t], prob = p)
 K_t[t+1] <- K_t[t] + C_t[t]
 N_t[t+1] <- N_t[t] - C_t[t]
}
lin_est <- lm(C_t \cdot K_t[1:5])
N_0_hat <- lin_est$coef[1]/-lin_est$coef[2]
return(N_0_hat)
}</pre>
```

3. proportional change in abundance of +5% per time step

```
"A_Pos" <- function(N_0 = 100, p = 0.5, delta_N = 0.05) {
 C_t <- vector()</pre>
 N_t <- vector()
 K_t <- vector()</pre>
 K t[1] <- 0
 N_t[1] <- N_0
 for(t in 1:5){
 C_t[t] \leftarrow rbinom(n = 1, size = N_t[t], prob = p)
 K_t[t+1] \leftarrow K_t[t] + C_t[t]
 N t[t+1] <- N t[t] - C t[t]
 N_t[t+1] \leftarrow as.integer(N_t[t+1] * (1 + delta_N))
 }
 lin_est \leftarrow lm(C_t \sim K_t[1:5])
 N_0_hat <- lin_est$coef[1]/-lin_est$coef[2]
 return(N_0_hat)
}
```

4. proportional change in abundance of -5% per time step

```
"A_Neg" <- function(N_0 = 100, p = 0.5, delta_N = -0.05) {
 C_t <- vector()
 N_t <- vector()
 K_t[1] <- 0
 N_t[1] <- N_0
 for(t in 1:5){
 C_t[t] <- rbinom(n = 1, size = N_t[t], prob = p)
 K_t[t+1] <- K_t[t] + C_t[t]
 N_t[t+1] <- N_t[t] - C_t[t]
 N_t[t+1] <- as.integer(N_t[t+1] * (1 + delta_N))
}
lin_est <- lm(C_t~K_t[1:5])
 N_0_hat <- lin_est$coef[1]/-lin_est$coef[2]
 return(N_0_hat)
}</pre>
```

Now, we run each senario 100 times to get a distribution of estimted abundances

```
Base_Results <- replicate(100, Base(N_0 = 100, p = 0.5))

P_Pos_Results <- replicate(100, P_Pos(N_0 = 100, p = 0.5, delta_p = 0.05))

P_Neg_Results <- replicate(100, P_Neg(N_0 = 100, p = 0.5, delta_p = -0.05))

A_Pos_Results <- replicate(100, A_Pos(N_0 = 100, p = 0.5, delta_N = 0.05))

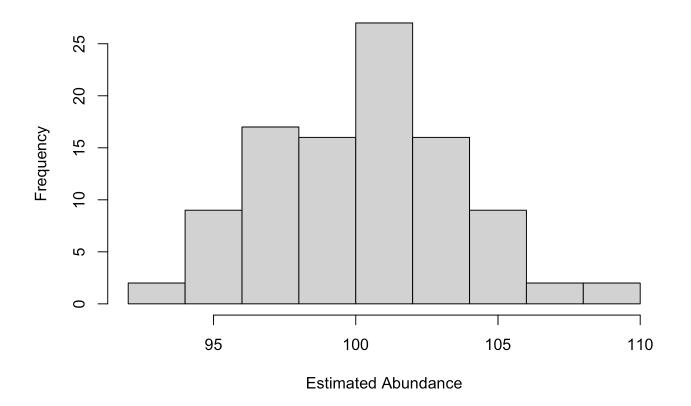
A_Neg_Results <- replicate(100, A_Neg(N_0 = 100, p = 0.5, delta_N = -0.05))
```

Finally, we visualize the results side by side for comparisons to be made in the questions below.

In the first senario, increasing the probability of capture overtime seems to result in an overestimation of population abundance. This is likely because the higher propbability in later captures results in a larger proprotion of the population being caught, which is then used to estimate the initial population size.

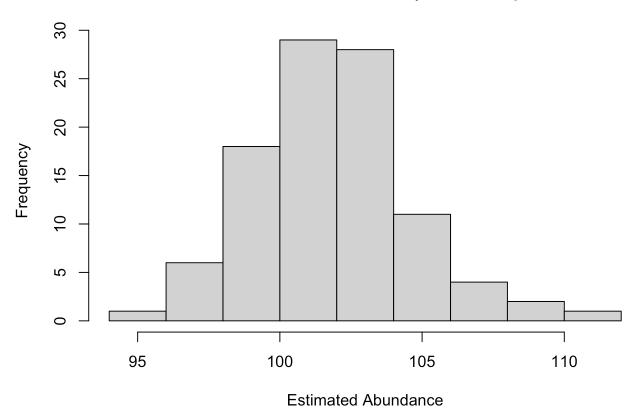
In the real world, this might be due a myriad of factors, such as the animals becoming habituauted to the capture methods, capture methods becoming more efficient over time, animals becoming less cuatios over time, or the population becoming more concentrated over time where the capture methods are deployed (where humans are). To curb these influnces on the estimate of initial abundance, researchers could conduct random stratified sampling and use a variety of capture methods.

```
hist(Base_Results, main = "Distribution of Estimated Abundances (Base)", xlab = "Estimat
ed Abundance")
```



 $hist(P_Pos_Results, main = "Distribution of Estimated Abundances (w/ +5% Capture Probability)", xlab = "Estimated Abundance")$ 

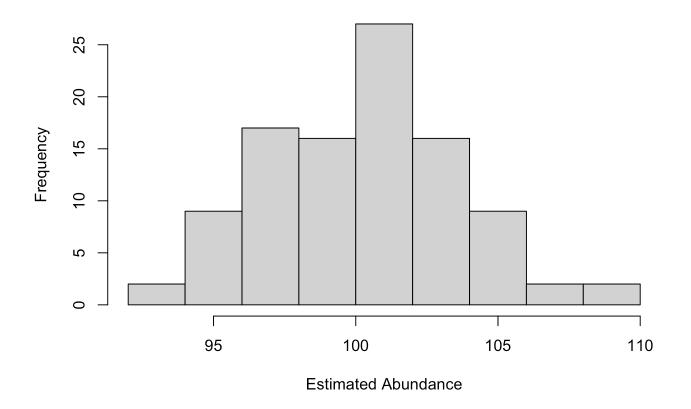
#### Distribution of Estimated Abundances (w/ +5% Capture Probability)



In the second senario, we see a an underestimation of population size. This is likely because the lower capture probability in later captures results in a smaller proprotion of the population being caught, in turn influencing the initial population size and the abundance estimate.

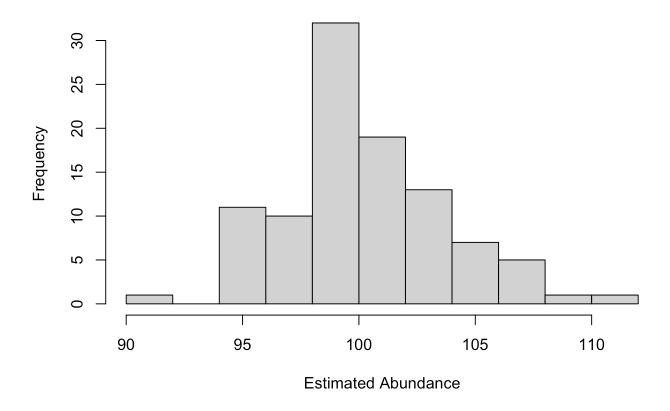
This might happen in the real world due to animals becoming more cautios and avoiding capture method or changes in the environmental conditions (e.g. temperature, water quality, etc.) resulting in more patchy distribution. To address these issues, researchers could again conduct random stratified sampling and use a variety of capture methods.

hist(Base\_Results, main = "Distribution of Estimated Abundances (Base)", xlab = "Estimat
ed Abundance")



hist(P\_Neg\_Results, main = "Distribution of Estimated Abundances (w/ -5% Capture Probabi lity)", xlab = "Estimated Abundance")

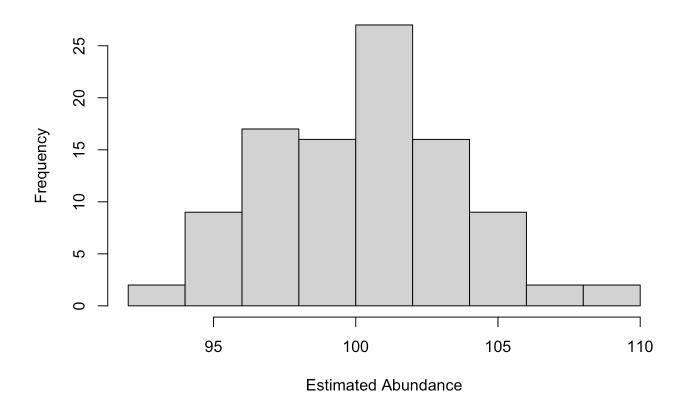
#### Distribution of Estimated Abundances (w/ -5% Capture Probability)



In the third senario, the increase of population size (+5 abundance) seems to lead to overestimating the abundance. This is because the model does not account for new animals entering the population.

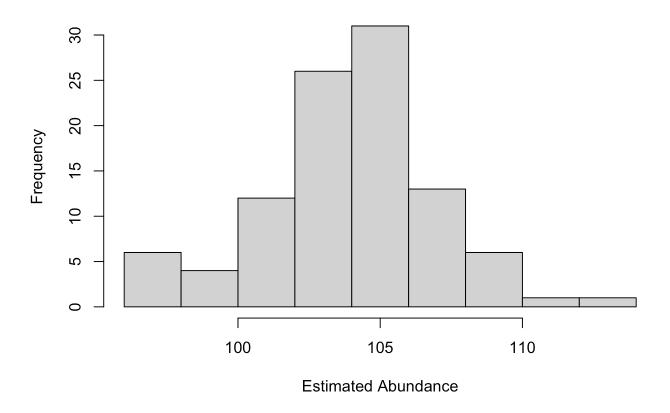
In the real world, this might happen through an increase in births, immigration, or a reduction in deaths or emigration. To address this, researchers could standardize the time period over which the population is sampled and adjust the model to account for these population dynamics.

hist(Base\_Results, main = "Distribution of Estimated Abundances (Base)", xlab = "Estimated Abundance")



 $hist(A_Pos_Results, main = "Distribution of Estimated Abundances (w/ +5% Abundance)", xl ab = "Estimated Abundance")$ 

#### Distribution of Estimated Abundances (w/ +5% Abundance)

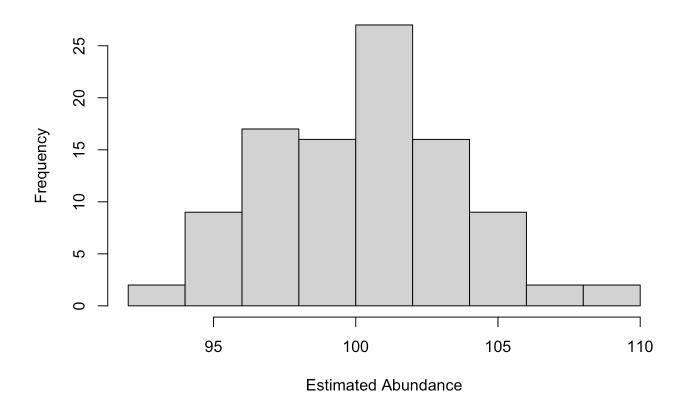


In the forth senario, the decrease of population size (-5 abundance) seems to lead to underestimating abundance. This is because the model does not account for new animals leaving the population via death or emigration.

In the real world, this might happen through a decrease in births, emigration, or an increase in deaths via predation, disease, or other factors such as habitat degreation or environmental stressors.

Again, to address this, researchers could standardize the time period over which the population is sampled and adjust the model to account for these population dynamics.

hist(Base\_Results, main = "Distribution of Estimated Abundances (Base)", xlab = "Estimat
ed Abundance")



hist(A\_Neg\_Results, main = "Distribution of Estimated Abundances (w/ -5% Abundance)", xl ab = "Estimated Abundance")

## Distribution of Estimated Abundances (w/ -5% Abundance)

