

- We are starting to probe only the two ends of this distribution
- We are doing so only in the 'cosmologically local' universe, $z < 1$

Heuristic scalings

We want compact accelerating systems
Consider a BH binary of mass M , and semimajor axis a

$$h \sim \frac{R_S}{a} \frac{R_S}{r} \sim \frac{(GM)^{5/3} (\pi f)^{2/3}}{c^4 r}$$

In astrophysical scales

$$h \sim 10^{-20} \frac{M}{M_\odot} \frac{\text{Mpc}}{D}$$

$$f \sim \frac{c}{2\pi R_s} \sim 10^4 \text{ Hz} \frac{M_\odot}{M}$$

$10 M_\odot$ binary at 100 Mpc: $h \sim 10^{-21}$, $f < 10^3$

$10^6 M_\odot$ binary at 10 Gpc: $h \sim 10^{-18}$, $f < 10^{-2}$

$10^9 M_\odot$ binary at 1 Gpc: $h \sim 10^{-14}$, $f < 10^{-5}$

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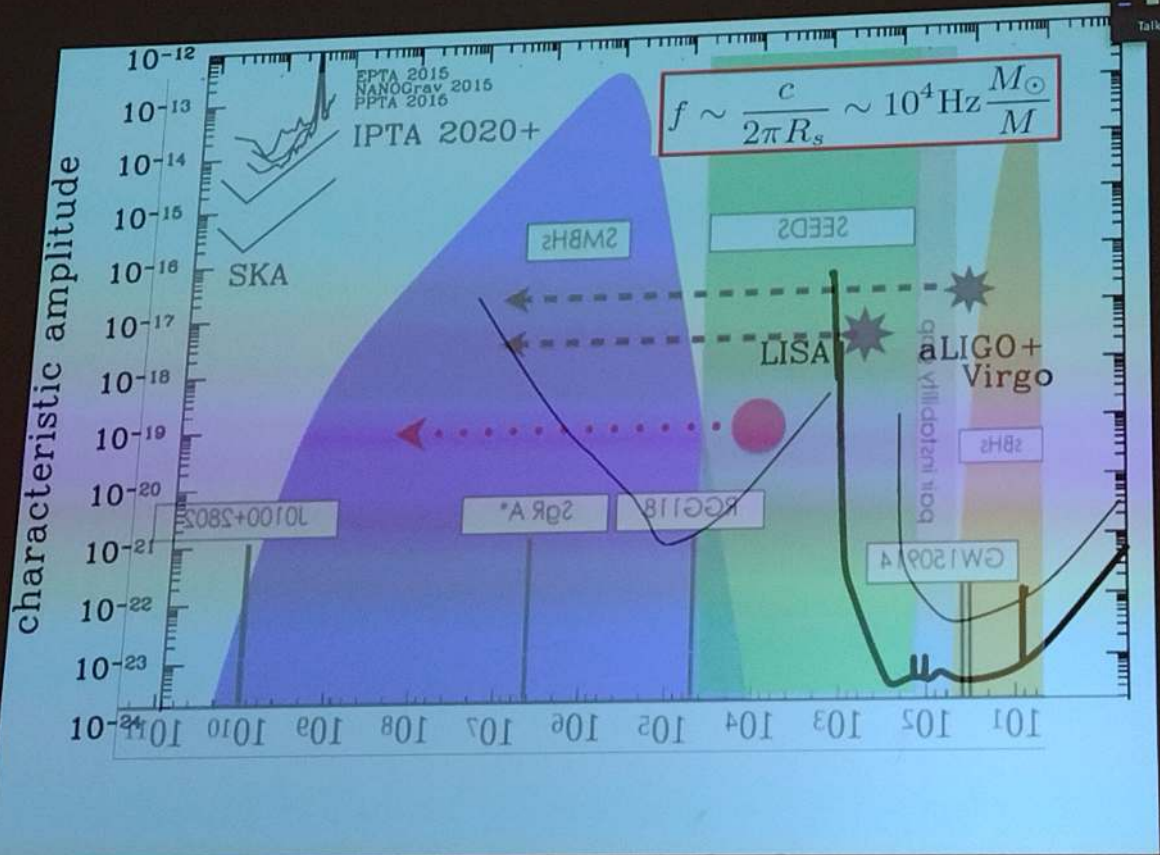
$$h \sim 10^{-20} \frac{M}{M_\odot} \frac{\text{Mpc}}{D}$$

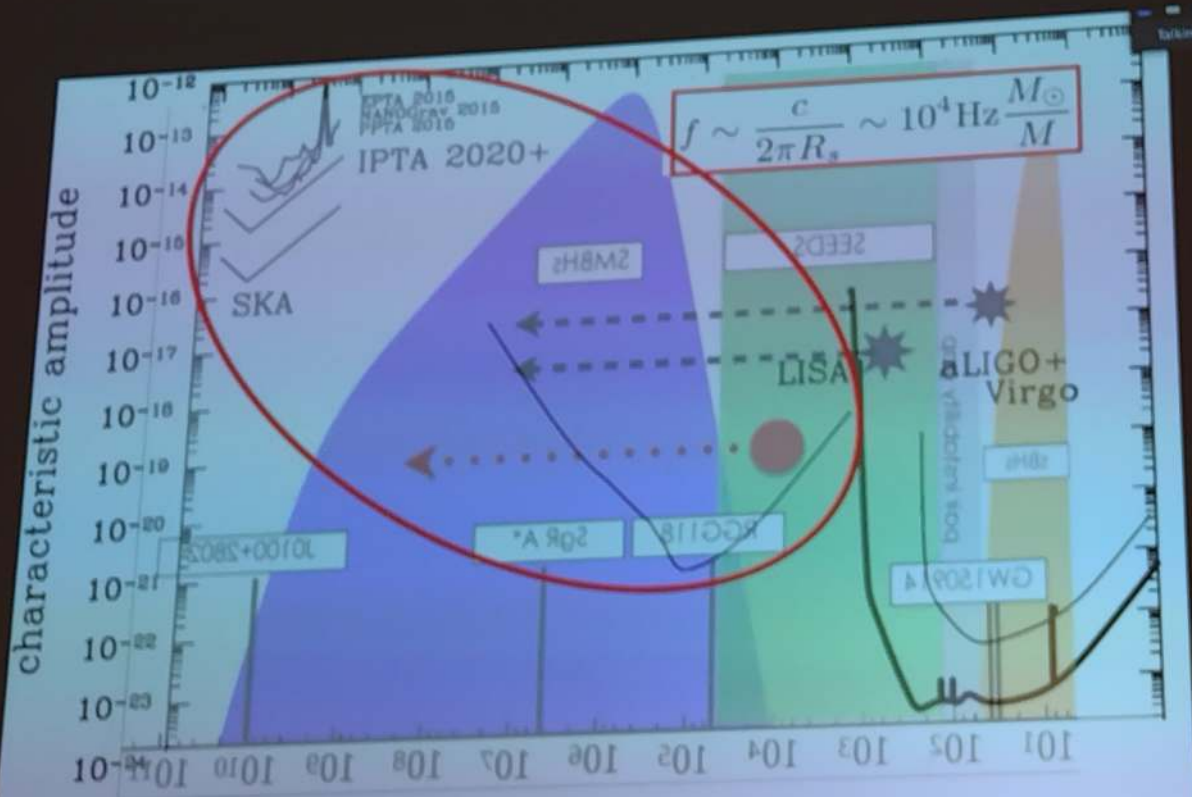
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The Laser Interferometer Space Antenna

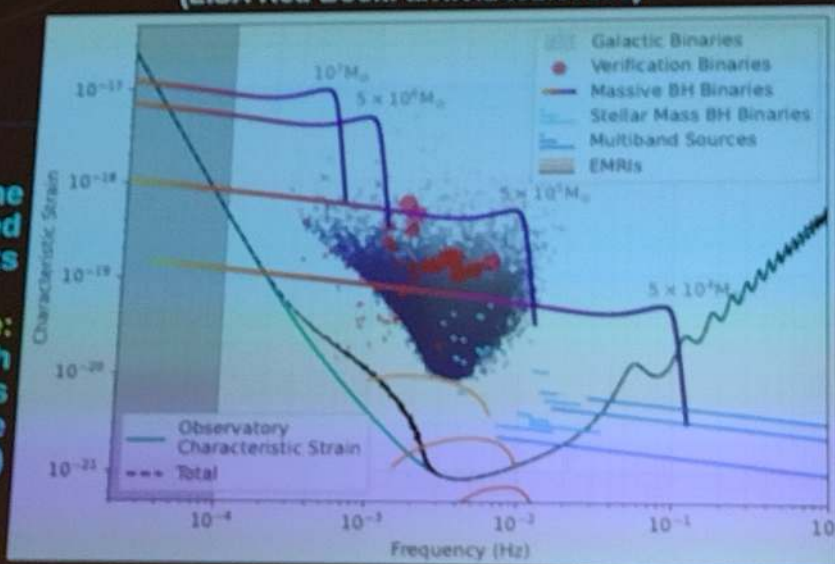
Sensitive in the mHz frequency range where massive black hole (MBH) binary (MBHB) evolution is fast (chirp)

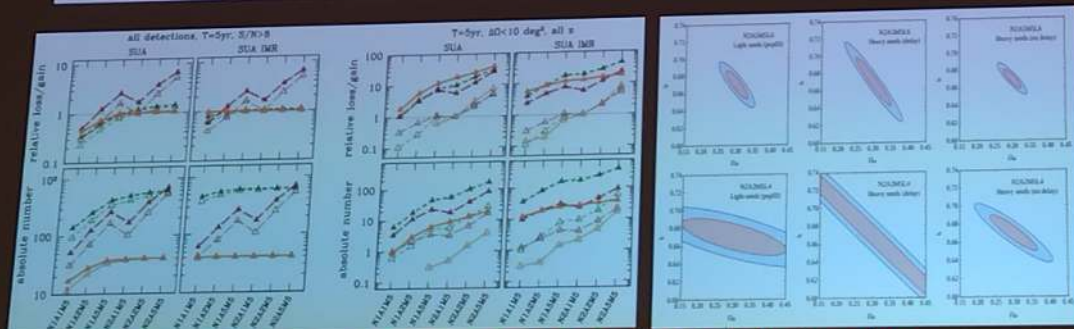
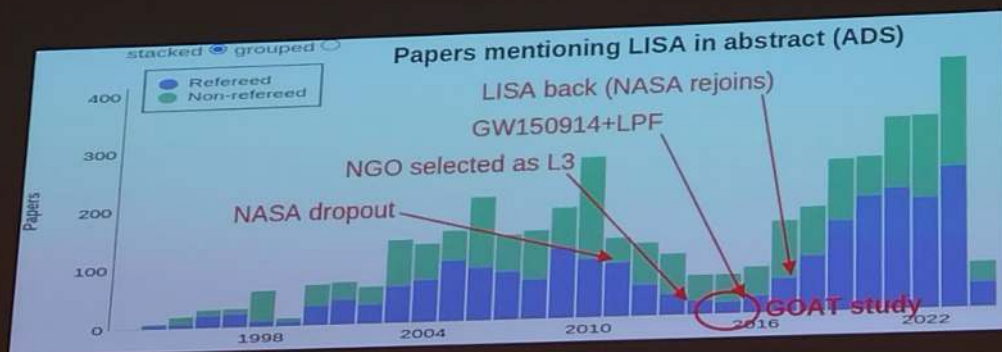
Observes the full inspiral/merger/ringdown

(LISA Red Book: arXiv:2402.07571)

3 satellites trailing the Earth connected through laser links

Proposed baseline:
2.5M km armlength
6 laser links
4.5 yr lifetime
(10 yr goal)

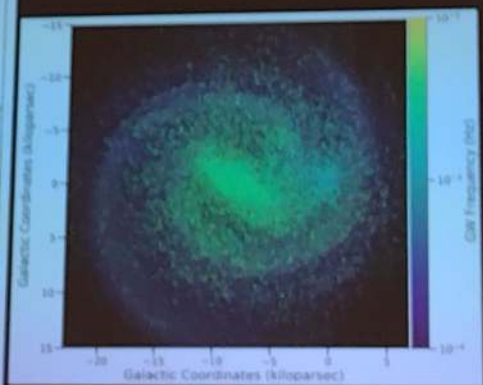
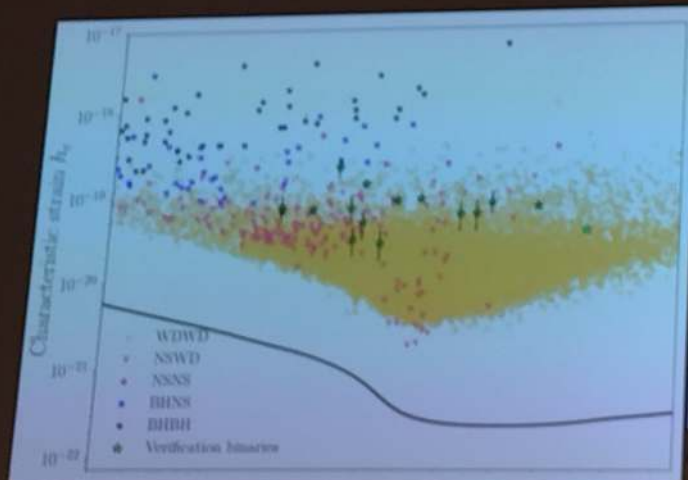




Comparative study of the capabilities of different LISA designs for astrophysics cosmolog and fundamental physics with MBH, EMRIs and more (Klein+16, Tamanini+16, Babak+17)

Galactic Binaries

- 100M WD binaries in the Galaxy
- 20k+ individual detection + stochastic GWB
- characterization of the structure of the galaxy
- rate of WD binary mergers in our galaxy (SN1a connection?)
- binary astrophysics
- multimessenger astrophysics
- NS/BH binaries



(LISA Red Book)

Extreme mass ratio inspirals (EMRIs)

Two body encounters can deflect compact objects in relativistic orbits around the central SMBH.

(Courtesy of P. Amaro-Seoane)

$$r_{\text{out}} \approx \frac{GM_{\bullet}}{v_{\text{orb}}^2} \approx 1 \text{ pc} \left(\frac{M_{\bullet}}{10^6 M_{\odot}} \right) \left(\frac{60 \text{ km/s}}{v_{\text{orb}}} \right)^2$$

$$\rho_{\text{gal}} \sim 0.01 M_{\odot} \text{ pc}^{-3}$$

$$\sigma_{\text{gal}} \sim 40 \text{ km s}^{-1}$$

$$t_{\text{enc, gal}} \sim 10^{11} \text{ yr}$$

$\times 1000$

Galactic dynamics
Newtonian, non-collisional



Cluster dynamics
Newtonian, collisional



$$\rho_{\text{cl}} \sim 10^5 - 10^6 M_{\odot} \text{ pc}^{-3}$$

$$\sigma_{\text{cl}} \sim 100 - 1000 \text{ km s}^{-1}$$

$$t_{\text{enc, cl}} \sim 10^5 - 10^6 \text{ yr}$$

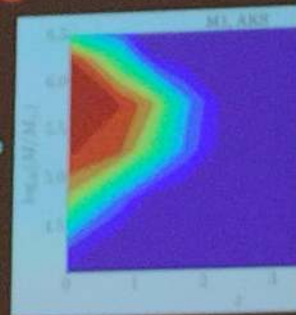
$\times 10^7$



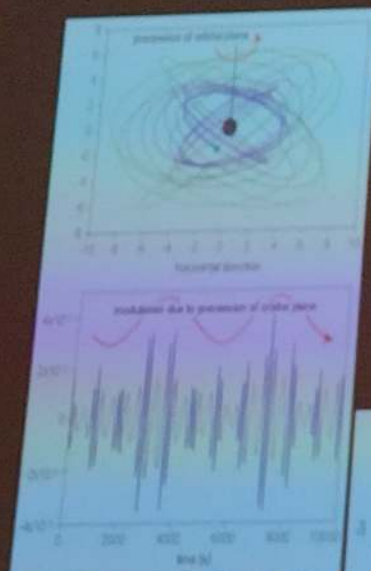
Relativistic dynamics
collisional or not (low N)
 $M_{\bullet} \sim 10^6 - 10^7 M_{\odot}$
 $R_{\text{SMBH}} \sim 10^{-7} - 10^{-4} \text{ pc}$

LISA potential for EMRIs

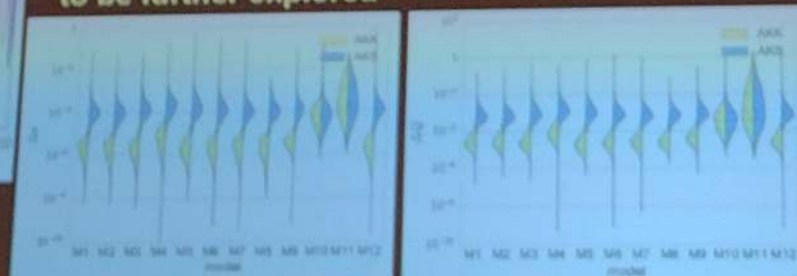
- 1-1000 detections/yr
- sky localization $< 10 \text{ deg}^2$
- distance to better than 10%
- MBH mass to better than 0.01%
- CO mass to better than 0.01%
- MBH spin to better than 0.001
- plunge eccentricity < 0.0001
- deviation from Kerr quadrupole moment to < 0.001



New tool for astrophysics (Gair et al 2010)
cosmology (McLeod & Hogan 2008, Laghi+22),
and fundamental physics (Gair et al 2013) ...
to be further explored

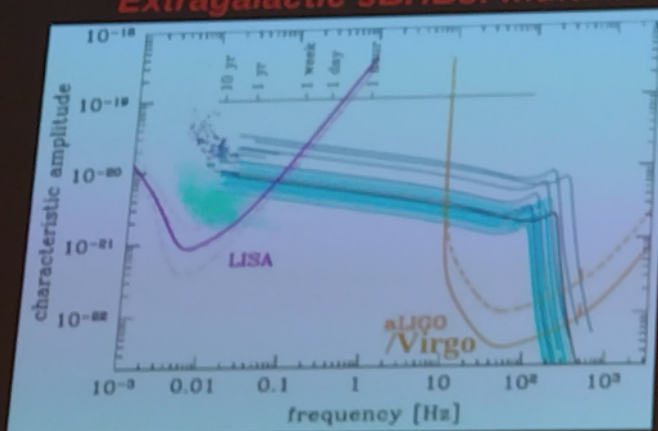


(Babak et al, 2017)



Extragalactic sBHBs: multi-band GW astronomy?

(AS 2016, PRL 116, 1102)



sBHB will be detected by LISA and cross to the LIGO/Virgo band, assuming a 4.5 year operation of LISA.

Expected rates do not seem great.

(LISA Red Book)

	sBHB type	definition	$\langle N \rangle$	90% confidence	no sBHB (%)
SI 4.1	detected	$\text{SNR} > 8$	4.9	0.4 – 9.8	2.2
	archival	$5 < \text{SNR} < 8$ & $t_c < 15 \text{ yr}$	5.6	0.8 – 10.0	1.4
SI 4.2	massive	$\text{SNR} > 8$ & $m_1 > 50 M_\odot$	1.3	0 – 3.6	34.1
SI 4.3	multiband	$\text{SNR} > 8$ & $t_c < 15 \text{ yr}$	1.5	0 – 3.8	26.7
		$\text{SNR} > 8$ & $t_c < 4.5 \text{ yr}$	0.4	0 – 1.4	67.7

(Volontari, Haardt & Madau 2003)

Protogalaxies can host BH that accrete mass and merge with each other following galaxy mergers

(muscle stimulation)

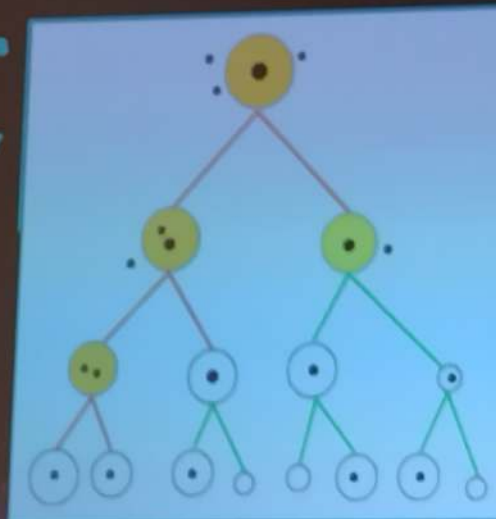
HIERARCHICAL GALAXY & MBH EVOLUTION

GENERAL FRAMEWORK:

Galaxies form hierarchically through a series of mergers and accretion events

Protoplanets can host seed BH that accrete mass and merge with each other following galaxy mergers

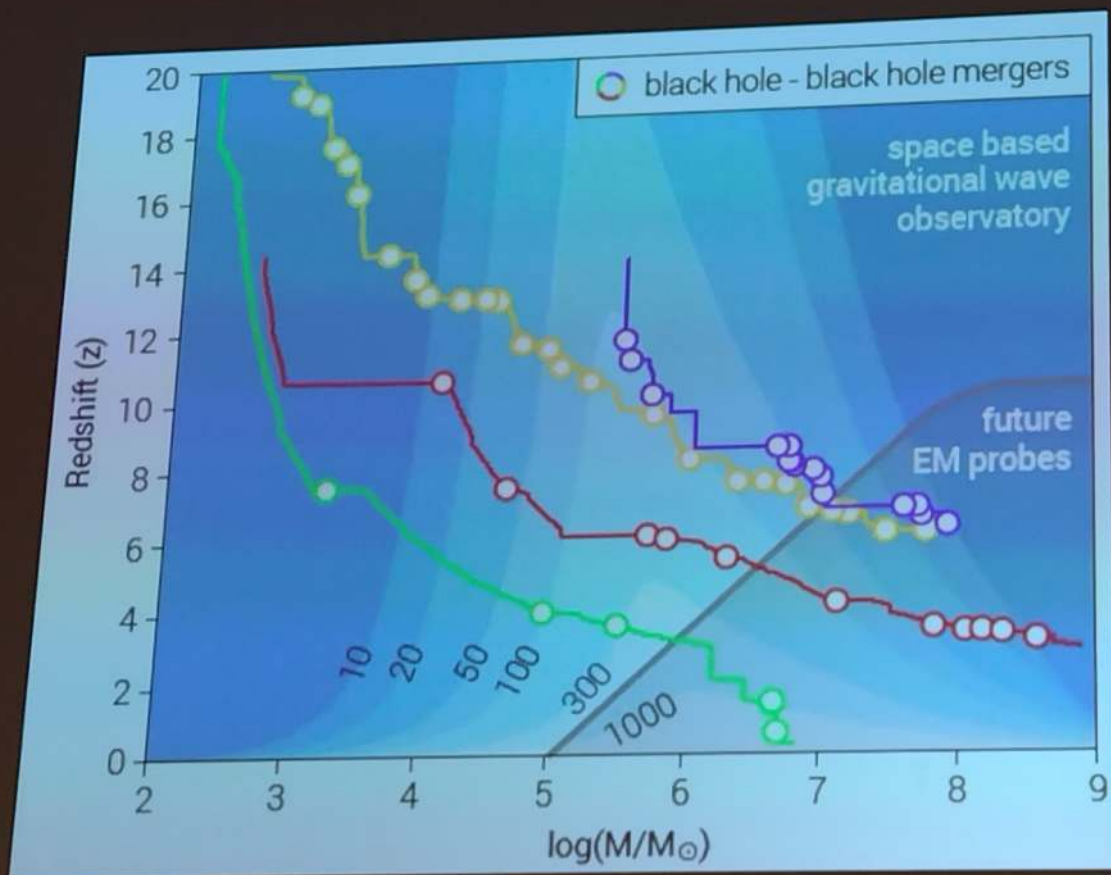
(Volonteri, Haardt & Madau 2003)



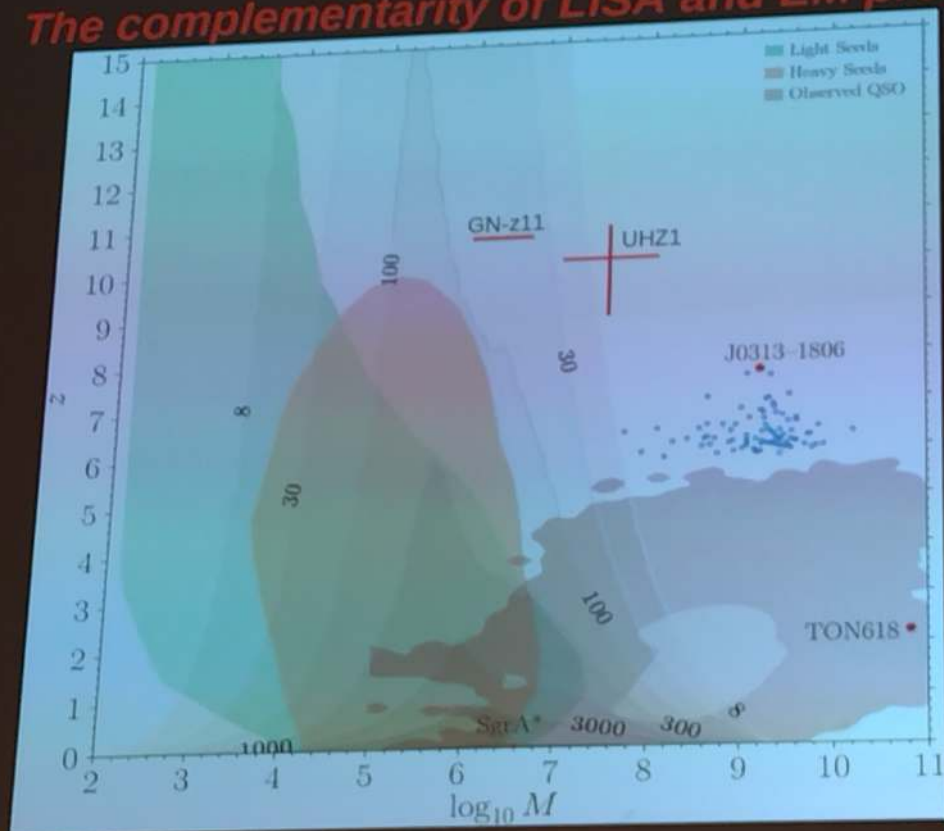
$Z=0$

$Z=20$

(Illustris simulation)



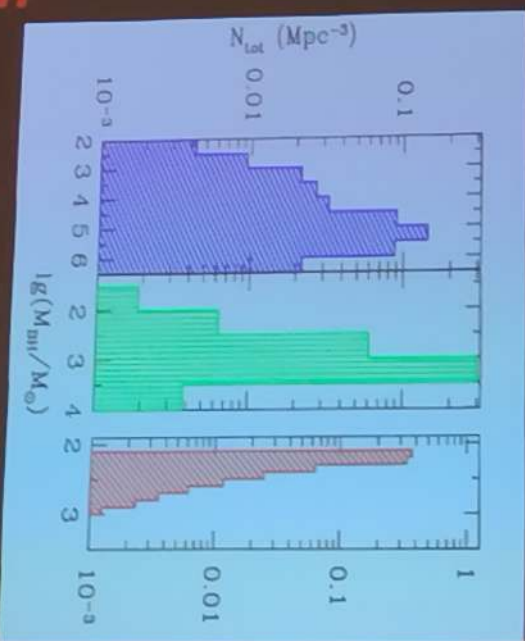
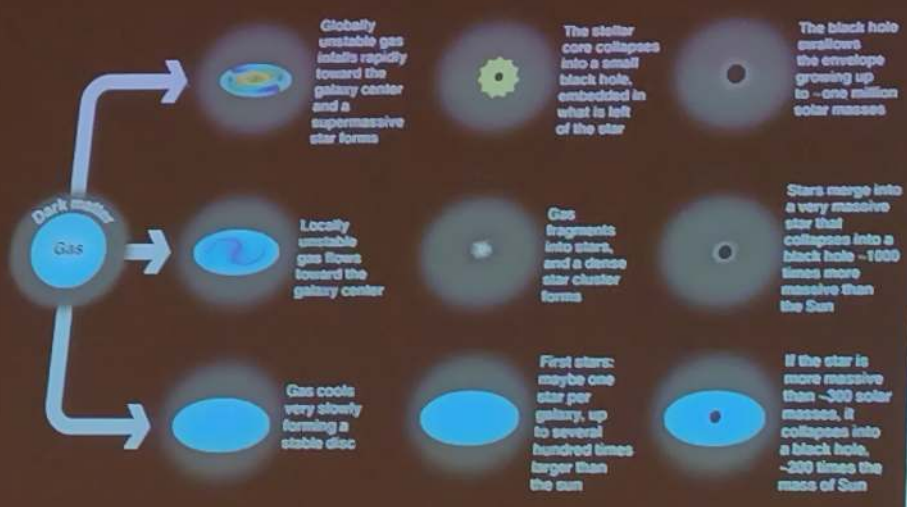
The complementarity of LISA and EM probes



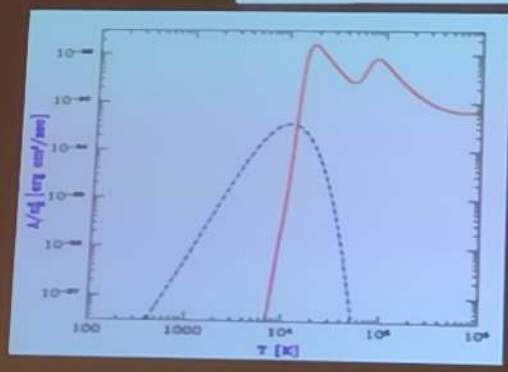
Talking: zoom-boersaal@mpim...

Figure 1 consists of two vertically stacked plots. The top plot is labeled 'no. spin, $q=0.2, w=0.5$ ' and shows a periodic oscillation of the spin Hall shift S_{SH} between approximately -4 and 4 arbitrary units. The bottom plot is labeled 'circular, $q=0.5$ ' and shows a more complex oscillation with a peak amplitude of about 6 arbitrary units. Both plots have a time axis from 0 to 100 arbitrary units.

Seed BH formation



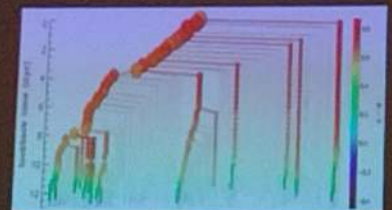
- Critically depends on:**
- content of H2
 - vicinity of an ionizing source
 - fragmentation
 - metallicity



MBH astrophysics with GW observations

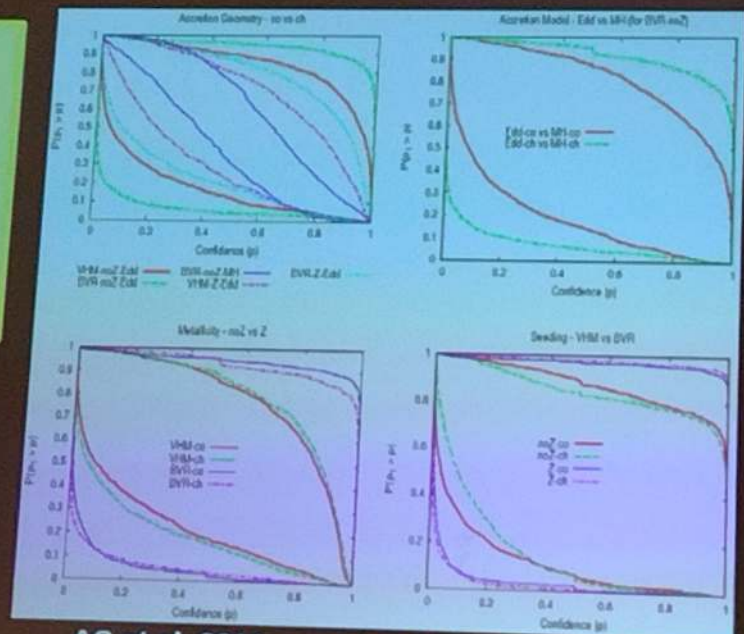
Astrophysical unknowns in MBH formation scenarios

- 1- MBH seeding mechanism (heavy vs light seeds)
- 2- Metallicity feedback (metal free vs all metallicities)
- 3- Accretion efficiency (Eddington?)
- 4- Accretion geometry (coherent vs. chaotic)



CRUCIAL QUESTION:
Given a set of LISA observation of coalescing MBH binaries, what astrophysical information about the underlying population can we recover?

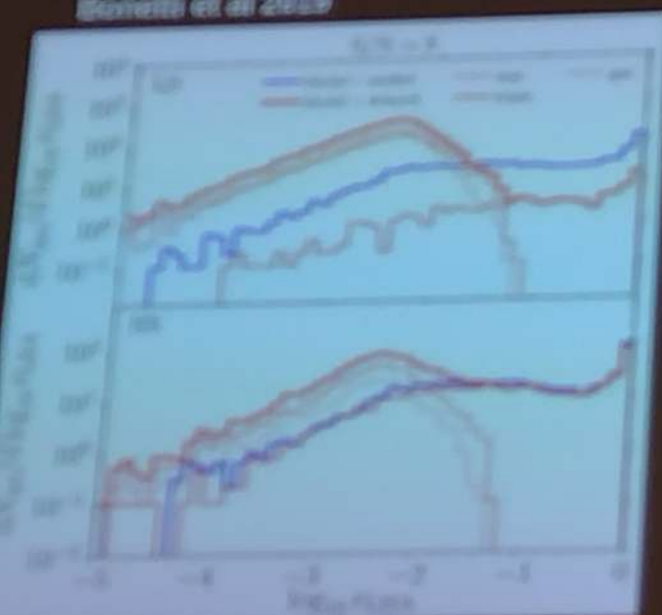
Create catalogues of observed binaries including errors from eLISA observations and compare observations with theoretical models



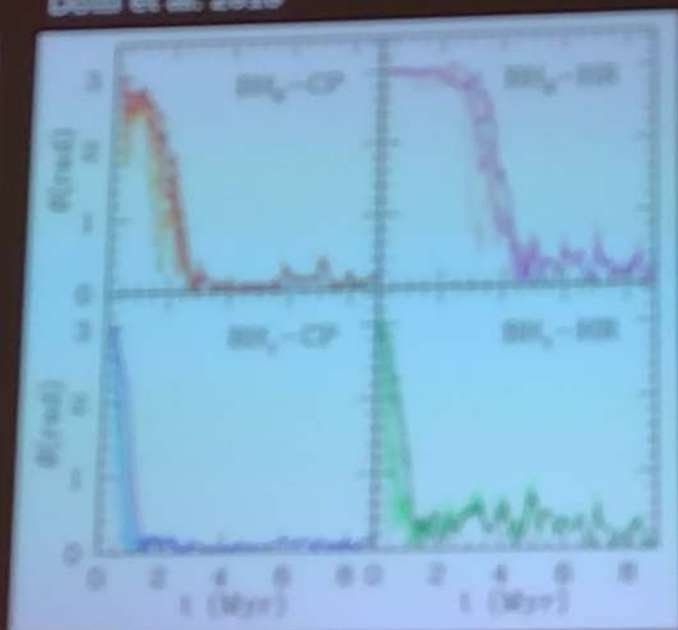
AS et al. 2011, see also Plowman et al 2011

Constrains on dynamics: eccentricity & Spins

Bonetti et al. 2019



Doti et al. 2019

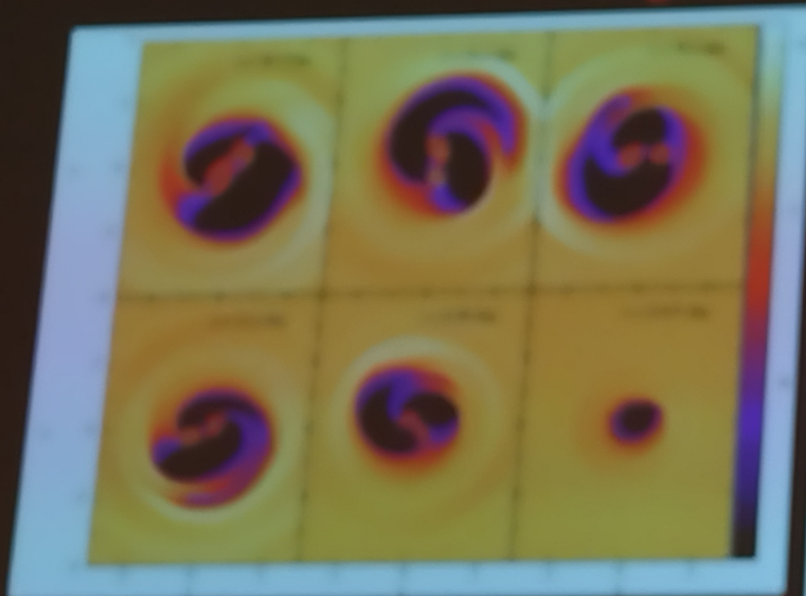


Triple interaction will give a substantial population of highly eccentric systems in the LISA band



Gas driven inspiral produces spins that are aligned with the orbital angular momentum

Lightcurves

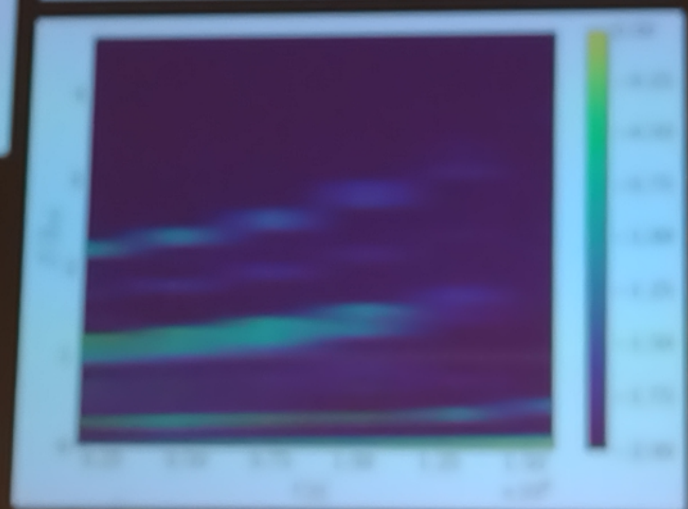
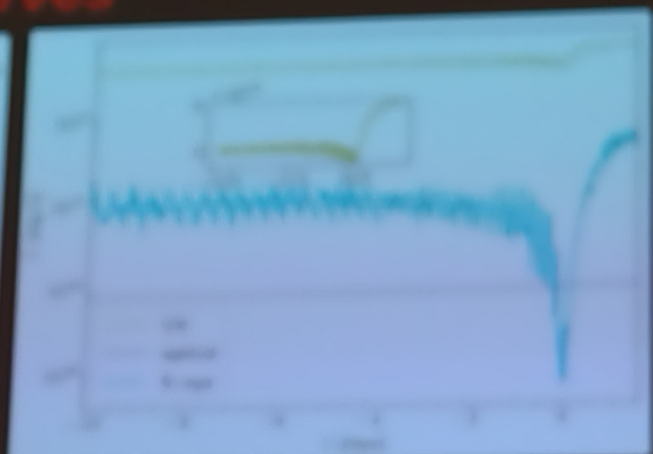


Franchini et al. 2024

Luminous all the way to merger

Clear X ray periodicity

More subtle periodicity in UV and optical

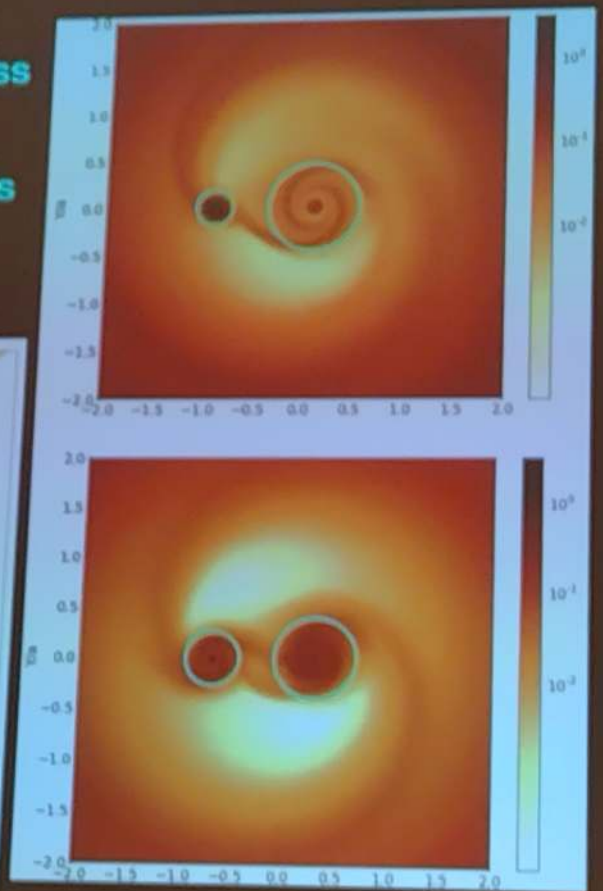


Why multimessenger?

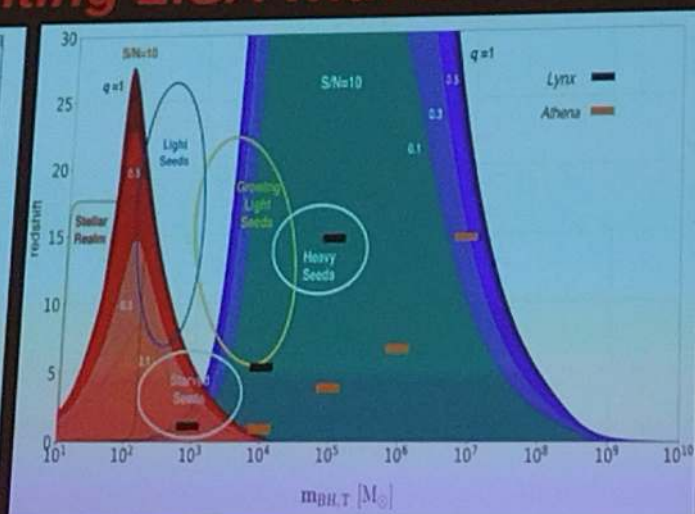
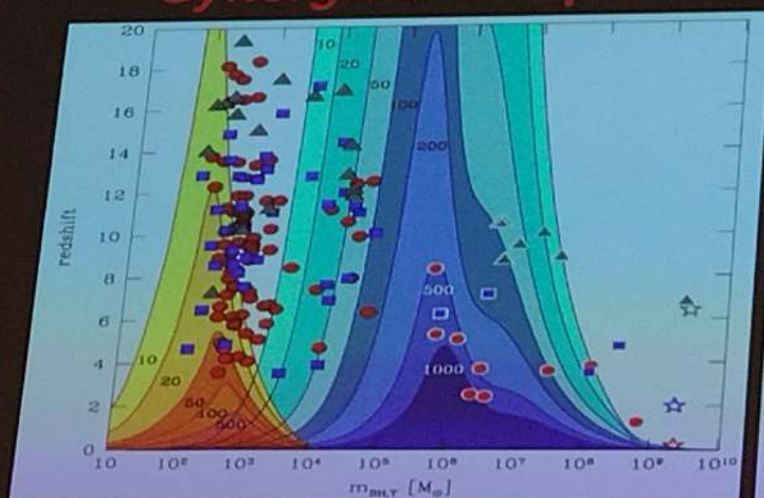
- Cosmology and cosmography at high z
- Study of accretion on MBHs with known mass and spins
- Test MBH-galaxy co-evolution
- Study of the interplay between MBHs and gas (torques, disk structure, disk models)
- Host galaxy, Jet launches, Quasar birth ...



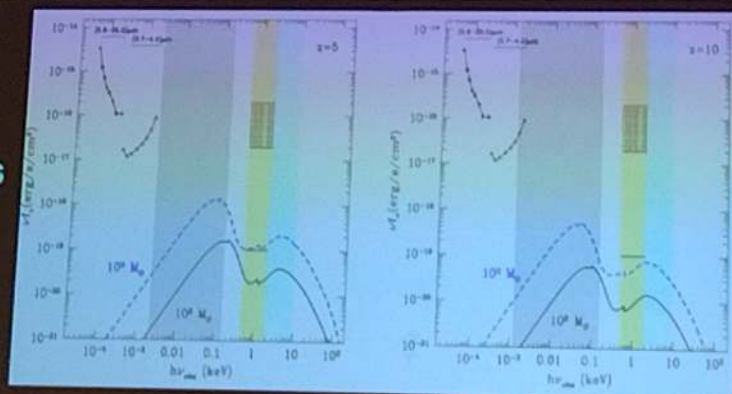
LISA Red Book



Synergies: complementing LISA with ET/CO



- ET is almost perfectly complementary to LISA
- can see the first mergers of popIII seeds up to high z
- it reaches deeper than EM probes



(Valiante+ 20)

What we need to fully exploit LISA

- prepare flexible astrophysical models for interpreting observations (particularly for EMRIs and MBHBs)
- connect dynamics to observables, understand environmental effects vs GR deviations
- model EM counterparts, get ready to multimessenger astronomy
- prepare exploitation of bright and dark sirens for cosmology
- put LISA in the EM and GW context of the mid 30s
 - fold in JWST results
 - explore synergies with ET/CO (and more?)

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Pulsar timing

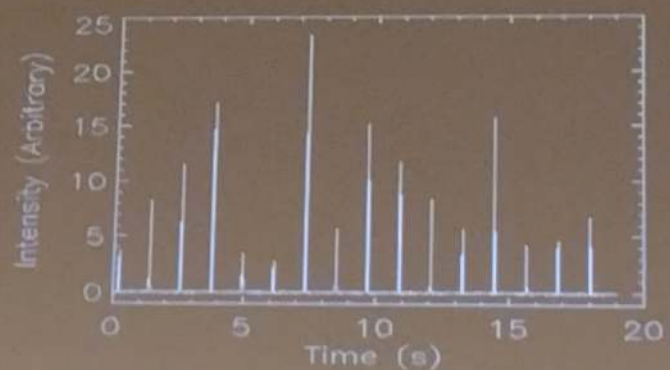
Pulsars are neutron stars seen through their regular radio pulses

Pulsar timing is the art of measuring the time of arrival (ToA) of each pulse and then subtracting off the expected time of arrival given by a theoretical model for the system

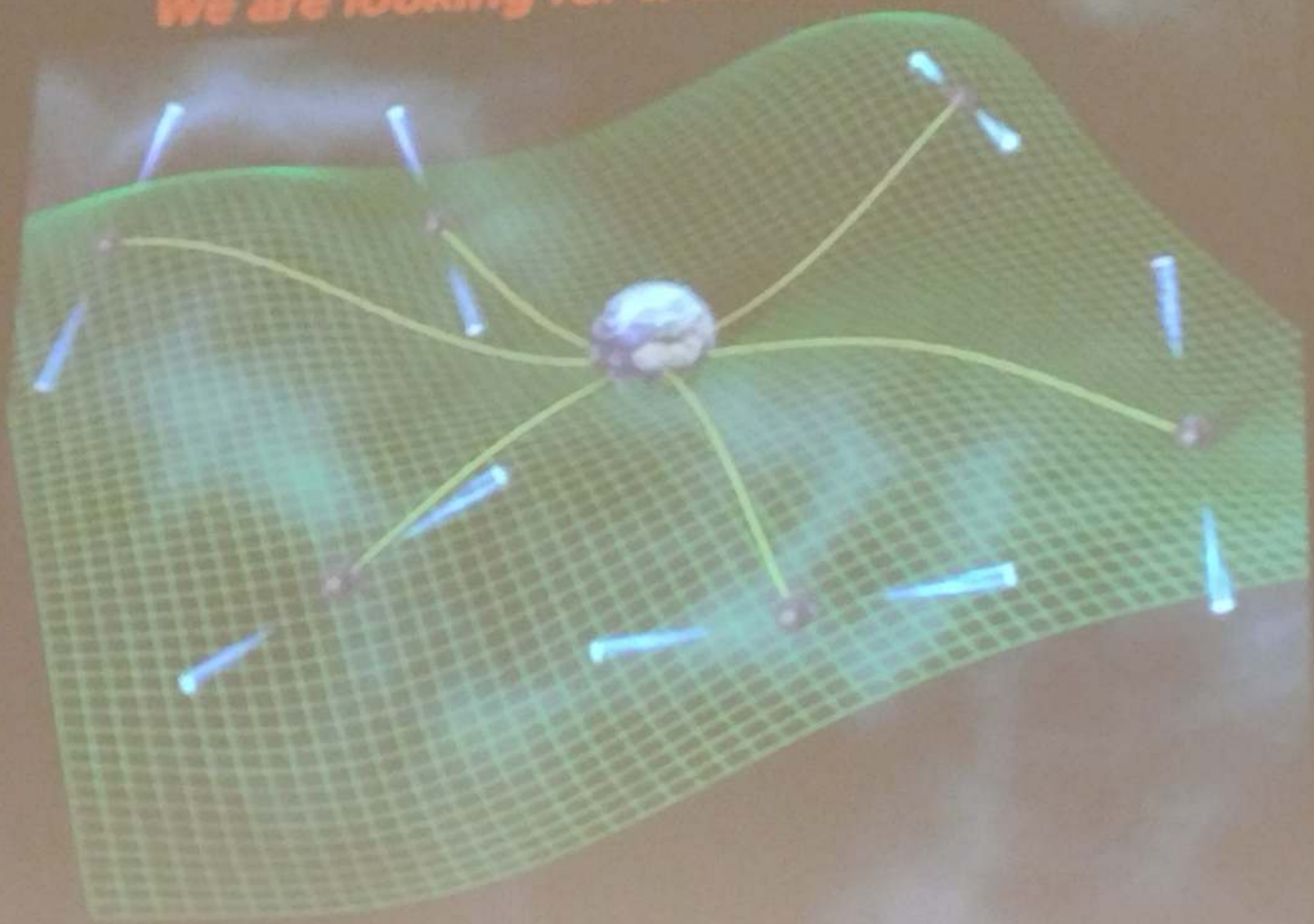
- 1-Observable a pulsar and measure the ToAs
- 2-Find the model which best fits the ToAs
- 3-Compute the timing residual R

$$R = \text{ToA} - \text{ToA}_m$$

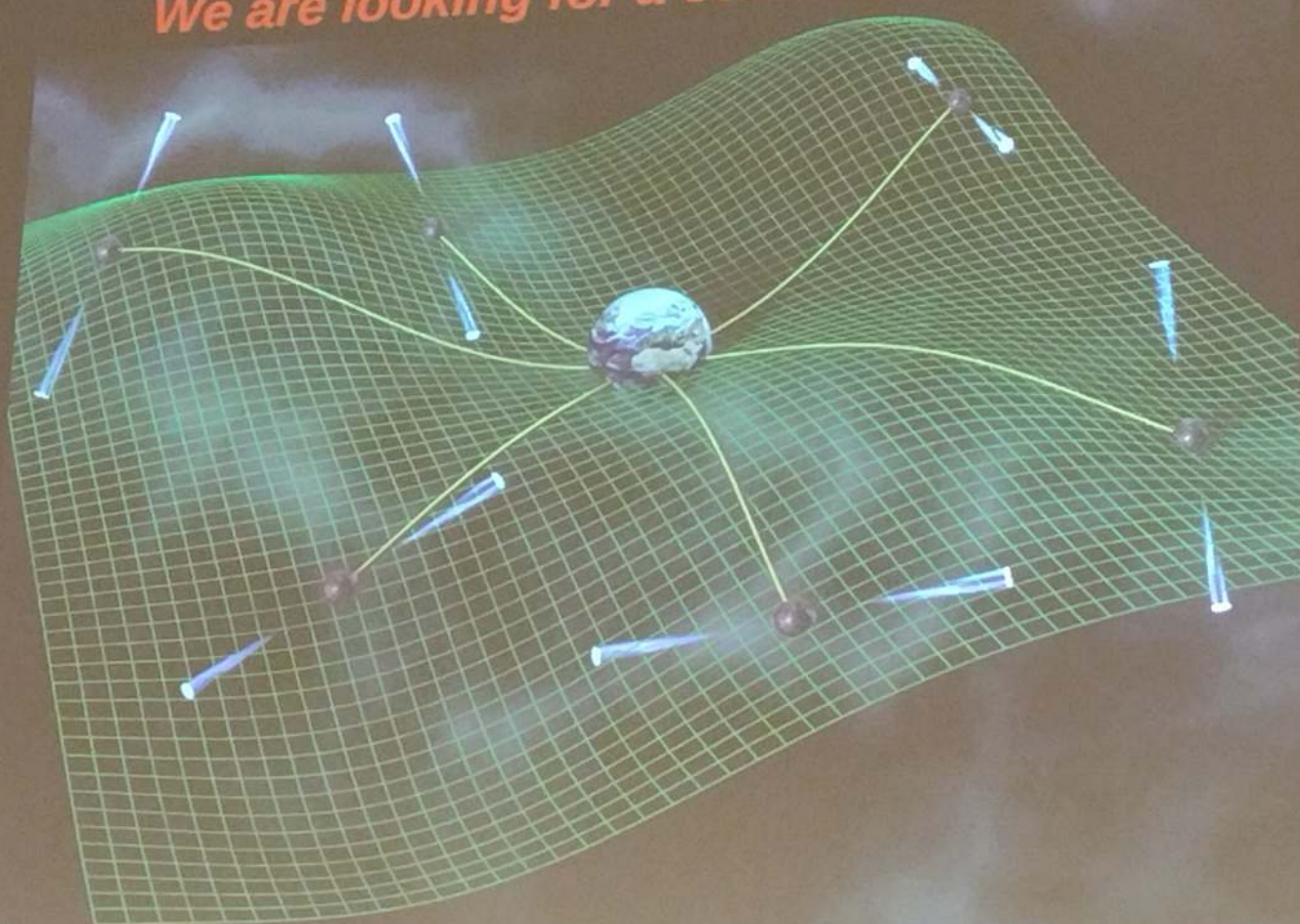
If the timing solution is perfect (and observations noiseless), then $R=0$. R contains all uncertainties related to the signal propagation and detection, plus the effect of unmodelled physics, like (possibly) gravitational waves



We are looking for a correlated signal



We are looking for a correlated signal



"Looking at the arxiv, can't help wondering: is there any early-Universe cosmological process that DOES NOT produce the stochastic gravitational-wave background observed by Pulsar-Timing Arrays?"

Yuri Levin

-It's Inflation!

-It's phase transitions!

-It's scalar perturbations!

-It's topological defects!

-It's domain walls!

**-It's turbulence induced
perturbations!**

s Inflation!

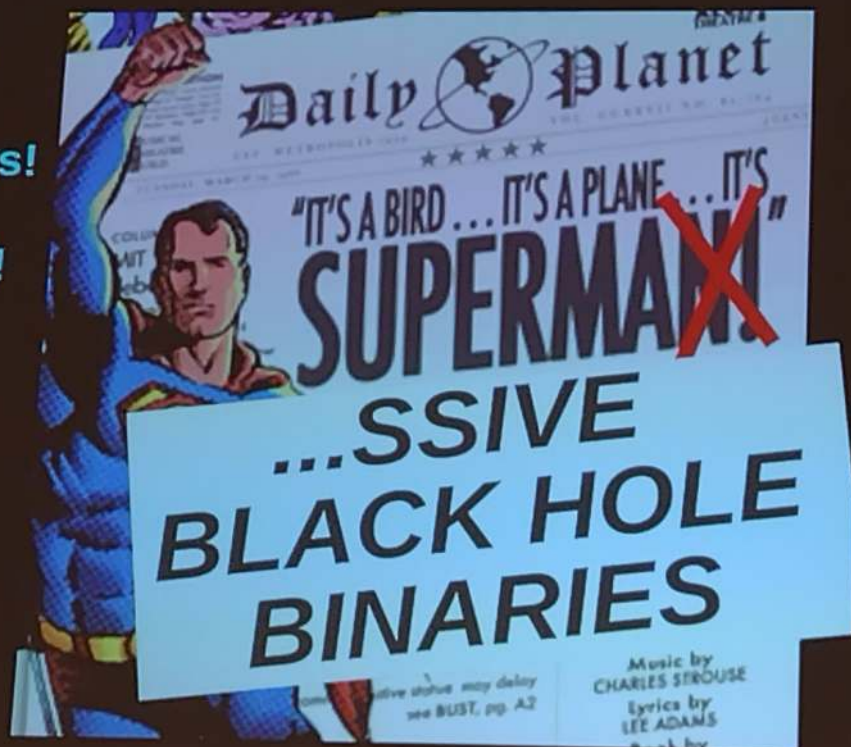
s phase transitions!

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topological defects!

domain walls!

turbulence induced
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The future of PTAs

- bring constructively together different groups to maximize data power
- refine analysis pipelines
- construct end-to-end inference pipelines
- match the nanoHz GW sky with all sky EM surveys
- model EM counterparts and unlock the potential of nanoHz multimessenger astronomy