



Rate Estimation Program for Tidal Disruption Events Manual

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This document serves as supplemental documentation for REPTiDE and should be consulted alongside the code paper Hannah et al. (2024).

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1 Installation

To install REPTiDE, use the following:

```
pip install git+https://github.com/christianhannah/reptide.git
```

2 Usage Examples

When downloaded, an additional directory named “Examples” can be found within the package directory containing three example scripts:

- `reptide_sb_to_density_example.py`: This script demonstrates how to use REPTiDE to convert a 1D surface brightness profile into a 3D stellar mass density profile via Abel inversion (as in Hannah et al., 2024).
- `reptide_single_example_analytic.py`: This script demonstrates a single TDE rate calculation for a density profile described by the analytic power law function described in Hannah et al. (2024).

- `reptide-single-example-discrete.py`: This script demonstrates a single TDE rate calculation for a discrete density profile (i.e. tabulated x and y data).

3 Execution

3.1 Inputs

The primary inputs required for this calculation are the central black hole mass (M_\bullet) and the radial 3D stellar density profile $\rho(r)$. There are two versions of the code that depend on the definition of the stellar density profile; this can be either “Discrete” or “Analytic.” In the discrete version, the density profile is supplied as a discrete, non-parametric set of data points. The analytic version uses a density profile that follows a power-law with exponential decay:

$$\rho(r) = \rho_{5\text{pc}} \left(\frac{r}{5 \text{ pc}} \right)^{-\gamma} \times \begin{cases} 1 & , r < r_d \\ \exp[-(r - r_d)/\sigma_d] & , r \geq r_d \end{cases} \quad (1)$$

Here, $\rho_{5\text{pc}}$ is the stellar density at a radius of 5 pc, γ is the power-law slope, r_d is the radius where the exponential decay starts, and σ_d is the width of the decay.

In addition to the density profile and MBH mass, there are some additional parameters that must be defined for REPTiDE, and these differ slightly between versions. Both versions require the following inputs:

- *name*: Galaxy identifier - used for personal object identification.
- *M_BH*: Black hole mass [kg]
- *bw_cusp*: (optional; default=False) Boolean to indicate the application of a Bachall-Wolf cusp to the density profile at small radii.
- *bw_rad*: (optional; default=1e – 300) Radius to begin the Bachall-Wolf cusp if *bw_cusp*=True.
- *M_min*: (optional; default=0.08) Minimum stellar mass to consider in the present-day mass function [M_\odot].
- *M_max*: (optional; default=1.0) Maximum stellar mass to consider in the present-day mass function [M_\odot].
- *quiet*: (optional; default=True) Boolean to toggle status printing during calculation.

Input parameters that are unique to each version of REPTiDE are described below.

Discrete:

- *rads*: radii for the density measurements [m]
- *dens*: 3D stellar densities [kg/m³]
- *sflag*: boolean to indicate fixed inner density slope (see Section ?? for details)
- *s*: inner power-law density slope applied if *sflag* = True; if *bw_cusp*=True, this will always be -7/4 (see Section ?? for details)

Analytic:

- *slope*: power-law slope of the density profile
- *rho_5pc*: 3D stellar density at a radius of 5 pc [kg/m³]
- *decay_start*: radius to begin exponential decay [m]
- *decay_width*: width of the exponential decay [m]
- *smooth*: width of the exponential decay [m]

3.2 Outputs

The output from REPTiDE also depends on the version of REPTiDE being used, but the following outputs are identical for both:

- *name*: Galaxy identifier.
- *M_BH*: Black hole mass [kg].
- *TDE_rate_solar*: TDE rate for monochromatic population of $1 M_{\odot}$ stars.
- *TDE_rate_full*: TDE rate for a realistic Kroupa present-day mass function (PDMF).
- *orb_ens*: Array of orbital energies used for the calculations, ϵ [m^2/s^2].
- *DF*: Distribution function (over ϵ).
- *q*: Dimensionless diffusivity parameter (over ϵ).
- *masses*: Array of stellar masses used in the PDMF [kg].
- *LC_contributions_per_mass*: TDE rate per stellar mass in the PDMF.
- *LC_flux_per_mass*: Loss-cone flux curves for each stellar mass in the PDMF.
- *psi_rads*: Radii over which the gravitational potential is computed [m].
- *psi_tot*: Total potential [m^2/s^2].
- *psi_bh*: Potential from the black hole [m^2/s^2].
- *psi_enc*: Potential from the enclosed stellar mass [m^2/s^2].
- *psi_ext*: Potential from the external mass [m^2/s^2].
- *DF_integrals*: Integrals as a function of orbital energy used to compute the distribution function.
- *mu_integrals*: Integrals as a function of orbital energy used to compute dimensionless diffusivity parameters.
- *periods*: Orbital periods as a function of orbital energy.
- *mu*: Angular momentum diffusion coefficients as a function of orbital energy.
- *R_LC*: Squared ratio of the loss-cone angular momentum to the angular momentum of a circular orbit as a function of orbital energy.
- *bw_cusp*: Boolean parameter indicating if a Bachall-Wolf cusp was applied.
- *bw_rad*: Radius at which the Bachall-Wolf cusp was applied if *bw_cusp* = True
- *EHS*: Boolean parameter used to indicate the inclusion of event horizon TDE rate suppression.

Output parameters that differ between versions are listed below. **Discrete:**

- *radii*: Radii for the density measurements [m]
- *dens*: 3D stellar densities [kg/m^3]
- *sflag*: Boolean to indicate fixed inner density slope.
- *s*: Inner power-law density slope applied if *sflag* = True.

Analytic:

- *slope*: Power-law slope of the density profile.
- *rho_5pc*: 3D stellar density at a radius of 5 pc [kg/m^3].
- *smooth*: Width of the exponential decay [m].
- *decay_start*: Radius to begin exponential decay [m].
- *decay_width*: Width of the exponential decay [m].

3.3 Single vs Batch Rates

REPTiDE is a pip installable module that can be imported into any Python script to compute TDE rates. After defining the necessary input data arrays (outlined in Section 3.1), the user must use one of the following functions to build the input data table:

- *in_table* = `_reptide_.create_discrete_input_table()`
- *in_table* = `_reptide_.create_analytic_input_table()`

These functions return an AstroPy table object that is passed directly to REPTiDE’s primary function, “`_reptide_.run_reptide(in_table, analytic, n_energies, EHS)`,” which performs the rate calculation. Here, *analytic* is a boolean parameter indicating the version of REPTiDE to use: *analytic*=True uses the analytic version and vice versa, *n_energies* specifies the number of orbital energies used in the calculation (optional; default=1000), and *EHS* specifies whether or not to include event horizon suppression of the TDE rate in calculating the “full” TDE rate (optional; default=False).

If the user would like to compute TDE rates for a batch of galaxies utilizing multiprocessing, there is a wrapper script imported with the module titled “`reptide_batch_run.py`.” In this case, the user must define their input parameter arrays at the beginning of this file under the “User Defined Section.” In addition to the standard inputs discussed in Section 3.1, the user must also define the *analytic*, *n_energies*, and *EHS* parameters discussed above, the number of cores desired for multiprocessing (*cpu_count*; defaults to the maximum number available), and the path/filename for the output “.fits” file (*out_fn*).

3.4 1-D Surface Brightness to 3-D Stellar Density

REPTiDE is also equipped with a function designed to convert a supplied 1-D surface brightness profile into a 3-D stellar mass density profile under the assumption of spherical symmetry; “`_reptide_.SB_to_Density([inputs])`”. The details of this procedure are outlined in Hannah et al. (2024), while the inputs and outputs are described below.

Inputs:

- *rads*: Radii corresponding to the surface brightness measurements [arcsec].
- *SBs*: Surface brightness measurements [L_\odot/pc^2].
- *M_L*: Mass-to-light ratio for the system.
- *distance*: Distance to the system in pc.
- *ax_ratio*: (optional; default=1) Axial ratio for the system (b/a).
- *inc*: (default= 90°) Inclination angle for the system [deg].

Outputs:

- *rad_pc*: Radii in pc.
- *densities*: 3-D stellar mass densities [M_\odot/pc^3]
- *gausses*: Individual Gaussians used for the MGE fit to the SB profile.
- *summed_gauss*: Summed Gaussian fit to the SB profile.

4 Attribution

If you use this software in your work, please cite Hannah et al. (2024).

5 Dependencies

To use this software, make sure you have the following Python packages installed:

1. NumPy (v1.26.4)
2. SciPy (v1.13.0)
3. Astropy (v5.3.4)
4. tqdm (v4.66.2)
5. mgefit (v5.0.15)

The exact version of each package may not be required, but these are the versions the program was developed with.

References

Hannah, C. H., Seth, A. C., Stone, N. C., & van Velzen, S. 2024, , 168, 137, doi: <http://doi.org/10.3847/1538-3881/ad630a>

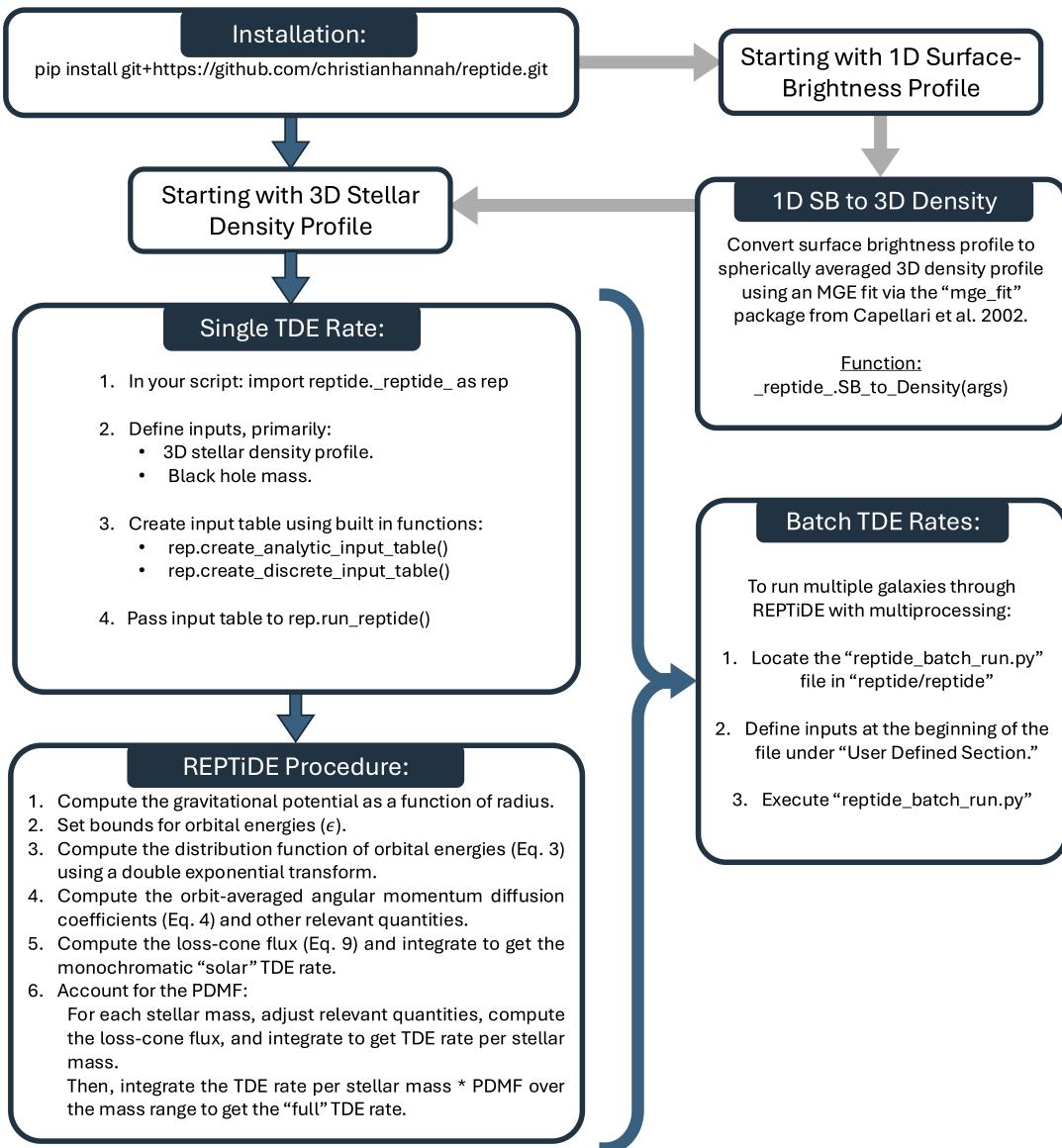


Figure 1: This figure serves to graphically explain the use of REPTiDE.