# The lecture starts at 13:15

Deep Learning for NLP

Florina Piroi



#### Relevant Literature

- Jurafsky & Martin, SLP, 3rd Edition: Chapters 6, 7
  - (including slides), references therein
- M. Nielsen, Neural Networks and Deep Learning, 2019



#### Contents

- Vector Semantics & Embeddings
  - Lexical and Vector Semantics
  - Words as Vectors
  - Measuring similarity & tf-idf
  - Word2Vec
- Neural Networks
  - Perceptron, units, activation functions
  - Feed forward
  - Training
- Neural Language Models



# Vector Semantics & Embeddings

# Distributional Hypothesis

- First formulated in 1950 (Joos), 1954 (Harris), 1957 (Firth)
- Observation: synonyms tend to occur in the same environment oculist and eye-doctor

"An oculist is just an eye-doctor under a fancier name"

near eye or examined (but not near lawyer)

"... Burns was an oculist, but since he didn't know the professional titles, he didn't realize that he could go to him to have his eyes examined"

• "Does a language have a distributional structure?" (Harris)

"occurrences of parts ... relative to other parts"

"without intrusion of other features" (meaning)



# Distributional Hypothesis

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- "Does a language have a distributional structure?" (Harris)

"occurrences of parts ... relative to other parts"

"without intrusion of other features" (meaning)

• Distribution of an element (of a part): sum of all its environments "An oculist is just an eye-doctor under a fancier name"

"... Burns was an oculist, but since he didn't ..."

"The distribution of an element will be understood as the sum of all its environments (contexts). An environment of an element A is an existing array of its co-occurrents, i.e. the other elements, each in a particular position, with which A occurs to yield an utterance."



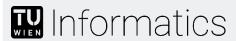
# Distributional Hypothesis

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"occurrences of parts ... relative to other parts"

"without intrusion of other features" (meaning)

- Words that are synonyms occur in the same environment
- Words occurring in similar contexts (environment) tend to have similar meanings"
- Difference in similarity between those two terms **correlates** with the difference in their environments.



# Distributional Hypothesis – Vector Semantics

- First formulated in 1950 (Joos), 1954 (Harris), 1957 (Firth)
- Words that are synonyms occur in the same environment
- Words occurring in similar contexts (environment) tend to have similar meanings"
- Difference in similarity between those two terms **correlates** with the difference in their environments.
- Vector semantics = instantiation of the distributional hypothesis
  - Representation learning (embeddings)



# **Lexical Semantics**

Q: How to represent the meaning of a word?

- N-Gram: string of letters/characters
- Index in a vocabulary list
- ...

#### But:

- cold vs. hot
- happy vs. sad

The trophy doesn't fit into the brown suitcase because it's too small.

-> Model of the meaning



# **Lexical Semantics**

-> Model of the meaning – why do we need one?

The trophy doesn't fit into the brown suitcase because it's too small.

Draw useful inferences to help us solve meaning-related tasks:

Q&A

Plagiarism & paraphrasing

Dialogue

Summarization

Lexical semantics refers to the linguistic study of the word meaning



# Lexical Semantics - Lemma and Senses

Lemma == dictionary form == citation form

```
mouse (N)

1. any of numerous small rodents...

2. a hand-operated device that controls a cursor... (polysemous)
```

mouse is the **lemma** for *mice* (will not be in the dictionary)

mice == word form



# **Lexical Semantics**

Look at relationship between:

different word senses

different word forms

... including other ingredients

mouse (N)

- any of numerous small rodents...
- 2. a hand-operated device that controls a cursor...

word senses (polysemous)

mouse is the **lemma** for *mice* (will not be in the dictionary)

mice == word form



# Lexical Semantics – Synonymy

How many synonyms per word (in the English language)?

- Identical meanings:
  - couch/sofa vomit/throw up car/automobile water / H2O
- Two words are synonyms if they are substitutable for each other in any sentence, without changing the truth [...] of the sentence (i.e. same propositional meaning).
- Truth preserving !≈ identical in meaning
   "I was hiking and my bottle of water was empty."

Principle of contrast: difference in form associated with difference in meaning



# Lexical Semantics – Antonymity

- Opposite senses, with respect to one feature of their meaning:
  - up / down hot / cold in / out
- Can define binary opposition
- Can be at the opposite ends of a scala (long / short)
- Can be reversives ( rise / fall )



# Lexical Semantics – Similarity

Similar meaning, but not synonyms

car, bicycle

cow, horse

Sense vs. sense

Word vs. word

| vanish | disappear  | 9.8  |
|--------|------------|------|
| behave | obey       | 7.3  |
| belief | impression | 5.95 |
| muscle | bone       | 3.65 |
| modest | flexible   | 0.98 |
| hole   | agreement  | 0.3  |

Similarity values between 0 and 10



# Lexical Semantics - Relatedness

# Words are related by

• Semantic fields

• ...

```
car, bicycle: similar
coffee, cup What's the relationship?
car, gasoline: related, not similar
```



# Lexical Semantics - Relatedness

# Words are related by

- Semantic fields (surgeon, scalpel, nurse, anaesthetic, hospital)
- ... (linguistic frameworks)

```
car, bicycle: similar coffee, cup What's the relationship?
```

car, gasoline: **related**, not similar

-> topic models: Latent Dirichlet Allocation, LDA – unsupervised learning on large set of texts, induce sets of associated words.



# Lexical Semantics – Superordinate / Subordinate

One sense is a **subordinate** of the other: the first is more specific (subclass of the other)

- car subordinate of vehicle.
- vehicle **superordinate** of car.



# Lexical Semantics – Connotations

Words have affective meanings

- positive connotations (happy)
- negative connotations (sad)

positive evaluation (great, love) negative evaluation (terrible, hate).

But: "terribly good!"



# **Vector Semantics**

Computational model to deal with these different aspects?

Combines the distributionalist intuition and the vector intuition.

Affective meaning variance along axes:

- Valence (pleasantness)
- Arousal (intensity of emotion)
- Dominance (degree of control)

|            | Valence | Arousal | Dominance |
|------------|---------|---------|-----------|
| courageous | 8.05    | 5.5     | 7.38      |
| music      | 7.67    | 5.57    | 6.5       |
| heartbreak | 2.45    | 5.65    | 3.58      |
| cub        | 6.71    | 3.95    | 4.24      |
| life       | 6.68    | 5.59    | 5.89      |



#### **Vector Semantics**

- Define words as vectors
- "embedding" embedded into a (multi-dimentional) space

Standard in NLP





# Types of Embeddings

- TF-IDF
  - Common baseline
  - Sparse vectors
  - Words as function of counts
- Word2vec
  - Dense vectors
  - Representations distinguish between near/far words.

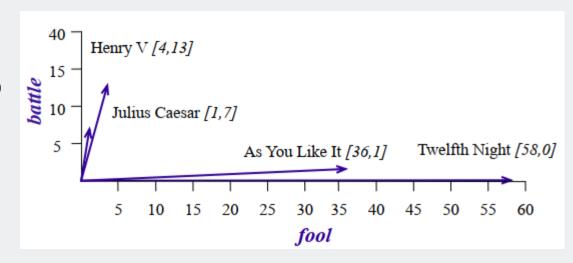


# From Words to Vectors

#### Term-document matrix

|        | As You Like It | Twelfth Night | Julius Caesar | Henry V |
|--------|----------------|---------------|---------------|---------|
| battle |                | 0             | 7             | 13      |
| good   | l 14           | 80            | 62            | 89      |
| fool   | 36             | 58            | 1             | 4       |
| wit    | 20             | 15            | 2             | 3       |

Vectors similar for the two comedies





# From Words to Vectors

#### Term vector

|        | As You Like It | Twelfth Night | Julius Caesar | Henry V |
|--------|----------------|---------------|---------------|---------|
| battle | 1              | 0             | 7             | 13      |
| good   | 114            | 80            | 62            | 89      |
| fool   | 36             | 58            | 1             | 4       |
| wit    | 20             | 15            | 2             | 3       |

Word-word matrix (term-context matrix)

# Term-context – Matrix

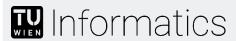
Two words are similar in meaning if their context vectors are similar

is traditionally followed by **cherry** often mixed, such as **strawberry** computer peripherals and personal digital a computer. This includes information available on the internet

pie, a traditional dessert rhubarb pie. Apple pie assistants. These devices usually

|             | aardvark | <br>computer | data | result | pie | sugar |  |
|-------------|----------|--------------|------|--------|-----|-------|--|
| cherry      | 0        | <br>2        | 8    | 9      | 442 | 25    |  |
| strawberry  | 0        | <br>0        | 0    | 1      | 60  | 19    |  |
| digital     | 0        | <br>1670     | 1683 | 85     | 5   | 4     |  |
| information | 0        | <br>3325     | 3982 | 378    | 5   | 13    |  |

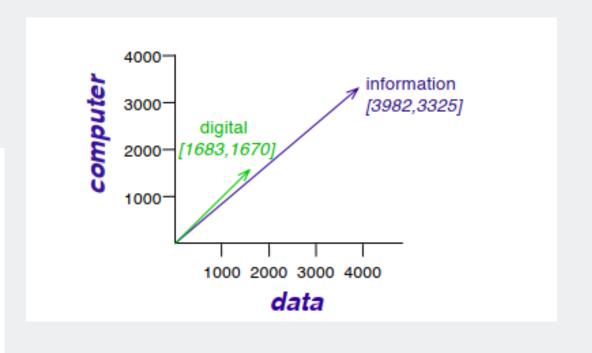
 $|V| \times |V|$  (10K – 50K words), sparse vectors!



# Cosine for Similarity

Measure the angle between vectors

$$cosine(\mathbf{v}, \mathbf{w}) = \frac{\mathbf{v} \cdot \mathbf{w}}{|\mathbf{v}||\mathbf{w}|} = \frac{\sum_{i=1}^{N} v_i w_i}{\sqrt{\sum_{i=1}^{N} v_i^2} \sqrt{\sum_{i=1}^{N} w_i^2}}$$



|             | aardvark | <br>computer | data | result | pie | sugar |  |
|-------------|----------|--------------|------|--------|-----|-------|--|
| cherry      | 0        | <br>2        | 8    | 9      | 442 | 25    |  |
| strawberry  | 0        | <br>0        | 0    | 1      | 60  | 19    |  |
| digital     | 0        | <br>1670     | 1683 | 85     | 5   | 4     |  |
| information | 0        | <br>3325     | 3982 | 378    | 5   | 13    |  |



# Cosine example

However ....

raw-frequencies are skewed non-discriminative

|             | pie | data | computer |
|-------------|-----|------|----------|
| cherry      | 442 | 8    | 2        |
| digital     | 5   | 1683 | 1670     |
| information | 5   | 3982 | 3325     |

$$\cos(\text{cherry, information}) = \frac{442*5+8*3982+2*3325}{\sqrt{442^2+8^2+2^2}\sqrt{5^2+3982^2+3325^2}} = .017$$

$$\cos(\text{digital, information}) = \frac{5*5+1683*3982+1670*3325}{\sqrt{5^2+1683^2+1670^2}\sqrt{5^2+3982^2+3325^2}} = .996$$

# TF-IDF

• TF: term frequency. frequency count (log-ransformed):

$$tf_{t,d} = \begin{cases} 1 + \log_{10} count(t,d) & \text{if } count(t,d) > 0 \\ 0 & \text{otherwise} \end{cases}$$

• IDF: inverse document frequency:

$$idf_t = \log_{10} \left( \frac{N}{df_t} \right)$$

! df - document frequency - is not collection frequency

# TF-IDF

• TF: term frequency. frequency count (log-ransformed):

$$tf_{t,d} = \begin{cases} 1 + \log_{10} count(t,d) & \text{if } count(t,d) > 0 \\ 0 & \text{otherwise} \end{cases}$$

• IDF: inverse document frequency:

$$idf_t = \log_{10} \left( \frac{N}{df_t} \right)$$

• TF-IDF weighted value:

$$w_{t,d} = \mathrm{tf}_{t,d} \times \mathrm{idf}_t$$

# TF-IDF vs Raw Frequencies

Raw frequencies

|        | As You Like It | Twelfth Night | Julius Caesar | Henry V |
|--------|----------------|---------------|---------------|---------|
| battle | 1              | 0             | 7             | 13      |
| good   | 114            | 80            | 62            | 89      |
| fool   | 36             | 58            | 1             | 4       |
| wit    | 20             | 15            | 2             | 3       |

TF-IDF frequencies

|        | As You Like It | Twelfth Night | Julius Caesar | Henry V |
|--------|----------------|---------------|---------------|---------|
| battle | 0.074          | 0             | 0.22          | 0.28    |
| good   | 0              | 0             | 0             | 0       |
| fool   | 0.019          | 0.021         | 0.0036        | 0.0083  |
| wit    | 0.049          | 0.044         | 0.018         | 0.022   |



# Recap

- Vector Semantics & Embeddings
  - Lexical and Vector Semantics
  - Words as Vectors
  - Measuring similarity & tf-idf
    - Sparse
  - Word2Vec



#### Dense Vectors – Word2Vec

#### TF-IDF vectors are

- long (length |V|= 20,000 to 50,000)
- sparse (most elements are zero)

#### Want vectors which are

- short (length 50-1000)
- dense (most elements are non-zero)



#### Dense Vectors – Word2Vec

# Why dense vectors?

- easier to use as features in machine learning (less weights to tune)
- generalize better than storing explicit counts
- They may do better at capturing synonymy, because:
  - car and automobile are synonyms; but are distinct dimensions in TF-IDF space
  - a word with car as a neighbour and a word with automobile as a neighbour should be similar, but in sparse vector/TF-IDF models they aren't
- In practice, they work better



# Where to look for Dense Embeddings

```
Word2vec (Mikolov et al.)
https://code.google.com/archive/p/word2vec/
```

Fasttext

http://www.fasttext.cc/

Glove (Pennington, Socher, Manning) http://nlp.stanford.edu/projects/glove/



# Word2Vec

- Popular embedding method
- Very fast to train
- Code available on the web

Idea: predict rather than count



# Word2Vec Intuition

• Instead of counting how often each word w occurs near "apricot" train a classifier on a binary prediction task:

# Is w likely to show up near "apricot"?

- We don't actually care about this task
  - But we'll take the learned classifier weights as the word embeddings



#### Brilliant Insight!

Use running text as implicitly supervised training data!

Take a word w near "apricot" see it as the gold 'correct answer' to the question:

"Is word w likely to show up near apricot?"

No need for hand-labeled supervision

The idea comes from neural language modeling (2003, 2011)



### Word2Vec: Skip-Gram

- "skip-gram with negative sampling" (SGNS)
- 1. Treat the target word and a neighboring context word as positive examples.
- 2. Randomly sample other words in the lexicon to get negative samples
- 3. Use logistic regression to train a classifier to distinguish those two cases
- 4. Use the weights as the embeddings



#### Word2Vec Classification Task

#### Training sentences:

```
... lemon, a tablespoon of apricot jam a pinch ... c1 c2 target c3 c4
```

Classification goal: Given a tuple (t, c) = target, context

- (apricot, jam)
- (apricot, aardvark)
- Compute the probability that *c* is a real context word:

$$P(+|t,c)$$

$$P(-|t,c) = 1 - P(+|t,c)$$

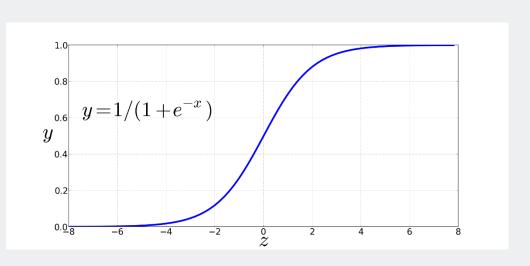
# How to compute P(+ | t,c)?

- Words are likely to appear near similar words
- Model similarity with dot-product!
- Similarity(t,c) ∝ t · c

#### Problem:

Dot product is not a probability!

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$



# Turning dot product into a probability

$$P(+|t,c) = \frac{1}{1+e^{-t\cdot c}}$$

$$P(-|t,c) = 1 - P(+|t,c)$$
$$= \frac{e^{-t \cdot c}}{1 + e^{-t \cdot c}}$$

One word in the context of t

$$P(+|t,c_{1:k}) = \prod_{i=1}^{\kappa} \frac{1}{1+e^{-t\cdot c_i}}$$

$$\log P(+|t,c_{1:k}) = \sum_{i=1}^{k} \log \frac{1}{1 + e^{-t \cdot c_i}}$$

All words in the context of t

Simplifying assumption!

# Skip-Gram Training Data

#### Training sentence:

```
... lemon, a tablespoon of apricot jam a pinch ...
           c1 c2 t c3 c4
```

#### positive examples +

apricot tablespoon

apricot of

apricot preserves

apricot or

#### negative examples -

apricot aardvark apricot twelve apricot puddle apricot hello apricot where apricot dear  $P_{\alpha}(w) = \frac{count(w)^{\alpha}}{\sum_{w'} count(w')^{\alpha}}$ apricot coaxial apricot forever

$$P_{\alpha}(w) = \frac{count(w)^{\alpha}}{\sum_{w'} count(w')^{\alpha}}$$

Noise words – selection by weighted unigram frequency

### Training Phase

#### Given:

- positive & negative training instances
- Initial set of embedding (random vector values) length 300

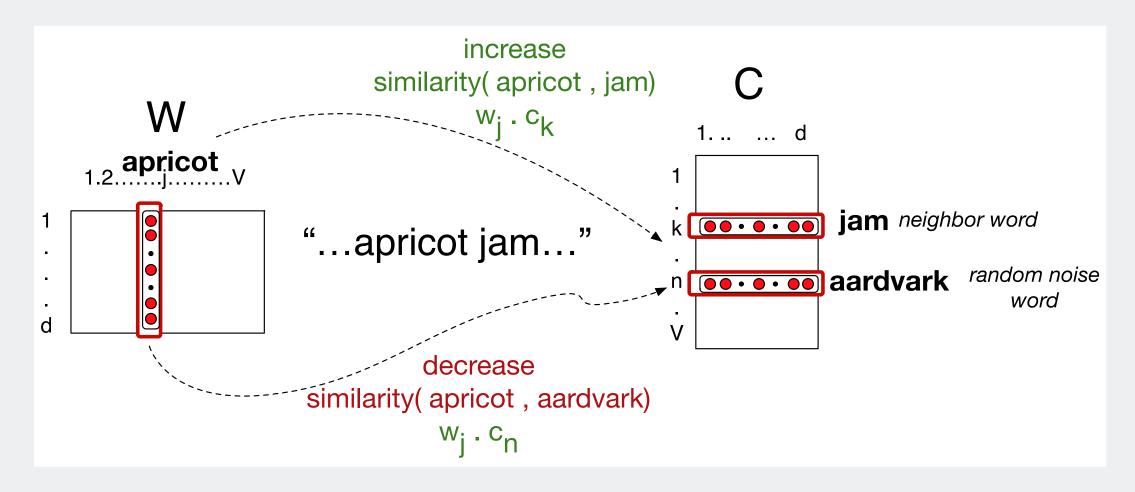
Goal: Adjust embeddings such that

- Positive (target, context) instance similarity is maximised
- Necative (target, context) instance similarity is minimized

$$L(\theta) = \sum_{(t,c)\in +} \log P(+|t,c) + \sum_{(t,c)\in -} \log P(-|t,c)$$

#### **Use Gradient Descent**

### Training Phase





# Summary: How to learn word2vec (skip-gram) embeddings

- Start with V random 300-dimensional vectors as initial embeddings
- Select positive / negative training data
- Use logistic regression
- Adjust weights by making positive pairs closer to each other (i.e. positive classification)
- Throw away the classifier code and keep the embeddings (regression weights!)

(V is the size of the vocabulary)

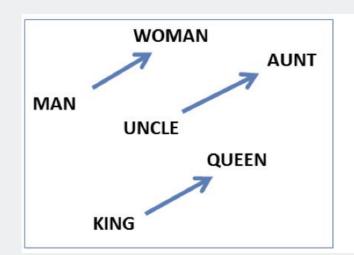


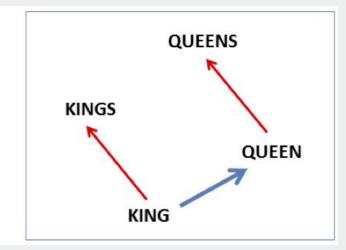
### Word2Vec Embeddings: Semantic Properties

Similarity depends on context window size:

- Short context windows similar words
- Long context windows similar topics

Analogy: relational meaning appears to be captured





vector('king') - vector('man') + vector('woman') ≈ vector('queen') vector('Paris') - vector('France') + vector('Italy') ≈ vector('Rome')



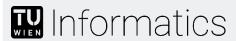
#### Cultural Bias in Embeddings

Bolukbasi, Tolga, Kai-Wei Chang, James Y. Zou, Venkatesh Saligrama, and Adam T. Kalai. "Man is to computer programmer as woman is to homemaker? debiasing word embeddings." In *Advances in Neural Information Processing Systems*, pp. 4349-4357. 2016.

```
Ask "Paris : France :: Tokyo : x" 
 x = Japan
```

```
Ask "father: doctor: mother: x" 
x = nurse
```

Ask "man : computer programmer :: woman : x" x = homemaker



#### Cultural Bias in Embeddings

Implicit Association test (Greenwald et al 1998): How associated are

- concepts (flowers, insects) & attributes (pleasantness, unpleasantness)
- Studied by measuring timing latencies for categorization.

Psychological findings on US participants:

- African-American names are associated with unpleasant words (more than European-American names)
- Male names associated more with math, female names with arts
- Old people's names with unpleasant words, young people with pleasant words.

Embeddings reflect and replicate all sorts of pernicious biases.

Debiasing

Greenwald, A. G., McGhee, D. E., and Schwartz, J. L. K. (1998). Measuring individual differences in implicit cognition: the implicit association test. Journal of personality and social psychology, 74(6), 1464–1480.



Caliskan, Aylin, Joanna J. Bruson and Arvind Narayanan. 2017. Semantics derived automatically from language corpora contain human-like biases. Science 356:6334, 183-186.

#### Recap

- Vector Semantics & Embeddings
  - Lexical and Vector Semantics
  - Words as Vectors
  - Measuring similarity & tf-idf
    - Sparse
  - Word2Vec
- Neural Networks

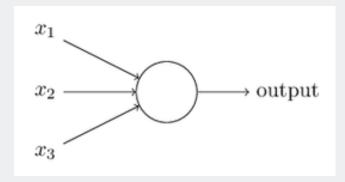


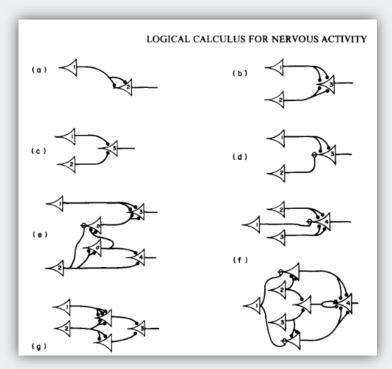
# Neural Networks



### Neural Networks – the beginnings

- In text processing NNs are a fundamental computational tool
- 1943 McCulloch-Pitts neuron -> simplified model of a neuron
- Propositional logic & temporal propositional expressions
- 1950s and '60s perceptron

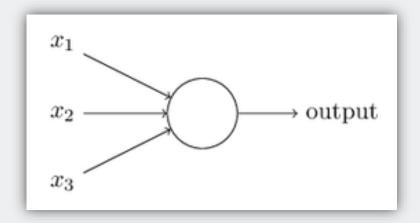






### The Perceptron

- Simple rule to compute the output {0, 1}
- Inputs x\_1, x\_2, x\_3
- Weights  $w_i$  for importance  $(w_i \text{ in } \mathbb{R})$
- Weighted sum greater than a threshold then output



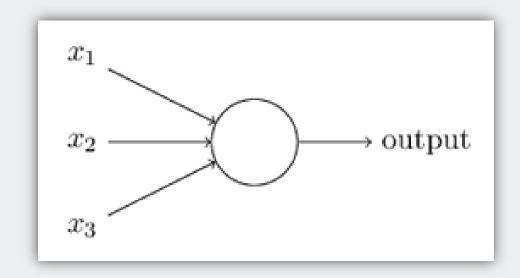
$$ext{output} = \left\{ egin{array}{ll} 0 & ext{if } \sum_{j} w_{j} x_{j} \leq ext{ threshold} \ 1 & ext{if } \sum_{j} w_{j} x_{j} > ext{ threshold} \end{array} 
ight.$$

- A cheese festival coming weekend. You like cheese, and decide whether or not to go to the festival.
- You might make your decision by weighing up four factors:
- 1. Is the weather good?
- 2. Does your friend/partner want to accompany you?
- 3. Is the festival near public transit? (You don't own a car)
- 4. Do I have enough money? Is there a Covid-19 curfew?



by weighting up evidence

- 1. Is the weather good?
- 2. Friend/partner Joining?
- 3. Public transportation
- 4. Do I have enough money?



1. Is the weather good?

2. Friend/partner Joining?

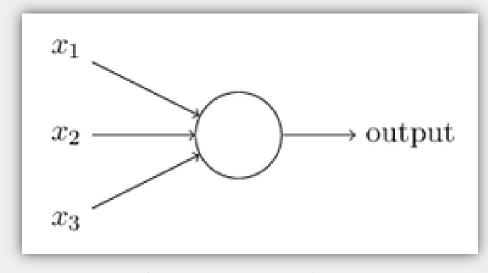
$$0 - no, 1 - yes$$

3. Public transportation

$$0 - no, 1 - yes$$

4. Do I have enough money?

$$0 - no, 1 - yes$$



1. Is the weather good?

$$0 - \text{bad}, 1 - \text{good}, w_1 = 6$$

2. Friend/partner Joining?

$$0 - \text{no}, 1 - \text{yes}$$
  $w_2 = 2$ 

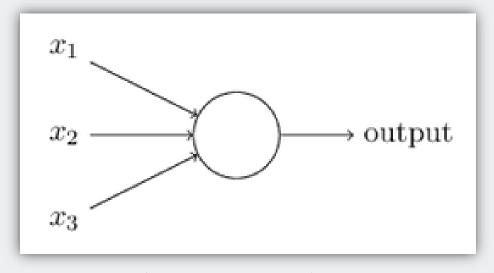
3. Public transportation

$$0 - \text{no}, 1 - \text{yes}$$
  $w_3 = 2$ 

4. Do I have enough money?

$$0 - \text{no}, 1 - \text{yes}$$
  $w_4 = -5$ 





1. Is the weather good?

$$0 - \text{bad}, 1 - \text{good}, w_1 = 6$$

2. Friend/partner Joining?

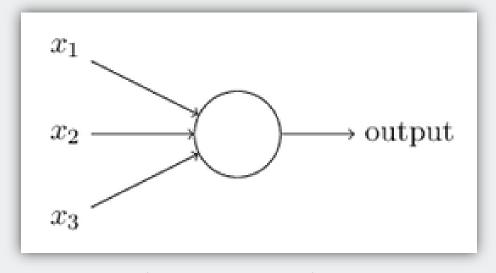
$$0 - \text{no}, 1 - \text{yes}$$
  $w_2 = 2$ 

3. Public transportation

$$0 - \text{no}, 1 - \text{yes}$$
  $w_3 = 2$ 

4. Do I have enough money?

$$0 - \text{no}, 1 - \text{yes}$$
  $w_4 = -5$ 



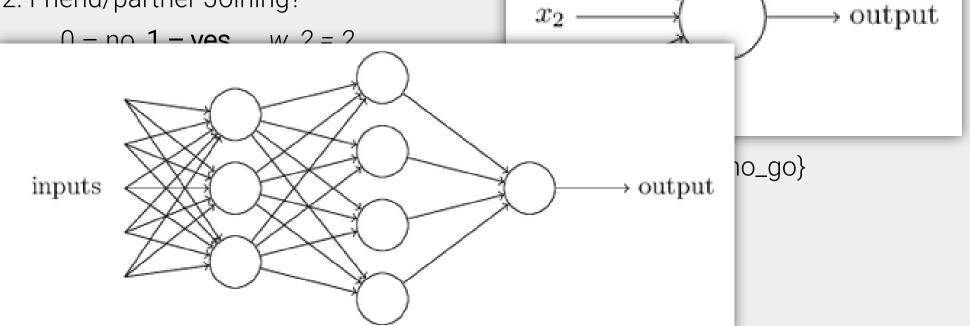
compute = 
$$\sum_{j} w_{j} x_{j}$$

8 (first three factors are 1, go) = 3 (all factors are 1, no\_go)

1. Is the weather good?

$$0 - \text{bad}, 1 - \text{good}, w_1 = 6$$

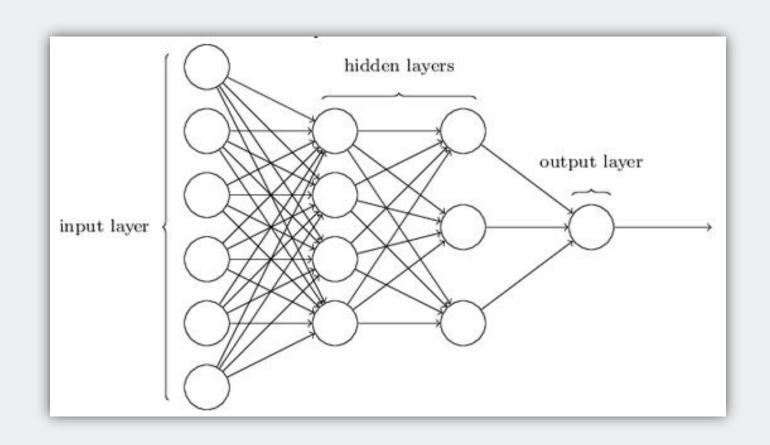
2. Friend/partner Joining?



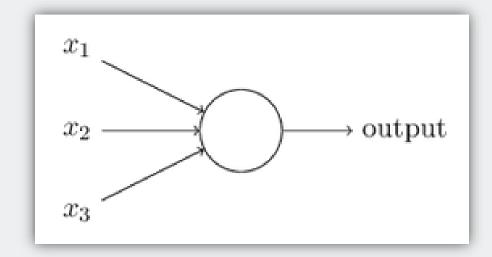
 $x_1$ 



### Architecture of a (feedforward) Neural Network



# Perceptron – some simplifications



 $oxed{w\cdot x \equiv \sum_j w_j x_j}$ 

 $b \equiv -\text{threshold}$ 

1 ⇔ "firing" an electrical pulse

b - how easy it is to "fire"

$$ext{output} = egin{cases} 0 & ext{if } w \cdot x + b \leq 0 \ 1 & ext{if } w \cdot x + b > 0 \end{cases}$$

 $ext{output} = \left\{ egin{array}{ll} 0 & ext{if } \sum_j w_j x_j \leq ext{ threshold} \ 1 & ext{if } \sum_j w_j x_j > ext{ threshold} \end{array} 
ight.$ 

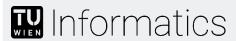
### Compute anything!

#### Perceptrons:

weigh evidence to make decisions compute elementary logic functions

- -> simulate an NAND gate (universality)
- + Powerful tool
- Just another NAND gate? actually, no

Learning algorithms



# Sigmoid Neuron

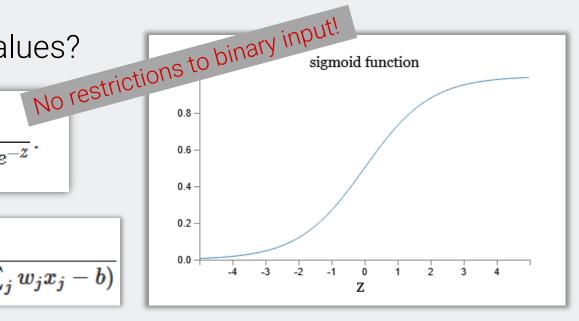
Perceptrons: small changes in intput cause large changes in output Reason: Nodes (neurons) have only two states: 0 or 1

Can we output a continuum of values?

Between 0 and 1?

$$\sigma(z) \equiv rac{1}{1+e^{-z}}.$$

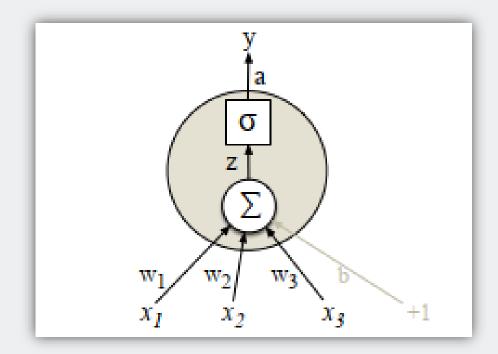
$$\frac{1}{1+\exp(-\sum_j w_j x_j - b)}$$





#### **Activation Functions**

- 1. Sigmoid function
- 2. Hyperbolic tan
- 3. Rectified Linear Unit (ReLU)
- 4. Leaky Rectified Linear Unit
- 5. Maxout
- 6. ..



#### **Activation Functions**

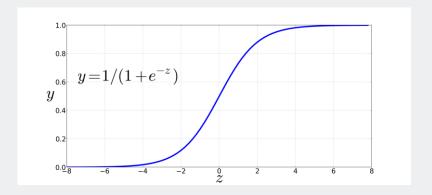
1. Sigmoid function

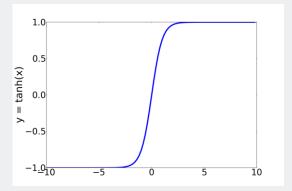
$$\frac{1}{1+e^{-z}}$$

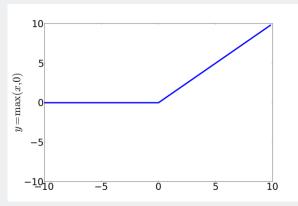
2. Hyperbolic tan

$$\frac{e^z - e^{-z}}{e^z + e^{-z}}$$

3. Rectified Linear Unit (ReLU)





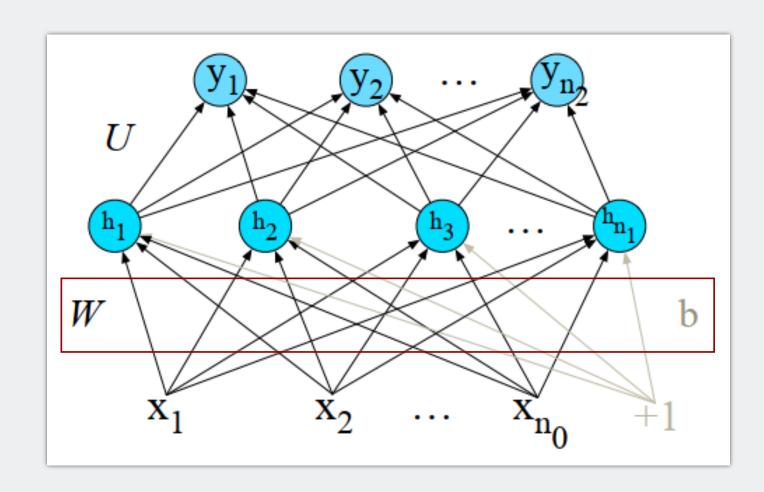


- Multilayer network
- Units connected without cycles
- Node types:
  - Input units
  - Hidden units
  - Output units



- Fully connected
- Hidden units sum over all inputs
- $W_{i,j}$  link between  $x_i$  and  $h_j$

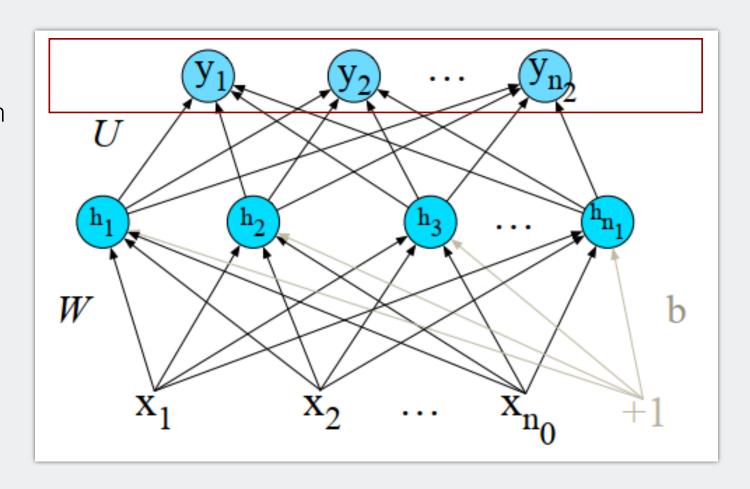
$$h = \sigma (Wx + b)$$
 (elementwise)



Output layer probability distribution

Hidden layer (hypothesis)

Input layer





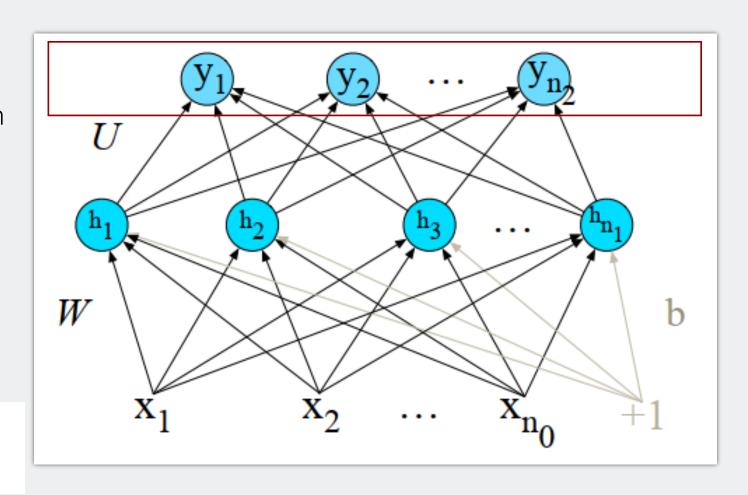
Output layer probability distribution

*U* output layer weight matrix

$$z = Uh - no output$$

#### Normalizing

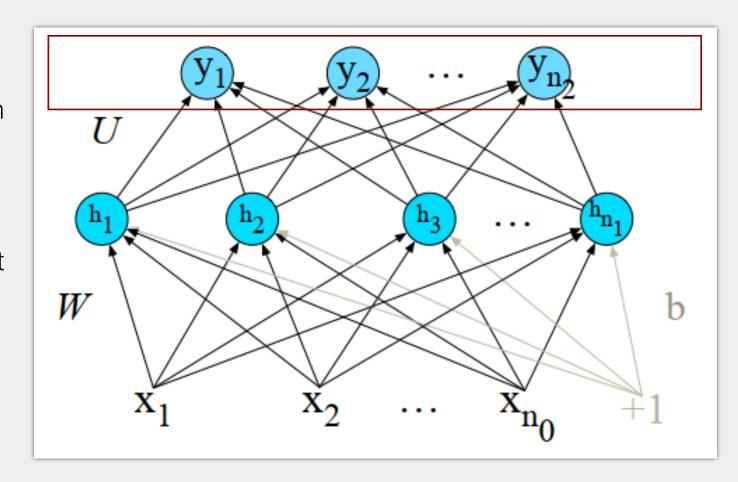
$$softmax(z_i) = \frac{e^{z_i}}{\sum_{j=1}^d e^{z_j}} \quad 1 \le i \le d$$



Output layer probability distribution

Hidden layer (hypothesis) representation of the input

Input layer



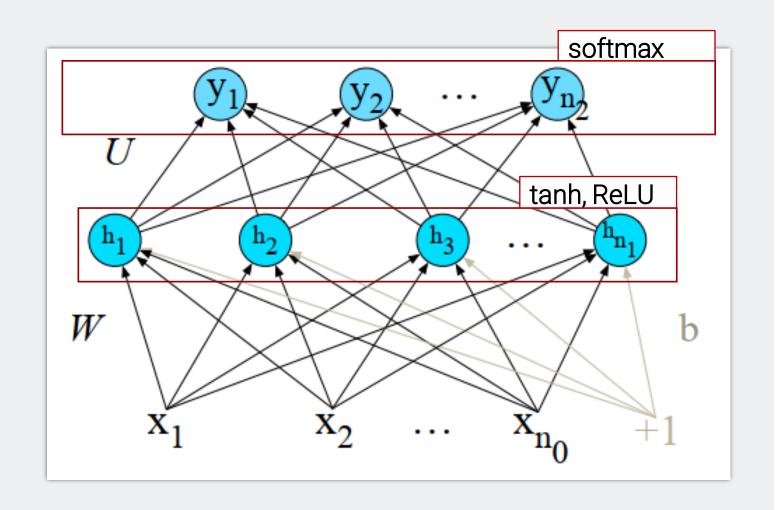


- ~ logistic regression:
- (a) with many layers,
- (b) induces the feature representations themselves (not "by hand").

$$h = \sigma(Wx+b)$$

$$z = Uh$$

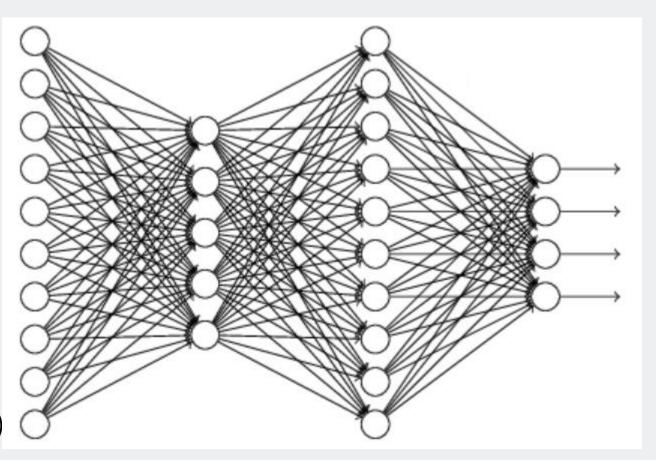
$$y = \text{softmax}(z)$$

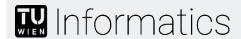




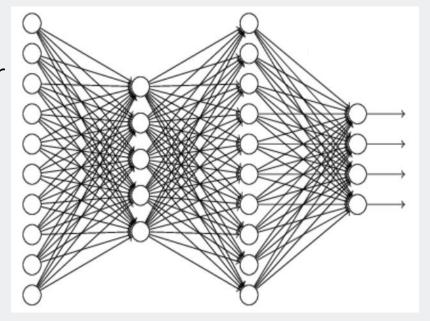
- Instance of supervised learning
- (x, y) training pairs
- ŷ system's estimate of y
- Find parameters W<sub>i</sub> and b<sub>i</sub> for each layer i s.t. ŷ as close to y as possible

Logistic regression (Chap 5, SLP3)



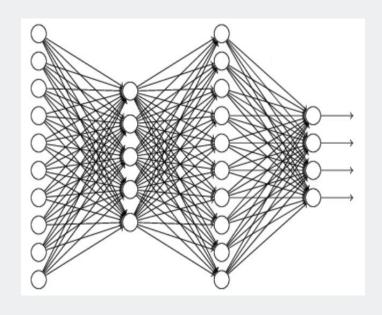


- Define a loss function (for ŷ and y)
  - Cross-entropy loss function
- Choose algorithm to minimize the loss function
  - Gradient descent
- Compute partial derivatives wrt. each parameter
- (1986) Error backpropagation a.k.a. reverse differentiation

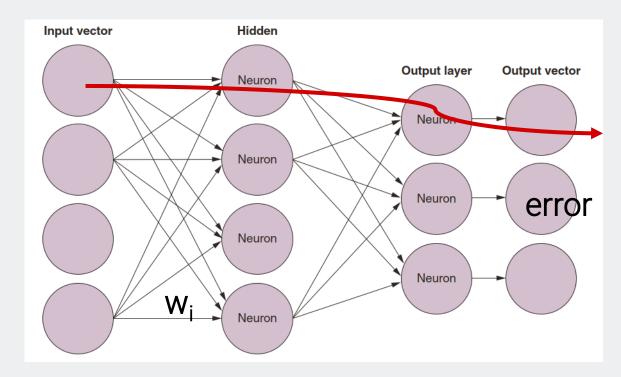




- Define a loss function (for ŷ and y)
  - Cross-entropy loss function
- Error backpropagation
- Requires activation functions that are continuously differentiable
- Derivative -> partial derivatives wrt. variables







LOSS(ŷ, y)

Composition of functions (dot products and activation functions)

Chain rule (general form)

$$(F'(x) =)$$
  $(f(g(x))' = f'(g(x))g'(x)$ 

Chain rule: Finds you the derivative for the activation functions:

- For each neuron
- Wrt. its input

 Includes learning rate as hyper parameter



# Weight Changes – when to apply them?

- Be specific about it
- Calculations depend on the network state
- Changes are applied in one go to all the weights of the network
  - For each input
  - Aggregated, and applied after all training data was looked at.
  - Batched
  - ...

- 1. Pass in all the inputs.
- 2. Get error for each input.
- 3. Backpropagate errors to each of the weights.
- 4. Update each weight with the total change in error

Steps 1.-4. for all training data

- EPOCH
- Can pass the data again -> new refinements
- Overfitting!



# Optimizing Learning

- Weight initialization with random, small numbers
- Normalize input values
- Dropout: avoid overfitting
- Tuning hyperparameters
  - · learning rate,
  - · mini-batch size,
  - number of layers,
  - nodes / layer
  - choice of activation functions
- Gradient decent variants
- Computational graphs (pythorch, tensorflow)



#### Recap

- Vector Semantics & Embeddings
  - Lexical and Vector Semantics
  - Words as Vectors
  - Measuring similarity & tf-idf
  - Word2Vec
- Neural Networks
  - Perceptron, units, activation functions
  - Feed forward
  - Training
- Neural Language Models

