Transition Rules

1.1 Abstract Syntax

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S ::= x := a \mid r[a_1] := a_2 \mid S_1; \ S_2 \mid \text{if } b \text{ do } S \mid \text{if } b \text{ do } S_1 \text{ else do } S_2 \mid \text{ while } b \text{ do } S \mid \text{from } x := a_1 \text{ to } a_2 \text{ step } a_3 \text{ do } S \mid \text{call } p(\vec{x}) \mid \text{begin } Q \text{ end} \mid \text{switch}(a) \text{ case } a_1 : \ S_1 \text{ break}; \ \dots \text{ case} a_k : \ S_k \text{ break}; \text{ default } : \ S \text{ break} Q ::= D_p \ Q \mid D_v \ Q \mid S \ Q \mid \varepsilon \quad a ::= n \mid x \mid a_1 + a_2 \mid a_1 - a_2 \mid a_1 * a_2 \mid a_1 / a_2 \mid (a) \mid r[a_i] \quad b ::= a_1 = a_2 \mid a_1 > a_2 \mid a_1 < a_2 \mid \neg b \mid b_1 \ \land \ b_2 \mid b_1 \ \lor \ b_2 \mid (b) D_V ::= \text{var } x := a; \ D_V \mid \varepsilon \quad D_P ::= \text{func } p \text{ is } S; \ D_P \mid \varepsilon \quad D_A ::= \operatorname{array} r[a_1]; \ D_A \mid \varepsilon
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Transitioner er på formen: $env_V, env_P \vdash \langle S, sto \rangle \rightarrow sto'$

$$[VAR-ASS] \qquad env_V, env_P \vdash \langle x < --a, sto \rangle \rightarrow sto[l \mapsto v]$$
 where $env_V, sto \vdash a \rightarrow_a v$ and $env_V \ x = l$
$$env_V, env_P \vdash \langle r[a_1] < --a_2, sto \rangle \rightarrow sto[l_2 \mapsto v_2]$$
 where $env_V, sto \vdash a_1 \rightarrow_a v_1$ and $env_V, sto \vdash a_2 \rightarrow_a v_2$ and $env_V \ r = l_1$ and $l_2 = l_1 + v_1$ and $v_3 = sto \ l_1$ and $1 \le v_1 \le v_3$

[COMP] $\frac{env_V, env_P \vdash \langle S_1, sto \rangle \to sto''}{\frac{env_V, env_P \vdash \langle S_2, sto'' \rangle \to sto'}{env_V, env_P \vdash \langle S_1; S_2, sto \rangle \to sto'}}$

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$$\text{where } env_P \; p = (S, \vec{z}, env_V', env_P') \\ \text{and } |\vec{a}| = |\vec{z}| \\ \text{and } env_V, sto \vdash a_i \to v_i \text{ for each } 1 \leq i \leq |\vec{a}| \\ \text{and } l_1 = env_V \text{ new} \\ \text{and } l_{i+1} = \text{new } l_i \text{ for each } 1 \leq i < |\vec{a}| \\ \frac{\langle D_V, env_V, sto \rangle \to_{DV} (env_V', sto'')}{env_V' \vdash \langle D_P, env_P \rangle \to_{DP} env_P'} \\ \frac{env_V' \vdash \langle D_P, env_P \rangle \to_{DP} env_P'}{env_V, env_P' \vdash \langle S, sto'' \rangle \to sto'} \\ \text{[BLOCK]} \\ \frac{\langle Q, env_P, env_V, sto \rangle \to_{Q} (env_V', env_P', sto'') \rangle \to sto'}{env_V, env_P \vdash \langle \text{begin } Q \text{ end}, sto \rangle \to sto'} \\ \text{Table 1.1: Statements}$$

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env_V, env_P \vdash (\text{switch}(a) \text{ begin case } a_1 : S_1 \text{ break}; \dots \text{ case } a_k : S_k \text{ break}; \text{ default} : S \text{ break}; \text{ end}, sto \rightarrow sto'
                                                                                    \rightarrow sto'
                                                                         env_V, env_P \vdash \langle \text{switch}(a) \text{ begin case } a_1 : S_1 \text{ break; default} : S \text{ break; end, } sto \rangle
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         env_V, env_P \vdash \langle S_1, sto \rangle \rightarrow sto'
env_V, env_P \vdash \langle S, sto \rangle \rightarrow (sto')
                                                                                                                                                                                                     Where env_V, sto \vdash a \rightarrow_a v
                                                                                                                                                                                                                                                                          and env_V, sto \vdash a_1 \rightarrow_a v_1
                                                                                                                                                                                                                                                                                                                                            and v \neq v_1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             [SWITCH-2]
                                [SWITCH-1]
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 $env_V, env_P \vdash (\text{switch}(a) \text{ begin case } a_1 : S_1 \text{ break}; \dots \text{ case } a_k : S_k \text{ break}; \text{ default} : S \text{ break}; \text{ end}, sto \rightarrow sto'$ $env_V, env_P \vdash \langle \text{switch}(a) \text{ begin case } a_2 : S_2 \text{ break}; \dots \text{ case } a_k : S_k \text{ break}; \text{ default } : S \text{ break}; \text{ end, } sto \rangle \to sto'$ [SWITCH-3]

and $env_V, sto \vdash a_1 \rightarrow_a v_1$

and $v = v_1$

and env_V , $sto \vdash a \rightarrow_a v$

Where k > 0

Where k > 1and env_V , $sto \vdash a \rightarrow_a v$ and env_V , $sto \vdash a_1 \rightarrow_a v_1$ and $v \neq v_1$

Table 1.2: Statements

Transitioner er på formen: env_V , $sto \vdash a \rightarrow_a v$

[NUM]
$$env_V, sto \vdash n \rightarrow_a v$$

if
$$\mathcal{N}[[n]] = v$$

[VAR]
$$env_V, sto \vdash x \rightarrow_a v$$

if
$$env_V x = l$$

and $sto l = v$

[ADD]
$$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 + a_2 \rightarrow_a v}$$

where
$$v = v_1 + v_2$$

[SUB]
$$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 - a_2 \rightarrow_a v}$$

where
$$v = v_1 - v_2$$

[MULT]
$$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 \cdot a_2 \rightarrow_a v}$$

where
$$v = v_1 \cdot v_2$$

[DIV]
$$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1/a_2 \rightarrow_a v}$$

where
$$v = v_1/v_2$$

[PAR]
$$\frac{env_V, sto \vdash a_1 \to_a v_1}{env_V, sto \vdash (a_1) \to_a v_1}$$

[ARR]
$$env_V, sto \vdash r[a_1] \rightarrow_a a_2$$

where
$$env_V$$
, $sto \vdash a_1 \rightarrow_a v_1$
and env_V , $sto \vdash a_2 \rightarrow_a v_2$
and $env_V r = l$
and $sto l = v_3$
and $0 < v_1 \le v_3$
and $sto(l + v_1) = v_2$

Table 1.3: Arithmetic expressions

Transitioner på formen: $env_V, sto \vdash b \rightarrow_b t$

[EQUAL-TRUE]
$$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 = a_2 \rightarrow_b \text{ true}}$$

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if
$$v_1 = v_2$$

[EQUAL-FALSE]
$$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 = a_2 \rightarrow_b \text{ false}}$$

if
$$v_1 \neq v_2$$

[GRT-TRUE]
$$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 > a_2 \rightarrow_b \text{ true}}$$

if
$$v_1 > v_2$$

$$[\text{GRT-FALSE}] \qquad \frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 > a_2 \rightarrow_b \text{false}}$$

if
$$v_1 \not> v_2$$

$$[\text{LESS-TRUE}] \qquad \frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 < a_2 \rightarrow_b \text{true}}$$

if
$$v_1 < v_2$$

$$[\text{LESS-FALSE}] \qquad \frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 < a_2 \rightarrow_b \text{ false}}$$

if
$$v_1 \not< v_2$$

[NOT-1]
$$\frac{env_V, sto \vdash b \to_b \text{ true}}{env_V, sto \vdash !b \to_b \text{ false}}$$

[NOT-2]
$$\frac{env_V, sto \vdash b \to_b \text{ true}}{env_V, sto \vdash !b \to_b \text{ false}}$$

[AND-TRUE]
$$\frac{env_V, sto \vdash b_1 \rightarrow_b \text{true} \quad env_V, sto \vdash b_2 \rightarrow_b \text{true}}{env_V, sto \vdash b_1 \land b_2 \rightarrow_b \text{true}}$$

[AND-FALSE]
$$\frac{env_V, sto \vdash b_i \to_b \text{ false}}{env_V, sto \vdash b_1 \land b_2 \to_b \text{ false}}$$

where
$$i \in 1, 2$$

[OR-TRUE]
$$\frac{env_V, sto \vdash b_i \to_b \text{ true}}{env_V, sto \vdash b_1 \lor b_2 \to_b \text{ true}}$$

where
$$i \in 1, 2$$

[OR-FALSE]
$$\frac{env_V, sto \vdash b_1 \rightarrow_b \text{ false} \quad env_V, sto \vdash b_2 \rightarrow_b \text{ false}}{env_V, sto \vdash b_1 \lor b_2 \rightarrow_b \text{ false}}$$

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[PAR-BOOL]
$$\frac{env_V, sto \vdash b \to_b v}{env_V, sto \vdash (b) \to_b v}$$

Table 1.4: Boolean expressions

Transitioner på formen: $\langle D_V, env_V, sto \rangle \rightarrow_{DV} (env_V', sto')$

[VAR-DEC]
$$\frac{\langle D_V, env_V'', sto[l \mapsto v] \rangle \to_{DV} (env_V', sto')}{\text{var } x < --a; D_V, env_V, sto \rangle \to_{DV} (env_V', sto')}$$

where env_V , $sto \vdash a \rightarrow_a v$ and $l = env_V$ next and $env_V'' = env_V[x \mapsto l][\text{next} \mapsto \text{new } l]$

[EMPTY-VAR] $\langle \varepsilon, env_V, sto \rangle \rightarrow_{DV} (env_V, sto)$

Transitioner på formen: $env_V \vdash \langle D_P, env_P \rangle \rightarrow_{DP} env_P'$

[FUNC-DEC]
$$\frac{env_V \vdash \langle D_P, env_P[p \mapsto (S, env_V, env_P)] \rangle \rightarrow_{DP} env_P'}{env_V \vdash \langle \operatorname{proc} p \text{ is } S; D_P, env_P \rangle \rightarrow_{DP} env_P'}$$

[EMPTY-FUNC] $env_V \vdash \langle \varepsilon, env_P \rangle \rightarrow_{DP} env_P'$

Transitioner på formen: $\langle D_A, env_V, sto \rangle \rightarrow_{DA} (env_V', sto')$

[ARRAY-DEC]
$$\frac{\langle D_A, env_V[r \mapsto l, \text{next} \mapsto l+v+1], sto[l \mapsto v] \rangle \to_{DA} (env_V', sto')}{\langle r[a_1], D_A, env_V, sto \rangle \to_{DA} (env_V', sto')}$$

where $env_V, sto \vdash a_1 \rightarrow_a v$ and $l = env_V \text{next}$ and l > 0

[EMPTY-ARRAY] $\langle \varepsilon, env_V, sto \rangle \rightarrow_{DA} (env_V, sto)$

Table 1.5: Declarations