

Transition Rules

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1.1 Abstract Syntax

$$\begin{aligned}
S ::= & x := a \mid r[a_1] := a_2 \mid S_1; S_2 \mid \text{if } b \text{ do } S \mid \text{if } b \text{ do } S_1 \text{ else do } S_2 \mid \text{while } b \text{ do } S \\
& \mid \text{from } x := a_1 \text{ to } a_2 \text{ step } a_3 \text{ do } S \\
& \mid \text{switch}(a) \text{ case } a_1 : S_1 \text{ break; } \dots \text{ case } a_k : S_k \text{ break; default : } S \text{ break} \\
& \mid \text{call } p(\vec{x}) \mid \text{begin } D_V D_A D_P S \text{ end} \\
a ::= & n \mid x \mid a_1 + a_2 \mid a_1 - a_2 \mid a_1 * a_2 \mid a_1 / a_2 \mid (a) \mid r[a_i] \\
b ::= & a_1 = a_2 \mid a_1 > a_2 \mid a_1 < a_2 \mid \neg b \mid b_1 \wedge b_2 \mid b_1 \vee b_2 \mid (b) \\
D_V ::= & \text{var } x := a; D_V \mid \varepsilon \\
D_P ::= & \text{func } p \text{ is } S; D_P \mid \varepsilon \\
D_A ::= & \text{array } r[a_1]; D_A \mid \varepsilon
\end{aligned}$$

Transitioner er på formen: $env_V, env_P \vdash \langle S, sto \rangle \rightarrow sto'$

[VAR-ASS] $env_V, env_P \vdash \langle x \leftarrow a, sto \rangle \rightarrow sto[l \mapsto v]$

where $env_V, sto \vdash a \rightarrow_a v$
and $env_V x = l$

[ARR-ASS] $env_V, env_P \vdash \langle r[a_1] \leftarrow a_2, sto \rangle \rightarrow sto[l_2 \mapsto v_2]$

where $env_V, sto \vdash a_1 \rightarrow_a v_1$
and $env_V, sto \vdash a_2 \rightarrow_a v_2$
and $env_V r = l_1$
and $l_2 = l_1 + v_1$

[COMP]
$$\frac{env_V, env_P \vdash \langle S_1, sto \rangle \rightarrow sto' \quad env_V, env_P \vdash \langle S_2, sto' \rangle \rightarrow sto''}{env_V, env_P \vdash \langle S_1; S_2, sto \rangle \rightarrow sto''}$$

[IF-TRUE]
$$\frac{env_V, env_P \vdash \langle S, sto \rangle \rightarrow sto'}{env_V, env_P \vdash \langle \text{if } b \text{ begin } S \text{ end}, sto \rangle \rightarrow sto'}$$

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	if $env_V, sto \vdash b \rightarrow_b \text{true}$
[IF-FALSE]	$env_V, env_P \vdash \langle \text{if } b \text{ begin } S \text{ end, } sto \rangle \rightarrow sto$
	if $env_V, sto \vdash b \rightarrow_b \text{false}$
[IF-ELSE-TRUE]	$\frac{env_V, env_P \vdash \langle S_1, sto \rangle \rightarrow sto'}{env_V, env_P \vdash \langle \text{if } b \text{ begin } S_1 \text{ end else begin } S_2 \text{ end, } sto \rangle \rightarrow sto'}$
	if $env_V, sto \vdash b \rightarrow_b \text{true}$
[IF-ELSE-FALSE]	$\frac{env_V, env_P \vdash \langle S_2, sto \rangle \rightarrow sto'}{env_V, env_P \vdash \langle \text{if } b \text{ begin } S_1 \text{ end else begin } S_2 \text{ end, } sto \rangle \rightarrow sto'}$
	if $env_V, sto \vdash b \rightarrow_b \text{false}$
[WHILE-TRUE]	$\frac{env_V, env_P \vdash \langle S, sto \rangle \rightarrow sto'' \quad env_V, env_P \vdash \langle \text{while } b \text{ begin } S \text{ end, } sto'' \rangle \rightarrow sto'}{env_V, env_P \vdash \langle \text{while } b \text{ begin } S \text{ end, } sto \rangle \rightarrow sto'}$
	if $env_V, sto \vdash b \rightarrow_b \text{true}$
[WHILE-FALSE]	$env_V, env_P \vdash \langle \text{while } b \text{ begin } S \text{ end, } sto \rangle \rightarrow sto$
	if $env_V, sto \vdash b \rightarrow_b \text{false}$
[FROM-TRUE]	$\frac{env_V, env_P \vdash \langle S, sto[l \vdash v_1] \rangle \rightarrow sto'' \quad \langle \text{from } x < - - a_1 + a_3 \text{ to } a_2 \text{ step } a_3 \text{ begin } S \text{ end, } sto'' \rangle \rightarrow sto'}{env_V, env_P \vdash \langle \text{from } x < - - a_1 \text{ to } a_2 \text{ step } a_3 \text{ begin } S \text{ end, } sto \rangle \rightarrow sto'}$
	where $env_V, sto \vdash a_1 \rightarrow_a v_1$ and $env_V, sto \vdash a_2 \rightarrow_a v_2$ and $env_V, sto \vdash a_3 \rightarrow_a v_3$ and $v_1 \leq v_2$ and $l = env_V x$
[FROM-FALSE]	$env_V, env_P \vdash \langle \text{from } x < - - a_1 \text{ to } a_2 \text{ step } a_3 \text{ begin } S \text{ end, } sto \rangle \rightarrow sto$
	where $env_V, sto \vdash a_1 \rightarrow_a v_1$ and $env_V, sto \vdash a_2 \rightarrow_a v_2$ and $env_V, sto \vdash a_3 \rightarrow_a v_3$ and $v_1 > v_2$
	FiXme Fatal: Disse 3 herunder skal ligges ned!!
[SWITCH-1]	$\frac{env_V, env_P \vdash \langle S, sto \rangle \rightarrow (sto')}{env_V, env_P \vdash \langle \text{switch}(a) \text{ begin case } a_1 : S_1 \text{ break; default : } S \text{ break; end, } sto \rangle \rightarrow sto'}$
	Where $k > 0$ and $env_V, sto \vdash a \rightarrow_a v$

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	$\text{and } env_V, sto \vdash a_1 \rightarrow_a v_1$ $\text{and } v \neq v_1$
[SWITCH-2]	$\frac{env_V, env_P \vdash \langle S_1, sto \rangle \rightarrow sto'}{env_V, env_P \vdash \langle \text{switch}(a) \text{ begin case } a_1 : S_1 \text{ break; } \dots \text{ case } a_k : S_k \text{ break; default : } \dots \rangle \rightarrow sto'}$ <p>Where $k > 1$ $\text{and } env_V, sto \vdash a \rightarrow_a v$ $\text{and } env_V, sto \vdash a_1 \rightarrow_a v_1$ $\text{and } v = v_1$</p>
[SWITCH-3]	$\frac{env_V, env_P \vdash \langle \text{switch}(a) \text{ begin case } a_2 : S_2 \text{ break; } \dots \text{ case } a_k : S_k \text{ break; default : } \dots \rangle \rightarrow sto'}{env_V, env_P \vdash \langle \text{switch}(a) \text{ begin case } a_1 : S_1 \text{ break; } \dots \text{ case } a_k : S_k \text{ break; default : } \dots \rangle \rightarrow sto'}$ <p>Where $k > 1$ $\text{and } env_V, sto \vdash a \rightarrow_a v$ $\text{and } env_V, sto \vdash a_1 \rightarrow_a v_1$ $\text{and } v \neq v_1$</p>
[CALL]	$\frac{env'_V[\vec{z} \mapsto \vec{l}], env'_P \vdash \langle S, sto[\vec{l} \mapsto \vec{v}] \rangle \rightarrow sto'}{env_V, env_P \vdash \langle \text{call } p(\vec{a}), sto \rangle \rightarrow sto'}$ <p>where $env_P p = (S, \vec{z}, env'_V, env'_P)$ $\text{and } \vec{a} = \vec{z}$ $\text{and } env_V, sto \vdash a_i \rightarrow v_i \text{ for each } 1 \leq i \leq \vec{a}$ $\text{and } l_1 = env_V \text{ new}$ $\text{and } l_{i+1} = l_i \text{ for each } 1 < i < \vec{a}$</p>
[BLOCK]	$\frac{\begin{array}{l} \langle D_V, env_V, sto \rangle \rightarrow_{D_V} (env'_V, sto'') \\ env'_V \vdash \langle D_P, env_P \rangle \rightarrow_{D_P} env'_P \\ env'_V, env'_P \vdash \langle S, sto'' \rangle \rightarrow sto' \end{array}}{env_V, env_P \vdash \langle \text{begin } D_V \ D_P \ S \text{ end, } sto \rangle \rightarrow sto'}$

Table 1.1: Statements

Transitioner er på formen: $env_V, sto \vdash a \rightarrow_a v$

[NUM] $env_V, sto \vdash n \rightarrow_a v$

if $\mathcal{N}[[n]] = v$

[VAR] $env_V, sto \vdash x \rightarrow_a v$

if $env_V x = l$

and $sto l = v$

[ADD]
$$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 + a_2 \rightarrow_a v}$$

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	where $v = v_1 + v_2$
[SUB]	$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 - a_2 \rightarrow_a v}$
	where $v = v_1 - v_2$
[MULT]	$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 \cdot a_2 \rightarrow_a v}$
	where $v = v_1 \cdot v_2$
[DIV]	$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 / a_2 \rightarrow_a v}$
	where $v = v_1 / v_2$
[PAR]	$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1}{env_V, sto \vdash (a_1) \rightarrow_a v_1}$
[ARR]	$env_V, sto \vdash r[a_1] \rightarrow_a a_2$
	where $env_V, sto \vdash a_1 \rightarrow_a v_1$ and $env_V, sto \vdash a_2 \rightarrow_a v_2$ and $env_V r = l$ and $sto l = v_3$ and $0 < v_1 \leq v_3$ and $sto(l + v_1) = v_2$

Table 1.2: Arithmetic expressions

Transitioner på formen: $env_V, sto \vdash b \rightarrow_b t$

[EQUAL-TRUE]	$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 = a_2 \rightarrow_b \text{true}}$
	if $v_1 = v_2$
[EQUAL-FALSE]	$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 = a_2 \rightarrow_b \text{false}}$
	if $v_1 \neq v_2$
[GRT-TRUE]	$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 > a_2 \rightarrow_b \text{true}}$
	if $v_1 > v_2$

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[GRT-FALSE]	$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 > a_2 \rightarrow_b \text{false}}$ <p>if $v_1 \not\leq v_2$</p>
[LESS-TRUE]	$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 < a_2 \rightarrow_b \text{true}}$ <p>if $v_1 < v_2$</p>
[LESS-FALSE]	$\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 < a_2 \rightarrow_b \text{false}}$ <p>if $v_1 \not< v_2$</p>
[NOT-1]	$\frac{env_V, sto \vdash b \rightarrow_b \text{true}}{env_V, sto \vdash !b \rightarrow_b \text{false}}$
[NOT-2]	$\frac{env_V, sto \vdash b \rightarrow_b \text{true}}{env_V, sto \vdash !b \rightarrow_b \text{false}}$
[AND-TRUE]	$\frac{env_V, sto \vdash b_1 \rightarrow_b \text{true} \quad env_V, sto \vdash b_2 \rightarrow_b \text{true}}{env_V, sto \vdash b_1 \wedge b_2 \rightarrow_b \text{true}}$
[AND-FALSE]	$\frac{env_V, sto \vdash b_i \rightarrow_b \text{false}}{env_V, sto \vdash b_1 \wedge b_2 \rightarrow_b \text{false}}$ <p>where $i \in 1, 2$</p>
[OR-TRUE]	$\frac{env_V, sto \vdash b_i \rightarrow_b \text{true}}{env_V, sto \vdash b_1 \vee b_2 \rightarrow_b \text{true}}$ <p>where $i \in 1, 2$</p>
[OR-FALSE]	$\frac{env_V, sto \vdash b_1 \rightarrow_b \text{false} \quad env_V, sto \vdash b_2 \rightarrow_b \text{false}}{env_V, sto \vdash b_1 \vee b_2 \rightarrow_b \text{false}}$
[PAR-BOOL]	$\frac{env_V, sto \vdash b \rightarrow_b v}{env_V, sto \vdash (b) \rightarrow_b v}$

Table 1.3: Boolean expressions

Transitioner på formen: $\langle D_V, env_V, sto \rangle \rightarrow_{DV} (env'_V, sto')$

$$[\text{VAR-DEC}] \quad \frac{\langle D_V, env''_V, sto[l \mapsto v] \rangle \rightarrow_{DV} (env'_V, sto')}{\text{var } x < - a; D_V, env_V, sto \rangle \rightarrow_{DV} (env'_V, sto')}$$

where $env_V, sto \vdash a \rightarrow_a v$

and $l = env_V \text{ next}$

and $env''_V = env_V[x \mapsto l][\text{next} \mapsto \text{new } l]$

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[EMPTY-VAR]	$\langle \varepsilon, env_V, sto \rangle \rightarrow_{DV} (env_V, sto)$ Transitioner på formen: $env_V \vdash \langle D_P, env_P \rangle \rightarrow_{DP} env'_P$
[FUNC-DEC]	$\frac{env_V \vdash \langle D_P, env_P[p \mapsto (S, env_V, env_P)] \rangle \rightarrow_{DP} env'_P}{env_V \vdash \langle \text{proc } p \text{ is } S; D_P, env_P \rangle \rightarrow_{DP} env'_P}$
[EMPTY-FUNC]	$env_V \vdash \langle \varepsilon, env_P \rangle \rightarrow_{DP} env'_P$ Transitioner på formen: $\langle D_A, env_V, sto \rangle \rightarrow_{DA} (env'_V, sto')$
[ARRAY-DEC]	$\frac{\langle D_A, env_V[r \mapsto l, \text{next} \mapsto l + v + 1], sto[l \mapsto v] \rangle \rightarrow_{DA} (env'_V, sto')}{\langle r[a_1], D_A, env_V, sto \rangle \rightarrow_{DA} (env'_V, sto')}$ where $env_V, sto \vdash a_1 \rightarrow_a v$ and $l = env_V \text{next}$ and $l > 0$
[EMPTY-ARRAY]	$\langle \varepsilon, env_V, sto \rangle \rightarrow_{DA} (env_V, sto)$

Table 1.4: Declarations