Transition Rules

1.1 Abstract Syntax

[VAR-ASS]

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S ::= x := a \mid r[a_1] := a_2 \mid S_1; \ S_2 \mid \text{if } b \text{ do } S \mid \text{if } b \text{ do } S_1 \text{ else do } S_2 \mid \text{ while } b \text{ do } S \mid \text{ from } x := a_1 \text{ to } a_2 \text{ step } a_3 \text{ do } S \mid \text{ call } p(\vec{x}) \mid \text{ begin } D_V \ D_A \ D_P \ S \text{ end} a ::= n \mid x \mid a_1 + a_2 \mid a_1 - a_2 \mid a_1 * a_2 \mid a_1/a_2 \mid (a) \mid r[a_i] b ::= a_1 = a_2 \mid a_1 > a_2 \mid a_1 < a_2 \mid \neg b \mid b_1 \ \land \ b_2 \mid b_1 \ \lor \ b_2 \mid (b) D_V ::= \text{var } x := a; \ D_V \mid \varepsilon D_P ::= \text{func } p \text{ is } S; \ D_P \mid \varepsilon D_A ::= \operatorname{array} r[a_1]; \ D_A \mid \varepsilon
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Transitioner er på formen: $env_V, env_P \vdash \langle S, sto \rangle \rightarrow sto'$

 $env_V, env_P \vdash \langle x < --a, sto \rangle \rightarrow sto[l \mapsto v]$

where
$$env_V$$
, $sto \vdash a \rightarrow_a v$ and $env_V \ x = l$
$$[ARR-ASS] \qquad env_V, env_P \vdash \langle r[a_1] < --a_2, sto \rangle \rightarrow sto[l_2 \mapsto v_2]$$
 where env_V , $sto \vdash a_1 \rightarrow_a v_1$ and env_V , $sto \vdash a_2 \rightarrow_a v_2$ and $env_V \ r = l_1$ and $l_2 = l_1 + v_1$

[COMP]
$$\frac{env_V, env_P \vdash \langle S_1, sto \rangle \to sto''}{\frac{env_V, env_P \vdash \langle S_2, sto'' \rangle \to sto'}{env_V, env_P \vdash \langle S_1; S_2, sto \rangle \to sto'}}$$

[IF-TRUE]
$$\frac{env_V, env_P \vdash \langle S, sto \rangle \to sto'}{env_V, env_P \vdash \langle \text{if } b \text{ begin } S \text{ end}, sto \rangle \to sto'}$$

if env_V , $sto \vdash b \rightarrow_b true$

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[IF-FALSE]
                                      env_V, env_P \vdash \langle \text{if } b \text{ begin } S \text{ end}, sto \rangle \rightarrow sto
                                                     if env_V, sto \vdash b \rightarrow_b false
                                        \frac{env_V, env_P \vdash \langle S_1, sto \rangle \to sto'}{env_V, env_P \vdash \langle \text{if } b \text{ begin } S_1 \text{ end else begin } S_2 \text{ end, } sto \rangle \to sto'}
[IF-ELSE-TRUE]
                                                    if env_V, sto \vdash b \rightarrow_b true
                                       \frac{env_V, env_P \vdash \langle S_2, sto \rangle \to sto'}{env_V, env_P \vdash \langle \text{if } b \text{ begin } S_1 \text{ end else begin } S_2 \text{ end}, sto \rangle \to sto'}
[IF-ELSE-FALSE]
                                                    if env_V, sto \vdash b \rightarrow_b false
                                                         env_V, env_P \vdash \langle S, sto \rangle \rightarrow sto''
                                       \frac{env_V, env_P \vdash \langle \text{while } b \text{ begin } S \text{ end}, sto'' \rangle \rightarrow sto'}{env_V, env_P \vdash \langle \text{while } b \text{ begin } S \text{ end}, sto \rangle \rightarrow sto'}
[WHILE-TRUE]
                                                     if env_V, sto \vdash b \rightarrow_b true
[WHILE-FALSE]
                                       env_V, env_P \vdash \langle \text{while } b \text{ begin } S \text{ end}, sto \rangle \rightarrow sto
                                                    if env_V, sto \vdash b \rightarrow_b false
                                                                       env_V, env_P \vdash \langle S, sto[l \vdash v_1] \rangle \rightarrow sto''
                                                \langle \text{from } x < --a_1 + a_3 \text{ to } a_2 \text{ step } a_3 \text{ begin } S \text{ end}, sto'' \to sto'
[FROM-TRUE]
                                        env_V, env_P \vdash \langle \text{from } x < --a_1 \text{ to } a_2 \text{ step } a_3 \text{ begin } S \text{ end}, sto \rangle \rightarrow sto'
                                                     where env_V, sto \vdash a_1 \rightarrow_a v_1
                                                     and env_V, sto \vdash a_2 \rightarrow_a v_2
                                                     and env_V, sto \vdash a_3 \rightarrow_a v_3
                                                     and v_1 \leq v_2
                                                     and l = env_V x
[FROM-FALSE]
                                       env_V, env_P \vdash \langle \text{from } x < --a_1 \text{ to } a_2 \text{ step } a_3 \text{ begin } S \text{ end}, sto \rangle \rightarrow sto
                                                     where env_V, sto \vdash a_1 \rightarrow_a v_1
                                                     and env_V, sto \vdash a_2 \rightarrow_a v_2
                                                     and env_V, sto \vdash a_3 \rightarrow_a v_3
                                                     and v_1 > v_2
                                       FiXme Fatal: Disse 3 herunder skal ligges ned!!
                                                                                            env_V, env_P \vdash \langle S, sto \rangle \rightarrow (sto')
[SWITCH-1]
                                        env_V, env_P \vdash \langle \text{switch}(a) \text{ begin case } a_1 : S_1 \text{ break}; \text{ default} : S \text{ break}; \text{ end}, sto \rangle \rightarrow sto'
                                                     Where k > 0
                                                     and env_V, sto \vdash a \rightarrow_a v
                                                     and env_V, sto \vdash a_1 \rightarrow_a v_1
                                                     and v \neq v_1
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\frac{env_V, env_P \vdash \langle S_1, sto \rangle \rightarrow sto'}{env_V, env_P \vdash \langle \text{switch}(a) \text{ begin case } a_1 : S_1 \text{ break}; \dots \text{ case } a_k : S_k \text{ break}; \text{ default } :
[SWITCH-2]
                                                    Where k > 1
                                                    and env_V, sto \vdash a \rightarrow_a v
                                                    and env_V, sto \vdash a_1 \rightarrow_a v_1
                                                    and v = v_1
                                       env_V, env_P \vdash \langle \text{switch}(a) \text{ begin case } a_2 : S_2 \text{ break}; \dots \text{ case } a_k : S_k \text{ break}; \text{ default } :
[SWITCH-3]
                                       env_V, env_P \vdash \langle \text{switch}(a) \text{ begin case } a_1 : S_1 \text{ break}; \dots \text{ case } a_k : S_k \text{ break}; \text{ default } :
                                                    Where k > 1
                                                    and env_V, sto \vdash a \rightarrow_a v
                                                    and env_V, sto \vdash a_1 \rightarrow_a v_1
                                                    and v \neq v_1
                                       \frac{env'_V[\vec{z} \mapsto \vec{l}], env'_P \vdash \langle S, sto[\vec{l} \mapsto \vec{v}] \rangle \to sto'}{env_V, env_P \vdash \langle \text{call } p(\vec{a}), sto \rangle \to sto'}
[CALL]
                                                    where env_P p = (S, \vec{z}, env'_V, env'_P)
                                                    and |\vec{a}| = |\vec{z}|
                                                    and env_V, sto \vdash a_i \rightarrow v_i for each 1 \leq i \leq |\vec{a}|
                                                    and l_1 = env_V new
                                                    and l_{i+1} = l_i for each 1 < i < |\vec{a}|
                                                   \langle D_V, env_V, sto \rangle \rightarrow_{DV} (env_V', sto'')
                                                      env'_V \vdash \langle D_P, env_P \rangle \rightarrow_{DP} env'_P

env'_V, env'_P \vdash \langle S, sto'' \rangle \rightarrow sto'
[BLOCK]
                                       env_V, env_P \vdash \langle \text{begin } D_V D_P S \text{ end}, sto \rangle \rightarrow sto'
                                                                                                    Table 1.1: Statements
                                                Transitioner er på formen: env_V, sto \vdash a \rightarrow_a v
                            [NUM]
                                                env_V, sto \vdash n \rightarrow_a v
                                                            if \mathcal{N}[[n]] = v
                            [VAR]
                                                env_V, sto \vdash x \rightarrow_a v
                                                             if env_V x = l
                                                             and sto l = v
                                                \frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 + a_2 \rightarrow_a v}
                            [ADD]
                                                             where v = v_1 + v_2
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$$[SUB] \qquad \frac{env_{V}, sto \vdash a_{1} \rightarrow_{a} v_{1} \quad env_{V}, sto \vdash a_{2} \rightarrow_{a} v_{2}}{env_{V}, sto \vdash a_{1} - a_{2} \rightarrow_{a} v}$$

$$\text{where } v = v_{1} - v_{2}$$

$$[MULT] \qquad \frac{env_{V}, sto \vdash a_{1} \rightarrow_{a} v_{1} \quad env_{V}, sto \vdash a_{2} \rightarrow_{a} v_{2}}{env_{V}, sto \vdash a_{1} \cdot a_{2} \rightarrow_{a} v}$$

$$\text{where } v = v_{1} \cdot v_{2}$$

$$[DIV] \qquad \frac{env_{V}, sto \vdash a_{1} \rightarrow_{a} v_{1} \quad env_{V}, sto \vdash a_{2} \rightarrow_{a} v_{2}}{env_{V}, sto \vdash a_{1} / a_{2} \rightarrow_{a} v}$$

$$\text{where } v = v_{1} / v_{2}$$

$$[PAR] \qquad \frac{env_{V}, sto \vdash a_{1} \rightarrow_{a} v_{1}}{env_{V}, sto \vdash (a_{1}) \rightarrow_{a} v_{1}}$$

$$[ARR] \qquad env_{V}, sto \vdash r[a_{1}] \rightarrow_{a} a_{2}$$

$$\text{where } env_{V}, sto \vdash a_{1} \rightarrow_{a} v_{1}$$

$$\text{and } env_{V}, sto \vdash a_{2} \rightarrow_{a} v_{2}$$

$$\text{and } env_{V}, sto \vdash a_{3} \rightarrow_{a} v_{2}$$

$$\text{and } sto l = v_{3}$$

$$\text{and } 0 < v_{1} \leq v_{3}$$

$$\text{and } sto (l + v_{1}) = v_{2}$$

Table 1.2: Arithmetic expressions

Transitioner på formen: env_V , $sto \vdash b \rightarrow_b t$ $env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2$ [EQUAL-TRUE] $env_V, sto \vdash a_1 = a_2 \rightarrow_b true$ if $v_1 = v_2$ $env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2$ [EQUAL-FALSE] $env_V, sto \vdash a_1 = a_2 \rightarrow_b \text{ false}$ if $v_1 \neq v_2$ $env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2$ [GRT-TRUE] $env_V, sto \vdash a_1 > a_2 \rightarrow_b true$ if $v_1 > v_2$ $\frac{env_V, sto \vdash a_1 \rightarrow_a v_1 \quad env_V, sto \vdash a_2 \rightarrow_a v_2}{env_V, sto \vdash a_1 > a_2 \rightarrow_b \text{ false}}$ [GRT-FALSE] Continued on the next page

$$[LESS-TRUE] \qquad \frac{env_{V}, sto \vdash a_{1} \rightarrow_{a} v_{1} \quad env_{V}, sto \vdash a_{2} \rightarrow_{a} v_{2}}{env_{V}, sto \vdash a_{1} \rightarrow_{a} v_{1} \quad env_{V}, sto \vdash a_{2} \rightarrow_{a} v_{2}}$$

$$env_{V}, sto \vdash a_{1} \rightarrow_{a} v_{1} \quad env_{V}, sto \vdash a_{2} \rightarrow_{a} v_{2}}$$

$$env_{V}, sto \vdash a_{1} \rightarrow_{a} v_{1} \quad env_{V}, sto \vdash a_{2} \rightarrow_{a} v_{2}}$$

$$env_{V}, sto \vdash a_{1} < a_{2} \rightarrow_{b} \text{ false}}$$

$$if \ v_{1} \not< v_{2}$$

$$[NOT-1] \qquad \frac{env_{V}, sto \vdash b \rightarrow_{b} \text{ true}}{env_{V}, sto \vdash !b \rightarrow_{b} \text{ false}}$$

$$[NOT-2] \qquad \frac{env_{V}, sto \vdash b \rightarrow_{b} \text{ true}}{env_{V}, sto \vdash !b \rightarrow_{b} \text{ false}}$$

$$[AND-TRUE] \qquad \frac{env_{V}, sto \vdash b_{1} \rightarrow_{b} \text{ true}}{env_{V}, sto \vdash b_{1} \wedge b_{2} \rightarrow_{b} \text{ true}}$$

$$env_{V}, sto \vdash b_{1} \rightarrow_{b} \text{ false}}$$

$$env_{V}, sto \vdash b_{1} \wedge b_{2} \rightarrow_{b} \text{ false}}$$

$$where \ i \in 1, 2$$

$$[OR-TRUE] \qquad \frac{env_{V}, sto \vdash b_{1} \rightarrow_{b} \text{ true}}{env_{V}, sto \vdash b_{1} \vee b_{2} \rightarrow_{b} \text{ true}}$$

$$env_{V}, sto \vdash b_{1} \rightarrow_{b} \text{ false}}$$

$$env_{V},$$

Table 1.3: Boolean expressions

[PAR-BOOL]

Transitioner på formen: $\langle D_V, env_V, sto \rangle \rightarrow_{DV} (env_V', sto')$ $\frac{\langle D_V, env_V'', sto[l \mapsto v] \rangle \to_{DV} (env_V', sto')}{\text{var } x < --a; D_V, env_V, sto\rangle \to_{DV} (env_V', sto')}$ [VAR-DEC] where env_V , $sto \vdash a \rightarrow_a v$ and $l = env_V$ next and $env_V'' = env_V[x \mapsto l][\text{next} \mapsto \text{new } l]$ [EMPTY-VAR] $\langle \varepsilon, env_V, sto \rangle \rightarrow_{DV} (env_V, sto)$ Continued on the next page

Transitioner på formen: $env_V \vdash \langle D_P, env_P \rangle \rightarrow_{DP} env_P'$

$$[\text{FUNC-DEC}] \qquad \frac{env_V \vdash \langle D_P, env_P[p \mapsto (S, env_V, env_P)] \rangle \rightarrow_{DP} env_P'}{env_V \vdash \langle \text{proc } p \text{ is } S; D_P, env_P \rangle \rightarrow_{DP} env_P'}$$

[EMPTY-FUNC]
$$env_V \vdash \langle \varepsilon, env_P \rangle \rightarrow_{DP} env_P'$$

Transitioner på formen: $\langle D_A, env_V, sto \rangle \rightarrow_{DA} (env_V', sto')$

[ARRAY-DEC]
$$\frac{\langle D_A, env_V[r \mapsto l, \text{next} \mapsto l + v + 1], sto[l \mapsto v] \rangle \rightarrow_{DA} (env_V', sto')}{\langle r[a_1], D_A, env_V, sto \rangle \rightarrow_{DA} (env_V', sto')}$$

where $env_V, sto \vdash a_1 \rightarrow_a v$ and $l = env_V$ next and l > 0

[EMPTY-ARRAY] $\langle \varepsilon, env_V, sto \rangle \rightarrow_{DA} (env_V, sto)$

Table 1.4: Declarations