

$$\begin{aligned}
\langle \textit{program} \rangle &\rightarrow \langle \textit{roots} \rangle \\
\langle \textit{roots} \rangle &\rightarrow \langle \textit{root} \rangle \\
&\quad | \quad \langle \textit{root} \rangle \langle \textit{roots} \rangle \\
\langle \textit{root} \rangle &\rightarrow \langle \textit{function} \rangle \\
&\quad | \quad \langle \textit{dcl} \rangle; \\
\langle \textit{dcl} \rangle &\rightarrow \langle \textit{type} \rangle \langle \textit{id} \rangle \\
&\quad | \quad \langle \textit{type} \rangle \langle \textit{assign} \rangle \\
\langle \textit{id} \rangle &\rightarrow \langle \textit{letter} \rangle \\
&\quad | \quad \langle \textit{id} \rangle \langle \textit{letter} \rangle \\
&\quad | \quad \langle \textit{id} \rangle \langle \textit{digit} \rangle \\
\langle \textit{letter} \rangle &\rightarrow [\text{a-z}] \\
&\quad | \quad [\text{A-Z}] \\
\langle \textit{digit} \rangle &\rightarrow [0-9] \\
\langle \textit{assign} \rangle &\rightarrow \langle \textit{id} \rangle \leftarrow \langle \textit{expr} \rangle \\
\langle \textit{type} \rangle &\rightarrow \langle \textit{primitive-type} \rangle \\
&\quad | \quad \langle \textit{array-type} \rangle \\
\langle \textit{primitive-type} \rangle &\rightarrow \text{bool} \\
&\quad | \quad \text{double} \\
&\quad | \quad \text{int} \\
&\quad | \quad \text{char} \\
\langle \textit{array-type} \rangle &\rightarrow \langle \textit{type} \rangle [ ] \\
&\quad | \quad \text{string} \\
\langle \textit{function} \rangle &\rightarrow \text{function } \langle \textit{id} \rangle \text{ returns } \langle \textit{type} \rangle \text{ using } (\langle \textit{params} \rangle) \text{ begin } \langle \textit{stmts} \rangle \text{ return } \\
&\quad \langle \textit{expr} \rangle; \text{ end} \\
&\quad | \quad \text{function } \langle \textit{id} \rangle \text{ returns nothing using } (\langle \textit{params} \rangle) \text{ begin } \langle \textit{stmts} \rangle \text{ return nothing; end} \\
\langle \textit{params} \rangle &\rightarrow \langle \textit{subparams} \rangle \\
&\quad | \quad \varepsilon \\
\langle \textit{subparams} \rangle &\rightarrow \langle \textit{type} \rangle \langle \textit{id} \rangle, \langle \textit{subparams} \rangle \\
&\quad | \quad \langle \textit{type} \rangle \langle \textit{id} \rangle \\
\langle \textit{stmts} \rangle &\rightarrow \langle \textit{stmt} \rangle \\
&\quad | \quad \langle \textit{stmt} \rangle \langle \textit{stmts} \rangle
\end{aligned}$$

$$\begin{aligned}
\langle stmt \rangle &\rightarrow \langle assign \rangle; \\
&| \langle if \rangle \\
&| \langle while \rangle \\
&| \langle from \rangle \\
&| \varepsilon \\
&| \langle dcl \rangle; \\
&| \langle functioncall \rangle; \\
&| \langle switch \rangle \\
\\
\langle expr \rangle &\rightarrow \langle expr \rangle + \langle term \rangle \\
&| \langle expr \rangle - \langle term \rangle \\
&| \langle term \rangle \\
\\
\langle term \rangle &\rightarrow \langle term \rangle * \langle factor \rangle \\
&| \langle term \rangle / \langle factor \rangle \\
&| \langle factor \rangle \\
\\
\langle factor \rangle &\rightarrow ( \langle expr \rangle ) \\
&| \langle id \rangle \\
&| \langle digit \rangle \\
&| " \langle string \rangle " \\
\\
\langle string \rangle &\rightarrow \langle letter \rangle \\
&| \langle digit \rangle \\
&| \langle digit \rangle \langle string \rangle \\
&| \langle letter \rangle \langle string \rangle \\
&| \varepsilon \\
\\
\langle switch \rangle &\rightarrow \text{switch } ( \langle expr \rangle ) \text{ begin } \langle cases \rangle \text{ end} \\
\\
\langle cases \rangle &\rightarrow \text{case } \langle expr \rangle : \langle stmts \rangle \langle endcase \rangle \\
\\
\langle endcase \rangle &\rightarrow \langle cases \rangle \\
&| \text{break;} \\
&| \text{break;} \langle cases \rangle \\
&| \text{default: } \langle stmts \rangle \text{ break;} \\
&| \text{break; default: } \langle stmts \rangle \text{ break;} \\
\\
\langle from \rangle &\rightarrow \text{from } \langle expr \rangle \text{ to } \langle logexpr \rangle \text{ step } \langle expr \rangle \text{ begin } \langle stmts \rangle \text{ end} \\
\\
\langle while \rangle &\rightarrow \text{while } ( \langle logexpr \rangle ) \text{ begin } \langle stmts \rangle \text{ end} \\
\\
\langle if \rangle &\rightarrow \text{if } ( \langle logexpr \rangle ) \text{ begin } \langle stmts \rangle \langle endif \rangle \\
\\
\langle endif \rangle &\rightarrow \text{end else } \langle if \rangle \\
&| \text{end else begin } \langle stmts \rangle \text{ end} \\
&| \text{end}
\end{aligned}$$

$$\langle \textit{logexpr} \rangle \rightarrow \langle \textit{logexpr} \rangle \text{ OR } \langle \textit{andcomp} \rangle$$

$$\quad | \quad \langle \textit{andcomp} \rangle$$

$$\langle \textit{andcomp} \rangle \rightarrow \langle \textit{andcomp} \rangle \text{ AND } \langle \textit{comp} \rangle$$

$$\quad | \quad \langle \textit{comp} \rangle$$

$$\langle \textit{comp} \rangle \rightarrow \langle \textit{boolean-operand} \rangle \langle \textit{comparison-operator} \rangle \langle \textit{boolean-operand} \rangle$$

$$\langle \textit{boolean-operand} \rangle \rightarrow \text{true}$$

$$\quad | \quad \text{false}$$

$$\quad | \quad \langle \textit{expr} \rangle$$

$$\quad | \quad \langle \textit{boolean} \rangle$$

$$\langle \textit{boolean} \rangle \rightarrow \neg(\langle \textit{logexpr} \rangle)$$

$$\quad | \quad (\langle \textit{logexpr} \rangle)$$

$$\langle \textit{comparison-operator} \rangle \rightarrow >$$

$$\quad | \quad <$$

$$\quad | \quad <=$$

$$\quad | \quad >=$$

$$\quad | \quad !=$$

$$\quad | \quad =$$

$$\langle \textit{functioncall} \rangle \rightarrow \text{call } \langle \textit{id} \rangle(\langle \textit{params} \rangle)$$