Exercise 4 12.10.2021

#1 Risk measures

Let us revisit the three investment opportunities A1, A2, and A3 from Problem #3 of Exercise 3. The probability distributions of the investment opportunities are re-represented below. Compute VaR-10% and CVaR-10% for all three alternatives. How do the results reflect the ones that were obtained in Exercise 3?

Probability	0.05	0.05	0.1	0.2	0.3	0.15	0.1	0.05
A1	1	1.5	2	2.5	4	6	7	7.5
A2	1.5	3	4	4.5	6	9	9.5	10
А3	5	5.5	6	6.5	7	8	9	10

#2 Risk measures with Matlab

The DM is considering 10 different investment opportunities A1-A10. Their monetary outcomes follow probability distributions as follows:

A1	UNI(80,120)	A6	$LogN(4.5,0.9^2)$
A2	UNI(65,140)	A7	Exp(100)
А3	$N(120,40^2)$	A8	Exp(125)
A4	$N(100,15^2)$	A9	Weib(105,2)
A5	$LogN(4.8,0.7^2)$	A10	Weib(130,3)

Some of the probability distribution functions are coded into variables pd1, ..., pd10 in the "exercise4task2template" -file.

- a) Fill in the missing code for variables pd2, pd4, pd6, pd8 and pd10.
- b) Plot the PDFs of A2, A3, A6 and A7 between 0 and 200 in a single figure.
- c) Using Monte Carlo simulation with 5000 samples, compute the expected value, 1% VaR, 5% VaR, 10% VaR, 1% CVaR, 5% CVaR and 10% CVaR for each investment opportunity.
- d) Visualize the results of task c) for all 10 investment opportunities on a figure of 6 scatter plots with expected value on the horizontal and a risk measure on the vertical axis. Label the points A1-A10.
- e) Based on the figure, which investment opportunities seem better than others and why?
- f) The below figure illustrates the investment opportunities' CVaR for all $\alpha \in \{1\%, 2\%, ..., 100\%\}$ Which investment opportunities could not be selected by a risk averse DM? Why?
- g) In the template, fill in the code which creates the given figure.
- h) Plot the CDFs of A5 and A7 between 0 and 500 in a single figure.

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