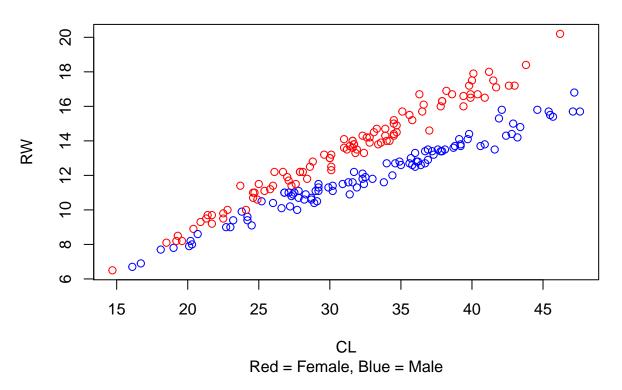
# Lab2

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### Assignment 1

#### Task 1

## Plot of carapace length versus rear width depending on sex

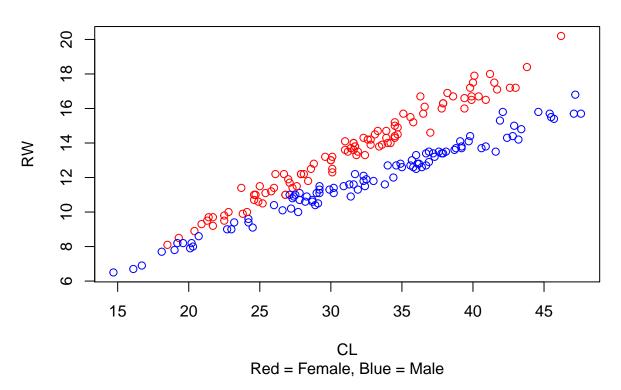


As we can see in the graph it looks like it would be suitable to classify this data using linear discriminative analysis since the pattern of both the red and blue is linear.

```
#Create function for misclassification rate
missclass=function(conf_matrix, fit_matrix){
   n=length(fit_matrix[,1])
```

```
return(1-sum(diag(conf_matrix))/n)
}
#LDA analysis with target Sex, and features CL and RW and proportional prior
library("MASS")
model = lda(sex ~ CL+RW, data=Dataframe)
predicted = predict(model, data=Dataframe)
confusion_matrix = table(Dataframe$sex, predicted$class)
misclass = missclass(confusion_matrix, Dataframe)
print(confusion_matrix)
##
##
            Female Male
##
     Female
                97
                      3
##
                     96
     Male
print(misclass)
## [1] 0.035
plot(CL, RW, main="Plot values of CL and RW depending on predicted sex",
     sub="Red = Female, Blue = Male",
     col=c("red", "blue")[predicted$class], xlab="CL", ylab="RW")
```

## Plot values of CL and RW depending on predicted sex



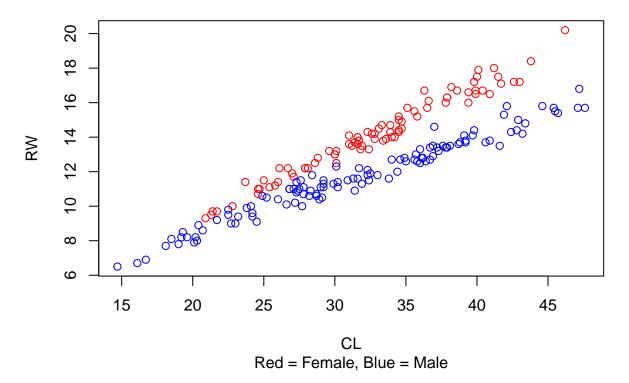
When comparing the graph from step 1 and the graph of the predicted values it is notable that the classifications do not differ that much. With a misclassification rate of only 0.035 and 200 datapoints it can be concluded that 7 observations were classified inaccurately. When comparing the graphs it is difficult to find the points

which have changed color (since they have been classified incorrectly) but one example is the point farthest to the left which was classified as *male* but should have been classified as *female*. The model classifies the data very accurately.

#### Task 3

```
#Repeat step 2 but use priors p(Male)=0.9 and p(Female)=0.1
model2 = lda(sex ~ CL+RW, data=Dataframe, prior=c(1,9)/10)
predicted2 = predict(model2, data=Dataframe)
confusion_matrix2 = table(Dataframe$sex, predicted2$class)
misclass2 = missclass(confusion_matrix2, Dataframe)
print(confusion matrix2)
##
##
            Female Male
##
     Female
                84
                     16
     Male
                 0 100
print(misclass2)
## [1] 0.08
plot(CL, RW, main="Predicted values of CL and RW with priors 0.9 (male) 0.1 (female)"
     , sub="Red = Female, Blue = Male", col=c("red", "blue")[predicted2$class], xlab="CL",
     ylab="RW")
```

## Predicted values of CL and RW with priors 0.9 (male) 0.1 (female)

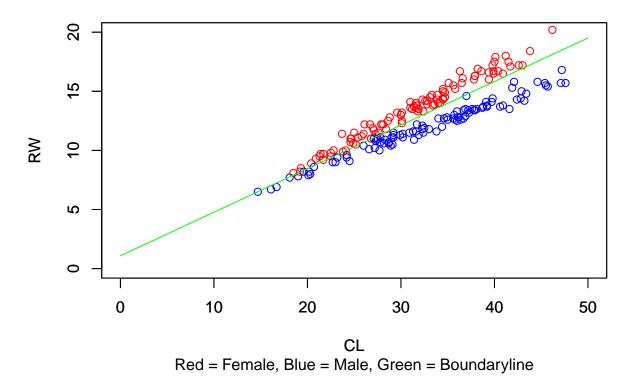


From this graph we can see that a few more data points were classified incorrectly. This is due to the higher prior set on classifying a data point as male, i.e. 0.9. It is noteable in the confusion matrix that no males

were classified incorrectly. This is also due to the high prior which basically says that it is not that likely that a datapoint will be classified as a female. When the model in fact classify a data point as female it has to be sure of it (since the low prior) and this can be seen as stated above in the confusion matrix. On the other hand, more females are classified as males inaccurately since the higher prior. This also results in a higher misclassification rate of 0.08.

```
#Repeat step 2 but now with logistic regression
model3 = glm(sex ~ CL+RW, data=Dataframe, family='binomial')
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
predicted3 = predict(model3, newdata=Dataframe, type='response')
sexvector = c()
for (i in predicted3) {
  if (i>0.5) {
    sexvector = c(sexvector, 'Male')
 } else {
    sexvector = c(sexvector, 'Female')
  }
}
sexvector_factor = as.factor(sexvector)
confusion_matrix3 = table(Dataframe$sex, sexvector_factor)
misclass3 = missclass(confusion_matrix3, Dataframe)
print(confusion_matrix3)
##
           sexvector_factor
##
            Female Male
##
    Female
                97
                      3
##
    Male
                 4
                     96
print(misclass3)
## [1] 0.035
plot(CL, RW, main="Predicted values of CL and RW but with logistic regression",
     col=c("red", "blue")[sexvector_factor], xlab="CL", ylab="RW", xlim=c(0,50),
     ylim=c(0,20))
boundaryline = function(length, coefficientvector, prior) {
  return(-coefficientvector[1]/coefficientvector[3]-
           (coefficientvector[2]/coefficientvector[3])*length+
           log(prior/(1-prior))/coefficientvector[3])
}
par(new=TRUE)
curve(boundaryline(x, model3$coefficients, 0.5), xlab="CL", ylab="RW", col="green",
      from=0, to=50, xlim=c(0,50), ylim=c(0,20),
      sub="Red = Female, Blue = Male, Green = Boundaryline")
```

## Predicted values of CL and RW but with logistic regression



When using logistic regression the results are similar as the first built model with LDA. This is simply a coincident and no real conclusion can be drawn regarding the exact same misclassification rate except from that the models seem to classify the data in the same way. When comparing which data points that are classified as females and males in the two models it can be concluded that the model using logistic regression classifies the data in a way which enables a boundary line more distinctly. This is due to the characteristics of the logistic regression model. The equation for the decision boundary is as follows:

$$\hat{RW} = -(\beta_0 + \beta_1)/\beta_2 * CL$$

### Assignment 2

```
#1: Read data and divide into train, validation and test sets

library("tree")

data=read.csv2("creditscoring.csv")
n=dim(data)[1]
set.seed(12345)
id=sample(1:n, floor(n*0.5))
train=data[id,]
id1=setdiff(1:n, id)
set.seed(12345)
id2=sample(id1, floor(n*0.25))
valid=data[id2,]
id3=setdiff(id1,id2)
```

```
#Create function for misclassification rate
misclass=function(conf_matrix, fit_matrix){
  n=length(fit_matrix[,1])
  return(1-sum(diag(conf_matrix))/n)
}
```

The data is divided into 50 % training data, 25 % validation data and 25 % test data.

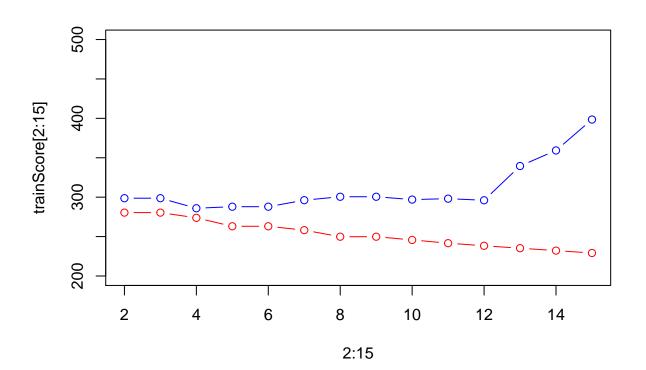
#### Task 2

```
#2: Fit a decision tree to train data using the measures of impurity gini and deviance.
#Report misclass rates and choose optimal measure moving forward.
fit_deviance=tree(good_bad~., data=train, split="deviance")
predicted deviance=predict(fit deviance, newdata=test, type="class")
confusionmatrix_deviance=table(test$good_bad, predicted_deviance)
misclass_deviance=misclass(confusionmatrix_deviance, test)
print(confusionmatrix_deviance)
##
         predicted_deviance
##
          bad good
##
           28
                48
     bad
##
     good
          19
              155
print(misclass_deviance)
## [1] 0.268
fit_gini=tree(good_bad~., data=train, split="gini")
predicted_gini=predict(fit_gini, newdata=test, type="class")
confusionmatrix_gini=table(test$good_bad, predicted_gini)
misclass_gini=misclass(confusionmatrix_gini, test)
print(confusionmatrix_gini)
##
         predicted_gini
##
          bad good
##
           18
                58
     bad
     good 34 140
print(misclass_gini)
## [1] 0.368
#Deviance has best misclass score
```

It can be concluded from the misclassification rates that the split method deviance, classifies the data in a better way than the split method gini. Since the method deviance performed better it will be the choses splitting method in the following steps.

```
#3: Use training and valid data to choose optimal tree depth. Present graphs of the #dependence of deviances for training and validation data on the number of leaves. #Report optimal tree, report it's depth and variables used bytree. Estimate #misclassification rate for the test data.
```

```
fit_optimaltree=tree(good_bad~., data=train, split="deviance")
summary(fit_optimaltree)
##
## Classification tree:
## tree(formula = good_bad ~ ., data = train, split = "deviance")
## Variables actually used in tree construction:
## [1] "savings" "duration" "history" "age"
                                                   "purpose"
                                                              "amount"
                                                                          "resident"
## [8] "other"
## Number of terminal nodes: 15
## Residual mean deviance: 0.9569 = 458.3 / 479
## Misclassification error rate: 0.2105 = 104 / 494
trainScore=rep(0,15)
testScore=rep(0,15)
for(i in 2:15){
  prunedTree=prune.tree(fit_optimaltree, best=i)
  pred=predict(prunedTree, newdata=valid, type="tree")
  #Divide by two since double of data points
  trainScore[i] = deviance(prunedTree)/2
  testScore[i] = deviance(pred)
}
plot(2:15, trainScore[2:15], type="b", col="red", ylim=c(200,500))
points(2:15, testScore[2:15], type="b", col="blue")
```



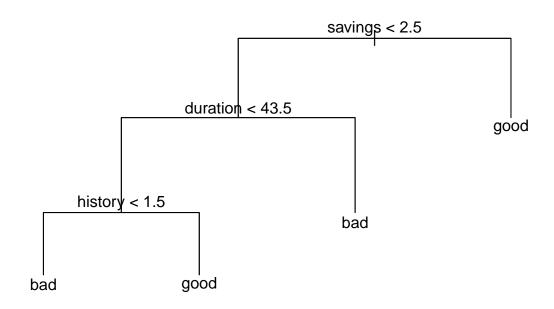
```
min_deviance=min(testScore[2:15])
print(min_deviance)

## [1] 285.9425

optimal_leaves=which(testScore[1:15] == min_deviance)
print(optimal_leaves)

## [1] 4

#*Optimal no of leaves is 4
finalTree=prune.tree(fit_optimaltree, best=4)
plot(finalTree)
text(finalTree, pretty=0)
```



```
#Final tree contains variables savings, duration and history. Since 3 vars => Depth of
#tree is 3.
predicted_test=predict(finalTree, newdata=test, type="class")
confusionmatrix_test=table(test$good_bad, predicted_test)
misclass_test=misclass(confusionmatrix_test, test)
print(confusionmatrix_test)
##
         predicted_test
##
          bad good
          18
##
     bad
              58
##
     good 6 168
```

```
print(misclass_test)
```

```
## [1] 0.256
```

The tree with the lowest deviance used 4 leaves which is the optimal tree. The variables used by the tree is savings, duration and history, and the depth of the tree is 3. As we can see from the tree the classification checks the feature saving first and if the feature is above or equal to 2.5, the customer will be classified as good. Otherwise the model moves down in the tree to check for duration. If duration is above or equal to 43.5, the customer will be classified as bad, otherwise the model moves even further down in the tree. Finally, if history is above or equal to 1.5 the customer will be classified as good, otherwise the customer will be classified as bad. The misclassification rate for the test data is 0.256.

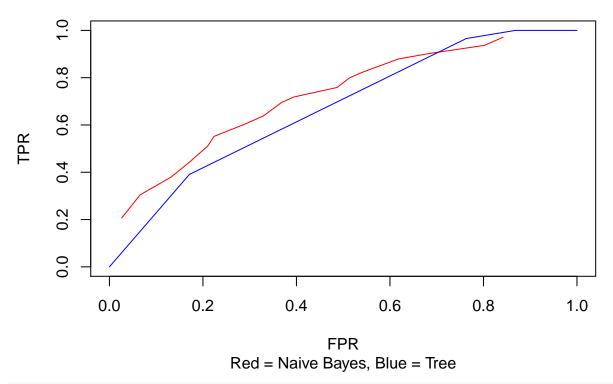
#### Task 4

```
#4: Use traning data to perform classification using Naives bayes and report the confusion
#matrices and misclassification rates for the traning and for the test data. Compare with
#results from previous steps.
#Load libraries
library(MASS)
library(e1071)
fit_naive=naiveBayes(good_bad~., data=train)
#Create function for predicting and creating confusion matrice and printing
#misclassification rate
compute_naive=function(model,data){
  predictedNaive=predict(model, newdata=data, type="class")
  confusionmatrixNaive=table(data$good_bad,predictedNaive)
  misclass = misclass(confusionmatrixNaive, data)
  print(confusionmatrixNaive)
  print(misclass)
  return(predictedNaive)
predictedNaive_train=compute_naive(fit_naive,train)
##
         predictedNaive
##
          bad good
##
           95
                52
     bad
##
     good
           98
               255
  [1] 0.3
predictedNaive_test=compute_naive(fit_naive, test)
##
         predictedNaive
##
          bad good
##
     bad
           46
                30
     good 49
               125
##
## [1] 0.316
```

With the Naïve Bayes method the misclassification rate is higher than what was concluded in step 3 (using decision trees). The misclassification rate for test data for the Naïve Bayes method is 0.316 and the misclassification rate for the decision tree method from step 3 is 0.256. This indicates that the decision tree method classifies the data more accurately than what the model which uses the Naïve Bayes method does.

```
#5: Use optimal tree and Naives Bayes to classify the test data by using principle:
#classified as 1 if bigger than 0.05, 0.1, 0.15, ..., 0.9, 0.95. Compute the TPR
#and FPR for two models and plot corresponsing ROC curves.
#Writing function for classifying data
class=function(data, class1, class2, prior){
  vector=c()
  for(i in data) {
    if(i>prior){
      vector=c(vector,class1)
    } else {
      vector=c(vector,class2)
    }
  }
  return(vector)
x \text{ vector} = seq(0.05, 0.95, 0.05)
tpr_tree=c()
fpr_tree=c()
tpr_naive=c()
fpr_naive=c()
treeVector=c()
treeConfusion = c()
naiveConfusion = c()
treeClass = c()
naiveClass = c()
#Reusing optimal tree found in task 3 but returntype is response instead
predictTree=data.frame(predict(finalTree, newdata=test, type="vector"))
predictNaive=data.frame(predict(fit_naive, newdata=test, type="raw"))
for(prior in x vector){
  treeClass = class(predictTree$good, 'good', 'bad', prior)
  treeConfusion=table(test$good_bad, treeClass)
  if(ncol(treeConfusion)==1){
    if(colnames(treeConfusion)=="good"){
      treeConfusion=cbind(c(0,0), treeConfusion)
      treeConfusion=cbind(treeConfusion,c(0,0))
  totGood=sum(treeConfusion[2,])
  totBad=sum(treeConfusion[1,])
  tpr_tree=c(tpr_tree, treeConfusion[2,2]/totGood)
  fpr_tree=c(fpr_tree, treeConfusion[1,2]/totBad)
  naiveClass=class(predictNaive$good, 'good', 'bad', prior)
  naiveConfusion=table(test$good_bad, naiveClass)
  if(ncol(naiveConfusion)==1){
    if(colnames(naiveConfusion) == "good") {
      naiveConfusion=cbind(c(0,0), naiveConfusion)
      naiveConfusion=cbind(naiveConfusion,c(0,0))
```

## **ROC** curve



#Naive has greatest AOC => should choose Naive

From the ROC-curve we can see that the total area under the curve (AOC) is the biggest for the Naïve Bayes method. Therefore this method should be the one to use instead of the decision tree method.

```
#6: Repeate Naive Bayes with loss matrix punishing with factor 10 if predicting good when #bad and 1 if predicting bad when good.

naiveModel=naiveBayes(good_bad~., data=train)

train_loss=predict(naiveModel, newdata=train, type="raw")

test_loss=predict(naiveModel, newdata=test, type="raw")

confusion_trainLoss=table(train$good_bad, ifelse(train_loss[,2]/train_loss[,1]>10, "good", "bad"))

misclass_trainLoss=misclass(confusion_trainLoss, train)
```

```
print(confusion_trainLoss)
##
##
          bad good
##
     bad 137
                10
##
     good 263
                90
print(misclass_trainLoss)
## [1] 0.546
confusion_testLoss=table(test$good_bad, ifelse(test_loss[,2]/test_loss[,1]>10, "good",
                                                 "bad"))
misclass_testLoss=misclass(confusion_testLoss, test)
print(confusion testLoss)
##
##
          bad good
##
     bad
           71
                 5
     good 122
print(misclass_testLoss)
```

From the confusion matrices and the misclassification rates it is noteable that the misclassification rates have gone up. More datapoints are being classified incorrectly. However, this is due to the defined loss matrix which describes a bigger loss when classifying a customer as good when the customer in fact was bad. This can also be seen in the confusion matrices where there are few customers being classified as good incorrectly (from 52 to 10 in train data and from 30 to 5 in test data). When the model in fact classifies a customer as good it is more often correct than not. In comparison it is noteable that the model is more often wrong regarding the classification bad which is due to the defined loss when misclassifying a customer as bad which is less than when misclassifying a customer as good.

### Assignment 4

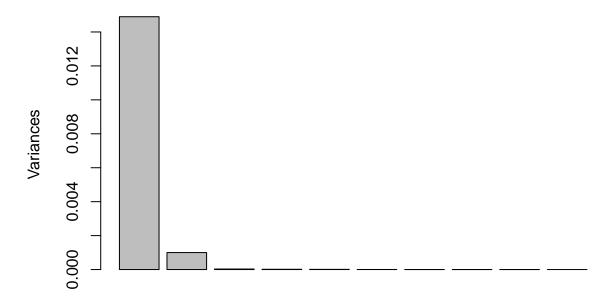
## [1] 0.508

```
#1: Read data

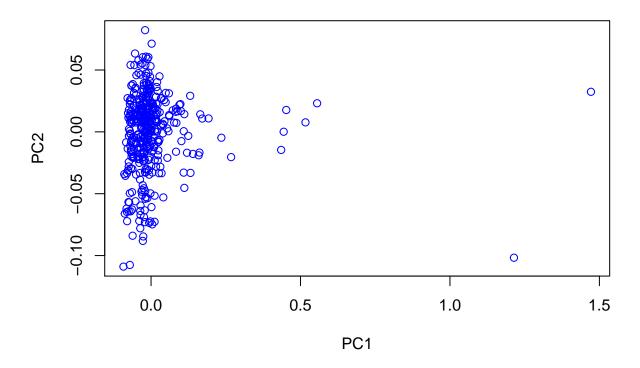
data=read.csv2("NIRspectra.csv")
data$Viscosity=c()
n=dim(data)[1]

#1: Conduct standard PCA using the feature space and provide a plot explaining how much
#variation is explained by each feature. Provide plot that show the scores of PC1 vs PC2.
#Are there unusual diesel fuels according to this plot.
pcaAnalysis=prcomp(data)
#Eigenvalues
lambda=pcaAnalysis$sdev^2
#Proportion of variation
propVar= lambda/sum(lambda)*100
screeplot(pcaAnalysis, main="Total variation from PCA components")
```

# **Total variation from PCA components**



## PC1 vs PC2



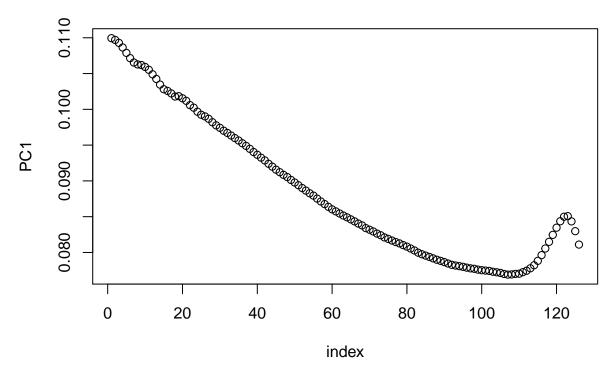
#We can see from the graph that the data is very accurately described by PC1.

From the screeplot it can be concluded that two components captures almost all of the variation in the data. Therefore a PCA analysis is suitable for the data. Two components captures 99.5957% of the variation and therefore these two components will be used in the following steps. Most of the data points is around 0 for PC1 but there are some data points which can be described as outliers located to the farthest right in the score plot.

```
#2: Make trace plots of the loadings of the components selected in step 1. Is there any #principle component that is explaines by mainly a few original features?

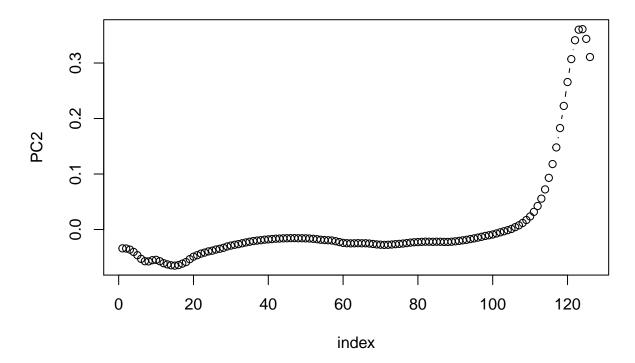
U=pcaAnalysis$rotation
plot(U[,1], main="Traceplot, PC1", xlab="index", ylab="PC1", type="b")
```

Traceplot, PC1



plot(U[,2], main="Traceplot, PC2", xlab="index", ylab="PC2", type="b")

## **Traceplot, PC2**



#We can see from graph that PC2 is not described by so many original features since it is #close to zero for many of the features. The last 30 or so variables have an effect on PC2.

As seen in the trace plots of the loadings of PC1 and PC2, it can be concluded that for PC2 many features have PC2-values close to 0 which means that these features do not contribute to explain the PC2 axis. On the other hand no features are close to 0 in the PC1 plot which means that all features contribute to explain the PC1 axis.

#### Task 3

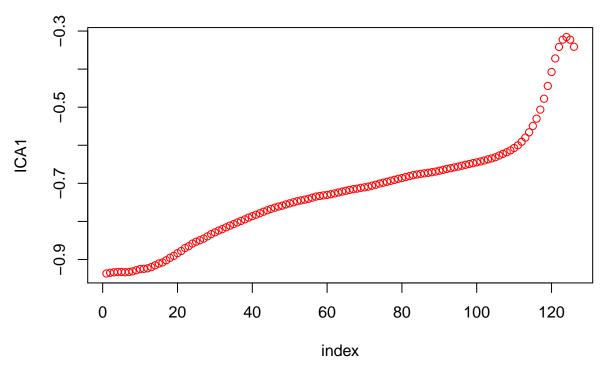
## Whitening

```
#3: Perform independent Component Analysis (ICA) with no of components selected in step1
#(set seed 12345). Check the documentation of R for fastICA method and do following:
# Compute W'=K*W and present columns of W' in form of the trace plots. Compare with trace
# plots in step 2 and make conclusions. What kind of measure is represented by the matrix W'.
# Make a plot of the scores of the first two latent features and compare it with the score
# plot from step 1.
#Install package fastICa
#install.packages("fastICA")
library("fastICA")

set.seed(12345)
icaModel = fastICA(data, n.comp=2, verbose=TRUE)
## Centering
```

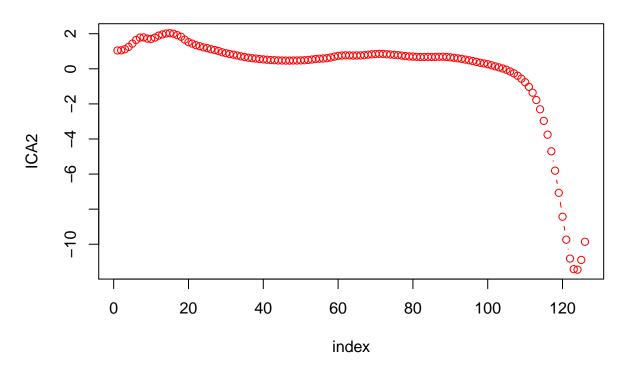
```
## Symmetric FastICA using logcosh approx. to neg-entropy function
## Iteration 1 tol = 0.01930239
## Iteration 2 tol = 0.01303959
## Iteration 3 tol = 0.002393582
## Iteration 4 tol = 0.0006708454
## Iteration 5 tol = 0.0001661602
## Iteration 6 tol = 3.521604e-05
W=icaModel$W
K=icaModel$K
W_est=K%**,W
plot(W_est[,1], main="Traceplot, ICA1", xlab="index", ylab="ICA1", type="b", col="red")
```

# Traceplot, ICA1

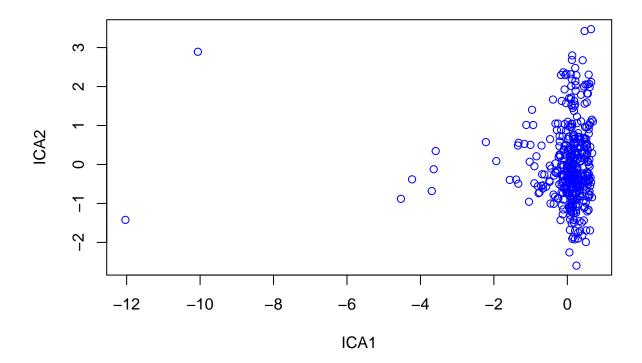


plot(W\_est[,2], main="Traceplot, ICA2", xlab="index", ylab="ICA2", type="b", col="red")

# **Traceplot, ICA2**



## ICA1 vs ICA2



#We can see from the plot that the dat is pretty well described by ICA2 whereas ICA1 is #not that significant in describing the data (since it is close to 0 most of the cases). #Some outliers are however described by ICA1.

When comparing the trace plots of ICA1 and ICA2 with PC1 and PC2 from step 2, it is noteable that for the first component the dependency on the features decreases as the index increases, whereas for the second component the dependency on the features increases as the index increases. It is also noteable that the plots for the different components appear to be each others mirrors. This is reasonable because PCA tries to maximize the variance, i.e. look for correlation between the different features, whereas ICA tries to do the exact opposite, i.e. maximizing the independence between the different features by creating an orthogonal coordinate system. The parameter W' which is computed by  $\hat{W} = K*W$  describes how the features explain the principal components ICA1 and ICA2.

When comparing the last score plot with the score plot from step 1 it can also be concluded that the score plot of ICA is mirroring the score plot of PCA. However, the axis of the coordinate system of ICA have been standardized which is the difference between the plots.

## Appendix

```
### Assignment 1
RNGversion('3.5.1')
Dataframe=read.csv("australian-crabs.csv")
n = length(Dataframe[,1])
CL = Dataframe$CL
RW = Dataframe$RW
plot(CL, RW, main="Plot of carapace length versus rear width depending on sex", sub="Red = Female, Blue
     col=c("red", "blue")[Dataframe$sex], xlab="CL", ylab="RW")
missclass=function(conf_matrix, fit_matrix){
  n=length(fit_matrix[,1])
  return(1-sum(diag(conf_matrix))/n)
}
library("MASS")
model = lda(sex ~ CL+RW, data=Dataframe)
predicted = predict(model, data=Dataframe)
confusion_matrix = table(Dataframe$sex, predicted$class)
misclass = missclass(confusion_matrix, Dataframe)
print(confusion_matrix)
print(misclass)
plot(CL, RW, main="Plot predicted values of CL and RW depending on sex", sub="Red = Female, Blue = Male
     col=c("red", "blue")[predicted$class], xlab="CL", ylab="RW")
model2 = lda(sex ~ CL+RW, data=Dataframe, prior=c(1,9)/10)
predicted2 = predict(model2, data=Dataframe)
confusion_matrix2 = table(Dataframe$sex, predicted2$class)
misclass2 = missclass(confusion_matrix2, Dataframe)
print(confusion_matrix2)
print(misclass2)
plot(CL, RW, main="Plot predicted values of CL and RW with priors p(Male)=0.9 and p(Female)=0.1"
     , sub="Red = Female, Blue = Male", col=c("red", "blue")[predicted2$class], xlab="CL", ylab="RW")
model3 = glm(sex ~ CL+RW, data=Dataframe, family='binomial')
predicted3 = predict(model3, newdata=Dataframe, type='response')
sexvector = c()
for (i in predicted3) {
  if (i>0.9) {
    sexvector = c(sexvector, 'Male')
  } else {
    sexvector = c(sexvector, 'Female')
}
print(sexvector)
sexvector_factor = as.factor(sexvector)
confusion_matrix3 = table(Dataframe$sex, sexvector_factor)
misclass3 = missclass(confusion matrix3, Dataframe)
print(confusion_matrix3)
print(misclass3)
plot(CL, RW, main="Plot predicted values of CL and RW but with logistic regression",
     col=c("red", "blue")[sexvector_factor], xlab="CL", ylab="RW", xlim=c(0,50), ylim=c(0,20))
```

```
boundaryline = function(length, coefficientvector, prior) {
  return(-coefficientvector[3]/coefficientvector[3])*length+
}
par(new=TRUE)
curve(boundaryline(x, model3$coefficients, 0.9), xlab="CL", ylab="RW", col="green", from=0, to=50, xlim
      sub="Red = Female, Blue = Male, Green = Boundaryline")
### Assignment 2
library("tree")
RNGversion('3.5.1')
data=read.csv2("creditscoring.csv")
n=dim(data)[1]
set.seed(12345)
id=sample(1:n, floor(n*0.5))
train=data[id,]
id1=setdiff(1:n, id)
set.seed(12345)
id2=sample(id1, floor(n*0.25))
valid=data[id2,]
id3=setdiff(id1,id2)
test=data[id3,]
misclass=function(conf_matrix, fit_matrix){
 n=length(fit_matrix[,1])
 return(1-sum(diag(conf_matrix))/n)
}
fit_deviance=tree(good_bad~., data=train, split="deviance")
predicted_deviance=predict(fit_deviance, newdata=test, type="class")
confusionmatrix_deviance=table(test$good_bad, predicted_deviance)
misclass_deviance=misclass(confusionmatrix_deviance, test)
print(confusionmatrix_deviance)
print(misclass_deviance)
fit_gini=tree(good_bad~., data=train, split="gini")
predicted_gini=predict(fit_gini, newdata=test, type="class")
confusionmatrix gini=table(test$good bad, predicted gini)
misclass_gini=misclass(confusionmatrix_gini, test)
print(confusionmatrix_gini)
print(misclass_gini)
fit_optimaltree=tree(good_bad~., data=train, split="deviance")
summary(fit_optimaltree)
trainScore=rep(0,15)
testScore=rep(0,15)
for(i in 2:15){
  prunedTree=prune.tree(fit_optimaltree, best=i)
  pred=predict(prunedTree, newdata=valid, type="tree")
  #Divide by two since double of data points
  trainScore[i]=deviance(prunedTree)/2
  testScore[i] = deviance(pred)
}
```

```
plot(2:15, trainScore[2:15], type="b", col="red", ylim=c(200,500))
points(2:15, testScore[2:15], type="b", col="blue")
min_deviance=min(testScore[2:15])
print(min_deviance)
optimal_leaves=which(testScore[1:15] == min_deviance)
print(optimal_leaves)
finalTree=prune.tree(fit_optimaltree, best=4)
summary(finalTree)
plot(finalTree)
text(finalTree, pretty=0)
predicted_test=predict(finalTree, newdata=test, type="class")
confusionmatrix_test=table(test$good_bad, predicted_test)
misclass_test=misclass(confusionmatrix_test, test)
print(confusionmatrix_test)
print(misclass_test)
library(MASS)
library(e1071)
fit_naive=naiveBayes(good_bad~., data=train)
compute_naive=function(model,data){
  predictedNaive=predict(model, newdata=data, type="class")
  confusionmatrixNaive=table(data$good_bad,predictedNaive)
  misclass = misclass(confusionmatrixNaive, data)
  print(confusionmatrixNaive)
 print(misclass)
 return(predictedNaive)
predictedNaive_train=compute_naive(fit_naive,train)
predictedNaive_test=compute_naive(fit_naive, test)
class=function(data, class1, class2, prior){
  vector=c()
  for(i in data) {
    if(i>prior){
      vector=c(vector,class1)
    } else {
      vector=c(vector,class2)
  }
 return(vector)
x_{\text{vector}=\text{seq}}(0.05, 0.95, 0.05)
tpr tree=c()
fpr_tree=c()
tpr_naive=c()
fpr_naive=c()
treeVector=c()
treeConfusion = c()
naiveConfusion = c()
treeClass = c()
naiveClass = c()
set.seed(12345)
```

```
predictTree=data.frame(predict(finalTree, newdata=test, type="vector"))
predictNaive=data.frame(predict(fit_naive, newdata=test, type="raw"))
for(prior in x_vector){
  treeClass = class(predictTree$good, 'good', 'bad', prior)
  treeConfusion=table(test$good_bad, treeClass)
  if(ncol(treeConfusion)==1){
    if(colnames(treeConfusion)=="good"){
      treeConfusion=cbind(c(0,0), treeConfusion)
   } else {
      treeConfusion=cbind(treeConfusion,c(0,0))
   }
  }
  totGood=sum(treeConfusion[2,])
  totBad=sum(treeConfusion[1,])
  tpr_tree=c(tpr_tree, treeConfusion[2,2]/totGood)
  fpr_tree=c(fpr_tree, treeConfusion[1,2]/totBad)
  print(fpr_tree)
  naiveClass=class(predictNaive$good, 'good', 'bad', prior)
  naiveConfusion=table(test$good_bad, naiveClass)
  if(ncol(naiveConfusion)==1){
    if(colnames(naiveConfusion) == "good") {
      naiveConfusion=cbind(c(0,0), naiveConfusion)
     naiveConfusion=cbind(naiveConfusion,c(0,0))
  }
  totGood=sum(naiveConfusion[2,])
  totBad=sum(naiveConfusion[1,])
  tpr_naive=c(tpr_naive, naiveConfusion[2,2]/totGood)
  fpr_naive=c(fpr_naive, naiveConfusion[1,2]/totBad)
plot(fpr_naive, tpr_naive, main="ROC curve", sub="Red = Naive Bayes, Blue = Tree", type="l", col="red",
     ylim=c(0,1), xlab="FPR", ylab="TPR")
points(fpr_tree, tpr_tree, type="l", col="blue")
naiveModel=naiveBayes(good_bad~., data=train)
train_loss=predict(naiveModel, newdata=train, type="raw")
test_loss=predict(naiveModel, newdata=test, type="raw")
confusion_trainLoss=table(train$good_bad, ifelse(train_loss[,2]/train_loss[,1]>10, "good", "bad"))
misclass_trainLoss=misclass(confusion_trainLoss, train)
print(confusion_trainLoss)
print(misclass_trainLoss)
confusion_testLoss=table(test$good_bad, ifelse(test_loss[,2]/test_loss[,1]>10, "good", "bad"))
misclass testLoss=misclass(confusion testLoss, test)
print(confusion_testLoss)
print(misclass_testLoss)
### Assignment 4
RNGversion('3.5.1')
data=read.csv2("NIRspectra.csv")
data$Viscosity=c()
```

```
n=dim(data)[1]
pcaAnalysis=prcomp(data)
lambda=pcaAnalysis$sdev^2
print(lambda)
propVar= lambda/sum(lambda)*100
screeplot(pcaAnalysis)
print(propVar)
noOfVars=1
sumOfVariation=propVar[noOfVars]
while(sumOfVariation<99){</pre>
  noOfVars=noOfVars+1
  sumOfVariation=sumOfVariation+propVar[noOfVars]
print(noOfVars)
plot(pcaAnalysis\$x[,1],pcaAnalysis\$x[,2], ylim=c(-10,10), type="p", col="blue", main="PC1 vs PC2", xlab
U=pcaAnalysis$rotation
plot(U[,1], main="Traceplot, PC1", xlab="index", ylab="PC1", type="b")
plot(U[,2], main="Traceplot, PC2", xlab="index", ylab="PC2", type="b")
library("fastICA")
set.seed(12345)
icaModel = fastICA(data, n.comp=2, verbose=TRUE)
W=icaModel$W
K=icaModel$K
W_est=K%*%W
plot(W_est[,1], main="Traceplot, ICA1", xlab="index", ylab="ICA1", type="b", col="red")
plot(W_est[,2], main="Traceplot, ICA2", xlab="index", ylab="ICA2", type="b", col="red")
plot(icaModel$S[,1], icaModel$S[,2], main="ICA1 vs ICA2", xlab="ICA1", ylab="ICA2", type="p", col="blue
```