

Reference attribute grammar controlled graph rewriting

Motivation and overview

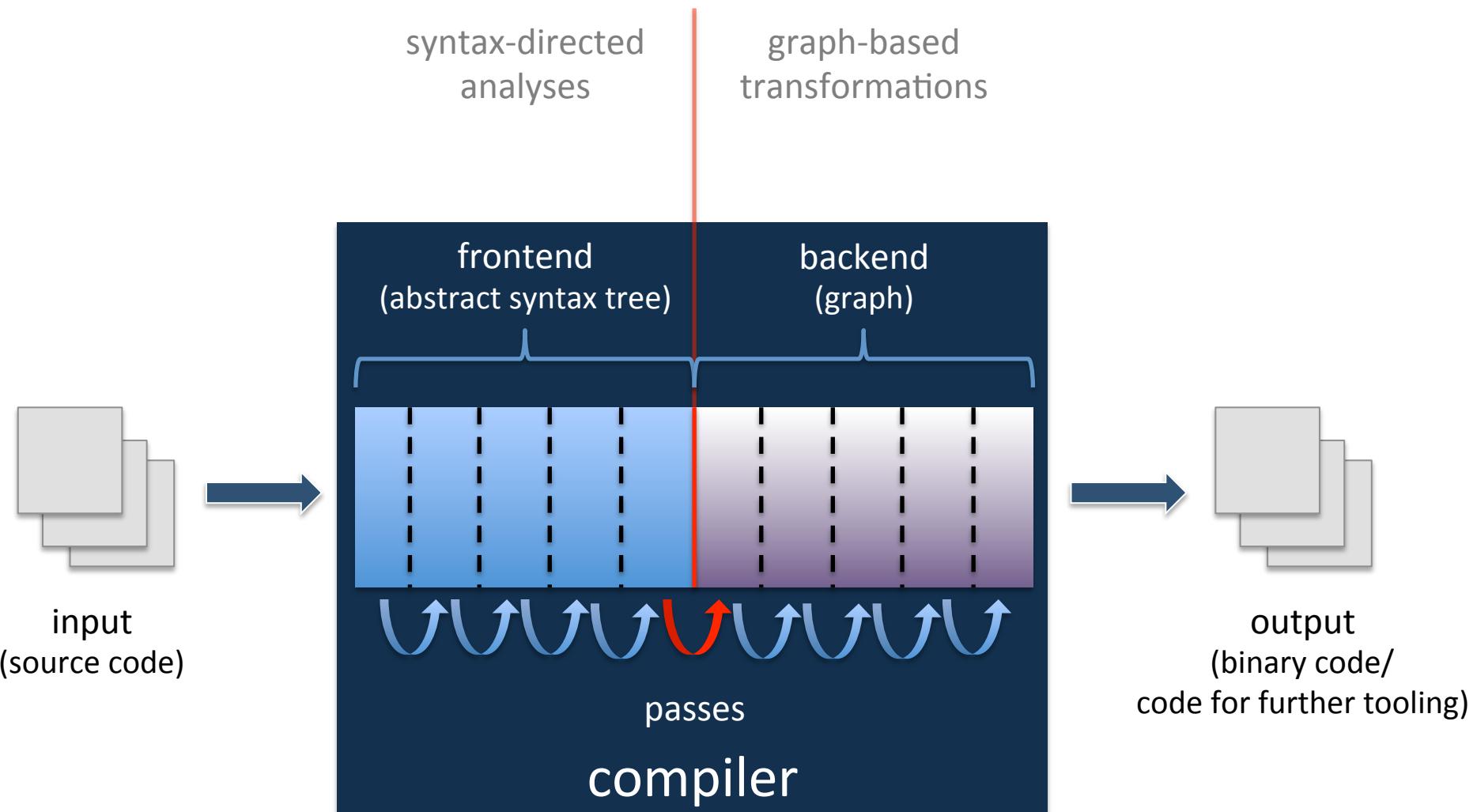
Christoff Bürger
christoff.buerger@gmail.com

The problem

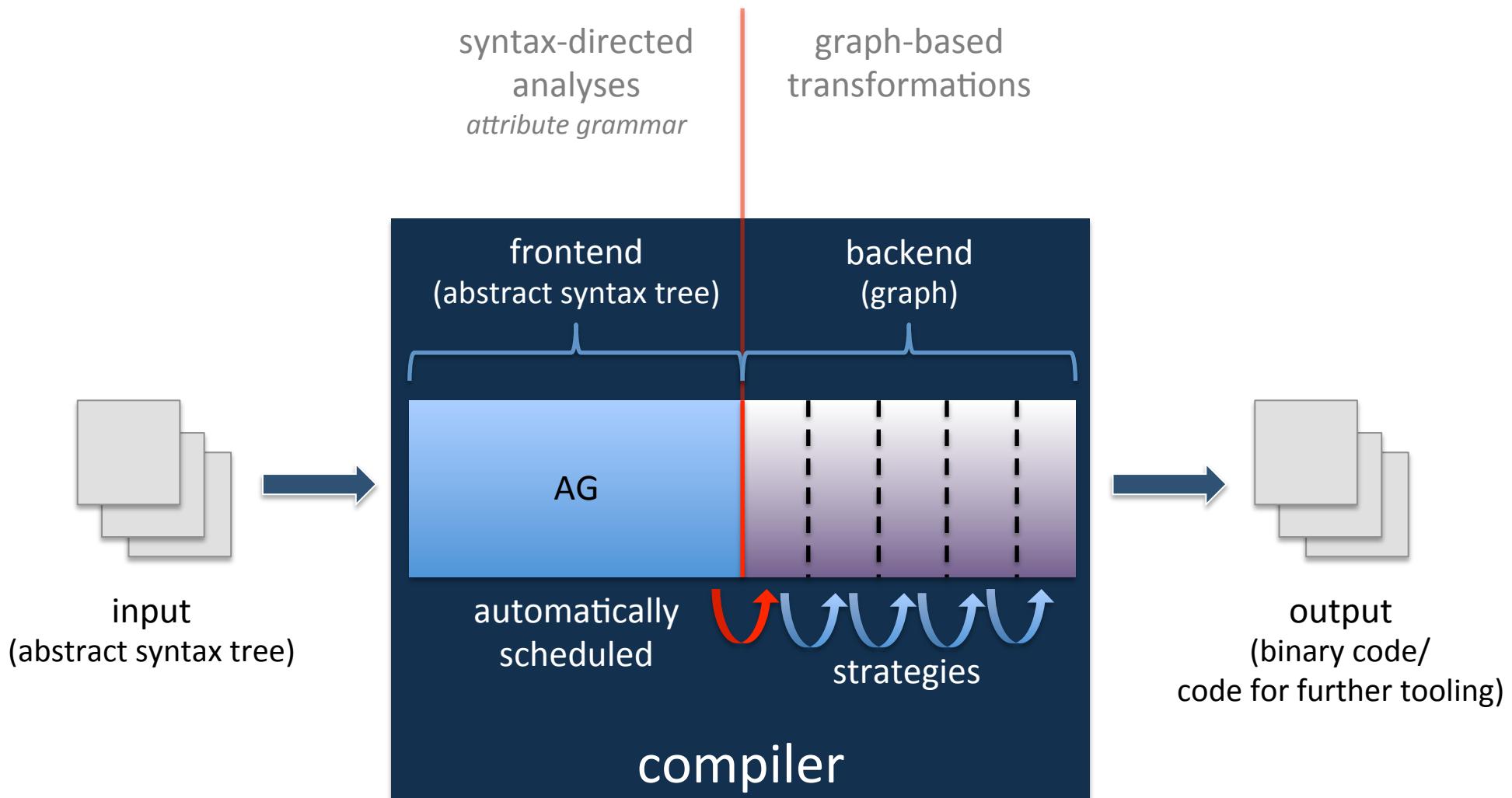
What do you want?

Interactive, mutual-dependent analyses
& transformations

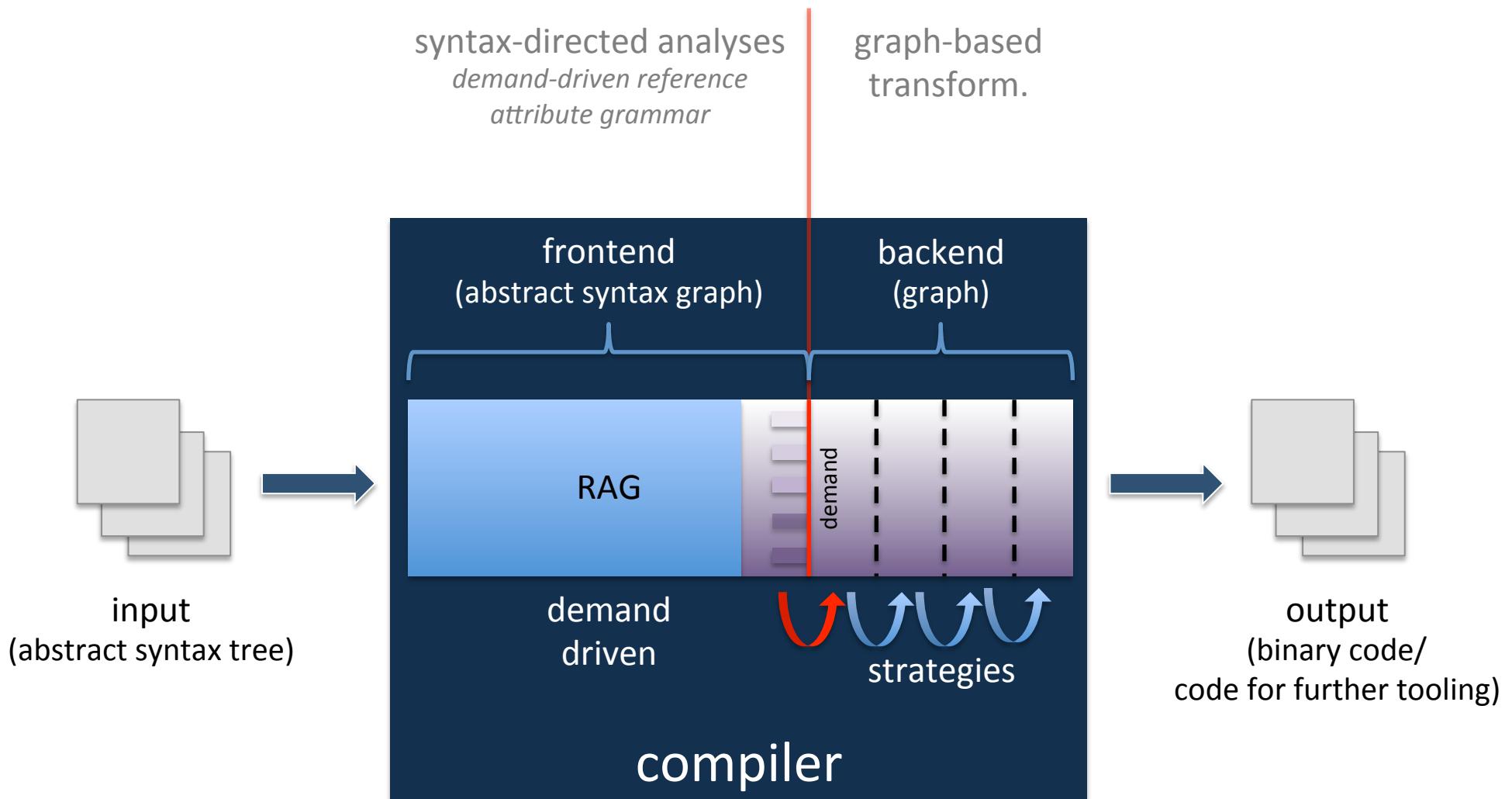
From batch to interactive



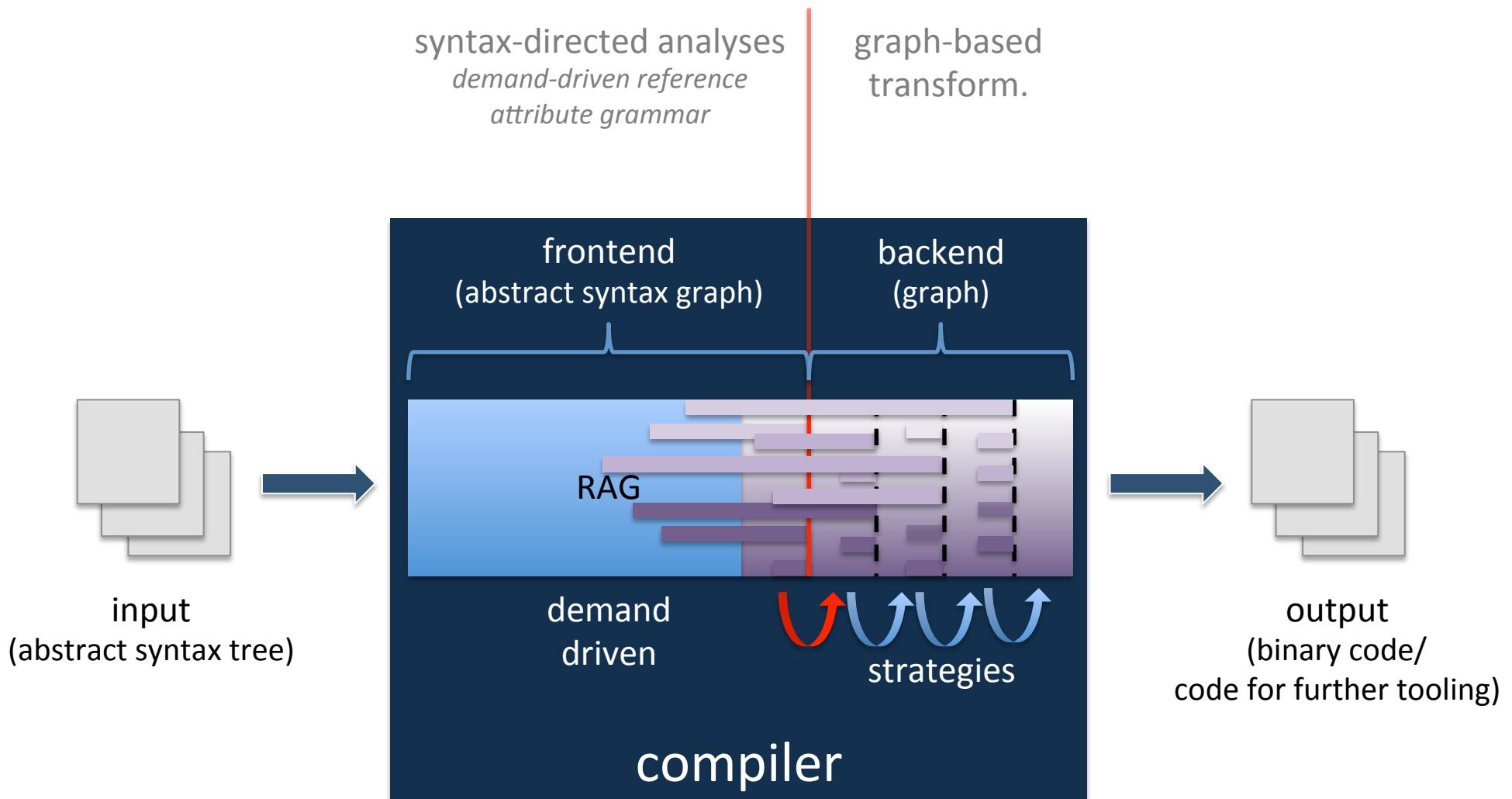
From batch to interactive



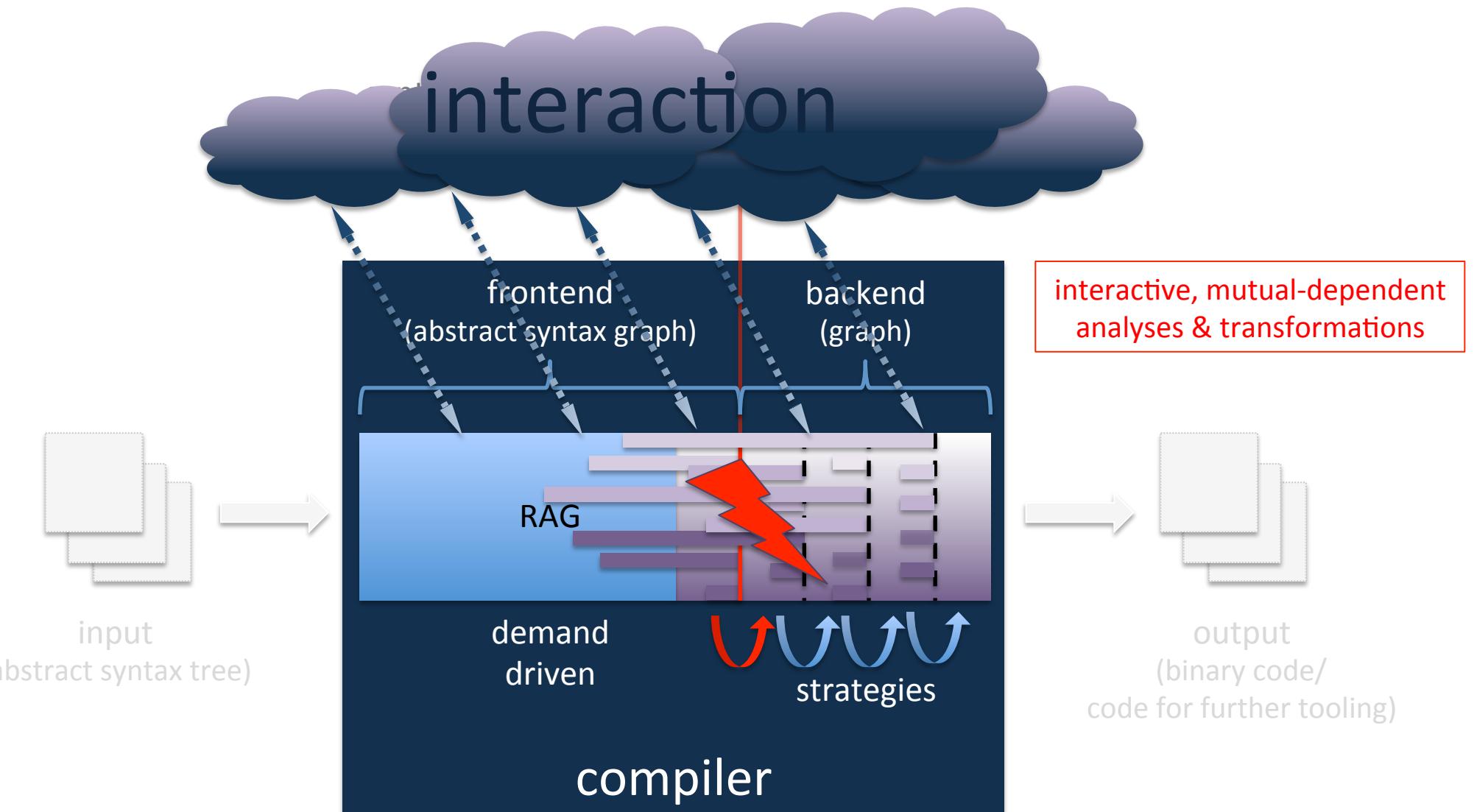
From batch to interactive



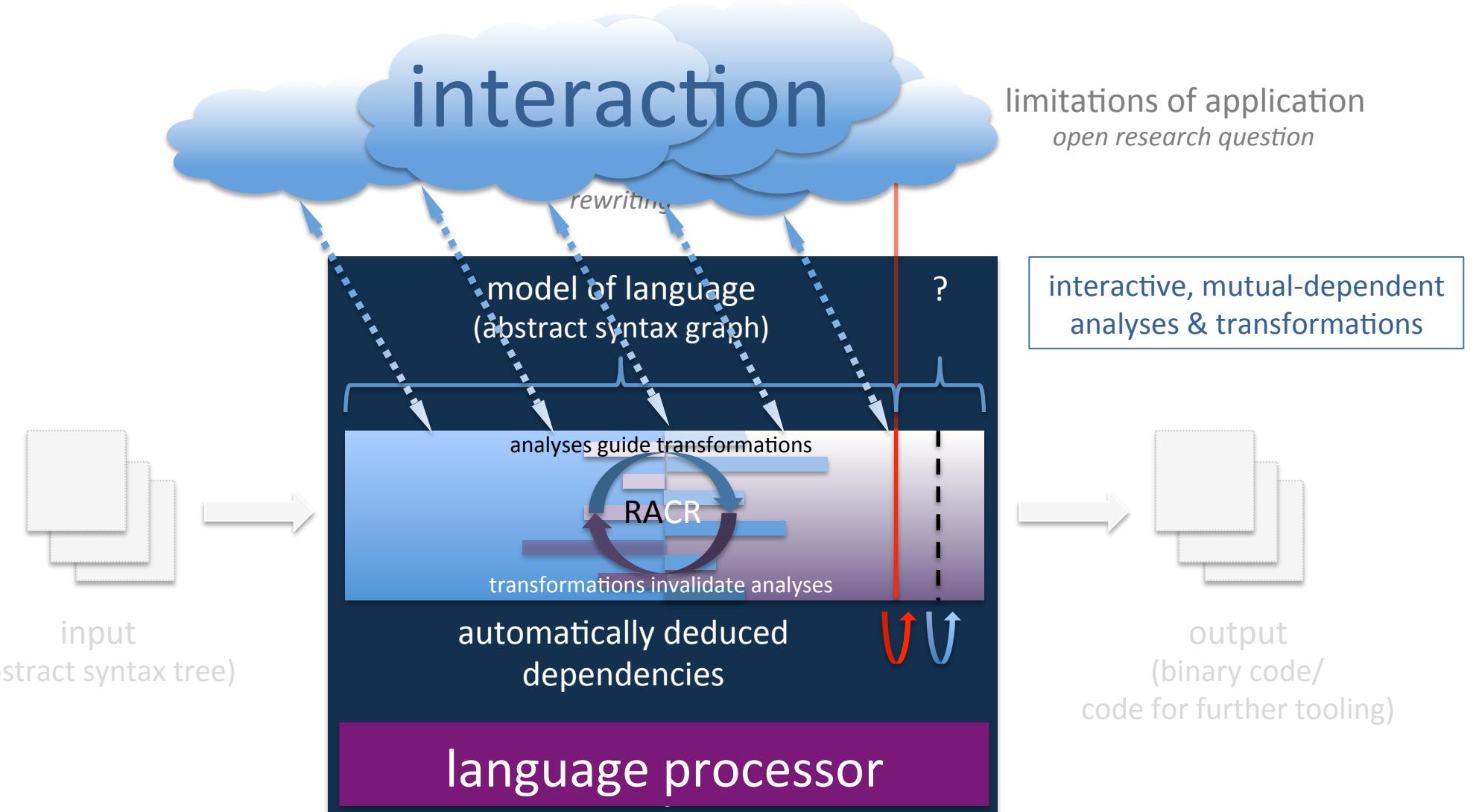
From batch to interactive



From batch to interactive



From batch to interactive



The solution

What is RAG-controlled rewriting?

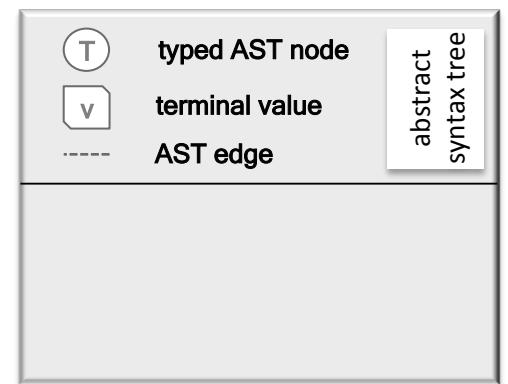
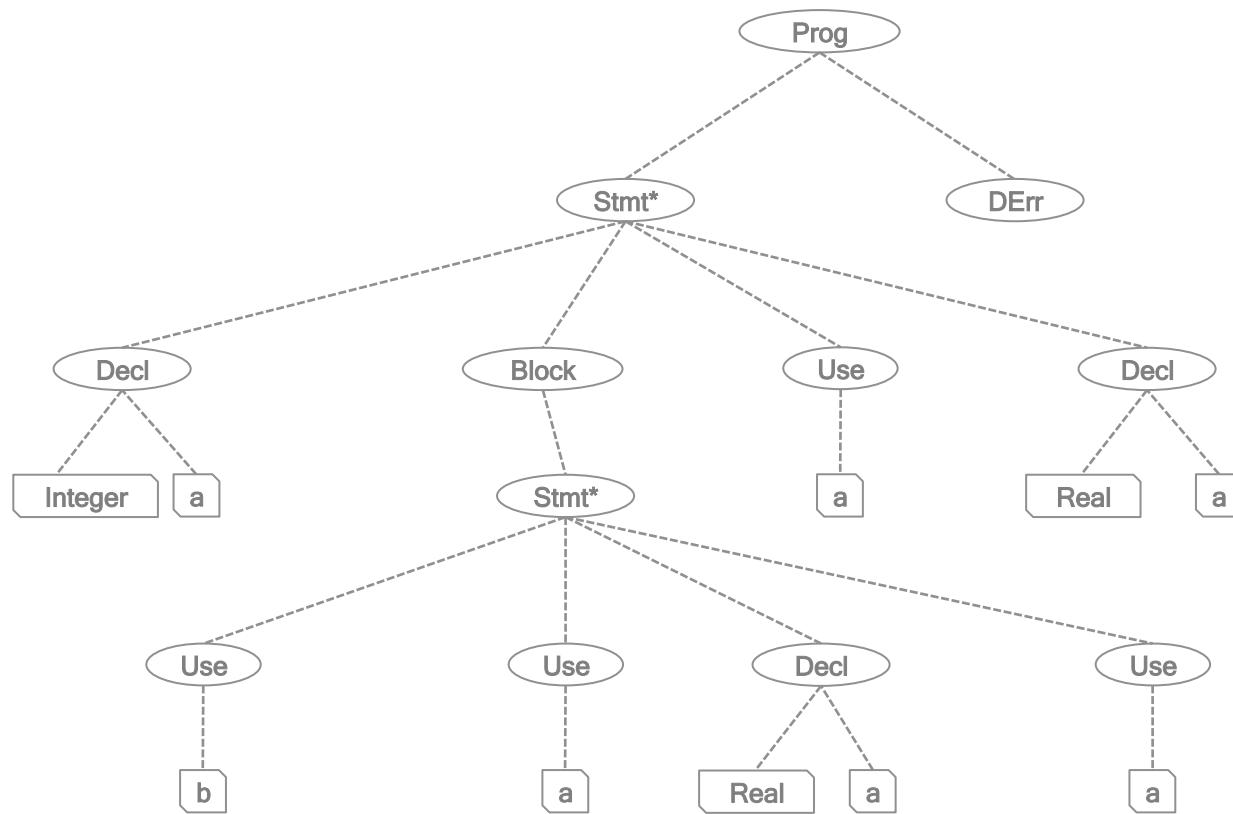
Reference attribute grammars, abstract
syntax graphs, RAG-controlled rewriting
& *RACR*¹

¹ <https://github.com/christoff-buerger/racr>

Reference attribute grammars & ASGs

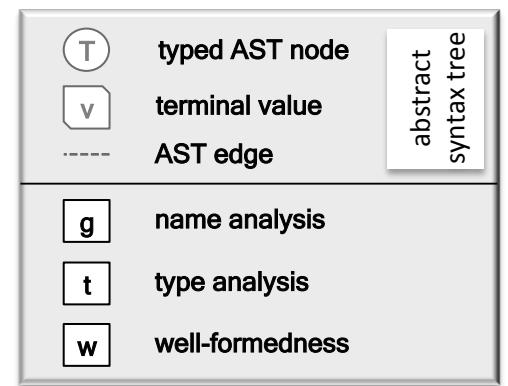
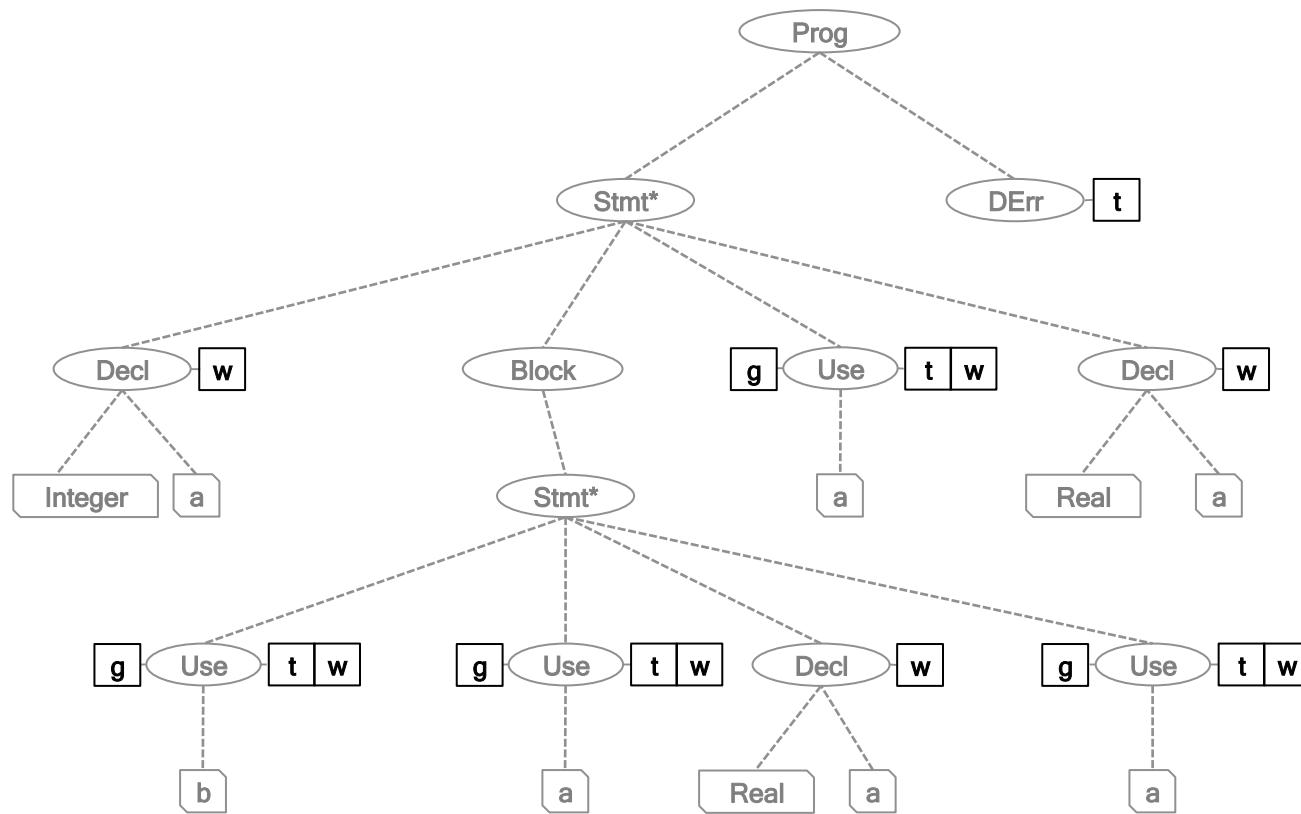
```
Program
  decl a : integer
  Begin
    use b ; Error
    use a
    decl a : real
    use a
  End
  use a
  decl a : real ; Error
End
```

Reference attribute grammars & ASGs



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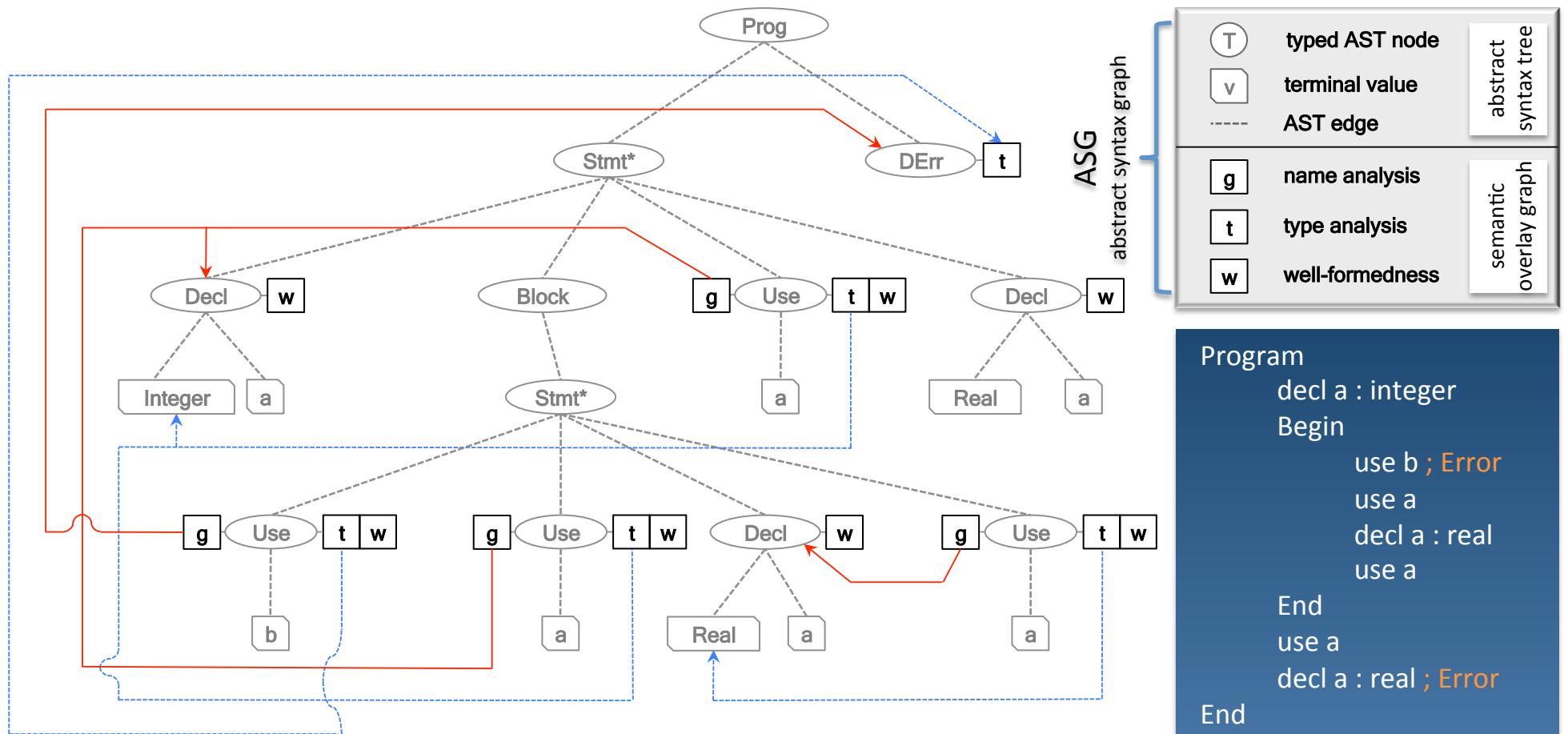
Reference attribute grammars & ASGs



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Reference attribute grammars & ASGs



RAG-controlled rewriting

- RAG-controlled rewriting = **RAGs** + **rewriting**
 - RAG for declarative **analyses**
 - graph rewriting for declarative ASG **transformations**
 - seamless combination:
 - use of analyses to deduce rewrites
 - rewrites automatically update analyses
- >> incremental
- 
- mutual control

RACR

Reference implementation of RAG-controlled
rewriting in *Scheme*.

<https://github.com/christoff-buerger/racr>

The implementation

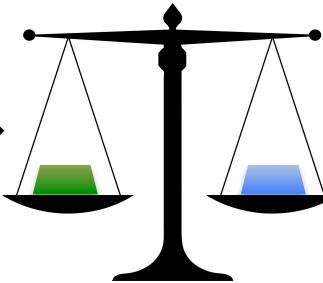
How works RAG-controlled rewriting?

Dynamic attribute dependency graphs &
incremental evaluation

Query & rewrite functions

well balanced set of functions

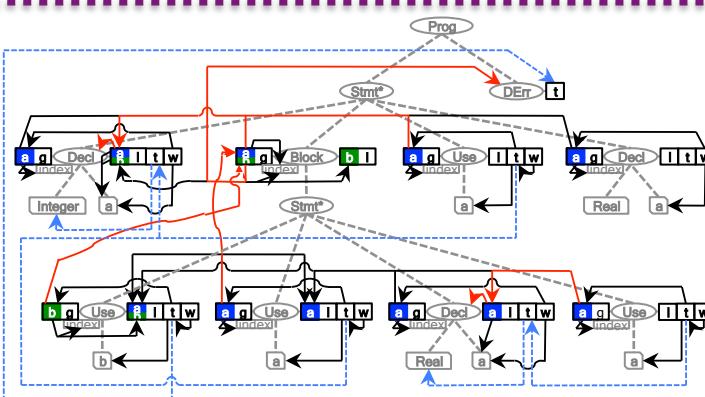
query functions to access ASG
add dependencies on queried information



rewrite functions to change ASG
invalidate attributes depending on rewritten information

query functions

- only way to query ASG
- used in attribute equations



construct

dynamic attribute
dependency graph

rewrite functions

- only way to change ASG
- used for transformations

invalidate

demand-driven evaluation avoids unnecessary computations

Query & rewrite functions

query functions

$(=Name n . a)$	value of attribute <i>Name</i>
$(->c n)$	child <i>c</i> of <i>n</i> (<i>c</i> can be index)
$(<- n)$	parent of <i>n</i>
$(->c? n)$	has <i>n</i> a <i>c</i> child (<i>c</i> can be index)
$(<-? n)$	has <i>n</i> a parent
$(index n)$	child-position of <i>n</i>
$(num-children n)$	number of children of <i>n</i>
$(T=? n)$	is <i>n</i> exactly of type <i>T</i>
$(T<? n)$	is <i>n</i> subtype of type <i>T</i>
$(T>? n)$	is <i>n</i> supertype of type <i>T</i>
$(\{=,<,>\}? n1 n2)$	is <i>n1</i> $\{\!=,\<,\>\}$ -type of <i>n2</i>
$(find f n . b)$	find child of <i>n</i> satisfying <i>f</i>

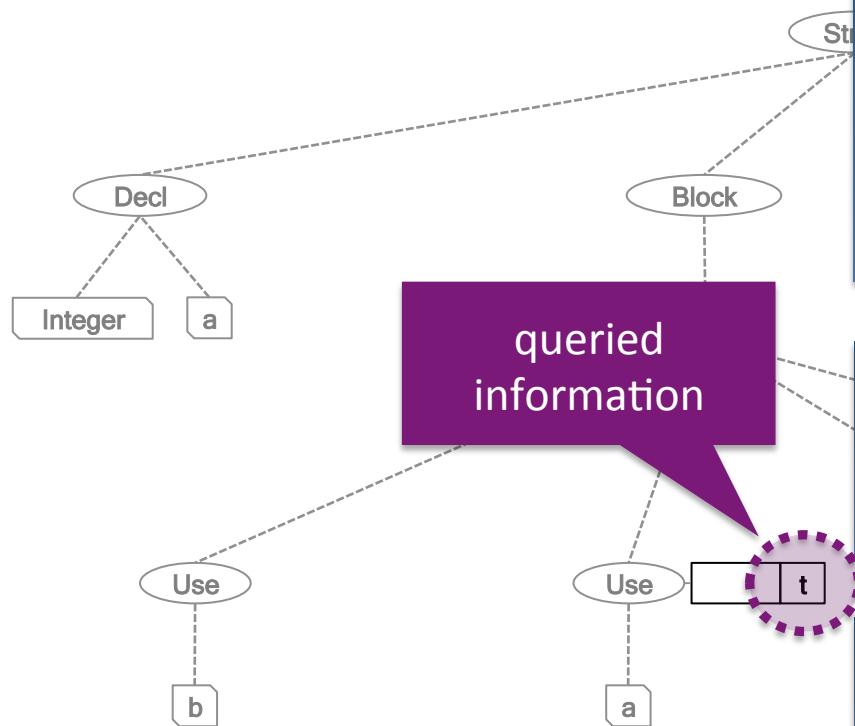
rewrite functions

$(r-subtree n1 n2)$	replace <i>n1</i> by <i>n2</i>
$(r-terminal t v)$	replace value of terminal <i>t</i>
$(add n l)$	add <i>n</i> to list <i>l</i>
$(insert n i l)$	insert <i>n</i> at position <i>i</i> in <i>l</i>
$(delete n)$	delete list element <i>n</i>
$(refine n T . c)$	refine <i>n</i> to subtype <i>T</i>
$(abstract n T)$	abstract <i>n</i> to supertype <i>T</i>

dependency types

value, exists, has-child(*child/index*), has-parent, index, num-children, type, subtype(*T*), supertype(*T*)

Dynamic attribute dependency graphs

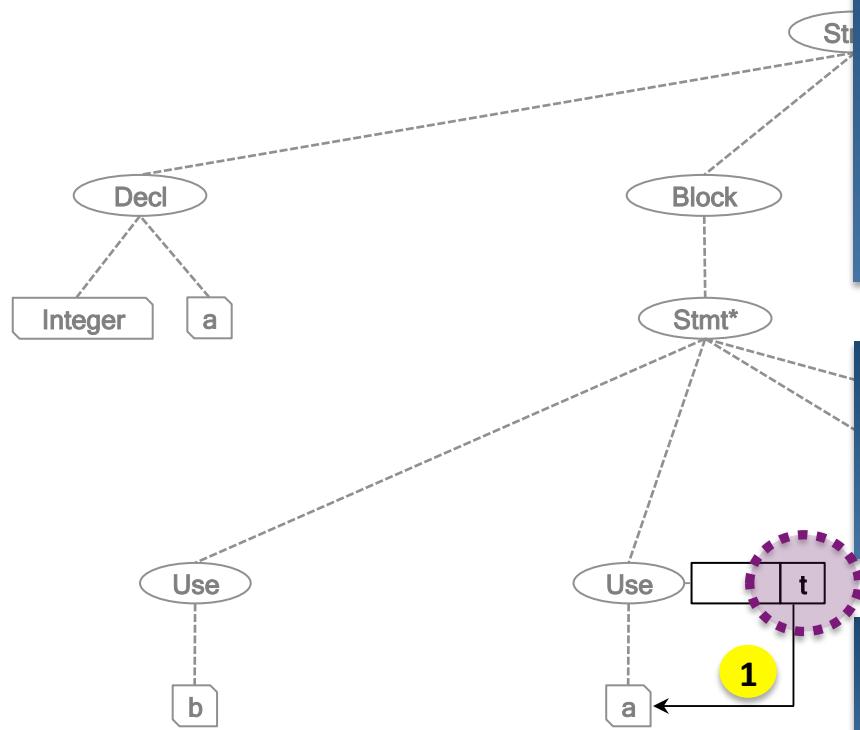


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((Block Stmt*) ; Equation for statements of blocks  
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Dynamic attribute dependency graphs



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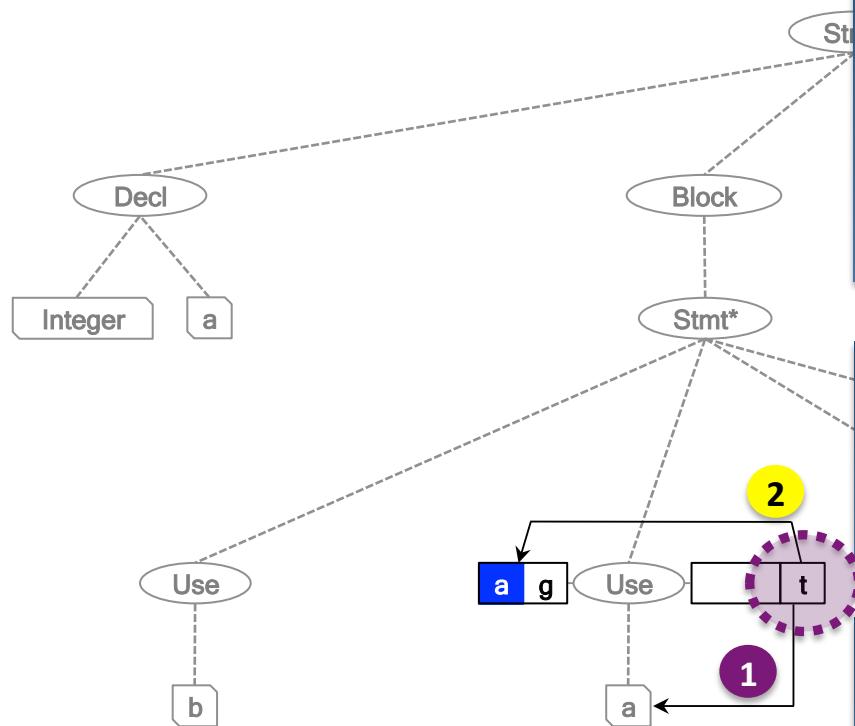
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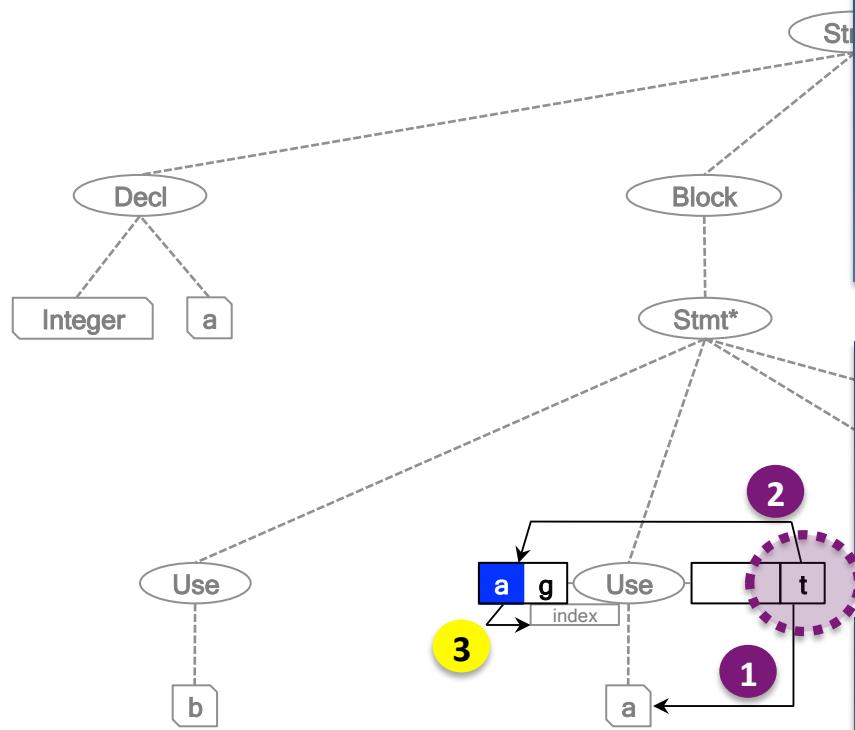


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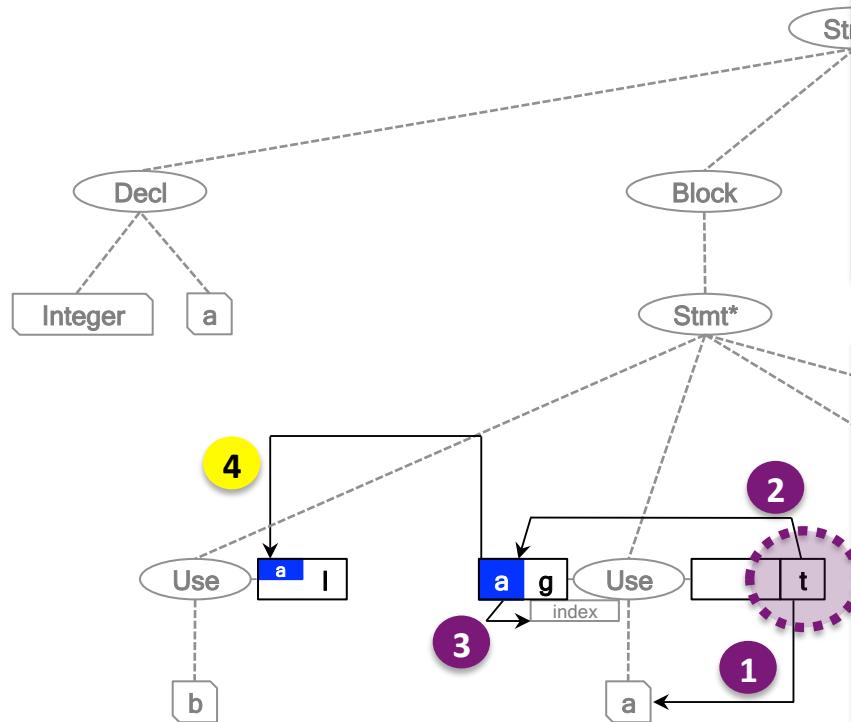


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Dynamic attribute dependency graphs



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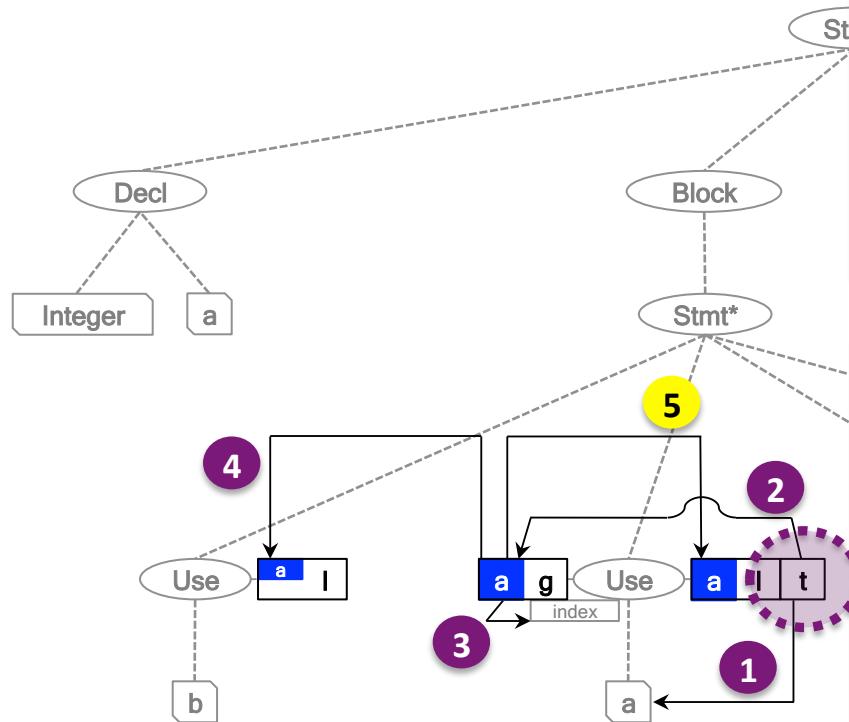


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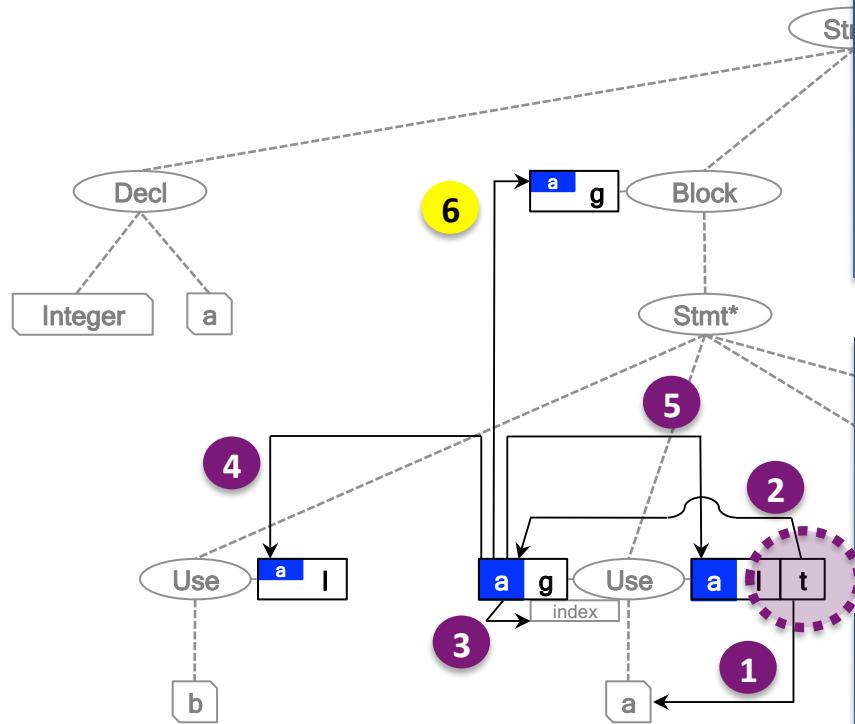


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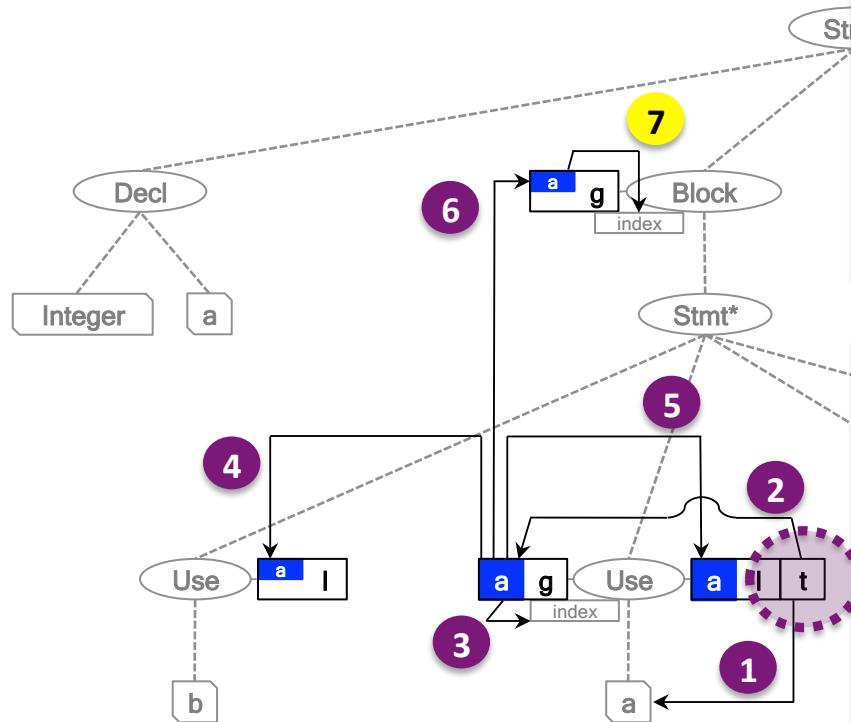


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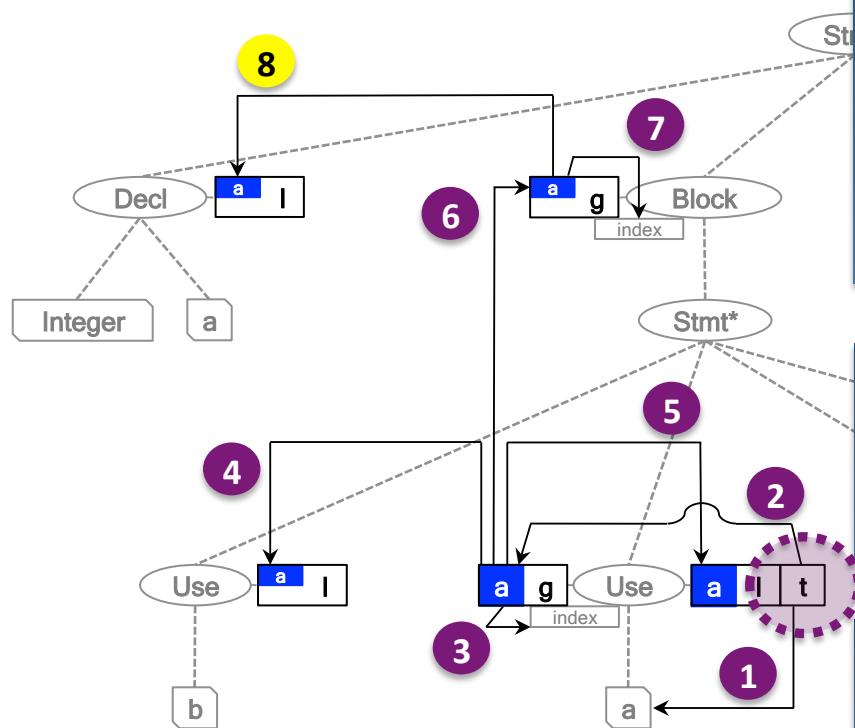


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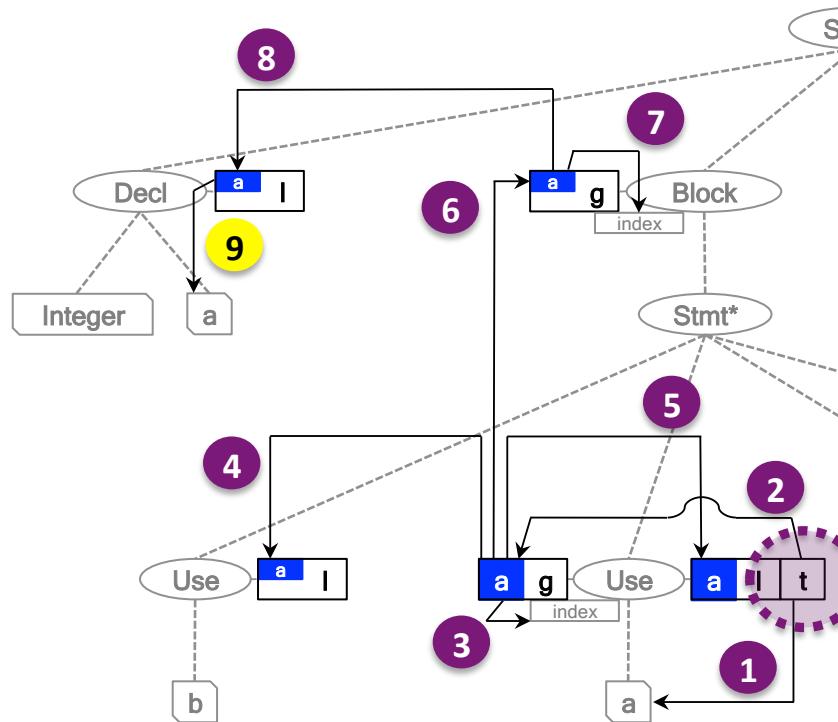


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Dynamic attribute dependency graphs

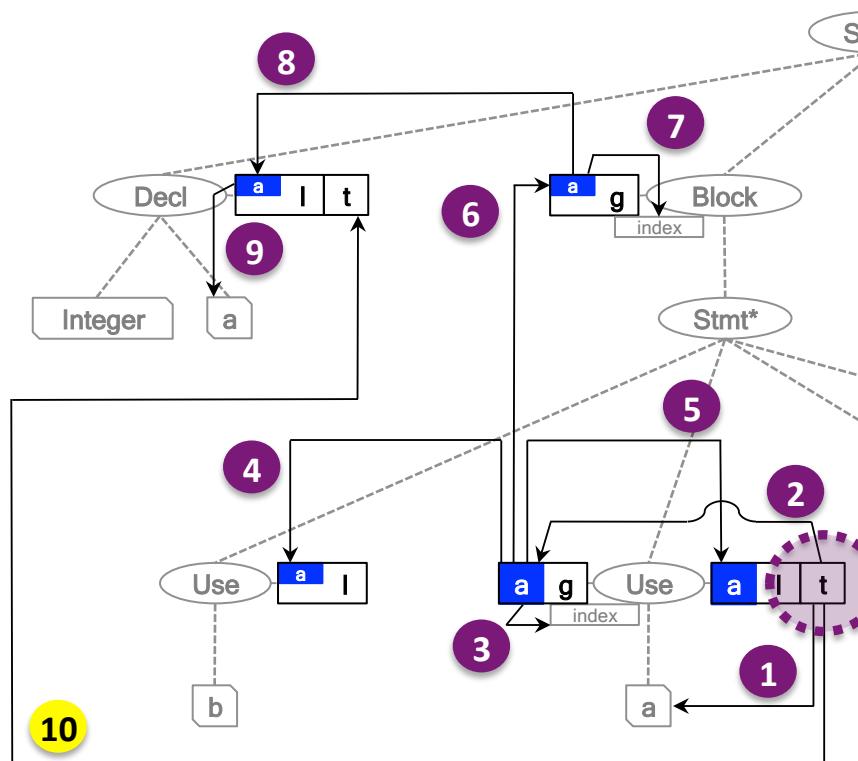


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Dynamic attribute dependency graphs

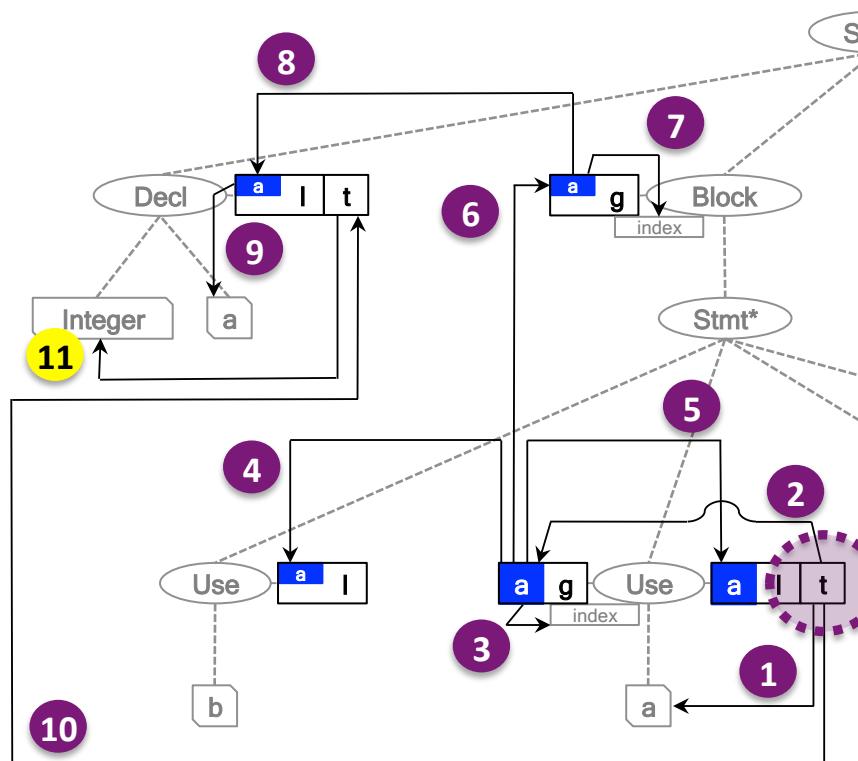


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Dynamic attribute dependency graphs



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Dynamic attribute dependency graphs

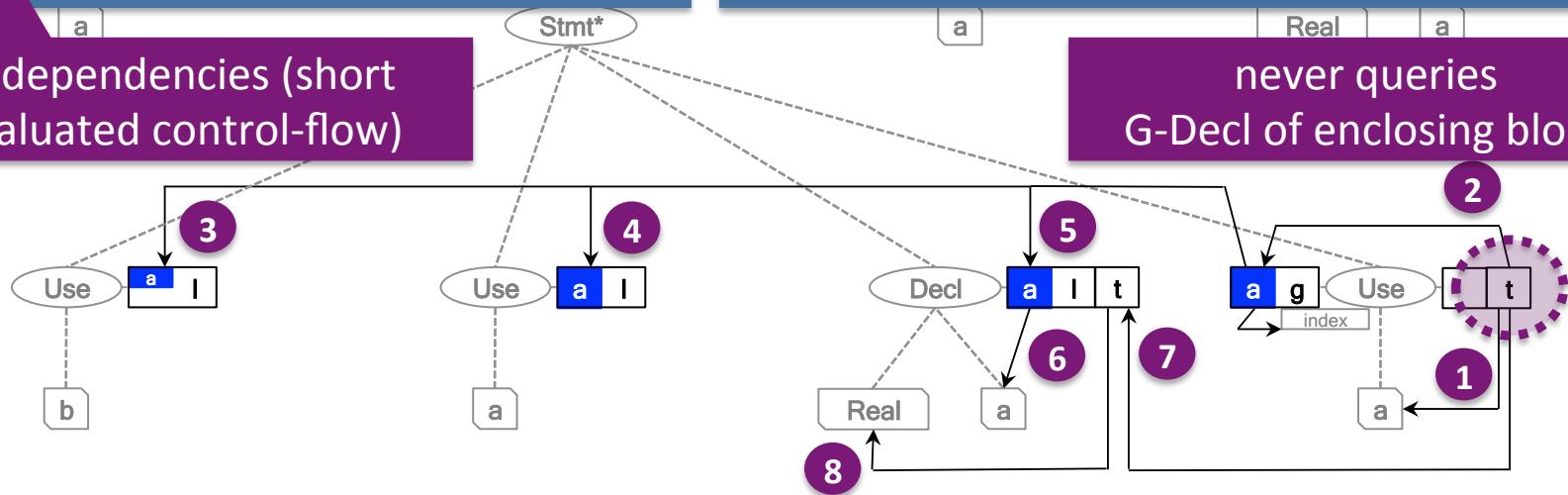
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  ((Prog Stmt*) ; Equation for statements of programs
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```

St

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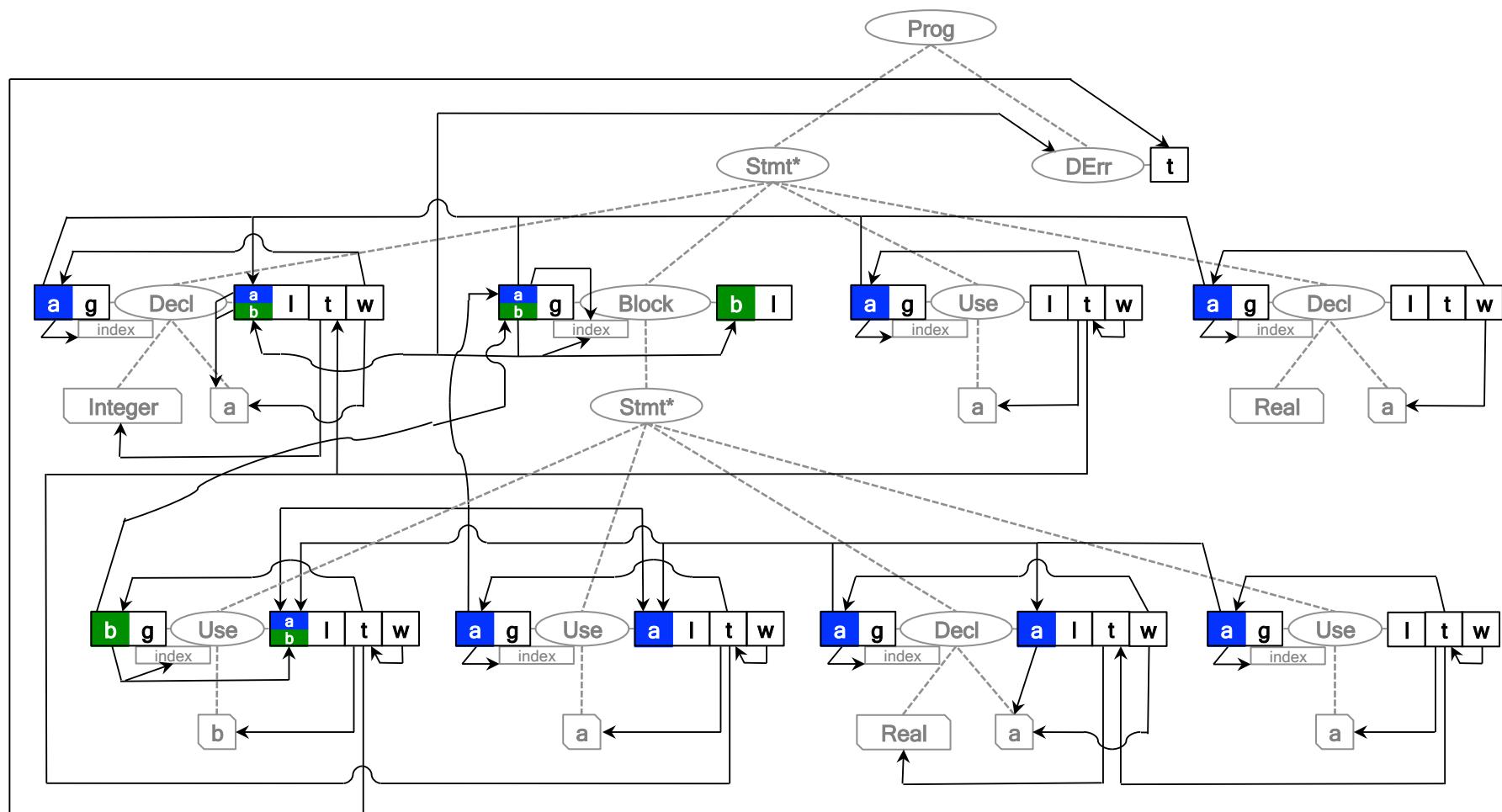
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a
dynamic dependencies (short circuit evaluated control-flow)



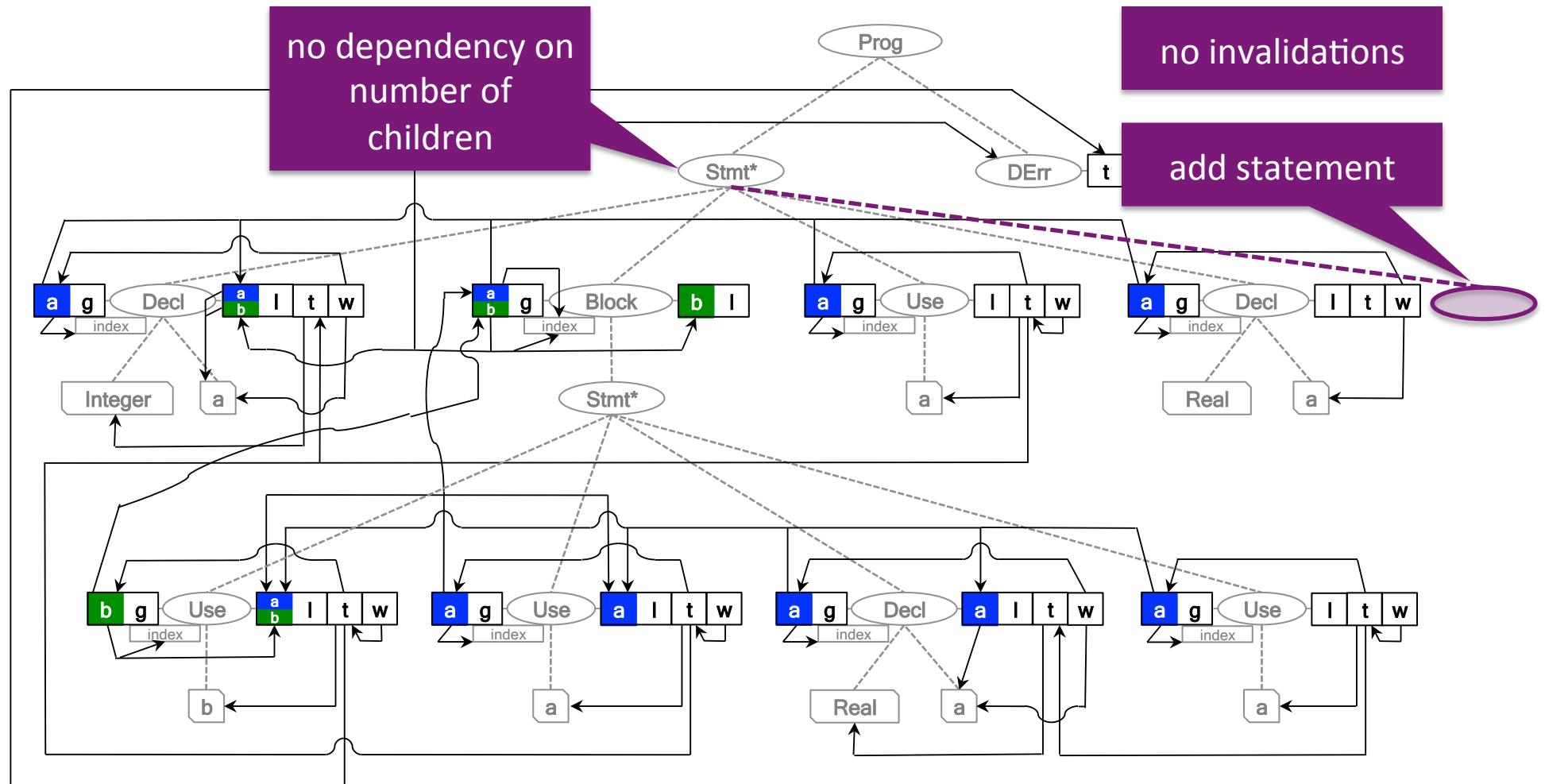
complex to achieve manually

Dynamic attribute dependency graphs

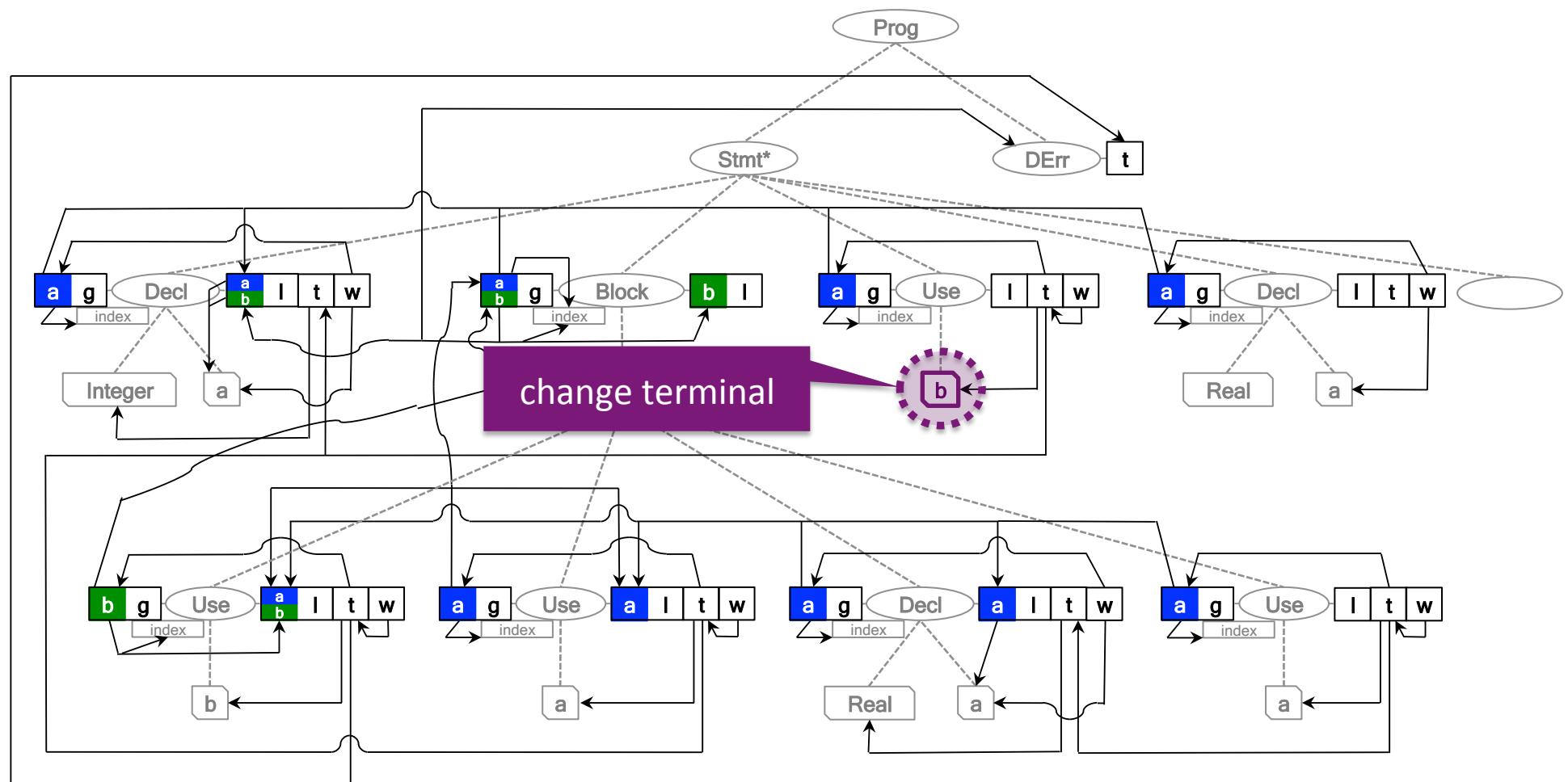


automatically in RAG-controlled rewriting

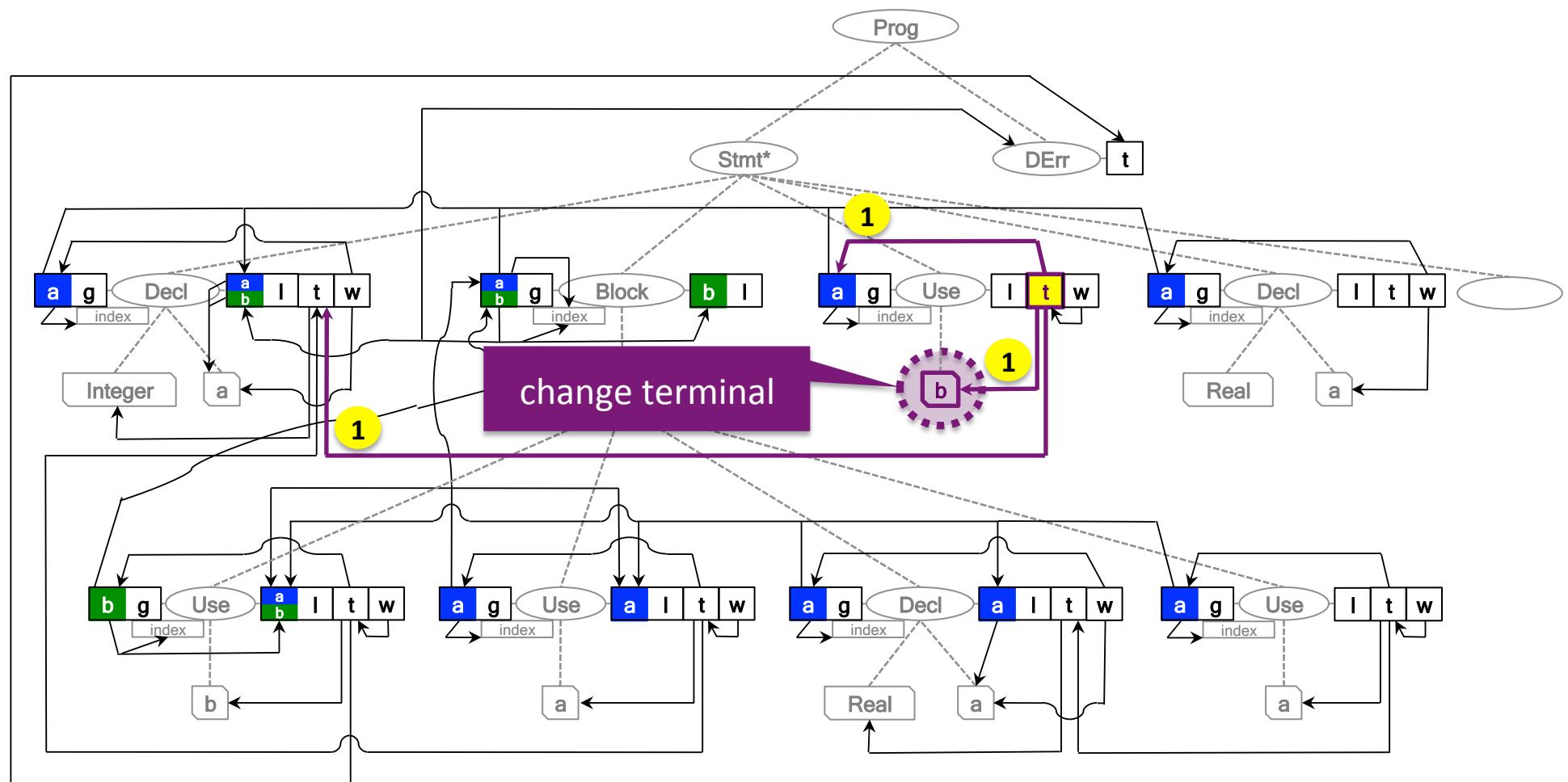
Incremental evaluation



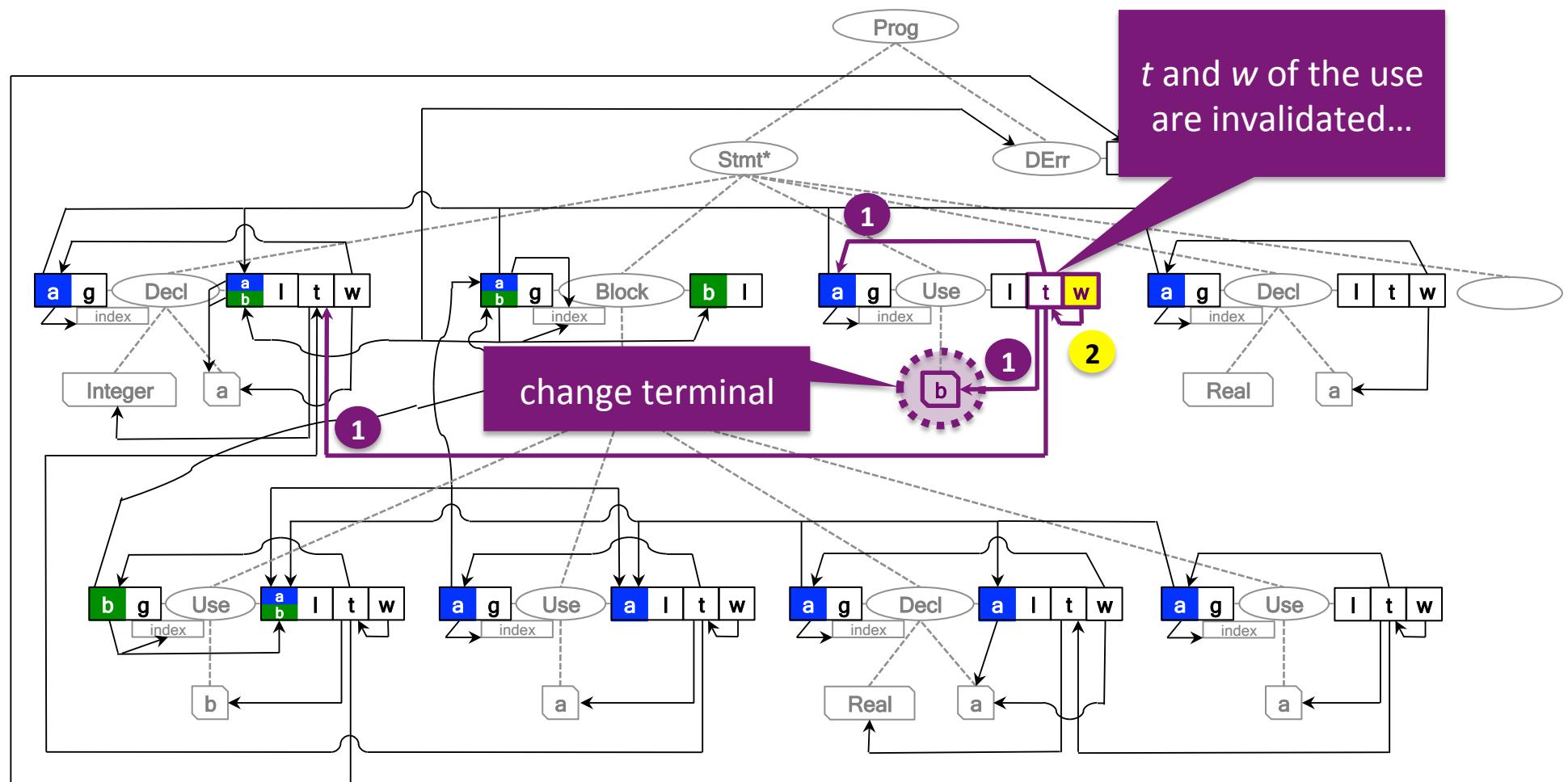
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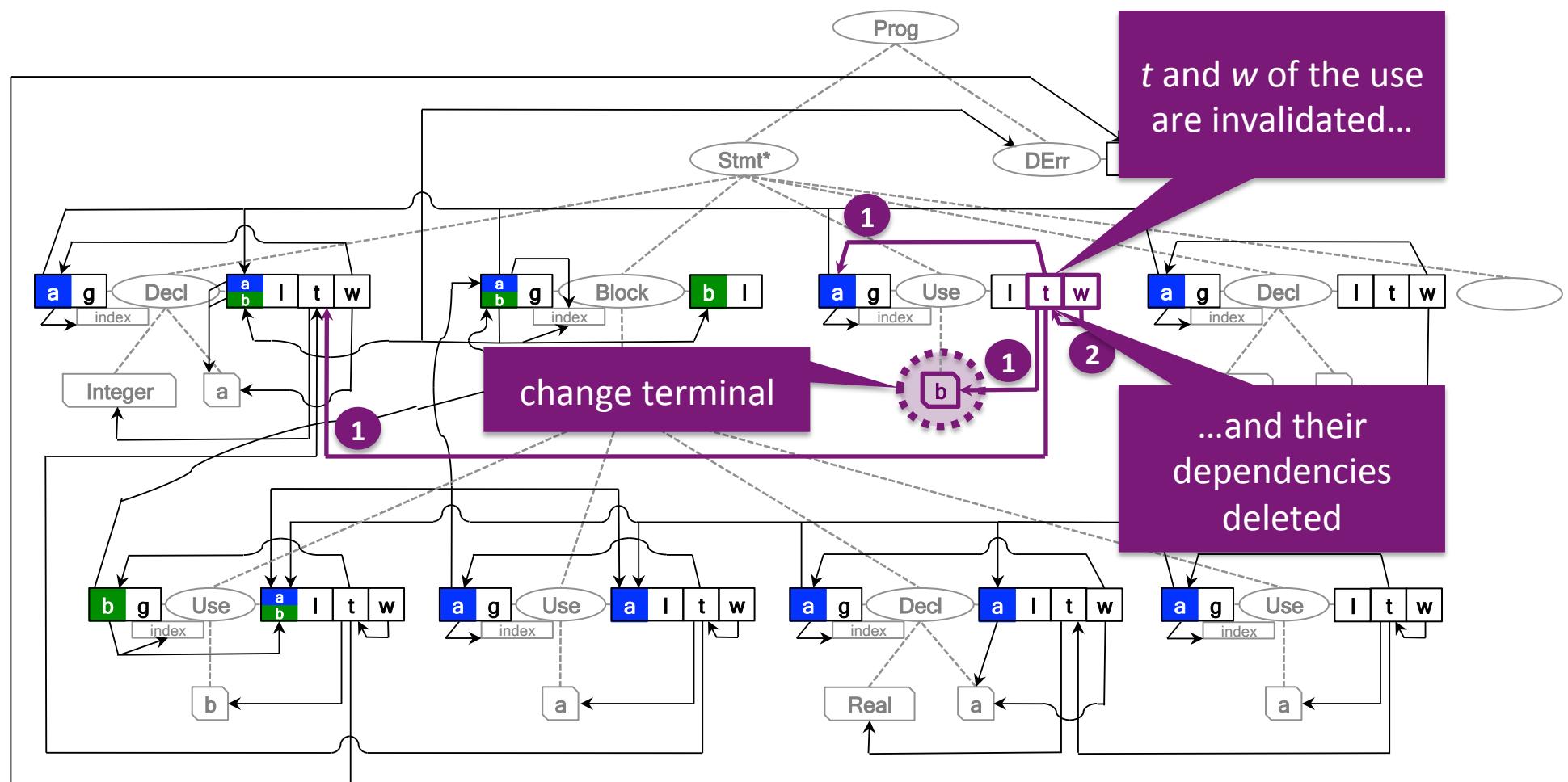
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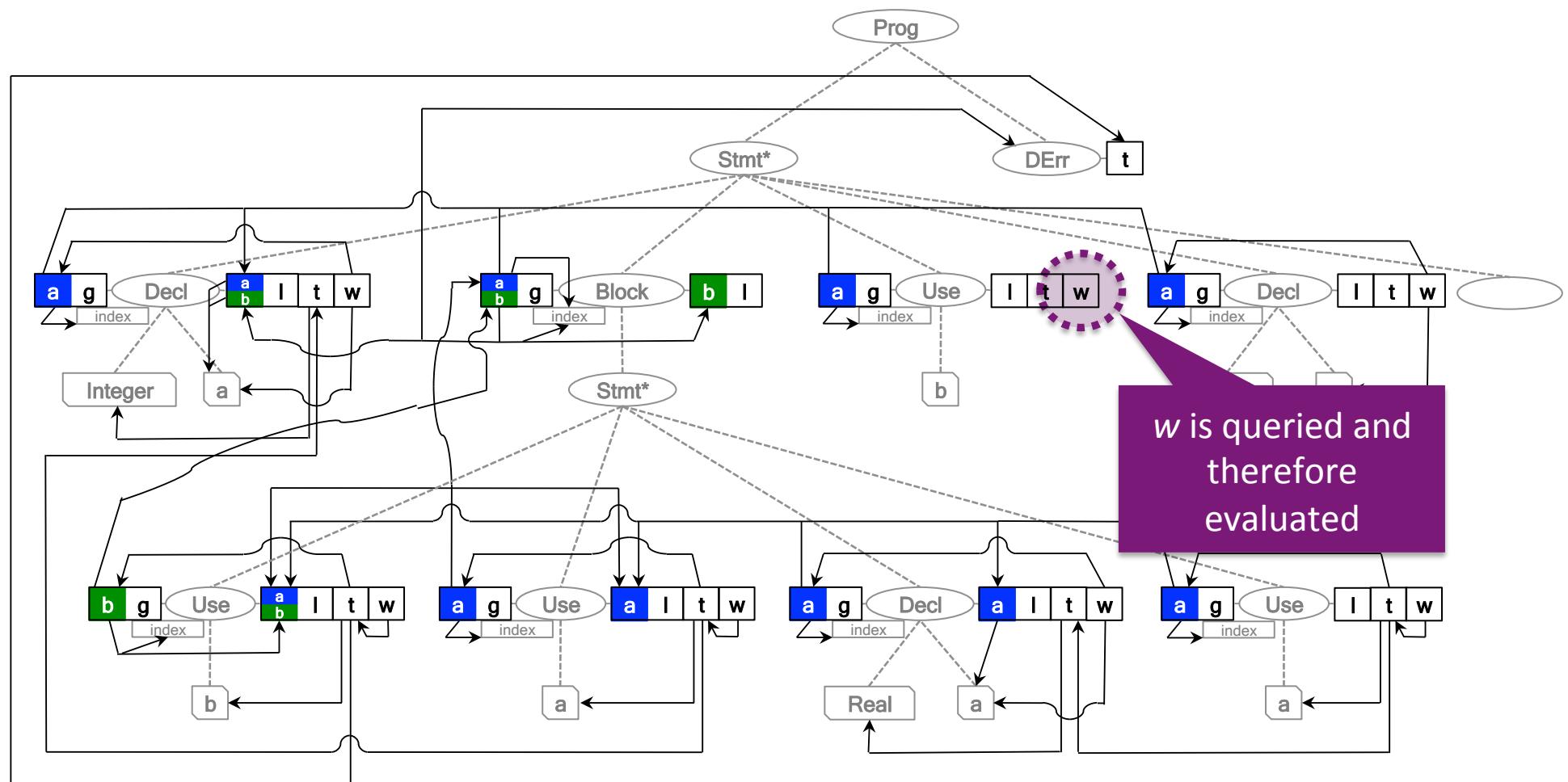
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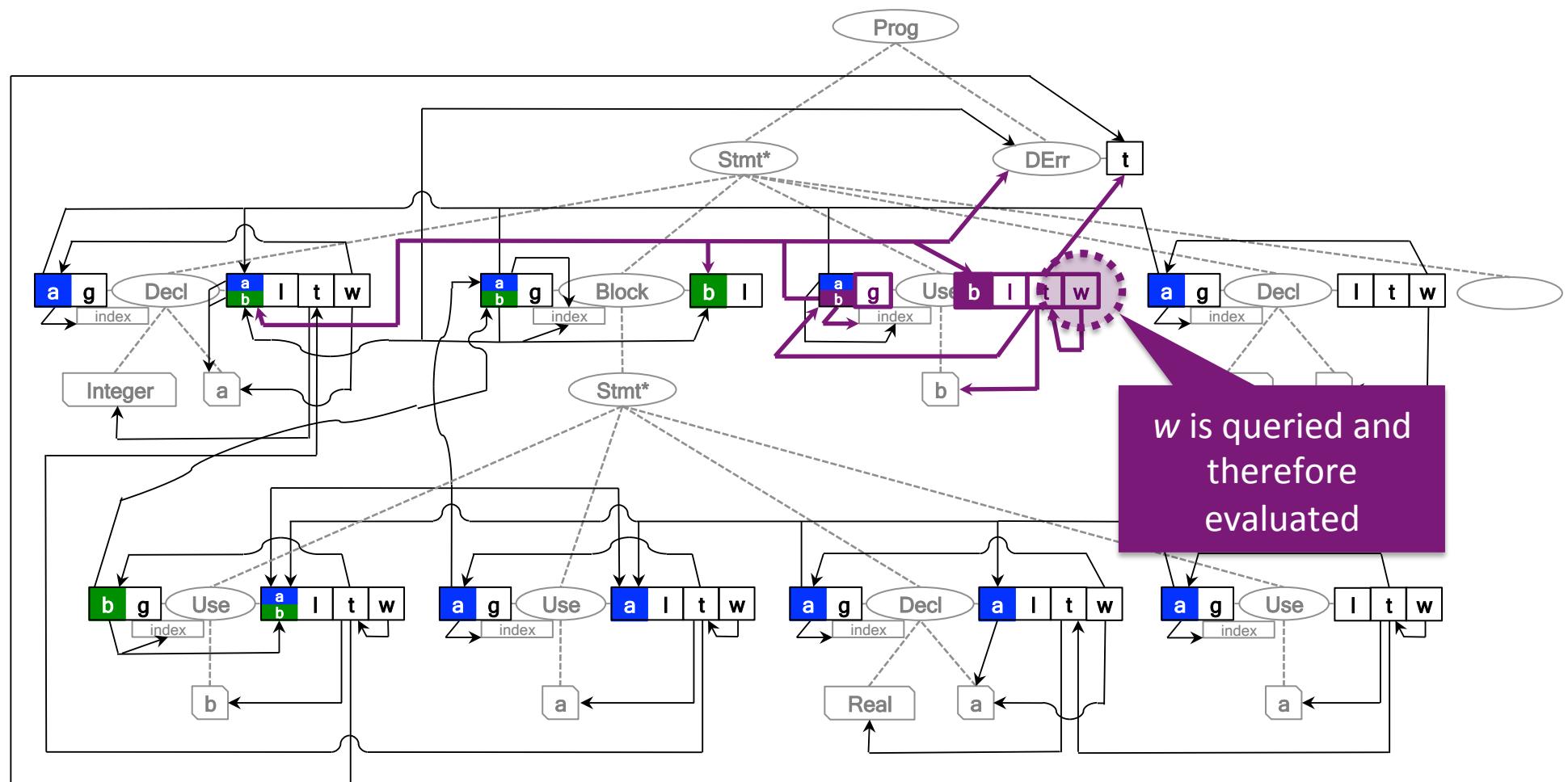
Incremental evaluation



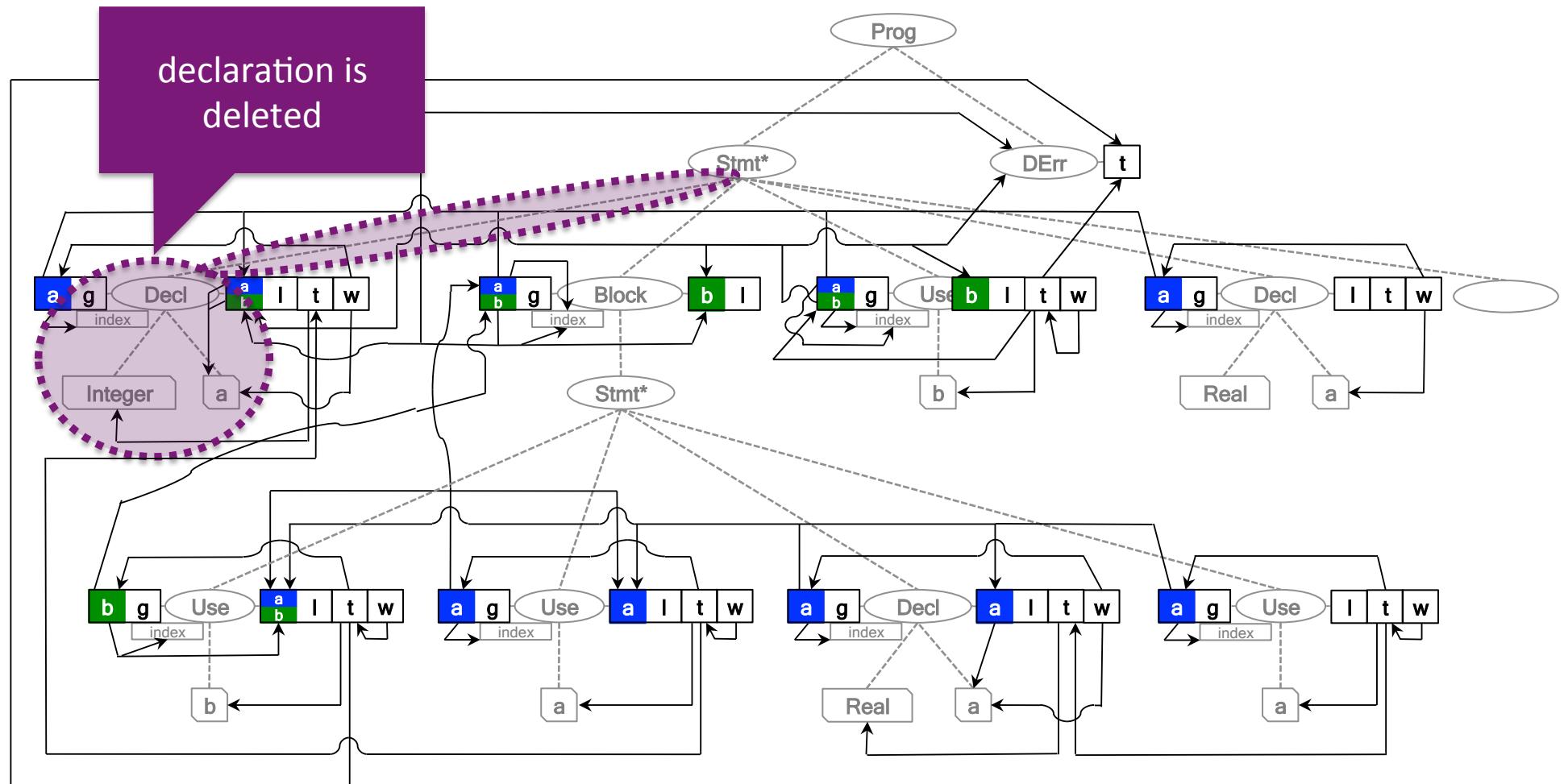
Incremental evaluation



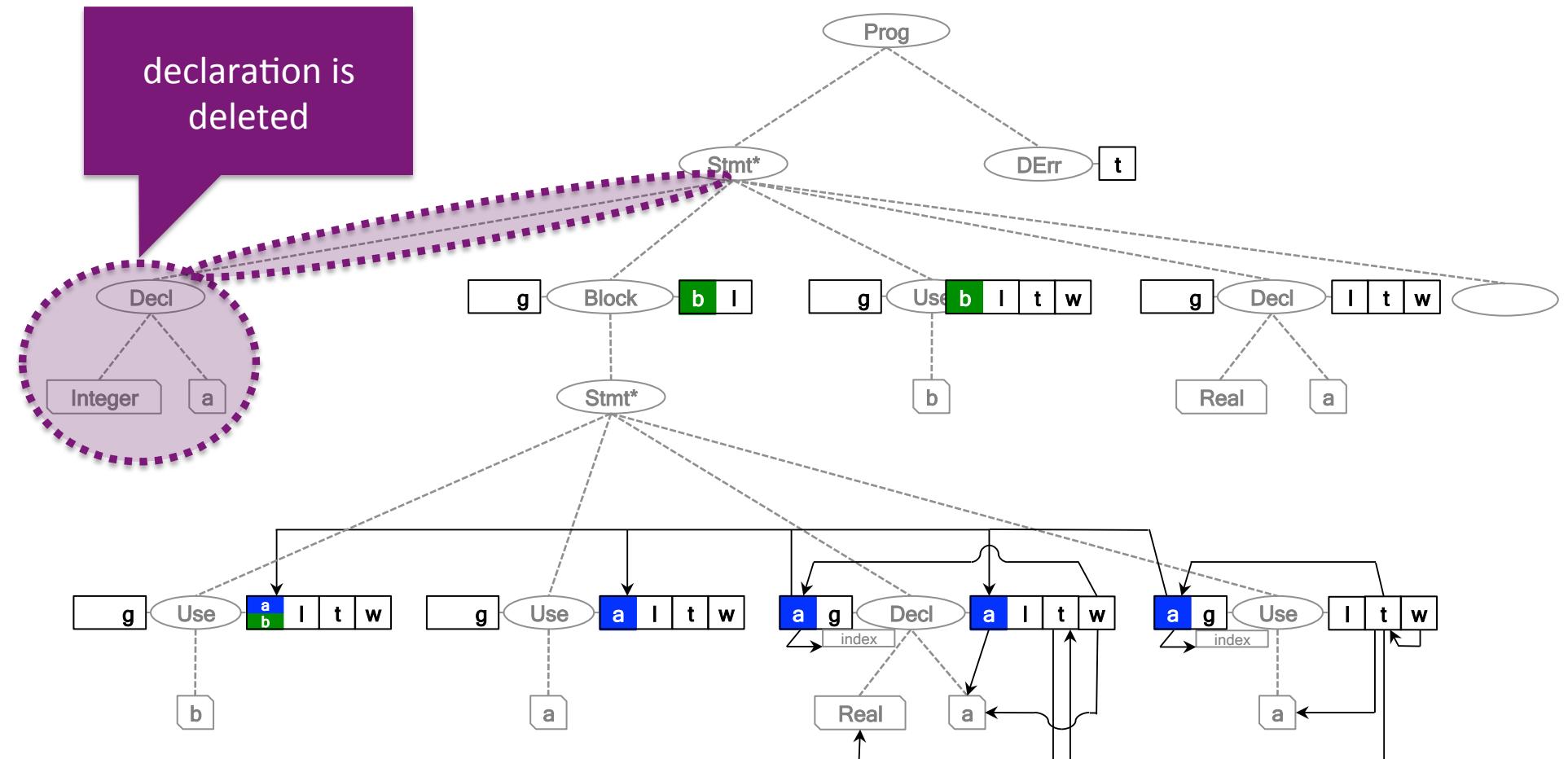
Incremental evaluation



Incremental evaluation



Incremental evaluation



The application

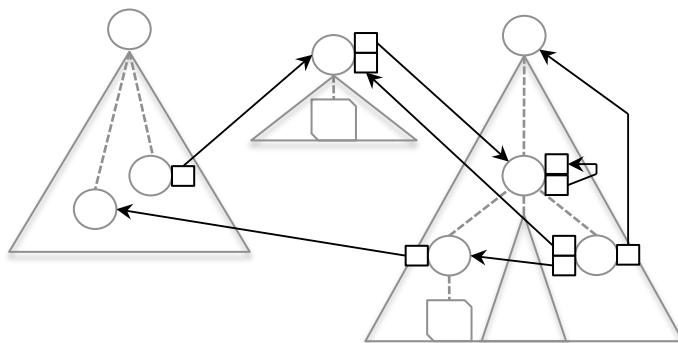
How works RAG-controlled rewriting!

Pattern attributes, transformer
attributes & rewrite deduction

Pattern attributes

Attributes can arbitrary query ASGs:

- including structural relations (reference attributes) and constraints (other attributes)



```
(ag-rule my-pattern ; Pattern attribute  
  (node-type-to-check-pattern-for  
    (lambda (n)  
      ; Query ASG and check constraints.  
      ; Return nodes relevant for rewriting.  
    )))
```

incremental evaluation >>
>> incremental pattern matching

pattern can be deduced
using analyses

Transformer attributes

Attribute values can be functions encapsulating deduced transformations.

```
(ag-rule my-transformation ; Transformer attribute
  (node-type-to-derive-transformation-for
    (lambda (n)
      ; Match fragments to transform (e.g., using pattern attributes).
      (and
        match? ; If transformation is not applicable return false, ...
        (lambda () ; ... otherwise a deduced function encapsulating rewrites.
          ; Apply rewrites on matched fragments.
        )))))
)))))
```

incremental

From programmed through RAG-controlled to ‘wild’ graph rewriting

programmed rewriting via primitive API

```
; Program with arbitrary interleaving of ASG queries & rewrites:  
(let ((c (->child n)  
      (n (if (=conditional-attribute c)  
            (=reference-attribute-1 c) (=reference-attribute-2 c)))  
      (r-subtree n some-new-fragment)))
```

RAG-controlled rewriting

```
; Interactive use of pattern & transformer attributes:  
(let ((trans? (find (lambda (n) (=transformer n)) nodes))  
      (and trans? (trans?))))
```

wild rewriting (fixpoint)

```
; Use generic graph rewriter with transformer attributes:  
(rewrite-all ‘bottom-up list-of-transformer-attributes ASG)
```

all forms supported by *RACR*

The evaluation

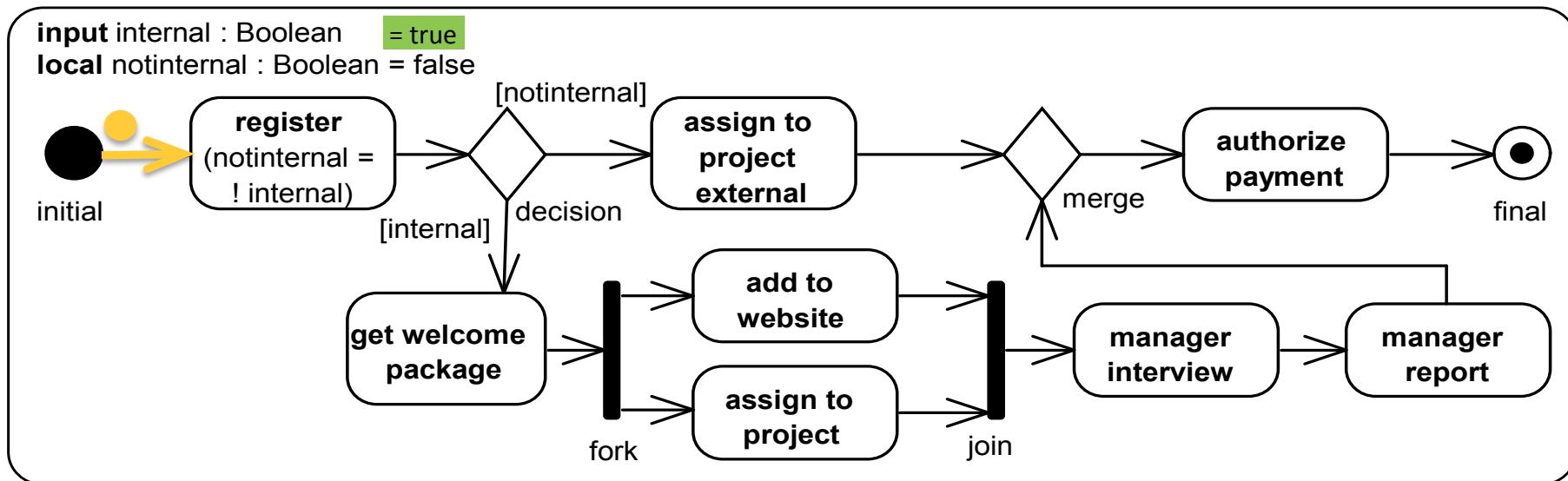
What is your proof of concept?

*fUML Activity Diagrams¹ of TTC 2015,
questionnaires¹ of LWC 2013,
energy auto-tuning case study*

¹ <https://github.com/christoff-buerger/racr>

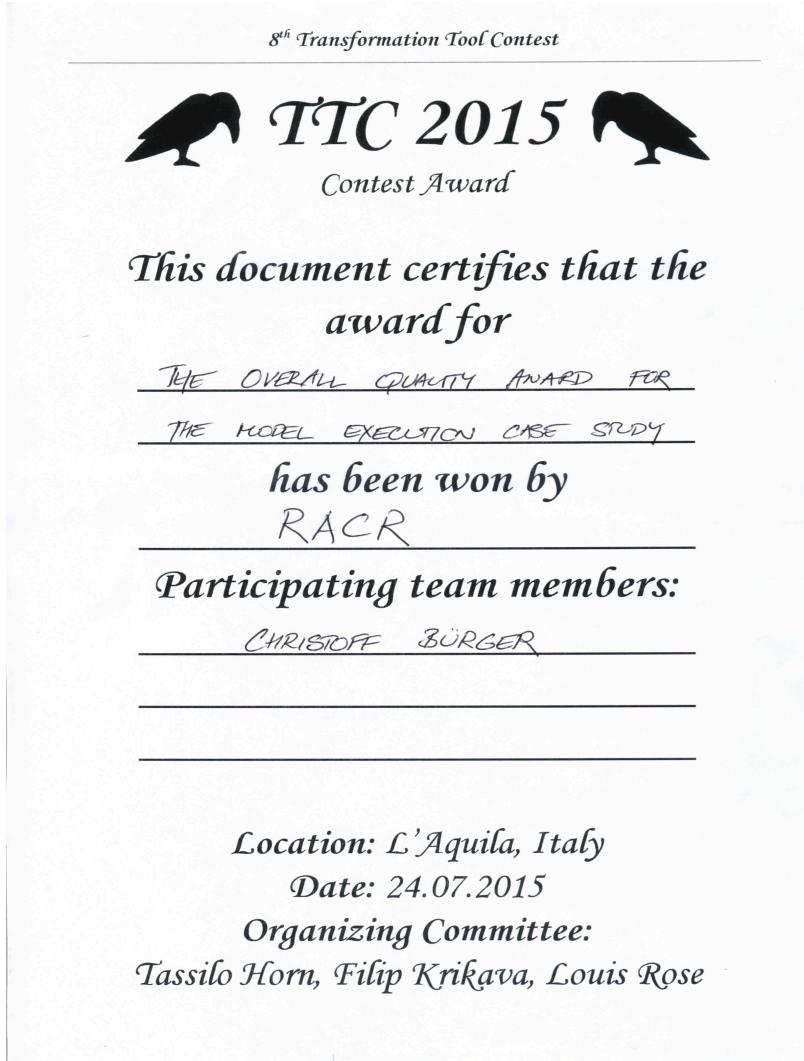
8th Transformation Tool Contest

Task: execution of *fUML Activity Diagrams*.



RACR solution: use enabled analyses to guide incremental state transformations.

8th Transformation Tool Contest

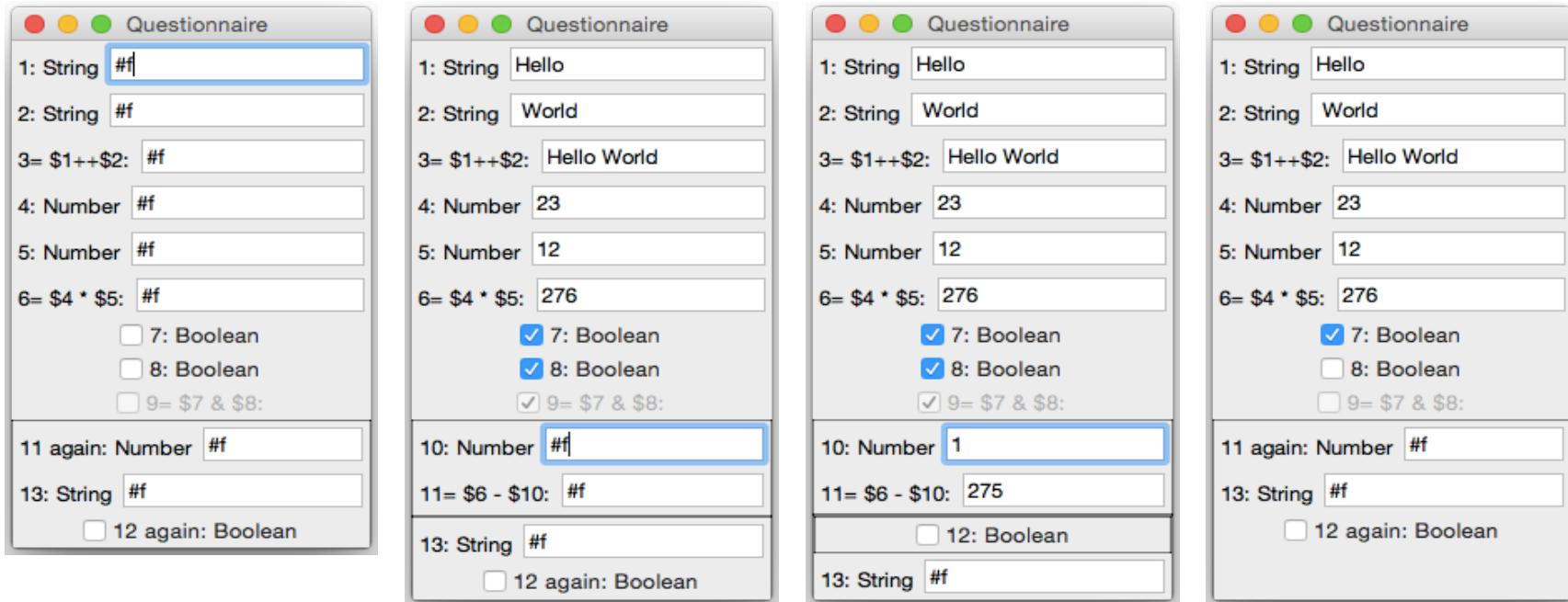


Reference

Christoff Bürger

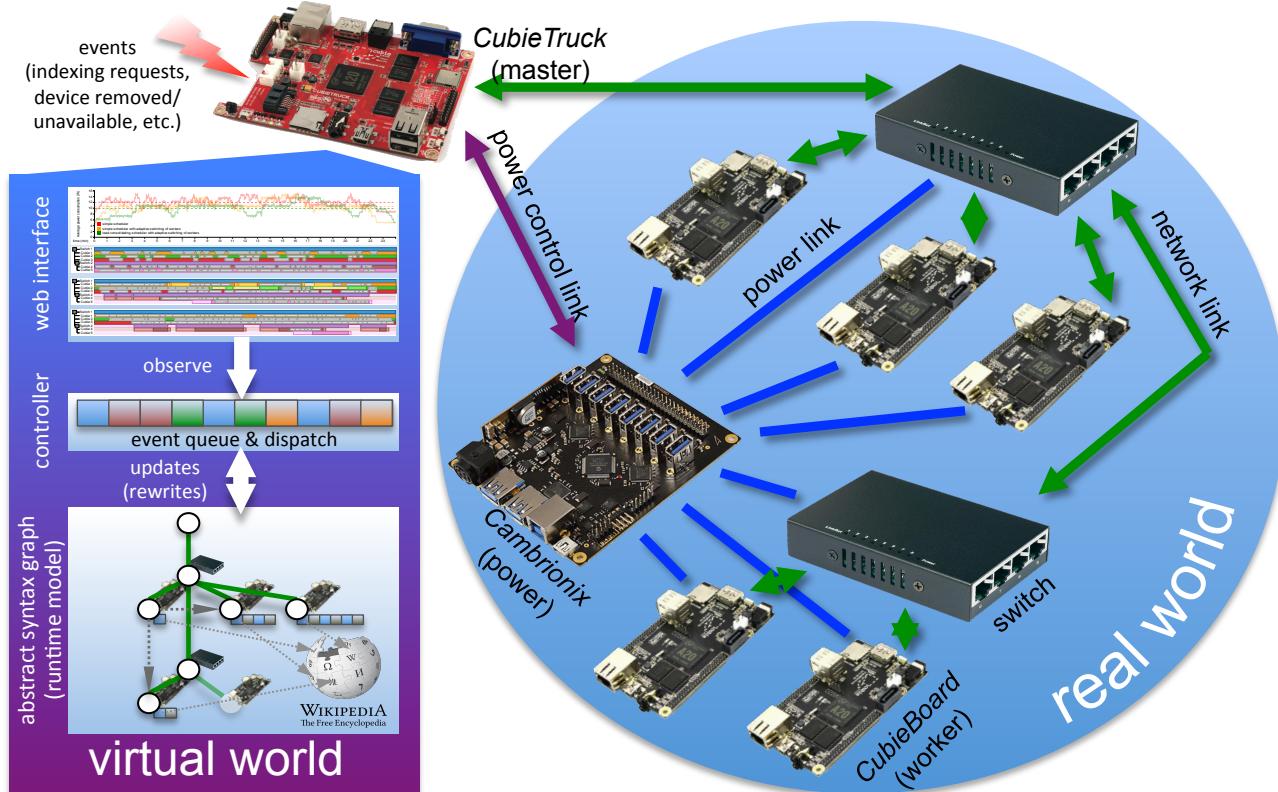
*fUML ACTIVITY DIAGRAMS WITH
RAG-CONTROLLED REWRITING:
A RACR SOLUTION OF THE TTC
2015 MODEL EXECUTION CASE
CEUR-WS.org, 2015*

Language Workbench Challenge 2013



RACR solution: incremental update of computed values & rendering.

Energy auto-tuning case study



Reference

Christoff Bürger et al.
USING REFERENCE ATTRIBUTE GRAMMAR-CONTROLLED REWRITING FOR ENERGY AUTO-TUNING

10th International
Workshop on
Models@run.time,
CEUR-WS.org, 2015

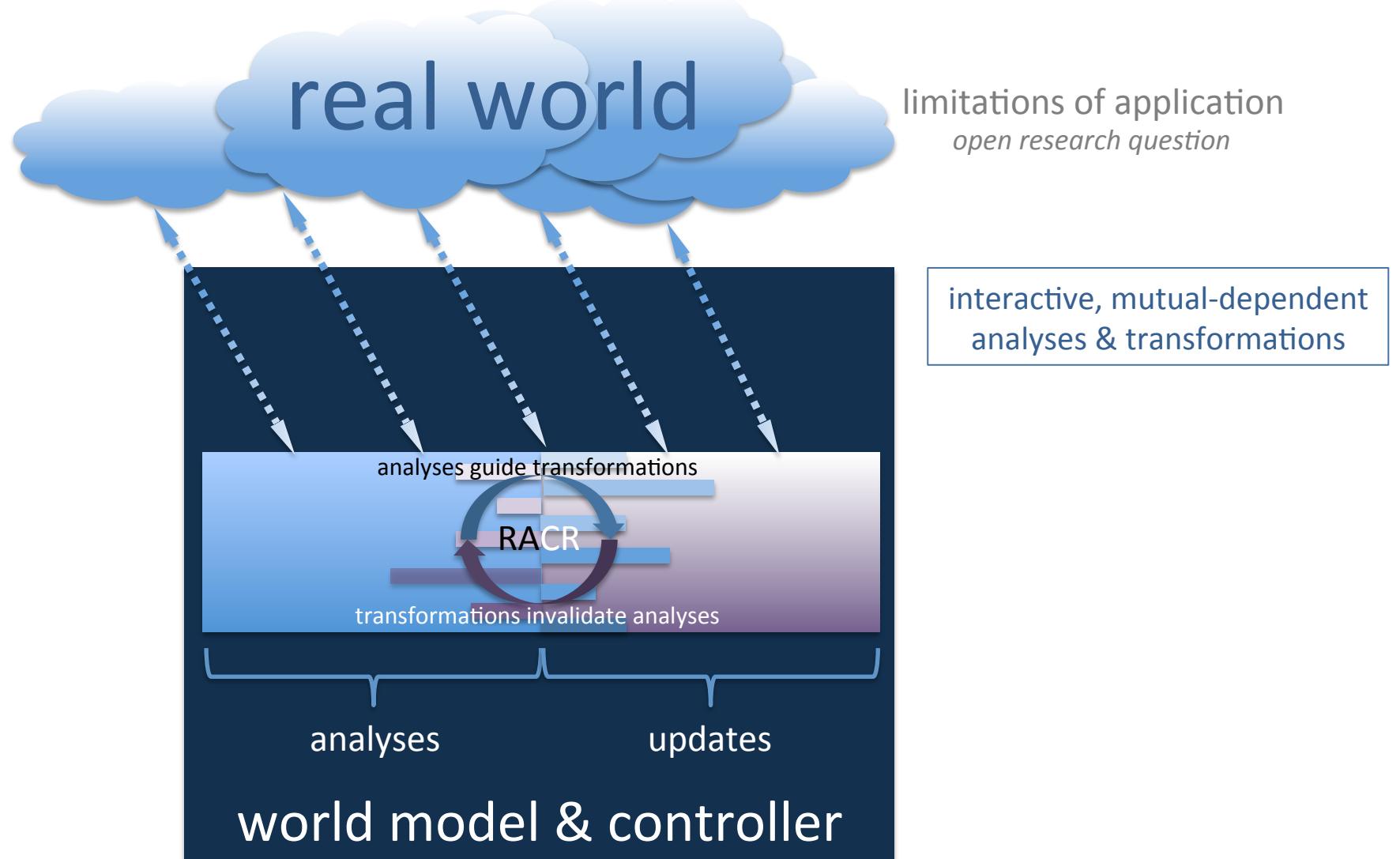
RACR solution: incremental energy efficient scheduling of indexing tasks.

The intention

What are you up to?

RAG-controlled rewriting for
incremental runtime models

Intended application: runtime models



The conclusion

What was it all about?

RAG-controlled rewriting enables incremental,
interactive, mutual-dependent analyses and
transformations

What was it all about?

RAG-controlled rewriting

- enables interactive, mutual-dependent ANALYSES and TRANSFORMATIONS
- by seamlessly combining REFERENCE ATTRIBUTE GRAMMARS and GRAPH REWRITING
 - such that ANALYSES CAN GUIDE AND DEDUCE REWRITES
 - and REWRITES UPDATE ANALYSES they influence
- using a well-balanced set of QUERY- and REWRITE-FUNCTIONS
 - constructing a DYNAMIC ATTRIBUTE DEPENDENCY GRAPH
 - that can be used for DYNAMIC ATTRIBUTE INVALIDATION
 - achieving INCREMENTAL ANALYSES AND TRANSFORMATIONS

incremental, interactive, mutual-dependent analyses and transformations

Backup slides

Dynamic dependency over-
approximations

Dynamic dependency over-approximations

