The $\ensuremath{\mathtt{C}}$ programs and their use

Christophe Pouzat

May 28, 2019

Contents

1	Intro	oductio	n	3
	1.1	Why C	C, gnuplot and the shell?	3
	1.2	Requir	red software and libraries	3
	1.3	A rem	ark on the code presentation	3
2	Defi	nitions	of structures and associated functions holding data	4
	2.1	ADU da	ata	4
		2.1.1	Data layout in the HDF5 files	4
		2.1.2	Data layout in the C code	4
		2.1.3	adu header and source	8
	2.2	DATA (Group mapping in C code	9
		2.2.1	adu_vector: an array of adu structures	9
		2.2.2	<pre>adu_vector header and source</pre>	14
	2.3	DYE		15
		2.3.1	DYE parameters in the HDF5 files	15
		2.3.2	DYE parameters layout in C code	15
		2.3.3	dye header and source	18
	2.4	ILLUM	INATION	18
		2.4.1	ILLUMINATION parameters in the HDF5 files	18
		2.4.2	ILLUMINATION parameters layout in C code	18
		2.4.3	illumination header and source	20
	2.5	CCD		21
		2.5.1	CCD parameters in the HDF5 files	21
		2.5.2	CCD parameters layout in C code	21
		2.5.3	ccd header and source	23
	2.6	Keepir	ng everything in one structure	23
		2.6.1	aba an added buffer approach structure:	24
		2.6.2	aba header and source	27
	2.7	Gettin	g [Fura] estimates	28
		2.7.1	time_series structure	

		2.7.2 Getting a [Fura] estimation	
		2.7.3 fura header and source	31
3	Wor	king the ratiometric estimator	32
	3.1	Some analytical details	32
	3.2	Goodness of fit functions definitions	33
		3.2.1 C code doing the tests	34
		3.2.2 gof header, source and test	36
	3.3	ratio structure and related functions	39
		3.3.1 C code related to ratio structures	39
		3.3.2 ratio header and source	52
4	Buil	ding the abaa library	5 3
		The abaa.h header file	53
	4.2	The Makefile	54
		4.2.1 Testing that everything works	56
	4.3	The SConstruct file	56
5	Our	<pre>first "user's" program: fit_ratiometric</pre>	57
•	5.1		57
	0.1	5.1.1 fit_ratiometric code	58
	5.2	Using fit_ratiometric	61
6	Get t 6.1	ting Fura concentration during a stimulation: fura_concentration	64
	0.1	Motivation	64
	6.0	6.1.1 fura_concentration code	
	6.2	Using fura_concentration	66
	6.3	fura_during_stim	67
	C 1	6.3.1 fura_during_stim code	68
	6.4	Using fura_during_stim	70
7		sing the time constant as a function of κ_F	71
	7.1	We start by fitting each of the free transients of data set DA_121219_E1.h5	
		7.1.1 First transient	
		7.1.2 Second transient	72
		7.1.3 Third transient	73
	7.2	Plotting $ au$ as a function of κ_F	74
8	А рі	ogram doing all that at once	74
	8.1	The aba_ratio program	74
		8.1.1 aba_ratio code	75
	8.2	Using aba_ratio	93
		8.2.1 Getting help	93
		822 Running aba ratio	94

8.2.3 Looking at the results		97
------------------------------	--	----

1 Introduction

We define in this document the C codes / programs developed for the analysis of the " β ecsin" data with the added buffer approach. Examples of use are also included.

1.1 Why C, gnuplot and the shell?

This document is the exploration of an idea: use the shell (bash or zsh) instead of the Python or R command line for interactive analysis and write the short functions performing the actual analysis in C. The motivation for this exploration comes from two books by Ben Klemens: Modeling With Data and 21st Century C. The main advantages of C compared to the other two languages are:

- Its stability (the programs written here are very likely to run unchanged in 20 years from now; what can be sure that this won't be true with Python).
- The development tools that come with it are just spectacular (see the very short and very clear book of Brian Gough An Introduction to GCC to understand what I mean by that).

1.2 Required software and libraries

Since a Bash or a Z shell are going to be used, Windows users will have to install Cygwin, Linux and MacOS users should have the bash shell by default and the zsh shell readily available from their package manager. To dig deeper into the amazing possibilities (and spectacular editorial support) of these tools, check From Bash to Z Shell. Conquering the Command Line by Kiddle, Peek and Stephenson.

The no-shell codes are going to be written in C, meaning that a C compiler together with the "classical" development tools (make, etc) are required. I'm going to use gcc here.

The heavy computational work is going to be performed mainly by the gsl (the GNU Scientific Library) that is easily installed through your package manager (from now one, for windows users, the "package manager" refers to the one of Cygwin). The graphs are be generated with gnuplot; for a quick tutorial check http://physicspmb.ukzn.ac.za/index.php/Gnuplot_tutorial, for an easy to navigate set of (sophisticated) recipes check http://www.gnuplotting.org/. The data sets are in HDF5 format and the C library, as well as the command line tools, developed by the HDF5 group are going to be heavily used here.

1.3 A remark on the code presentation

The literate programming approach is used here. This means that the code is broken into "manageable" pieces that are individually explained (when just reading the code

is not enough), they are then pasted together to give the code that will actually get compiled. These manageable pieces are called blocks and each block gets a name like: <<name-of-the-block>> upon definition. It is then referred to by this name when used in subsequent codes. See Schulte, Davison, Dye and Dominik (2010) A Multi-Language Computing Environment for Literate Programming and Reproducible Research for further explanations. The code blocks also include documentation in Doxygen format and we try to avoid writing twice the same thing, in the text and in the documentation. So if something is "missing" from the text description, please check the documentation within the block first to see if what you're looking for is there.

2 Definitions of structures and associated functions holding data

2.1 ADU data

2.1.1 Data layout in the HDF5 files

Our data stored in HDF5 format contain the actual ADU recordings in Groups called DATA. Each of those groups contains three datasets:

ADU an array of integers with 7 columns and as many rows as there were measurements. The first column is the time_index column, the second contains the ADU340 measurements (measurements at 340 nm in the ROI), then comes the ADU340B measurements (measurements at 340 nm in the ROB), the ADU360 measurements (at 360 nm in the ROI), the ADU360B measurements (at 360 nm in the ROB), the ADU380 measurements (at 380 nm in the ROI), the ADU380B measurements (at 380 nm in the ROB).

TIME_DELTA a scalar (see below).

TIME_OFFSET a scalar (see below).

To get the real time of each measurement, multiply the first column of ADU by TIME_DELTA and add TIME_OFFSET. The other columns of the ADU matrix contain the "raw" readings of the P of P_B pixels from the CCD chip.

2.1.2 Data layout in the C code

We will store these data in double format in a new type of structure called adu. Each of the seven column will become a single pointer to a <code>gsl_vector</code>. We define this structure in a specific code block in the next section.

adu type definition

adu_alloc definition It will be helpful to have an alloc function for adu structures:

adu_free definition It will also be helpful to have a free function for adu structures:

```
/** @brief Frees an [adu](@ref adu)

    @param[in,out] adu_ptr a pointer to an allocated [adu](@ref adu) structure
    @returns 0 if everything goes fine

*/
int adu_free(adu * adu_ptr) {
    gsl_vector_free(adu_ptr->ADU340);
    gsl_vector_free(adu_ptr->ADU340B);
    gsl_vector_free(adu_ptr->ADU360);
    gsl_vector_free(adu_ptr->ADU360B);
    gsl_vector_free(adu_ptr->ADU380B);
    gsl_vector_free(adu_ptr->ADU380B);
    gsl_vector_free(adu_ptr->ADU380B);
    gsl_vector_free(adu_ptr->TIME);
```

```
free(adu_ptr);
return 0;
}
```

adu_get_set **macro definitions** We define next macros with arguments giving an easy way to get and set values of specific members of adu structure:

```
/** @def adu_get(adu,member,i)
  * @brief A macro that returns value at index \a i of
  * member \a member from \a adu structure
  */
#define adu_get(adu,member,i) gsl_vector_get(adu->member,i)
/** @def adu_set(adu,member,i,x)
  * @brief A macro that sets value at index \a i of
  * member \a member from \a adu structure at \a x
  */
#define adu_set(adu,member,i,x) gsl_vector_set(adu->member,i,x)
```

adu_printf **definition** We now define a function that prints to the stdout the content of an adu structure:

```
/** @brief Prints [adu] (@ref adu) content to stdout
    @param[in] padu a pointer to an [adu](@ref adu) structure
    Oreturn 0 if everything goes fine
int adu_printf(adu * padu) {
  size_t nobs=(padu)->TIME->size;
 printf("# Time ADU340 ADU340B ADU360 ADU360B ADU380 ADU380B\n");
  for (size_t i=0; i<nobs; i++) {</pre>
   printf("%9.9g %8d %8d %8d %8d %8d \n",
          adu_get((padu),TIME,i),
          (int) adu_get(padu,ADU340,i),
           (int) adu_get(padu,ADU340B,i),
          (int) adu_get(padu,ADU360,i),
          (int) adu_get(padu,ADU360B,i),
          (int) adu_get(padu,ADU380,i),
          (int) adu_get(padu,ADU380B,i));
  }
 printf("\n\n");
 return 0;
```

adu_test **program definition** We now define a short program adu_test allowing us to test the functions we just defined. We store this program is a sub-directory called code.

```
/** @file adu_test.c
   * @brief Test program for adu structure and related
   * functions.
   */
#include <stdio.h>
```

```
#include <stdlib.h>
#include <string.h>
#include <gsl/gsl_vector.h>
<<adu-type-definition>>
<<adu_alloc>>
<<adu free>>
<<adu_get_set>>
<<adu_printf>>
int main()
  // Allocate an adu with 2 observations
  adu * adu_ptr = adu_alloc(2);
  printf("Allocated adu_ptr with two elements.\n");
  printf("Setting values of ADU340 field.\n");
  adu_set(adu_ptr,ADU340,0,1.0);
  adu_set(adu_ptr,ADU340,1,2.0);
  printf("Setting values of ADU340B field.\n");
  adu_set(adu_ptr,ADU340B,0,3.0);
  adu_set(adu_ptr,ADU340B,1,4.0);
  printf("Setting values of ADU360 field.\n");
  adu_set(adu_ptr,ADU360,0,5.0);
  adu_set(adu_ptr,ADU360,1,6.0);
  printf("Setting values of ADU360B field.\n");
  adu_set(adu_ptr,ADU360B,0,7.0);
  adu_set(adu_ptr,ADU360B,1,8.0);
  printf("Setting values of ADU380 field.\n");
  adu_set(adu_ptr,ADU380,0,9.0);
  adu_set(adu_ptr, ADU380, 1, 10.0);
  printf("Setting values of ADU380B field.\n");
  adu_set(adu_ptr,ADU380B,0,11.0);
  adu_set(adu_ptr,ADU380B,1,12.0);
  printf("Setting values of TIME field.\n");
  adu_set(adu_ptr,TIME,0,1.5);
  adu_set(adu_ptr,TIME,1,2.5);
  printf("The content of the structure is.\n");
  adu_printf(adu_ptr);
  // free allocated adu
  adu_free(adu_ptr);
  printf("Freed adu_ptr. Don't forget running valgrind!\n");
  return 0;
}
```

adu_test compilation, run, etc We compile the code with:

```
gcc -Wall -g -o code/adu_test code/adu_test.c -lgsl -lgslcblas -lm -std=gnu11

We run it with:

./code/adu_test

Allocated adu_ptr with two elements.
Setting values of ADU340 field.
Setting values of ADU340B field.
Setting values of ADU360 field.
Setting values of ADU360B field.
```

```
Setting values of ADU380 field.
Setting values of ADU380B field.
Setting values of TIME field.
The content of the structure is.
# Time ADU340 ADU340B ADU360 ADU360B ADU380 ADU380B
1.5 1 3 5 7 9 11
2.5 2 4 6 8 10 12
```

Freed adu_ptr. Don't forget running valgrind!

We run it with Valgrind to make sure that all the allocated memory has been freed upon program termination:

```
valgrind ./code/adu_test
==15210== Memcheck, a memory error detector
==15210== Copyright (C) 2002-2017, and GNU GPL'd, by Julian Seward et al.
==15210== Using Valgrind-3.14.0 and LibVEX; rerun with -h for copyright info
==15210== Command: ./code/adu_test
==15210==
Allocated adu_ptr with two elements.
Setting values of ADU340 field.
Setting values of ADU340B field.
Setting values of ADU360 field.
Setting values of ADU360B field.
Setting values of ADU380 field.
Setting values of ADU380B field.
Setting values of TIME field.
The content of the structure is.
   Time ADU340 ADU340B ADU360 ADU360B ADU380 ADU380B
     1.5
              1
                       3
                              5
                                      7
                                               9
     2.5
                         4
                                  6
                                          8
                                                  10
                                                           12
Freed adu_ptr. Don't forget running valgrind!
==15210==
==15210== HEAP SUMMARY:
==15210== in use at exit: 0 bytes in 0 blocks
==15210== total heap usage: 23 allocs, 23 frees, 4,656 bytes allocated
==15210==
==15210== All heap blocks were freed -- no leaks are possible
==15210==
==15210== For counts of detected and suppressed errors, rerun with: -v
==15210== ERROR SUMMARY: 0 errors from 0 contexts (suppressed: 0 from 0)
```

We are happy!

2.1.3 adu header and source

We define two code blocks for later use when we will define a library. Code block <<adu.h>> contains the types, macros and function prototypes we just defined.

```
<<adu-type-definition>>
adu * adu_alloc(size_t n_obs);
int adu_free(adu * adu_ptr);
<<adu_get_set>>
int adu_printf(adu * padu);
```

Code block <<adu.c>> contains the function definitions per se and gets stored in file code/adu.c:

```
/** \file adu.c
   \brief Definitions of functions related to [adu](@ref adu) structures
   */
#include "abaa.h"

<<adu_alloc>>
<<adu_free>>
<<adu_printf>></adu_printf>>
```

2.2 DATA Group mapping in C code

2.2.1 adu_vector: an array of adu structures

We will create a data type called adu_vector holding an array whose successive elements will be adu structures. Element 0 of our array will contain the load dataset and the following elements will contain the stim1, stim2, etc. datasets.

```
/** @brief Structure holding arrays of `adu` structures .
*/
typedef struct
{
    size_t nelt; //!< number of elements in the vector
    adu ** adu_v; //!< array of pointers to adu structures
} adu_vector;</pre>
```

adu_vector type definition

adu_vector_alloc **definition** It will be helpful to have an alloc function for adu_vector structures:

```
res->adu_v = malloc(nelt*sizeof(adu));
return res;
}
```

adu_vector_free **definition** It will also be helpful to have a free function for adu_vector structures:

```
/** @brief Frees an adu_vector

*
    * @param[in,out] adu_vector_ptr a pointer to an allocated adu_vector structure

* @returns 0 if everything goes fine

*/
int adu_vector_free(adu_vector * adu_vector_ptr) {
    for (size_t d_idx=0; d_idx<adu_vector_ptr->nelt; d_idx++)
        adu_free(adu_vector_ptr->adu_v[d_idx]);
    free(adu_vector_ptr->adu_v);
    free(adu_vector_ptr);
    return 0;
}
```

adu_vector_printf **definition** We now define a function that prints to the stdout the content of an adu_vector structure:

```
char dset[] = "/DATA";
hid_t gid = H5Gopen(file_id,dset,H5P_DEFAULT);
// Get info on group DATA
H5G_info_t group_info;
H5Gget_info(gid, &group_info);
size_t n_elt = (size_t) group_info.nlinks;
// Close Group
H5Gclose(gid);
return n_elt;
}
```

data_get_nelt

```
/** Obrief Allocates and initializes an `adu_vector` structure
* read from Group DATA in a file
* @param[in] file_id HDF5 file identifier
 * Creturn an allocated and initialized pointer to an adu_vector structure
adu_vector * adu_vector_read_from_file(hid_t file_id) {
 char *dsets[] = {"/DATA/load","/DATA/stim1","/DATA/stim2",
                   "/DATA/stim3","/DATA/stim4","/DATA/stim5",
                   "/DATA/stim6","/DATA/stim7","/DATA/stim8"};
 char STIM[256],DELTA[256],OFFSET[256];
  size_t n_elt = data_get_nelt(file_id);
 if (n_elt > 9) {
   fprintf(stderr, "Too many data sets (>9).\n");
   return NULL;
 adu_vector * data = adu_vector_alloc(n_elt);
 for (size_t d_idx=0; d_idx<n_elt; d_idx++) {
   STIM[0] = '\setminus 0';
   strcat(STIM,dsets[d_idx]);
   strcat(STIM,"/ADU");
    // load DataSet
   hsize_t dims[2];
   H5LTget_dataset_info(file_id,STIM,dims,NULL,NULL);
    size_t nobs = (size_t) dims[0];
    size_t ncol = (size_t) dims[1];
    int *ADU = malloc(nobs*ncol*sizeof(int));
   H5LTread_dataset_int(file_id,STIM,ADU);
   DELTA[0] = ' \setminus 0';
    strcat(DELTA,dsets[d_idx]);
    strcat(DELTA,"/TIME_DELTA");
    double delta;
   H5LTread_dataset_double(file_id,DELTA,&delta);
    OFFSET[0] = '\0';
    strcat(OFFSET,dsets[d_idx]);
    strcat(OFFSET,"/TIME_OFFSET");
   double offset;
   H5LTread_dataset_double(file_id,OFFSET,&offset);
    data->adu_v[d_idx] = adu_alloc(nobs);
   for (size_t i=0; i<nobs; i++) {</pre>
      adu_set((data->adu_v[d_idx]),TIME,i,offset+delta*((double) ADU[i*ncol]));
      adu_set((data->adu_v[d_idx]),ADU340,i,(double) ADU[i*ncol + 1]);
```

```
adu_set((data->adu_v[d_idx]),ADU340B,i,(double) ADU[i*ncol + 2]);
adu_set((data->adu_v[d_idx]),ADU360,i,(double) ADU[i*ncol + 3]);
adu_set((data->adu_v[d_idx]),ADU360B,i,(double) ADU[i*ncol + 4]);
adu_set((data->adu_v[d_idx]),ADU380,i,(double) ADU[i*ncol + 5]);
adu_set((data->adu_v[d_idx]),ADU380B,i,(double) ADU[i*ncol + 6]);
}
free(ADU);
}
return data;
}
```

adu_vector_read_from_file

adu_vector_test **program definition** The only "difficulty" in that code is the part that deals with opening / closing HDF5 files and Groups (within) those files.

```
/** Ofile adu_vector_test.c
* @brief test functions reading ADU data from an HDF5 file
         and printing them to the stdout
*/
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include <hdf5.h>
#include <hdf5_hl.h>
#include <gsl/gsl_vector.h>
<<adu-type-definition>>
<<adu_alloc>>
<<adu free>>
<<adu_get_set>>
<<adu_vector-type-definition>>
<<adu_vector_alloc>>
<<adu_vector_free>>
<<data_get_nelt>>
<<adu_vector_read_from_file>>
<<adu_printf>>
<<adu_vector_printf>>
#define FNAME "data_paper/data_beta_escin/DA_121219_E1.h5"
int main()
 // Open FILE
 char fname[] = FNAME;
 hid_t fid = H5Fopen (fname, H5F_ACC_RDONLY, H5P_DEFAULT);
 adu_vector * data = adu_vector_read_from_file(fid);
  // Close file
 H5Fclose (fid);
 if (data == NULL) return -1;
 adu_vector_printf(data);
 adu_vector_free(data);
 return 0;
}
```

adu_vector_test compilation, run, etc We compile the code with:

```
gcc -Wall -g -o code/adu_vector_test code/adu_vector_test.c -lgsl -lgslcblas -lhdf5 -lhdf5_hl -lm -std=gnu11
```

We test and "valgrind" it with:

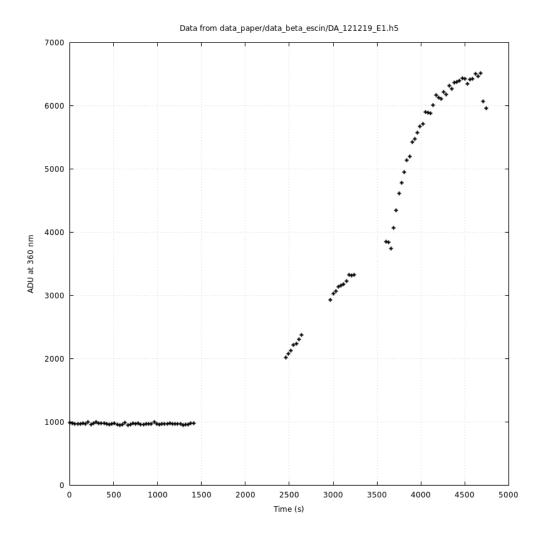
```
valgrind ./code/adu_vector_test > toto

==15218== Memcheck, a memory error detector
==15218== Copyright (C) 2002-2017, and GNU GPL'd, by Julian Seward et al.
==15218== Using Valgrind-3.14.0 and LibVEX; rerun with -h for copyright info
==15218== Command: ./code/adu_vector_test
==15218==
==15218==
==15218== in use at exit: 0 bytes in 0 blocks
==15218== in use at exit: 0 bytes in 0 blocks
==15218== total heap usage: 3,964 allocs, 3,964 frees, 1,666,868 bytes allocated
==15218==
==15218== All heap blocks were freed -- no leaks are possible
==15218==
==15218== For counts of detected and suppressed errors, rerun with: -v
```

We can make a few figures using gnuplot.

==15218== ERROR SUMMARY: 0 errors from 0 contexts (suppressed: 0 from 0)

```
unset key
set grid
set xlabel "Time (s)"
set ylabel "ADU at 360 nm"
plot 'toto' index 0 using 1:4 with points linecolor rgb "black" linewidth 2
```



2.2.2 adu_vector header and source

Again, we define two code blocks for later use with the library. First the "header" part <<adu_vector.h>>:

```
<<adu_vector-type-definition>>
adu_vector * adu_vector_alloc(size_t nelt);
int adu_vector_free(adu_vector * adu_vector_ptr);
int adu_vector_printf(adu_vector * padu_vector);
size_t data_get_nelt(hid_t file_id);
adu_vector * adu_vector_read_from_file(hid_t file_id);
```

Next, the function definitions <<adu_vector.c>> stored in file code/adu_vector.c:

```
/** \file adu_vector.c
  \brief Function definitions for [adu_vector](@ref adu_vector) structures
  */
#include "abaa.h"
```

```
<<adu_vector_alloc>>
<<adu_vector_free>>
<<data_get_nelt>>
<<adu_vector_read_from_file>>
<<adu_vector_printf>></adu_vector_printf>>
```

2.3 DYE

2.3.1 DYE parameters in the HDF5 files

The DYE group contains the following *scalar* datasets resulting from independent calibration experiments:

R_min_hat the estimated R_min parameter.

R_min_se the estimated R_min standard error.

R_max_hat the estimated R_max parameter.

R_max_se the estimated R_max standard error.

 K_{eff} the estimated K_{eff} parameter in μM .

K_eff_se the estimated K_eff standard error in μM .

 K_d hat the estimated K_d parameter in μM .

 K_d se the estimated K_d standard error in μM .

pipette_concentration the dye concentration in the pipette in μM .

2.3.2 DYE parameters layout in C code

We create a structure with that looks exactly like the corresponding HDF5 group.

```
/** @brief Structure holding dye parameters.
*/
typedef struct
{
    double R_min_hat; //!< estimated `R_min` parameter
    double R_min_se; //!< estimated `R_min` standard error
    double R_max_hat; //!< estimated `R_max` parameter
    double R_max_se; //!< estimated `R_max` standard error
    double K_eff_hat; //!< estimated `K_eff` parameter in \f$\mu{}M\f$
    double K_eff_se; //!< estimated `K_eff` standard error in \f$\mu{}M\f$
    double K_d_hat; //!< estimated `K_d` parameter in \f$\mu{}M\f$
    double K_d_se; //!< estimated `K_d` standard error in \f$\mu{}M\f$
    double pipette_concentration;//!< dye concentration in the pipette in \f$\mu{}M\f$
}
</pre>
```

dye type definition

```
/** @brief Returns a `dye` structure
* read from Group DYE in a file
 * @param[in] file_id HDF5 file identifier
 * @return a `dye` structure
dye dye_read_from_file(hid_t file_id) {
 dye res;
 H5LTread_dataset_double(file_id,"/DYE/R_min_hat",&res.R_min_hat);
 H5LTread_dataset_double(file_id,"/DYE/R_min_se",&res.R_min_se);
 H5LTread_dataset_double(file_id,"/DYE/R_max_hat",&res.R_max_hat);
 H5LTread_dataset_double(file_id,"/DYE/R_max_se",&res.R_max_se);
 H5LTread_dataset_double(file_id,"/DYE/K_eff_hat",&res.K_eff_hat);
 H5LTread_dataset_double(file_id,"/DYE/K_eff_se",&res.K_eff_se);
 H5LTread_dataset_double(file_id,"/DYE/K_d_hat",&res.K_d_hat);
 H5LTread_dataset_double(file_id,"/DYE/K_d_se",&res.K_d_se);
 {\tt H5LTread\_dataset\_double(file\_id,"/DYE/pipette\_concentration", \&res.pipette\_concentration);}
 return res;
}
```

<<dye_read_from_file>>

<<dye_printf>>

dye_test We now write a short program, dye_test.c, testing our new functions:

```
/** Offile dye_test.c
 * Obrief test functions reading DYE data from an HDF5 file
 * and printing them to the stdout
 */
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
```

```
#include <hdf5.h>
#include <hdf5_hl.h>
#include <gsl/gsl_vector.h>
<<dye-type-definition>>
<<dye_read_from_file>>
<<dye_printf>>
#define FNAME "data_paper/data_beta_escin/DA_121219_E1.h5"
int main()
 // Open FILE
  char fname[] = FNAME;
 hid_t fid = H5Fopen (fname, H5F_ACC_RDONLY, H5P_DEFAULT);
  dye dye_st = dye_read_from_file(fid);
  // Close file
 H5Fclose (fid);
  dye_printf(&dye_st);
 return 0;
```

dye_test compilation, run, etc We compile the code with:

```
gcc -Wall -g -o code/dye_test code/dye_test.c -lhdf5 -lhdf5_hl -lm -std=gnu11
```

We now run it with valgrind:

```
valgrind ./code/dye_test
```

```
==15226== Memcheck, a memory error detector
==15226== Copyright (C) 2002-2017, and GNU GPL'd, by Julian Seward et al.
==15226== Using Valgrind-3.14.0 and LibVEX; rerun with -h for copyright info
==15226== Command: ./code/dye_test
==15226==
# DYE parameters
# R_min_hat: 0.147143
# R_min_se: 0.00623826
# R_max_hat: 1.59923
# R_max_se: 0.0711322
# K_eff_hat: 1.09304
# K_eff_se: 0.362558
# K_d_hat: 0.225167
# K_d_se: 0.0114915
# pipette_concentration: 200
==15226==
==15226== HEAP SUMMARY:
==15226== in use at exit: 0 bytes in 0 blocks
==15226== total heap usage: 3,497 allocs, 3,497 frees, 1,233,749 bytes allocated
==15226==
==15226== All heap blocks were freed -- no leaks are possible
==15226==
==15226== For counts of detected and suppressed errors, rerun with: -v
==15226== ERROR SUMMARY: 0 errors from 0 contexts (suppressed: 0 from 0)
```

2.3.3 dye header and source

For later use, the "header part", <<dye.h>>:

```
<<dye-type-definition>>
dye dye_read_from_file(hid_t file_id);
int dye_printf(dye * pdye);
```

The function definitions <<dye.c>> stored in file code/dye.c:

```
/** \file dye.c
  \brief Function definitions for [dye](@ref dye) structures
  */
#include "abaa.h"
  <<dye_read_from_file>>
  <<dye_printf>>
```

2.4 ILLUMINATION

2.4.1 ILLUMINATION parameters in the HDF5 files

The ILLUMINATION group contains the following *scalar* datasets:

T_340 illumination duration at 340 nm in seconds.

T_360 illumination duration at 360 nm in seconds.

T_380 illumination duration at 380 nm in seconds.

2.4.2 ILLUMINATION parameters layout in C code

We create a structure with that looks exactly like the corresponding HDF5 group.

```
/** @brief Structure holding illumination parameters.
*/
typedef struct
{
    double T_340; //!< illumination duration at 340 nm (s)
    double T_360; //!< illumination duration at 360 nm (s)
    double T_380; //!< illumination duration at 380 nm (s)
} illumination;</pre>
```

illumination type definition

<<il>illumination_read_from_file>>

<<il>illumination_printf>>

```
/** Ofile illumination_test.c
* Obrief test functions reading ILLUMINATION data from an HDF5 file
          and printing them to the stdout
*/
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include <hdf5.h>
#include <hdf5_hl.h>
#include <gsl/gsl_vector.h>
<<il>illumination-type-definition>>
<<il><!re></re>illumination_read_from_file>>
#define FNAME "data_paper/data_beta_escin/DA_121219_E1.h5"
int main()
  // Open FILE
  char fname[] = FNAME;
  hid_t fid = H5Fopen (fname, H5F_ACC_RDONLY, H5P_DEFAULT);
```

```
illumination illumination_st = illumination_read_from_file(fid);
// Close file
H5Fclose (fid);
illumination_printf(&illumination_st);
return 0;
}
```

illumination_test compilation, run, etc We compile the code with:

```
gcc -Wall -g -o code/illumination_test code/illumination_test.c -lhdf5 -lhdf5_hl -lm -std=gnu11
```

We now run it with valgrind:

```
valgrind ./code/illumination_test
```

```
==15234== Memcheck, a memory error detector
==15234== Copyright (C) 2002-2017, and GNU GPL'd, by Julian Seward et al.
==15234== Using Valgrind-3.14.0 and LibVEX; rerun with -h for copyright info
==15234== Command: ./code/illumination_test
==15234==
# ILLUMINATION parameters
# T_340: 0.01
# T_360: 0.003
# T_380: 0.003
==15234==
==15234== HEAP SUMMARY:
==15234== in use at exit: 0 bytes in 0 blocks
==15234== total heap usage: 3,199 allocs, 3,199 frees, 964,286 bytes allocated
==15234== All heap blocks were freed -- no leaks are possible
==15234==
==15234== For counts of detected and suppressed errors, rerun with: -v
==15234== ERROR SUMMARY: 0 errors from 0 contexts (suppressed: 0 from 0)
```

2.4.3 illumination header and source

The header part in code block <<illumination.h>>:

```
<<iillumination-type-definition>>
illumination illumination_read_from_file(hid_t file_id);
int illumination_printf(illumination * pillumination);
```

The function definitions <<illumination.c>> stored in file code/illumination.c:

```
/** \file illumination.c
  \brief Function definitions for [illumination](@ref illumination) structures.
  */
#include "abaa.h"

<<illumination_read_from_file>>
<<illumination_printf>>
```

2.5 CCD

2.5.1 CCD parameters in the HDF5 files

The CCD group contains the following scalar datasets:

GAIN the CCD chip gain (from calibration experiments).

S_RO the read-out standard deviation of the CCD chip (from calibration experiments).

P the number of pixels in the Region Of Interest (ROI); the read-out variance should be added as many times as there are pixels when one computes the measurements variance.

P_B the number of pixels in the "background" Region Of Interest (ROB).

2.5.2 CCD parameters layout in C code

We create a structure with that looks exactly like the corresponding HDF5 group.

ccd **type definition** We store the *read-out variance* and not the read-out standard deviation.

```
/** @brief Structure holding ccd parameters.
*/
typedef struct
{
    double gain; //!< CCD chip gain
    double s2; //!< CCD chip read-out variance
    size_t P; //!< number of pixels in ROI
    size_t P_B; //!< number of pixels in ROB
} ccd;</pre>
```

```
return res;
}
```

<<cd_read_from_file>>

<<cd_printf>>

ccd_test We now write a short program, ccd_test.c, testing our new functions:

```
/** Ofile ccd_test.c
* @brief test functions reading CCD data from an HDF5 file
         and printing them to the stdout
*/
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include <hdf5.h>
#include <hdf5_hl.h>
#include <gsl/gsl_vector.h>
<<cd-type-definition>>
<<cd_read_from_file>>
<<cd_printf>>
#define FNAME "data_paper/data_beta_escin/DA_121219_E1.h5"
int main()
 // Open FILE
  char fname[] = FNAME;
 hid_t fid = H5Fopen (fname, H5F_ACC_RDONLY, H5P_DEFAULT);
 ccd ccd_st = ccd_read_from_file(fid);
  // Close file
 H5Fclose (fid);
  ccd_printf(&ccd_st);
 return 0;
```

ccd_test compilation, run, etc We compile the code with:

```
gcc -Wall -g -o code/ccd_test code/ccd_test.c -lhdf5 -lhdf5_hl -lm -std=gnu11
```

We now run it with valgrind:

```
valgrind ./code/ccd_test
```

```
==15242== Memcheck, a memory error detector
==15242== Copyright (C) 2002-2017, and GNU GPL'd, by Julian Seward et al.
==15242== Using Valgrind-3.14.0 and LibVEX; rerun with -h for copyright info
==15242== Command: ./code/ccd_test
==15242==
# CCD parameters
# Gain: 0.146
# Read-out variance: 268.96
# P: 3
# P_B: 448
==15242==
==15242== HEAP SUMMARY:
==15242== in use at exit: 0 bytes in 0 blocks
==15242== total heap usage: 3,251 allocs, 3,251 frees, 1,008,863 bytes allocated
==15242==
==15242== All heap blocks were freed -- no leaks are possible
==15242== For counts of detected and suppressed errors, rerun with: -v
==15242== ERROR SUMMARY: 0 errors from 0 contexts (suppressed: 0 from 0)
```

2.5.3 ccd header and source

The header part in code block <<cd.h>>:

```
<<ccd-type-definition>>
ccd ccd_read_from_file(hid_t file_id);
int ccd_printf(ccd * pccd);
```

The function definitions <<ccd.c>> stored in file code/ccd.c:

```
/** \file ccd.c
  \brif Function definitions for [ccd](@ref ccd) structures.
  */
#include "abaa.h"
  <<ccd_read_from_file>>
  <<ccd_printf>>
```

2.6 Keeping everything in one structure

We now define a new structure that holds everything.

2.6.1 aba an added buffer approach structure:

```
/** \brief Structure holding all the data
 */
typedef struct
{
   adu_vector * data; //!< a pointer to an adu_vector
   dye dye; //!< dye parameters
   illumination light; //!< illumination parameters
   ccd ccd; //!< ccd chip parameters
} aba;</pre>
```

aba type definition

```
/** \brief Allocates an [aba](@ref aba) structure
    The function allocates memory for an [aba](@ref aba) structure
    @returns a pointer to an allocated [aba](@ref aba)
*/
aba * aba_alloc()
{
    aba * res = malloc(sizeof(aba));
    return res;
}
```

aba_alloc

```
/** @brief Frees an [aba](@ref aba)

    @param[in,out] aba_ptr a pointer to an allocated [aba](@ref aba) structure
    @returns 0 if everything goes fine

*/
int aba_free(aba * paba)
{
    adu_vector_free(paba->data);
    free(paba);
    return 0;
}
```

aba_free

```
\return a pointer to an allocated and intialized [aba](@ref aba)
*/
aba * aba_read_from_file(hid_t file_id)
{
   aba * res = aba_alloc();
   res->data = adu_vector_read_from_file(file_id);
   res->dye = dye_read_from_file(file_id);
   res->light = illumination_read_from_file(file_id);
   res->ccd = ccd_read_from_file(file_id);
   return res;
}
```

aba_read_from_file

```
/** @brief Prints [aba](@ref aba) content to stdout
    @param[in] paba a pointer to an [aba](@ref aba) structure
    @return 0 if everything goes fine
    */
int aba_printf(aba * paba)
{
    dye_printf(&(paba->dye));
    ccd_printf(&(paba->ccd));
    illumination_printf(&(paba->light));
    adu_vector_printf(paba->data);
    return 0;
}
```

aba_printf

aba_test **program definition** We now write a short program, aba_test.c, testing our new functions:

```
/** Ofile aba_test.c
* Obrief test functions reading data from an HDF5 file
          and printing them to the stdout
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include <hdf5.h>
#include <hdf5_hl.h>
#include <gsl/gsl_vector.h>
<<adu-type-definition>>
<<adu_alloc>>
<<adu_free>>
<<adu_get_set>>
<<adu_vector-type-definition>>
<<adu_vector_alloc>>
<<adu_vector_free>>
<<data_get_nelt>>
<<adu_vector_read_from_file>>
<<adu_printf>>
```

```
<<adu_vector_printf>>
<<dye-type-definition>>
<<dye_read_from_file>>
<<dye_printf>>
<<il>illumination-type-definition>>
<<il>illumination_read_from_file>>
<<cd-type-definition>>
<<ccd_read_from_file>>
<<cd_printf>>
<<aba-type-definition>>
<<aba_alloc>>
<<aba_free>>
<<aba_read_from_file>>
<<aba_printf>>
#define FNAME "data_paper/data_beta_escin/DA_121219_E1.h5"
int main()
 // Open FILE
 char fname[] = FNAME;
 hid_t fid = H5Fopen (fname, H5F_ACC_RDONLY, H5P_DEFAULT);
 aba * paba = aba_read_from_file(fid);
  // Close file
 H5Fclose (fid);
 aba_printf(paba);
 aba_free(paba);
 return 0;
}
```

aba_test compilation and run We compile the code with:

```
gcc -Wall -g -o code/aba_test code/aba_test.c -lgsl -lgslcblas -lhdf5 -lhdf5_hl -lm -std=gnu11
```

We run it with valgrind:

```
valgrind ./code/aba_test > toto
```

```
==15250== Memcheck, a memory error detector
==15250== Copyright (C) 2002-2017, and GNU GPL'd, by Julian Seward et al.
==15250== Using Valgrind-3.14.0 and LibVEX; rerun with -h for copyright info
==15250== Command: ./code/aba_test
==15250==
==15250==
==15250== HEAP SUMMARY:
==15250== in use at exit: 0 bytes in 0 blocks
==15250== total heap usage: 4,834 allocs, 4,834 frees, 2,402,637 bytes allocated
==15250==
==15250== All heap blocks were freed -- no leaks are possible
==15250==
==15250== For counts of detected and suppressed errors, rerun with: -v
==15250== ERROR SUMMARY: 0 errors from 0 contexts (suppressed: 0 from 0)
```

We can check the first lines of the file with:

./code/aba_test | head -n 30

```
# DYE parameters
# R_min_hat: 0.147143
# R_min_se: 0.00623826
# R_max_hat: 1.59923
# R_max_se: 0.0711322
# K_eff_hat: 1.09304
# K_eff_se: 0.362558
# K_d_hat: 0.225167
# K_d_se: 0.0114915
# pipette_concentration: 200
# CCD parameters
# Gain: 0.146
# Read-out variance: 268.96
# P: 3
# P_B: 448
# ILLUMINATION parameters
# T_340: 0.01
# T_360: 0.003
# T_380: 0.003
# Loading curve with 104 elements
# Time ADU340 ADU340B ADU360 ADU360B ADU380 ADU380B

    0.021
    979
    142343
    988
    141856
    1049
    153272

    30.021
    943
    141974
    980
    141505
    1058
    153314

   30.021
   60.021 980 141816 973 141148 1051 153637
  90.021 962 141874 977 141411 1038 153397
120.021 978 142411 972 141660 1056 153538
150.021 979 141842 980 141473 1073 153736
```

And the last lines with:

./code/aba_test | tail

```
3469.215 3129 112060
                        3541 110349 4113 126799
3469.315 3143 112072
                        3559 110474 4113 126914
3469.415 3113 111978
                        3576 110281 4173 127001
       3125 112120
3099 112026
                        3525 110584
3578 110473
                                    4151
4196
3469.515
                                            126857
                                           126917
3469.615
3469.715 3130 111965
                        3575 110571 4132 126905
3469.815 3116 112025 3586 110532 4183 126895
3469.915 3104 112065 3519 110560 4171 127004
```

2.6.2 aba header and source

The header part in code block <<aba.h>>:

```
<<aba-type-definition>>
aba * aba_alloc();
int aba_free(aba * paba);
aba * aba_read_from_file(hid_t file_id);
int aba_printf(aba * paba);
```

The function definitions <<aba.c>> stored in file code/aba.c:

```
/** \file aba.c
  \brief Function definitions for [aba](@ref aba) structures.

*/
#include "abaa.h"

<<aba_alloc>>
<<aba_free>>
<<aba_read_from_file>>
<<aba_printf>></aba_printf>>
```

2.7 Getting [Fura] estimates

We define now a time_series structure and functions for getting [Fura] estimates from an aba structure.

2.7.1 time_series structure

ts type definition

```
/** \brief Allocates a [ts](@ref ts)

The function allocates memory for a [ts](@ref ts) structure

\param[in] n_obs the number of obserations
\returns a pointer to an allocated [ts](@ref ts)

*/

ts * ts_alloc(size_t n_obs) {
    ts * res = malloc(sizeof(ts));
    res->TIME = gsl_vector_alloc(n_obs);
    res->AMPLITUDE = gsl_vector_alloc(n_obs);
    return res;
}
```

```
/** @fn int ts_free(ts * pts)
    @brief Frees memory taken up by a [ts](@ref ts)

    @param[in,out] ptd a pointer to a [ts](@ref ts)
    @returns 0 if everything goes fine

*/
int ts_free(ts * pts) {
    gsl_vector_free(pts->TIME);
    gsl_vector_free(pts->AMPLITUDE);
    free(pts);
    return 0;
}
```

 ts_free

ts_fprintf **definition** We now define a function that prints to STREAM the content of an ts structure:

```
/** \struct ts_vector
  \brief Structure holding arrays of [ts](@ref ts) structures .

*/
typedef struct
{
    size_t nelt; //!< number of elements in the vector
    ts ** ts_v; //!< array of pointers to [ts](@ref ts) structures
} ts_vector;</pre>
```

ts_vector

ts_vector_alloc **definition** It will be helpful to have an alloc function for ts_vector structures:

```
/** @brief Allocates an [ts_vector](@ref ts_vector)

*
    * The function allocates memory for a [ts_vector](@ref ts_vector) structure

*
    * @param[in] nelt the number of stimulation
    * @returns a pointer to an allocated [ts_vector](@ref ts_vector)

*/

ts_vector * ts_vector_alloc(size_t nelt) {
    ts_vector * res = malloc(sizeof(ts_vector));
    res->nelt = nelt;
    res->ts_v = malloc(nelt*sizeof(ts));
    return res;
}
```

ts_vector_free **definition** It will also be helpful to have a free function for ts_vector structures:

ts_vector_fprintf **definition** We now define a function that prints to a stream the content of a ts_vector structure:

```
/** @brief Prints [ts_vector](@ref ts_vector) content to `stream`
    @param[in] stream a pointer to an output "file"
    @param[in] pts_vector a pointer to a [ts_vector](@ref ts_vector) structure
    @return 0 if everything goes fine

*/
int ts_vector_fprintf(FILE * stream, ts_vector * pts_vector) {
    for (size_t d_idx=0; d_idx<pts_vector->nelt; d_idx++) {
        size_t nobs=(pts_vector->ts_v[d_idx])->TIME->size;
        if (d_idx == 0) {
            fprintf(stream,"# Loading curve with %d elements\n", (int) nobs);
        } else {
            fprintf(stream,"# Stim %d with %d elements\n", (int) d_idx, (int) nobs);
        }
        ts_fprintf(stream,pts_vector->ts_v[d_idx]);
    }
    return 0;
}
```

2.7.2 Getting a [Fura] estimation

fura_est We define a function taking a pointer to an aba structure and returning the estimated [Fura] from it as a [ts_vector] structure.

```
/** \fn ts_vector * fura_est(aba * paba)
    \brief Get [Fura] time series from [aba](@ref aba) structure
    __It is assumed that when the maximal background subtracted fluorescence at
    360 nm is observed, the fura concentration in the cell and in the pipette
    are identical (no extrapolation based on a fit is performed).__
    \param[in] paba a pointer to an [aba](@ref aba) structure
    \return a pointer to an allocated and initialized [ts_vector](@ref ts_vector)
ts_vector * fura_est(aba * paba) {
  // Get the number of stim + 1 in paba
  size_t nelt=paba->data->nelt;
  // Allocates result
  ts_vector *res=ts_vector_alloc(nelt);
  // Get [Fura] in the pipette \,
  double F_p = paba->dye.pipette_concentration;
  // Get the inverse of the number of pixels in \ensuremath{\text{ROI}}
  double inv_P = 1.0/(double)paba->ccd.P;
  \ensuremath{/\!/} Get the inverse of the number of pixels in ROB
  double inv_P_B = 1.0/(double)paba->ccd.P_B;
  double max_adu;
  for (size_t i=0; i<nelt; i++) {</pre>
    gsl_vector *adu360 = paba->data->adu_v[i]->ADU360;
    gsl_vector *adu360B = paba->data->adu_v[i]->ADU360B;
    gsl_vector *time = paba->data->adu_v[i]->TIME;
    res->ts_v[i] = ts_alloc(adu360->size);
    for (size_t j=0; j<adu360->size; j++) {
      double fura_c = gsl_vector_get(adu360,j)*inv_P-
        gsl_vector_get(adu360B,j)*inv_P_B;
      gsl_vector_set(res->ts_v[i]->AMPLITUDE,j,fura_c);
     gsl_vector_set(res->ts_v[i]->TIME,j,gsl_vector_get(time,j));
    if (i == 0)
      max_adu = gsl_vector_max(res->ts_v[i]->AMPLITUDE);
    gsl_vector_scale(res->ts_v[i]->AMPLITUDE,F_p/max_adu);
  return res;
```

2.7.3 fura header and source

Again, we define two code blocks for later use with the library. First the "header" part <<fura.h>>:

```
<<ts-type-definition>>
<<ts_vector-type-definition>>
ts * ts_alloc(size_t n_obs);
```

```
int ts_free(ts * pts);
int ts_fprintf(FILE * stream, ts * pts);
ts_vector * ts_vector_alloc(size_t nelt);
int ts_vector_free(ts_vector * pts_vector);
int ts_vector_fprintf(FILE * stream, ts_vector * pts_vector);
ts_vector * fura_est(aba * paba);
```

Next, the function definitions <<fura.c>> stored in file code/fura.c:

```
/** \file fura.c
  \brief Function definitions for [Fura] related calculations
  */
#include "abaa.h"

<<ts_alloc>>
  <<ts_free>>
  <<ts_free>>
  <<ts_free>>
  <<ts_order="font-style="text-align: center;">
  <<ts_free>>
  <<ts_vector_alloc>>
  <<ts_vector_free>>
  <<ts_vector_free>>
  <<ts_vector_fprintf>>
  <<ts_vector_fprintf>>
  <<ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf>></ts_vector_fprintf</ts></t
```

3 Working the ratiometric estimator

3.1 Some analytical details

We keep going with the definition of functions allowing us to work with the "classical" ratiometric estimator that we write, at time t_i , as Joucla et al (2010), Eq. 8, p. 1133:

$$\widehat{Ca}(t_i) = K_{eff} \frac{r(t_i) - R_{min}}{R_{max} - r(t_i)},$$
(1)

where K_{eff} , R_{min} and R_{max} are calibrated parameters (assumed exactly known for now) and where Joucla et al (2010), Eq. 6, p. 1133:

$$r(t_i) = \frac{(P T_{e,340} G)^{-1} ADU_{340} - s_{B,340}}{(P T_{e,380} G)^{-1} ADU_{380} - s_{B,380}},$$
(2)

where the auto-fluorescence $s_{B,340}$ and $s_{B,380}$ are also assumed known for now. Our model for the fluorescence intensity at each wavelength is Joucla et al (2010), Eq. 2a and 2b:

$$F_{340} = \left\{ \frac{[Fura]_{total} \phi}{K_{Fura} + [Ca^{2+}]} \left(R_{min} K_{eff} + R_{max} [Ca^{2+}] \right) + s_{B,340} \right\} T_{e,340} P, \qquad (3)$$

and

$$F_{380} = \left\{ \frac{[Fura]_{total} \phi}{K_{Fura} + [Ca^{2+}]} \left(K_{eff} + [Ca^{2+}] \right) + s_{B,380} \right\} T_{e,380} P, \tag{4}$$

where K_{Fura} is a calibrated parameter, P is the number of pixels of the region of interest (ROI), $T_{e,\lambda}$ is the exposure time at wavelength λ , $s_{B,\lambda}$ is the auto-fluorescence at wavelength λ –assumed homogeneous among the P pixels of the ROI–, $[Fura]_{total} \phi$, is the total (bound plus free) concentration of Fura in the cell multiplied by a dimensionless experiment specific parameter, ϕ , lumping together the quantum efficiency, the neurite thickness, etc.

Under our assumptions (see the slide 56 of my lecture) we have:

$$ADU_{\lambda}(t_i) = G F_{\lambda}(t_i) + \epsilon G \sqrt{F_{\lambda}(t_i) + \sigma_{read-out}^2},$$
 (5)

where $F_{\lambda}(t_i)$ is given by Eq. 3 and 4 and where $\epsilon \sim \mathcal{N}(0,1)$ (ϵ is a Gaussian random variable with mean 0 and variance 1). In words: $ADU_{\lambda}(t_i)$ has a Gaussian distribution with mean $GF_{\lambda}(t_i)$ and variance $G^2(F_{\lambda}(t_i) + \sigma_{read-out}^2)$.

So, to have the variance of $\widehat{ADU_{\lambda}}(t_i)$ we need to know $F_{\lambda}(t_i)$ and for that we need to know $Ca(t_i)$ precisely what we want to estimate... But since $\widehat{EADU_{\lambda}}(t_i)$ (the expected value) is $\widehat{GF_{\lambda}}(t_i)$ we can use the observed value $\widehat{ADU_{\lambda}}(t_i)$ of $\widehat{ADU_{\lambda}}(t_i)$ as a guess for $\widehat{GF_{\lambda}}(t_i)$ leading to:

$$\hat{\sigma}_{ADU_{\lambda}(t_i)}^2 = G \, \widehat{ADU}_{\lambda}(t_i) + G^2 \, \sigma_{read-out}^2 \approx \sigma_{ADU_{\lambda}(t_i)}^2 \,. \tag{6}$$

Now that we have a $\hat{\sigma}^2_{ADU_{\lambda}(t_i)}$ we can work with, we want to get $\hat{\sigma}^2_{r(t_i)}$ and $\hat{\sigma}^2_{\widehat{Ca}(t_i)}$. We could use the propagation of uncertainty (or error propagation) together with Eq. 2 and 1 for that (and I will do it at some point), but now we will use a "quick and dirty" Monte Carlo approach. We will draw a thousand pair of vectors $\left(ADU_{340}^{[j]}(t_i), ADU_{380}^{[j]}(t_i)\right)$ $(j=1,\ldots,1000)$ from two independent Gaussian distributions:

$$ADU_{\lambda}^{[j]}(t_i) = ADU_{\lambda}(t_i) + \epsilon_i \,\hat{\sigma}_{ADU_{\lambda}(t_i)} \,, \tag{7}$$

plug-in these pairs into Eq. 2 giving us 1000 $r^{[j]}(t_i)$ before plugging in the latter into Eq. 1 leading to 1000 $\widehat{Ca}^{[j]}(t_i)$. The empirical variance of these observation will be used as $\widehat{\sigma}^2_{\widehat{Ca}(t_i)}$.

3.2 Goodness of fit functions definitions

Having a standard error for our ratiometric estimator (or at least an estimated standard error) gives us a yardstick for measuring the distance between observed data and a fitted

model like a mono-exponential relaxation. When we fit a mono-exponential relaxation to a transient, the normalized residuals—that is the difference between individual observations and their fitted values divided by the standard error of the observations—should (almost) follow a standard normal distribution (a normal distribution with mean 0 and variance 1)—I write almost because the model parameters have been fitted from the same data—. We can therefore check if the residual follow this theoretical standard normal distribution both with a formal test like an Anderson-Darling test and with a quantile-quantile plot. We can also check if the residual sum of squares follows a χ^2 distribution with the proper number of degrees of freedom (the number of observed values minus the number of fitted parameters). We should also check that the residuals do not exhibit any autocorrelation (they should be identically and *independently* drawn), we can check that with a graph of the empirical autocorrelation function of the residuals and with a formal test. We define next a few functions that perform these tests.

3.2.1 C code doing the tests

```
/** Obrief Returns the Anderson-Darling statistics assuming a
 * standard normal distribution for the data
 * The data are contained in the `gsl_vector` pointed to
   by `data`. If the content is not sorted (`sorted==false`)
 * the data are first copied before being sorted.
* Oparam[in] data pointer to a `gsl_vector` containing the data
* Oparam[in] sorted a boolean indicated if the `data` content is
              already sorted (`true`) or not (`false`)
* Oreturns a double with the Anderson-Darling statistics
double AndersonDarling_W2(gsl_vector * data, bool sorted)
 gsl_vector * data_s;
 if (sorted == false)
   data_s = gsl_vector_alloc(data->size);
   gsl_vector_memcpy(data_s,data);
   gsl_sort_vector(data_s);
 }
 else
 {
   data_s = data;
 size_t n = data->size:
 double n_d = (double) n;
 double A=0.;
 for (size_t i=1; i<=n; i++)
   double y = gsl_vector_get(data_s,i-1);
   double Phi_at_y = gsl_cdf_gaussian_P(y,1.0);
   A += (2*i-1.)*log(Phi_at_y)+(2*(n_d-i)+1)*log(1-Phi_at_y);
A /= -n_d;
```

```
if (sorted == false)
   gsl_vector_free(data_s);
   return A-n_d;
}
```

AndersonDarling_W2 definition

adinf **definition** This function returns the asymptotic value of the Anderson-Darling distribution. It is adapted from Marsaglia and Marsaglia (2004) Evaluating the Anderson-Darling Distribution.

AD_cdf_P **definition** This function returns $Pr\{W2 \mid = z\}$, where W2 is the Anderson-Darling statistics, using a correction for finite sample size, see Marsaglia and Marsaglia (2004) Evaluating the Anderson-Darling Distribution.

```
/** @brief Returns the finite sample cdf of the Anderson-Darling
    statistics.

Adaptation of function `AD` of Marsaglia & Marsaglia (2004)
[J. Stat. Software 9(2): 1-5](https://www.jstatsoft.org/article/view/v009i02).

@param[in] n an integer with the sample size
    @param[in] z a double the observed statistics value
    @returns a double Prob{W2 <= z}

*/
double AD_cdf_P(int n,double z)
{
    double x=adinf(z);
    if(x>.8)
    {
        v=(-130.2137+(745.2337-(1705.091-(1950.646-(1116.360-255.7844*x)*x)*x)*x)*x)*x)/n;
        return x+v;
    }
    double c=.01265+.1757/n;
```

```
if(x<c)
{
    v=x/c;
    v=sqrt(v)*(1.-v)*(49*v-102);
    return x+v*(.0037/(n*n)+.00078/n+.00006)/n;
}
v=(x-c)/(.8-c);
v=-.00022633+(6.54034-(14.6538-(14.458-(8.259-1.91864*v)*v)*v)*v)*v;
    return x+v*(.04213+.01365/n)/n;
}</pre>
```

3.2.2 gof header, source and test

The header part in code block <<gof.h>>:

```
double AndersonDarling_W2(gsl_vector * data, bool sorted);
double aspa_adinf(double z);
double AD_cdf_P(int n,double z);
```

The function definitions <<gof.c>> stored in file code/gof.c:

```
/** \file gof.c
  \brief Functions defining goodness of fit tests.
 */

<<AndersonDarling_W2>>
<<adinf>>
<<AD_cdf_P>>
```

We define next a program testing the goodness of fit functions

```
#include <stdio.h>
#include <stdlib.h>
#include <stdbool.h>
#include <string.h>
#include <math.h>
#include <gsl/gsl_math.h>
#include <gsl/gsl_vector.h>
#include <gsl/gsl_rng.h>
#include <gsl/gsl_randist.h>
#include <gsl/gsl_cdf.h>
#include <gsl/gsl_sort.h>
#include <gsl/gsl_sort_vector.h>
<<AndersonDarling_W2>>
<<adinf>>
<<AD_cdf_P>>
int main()
{
gsl_rng * r;
```

```
const gsl_rng_type * T;
gsl_rng_env_setup();
T = gsl_rng_default;
r = gsl\_rng\_alloc (T);
double w90 = 1.93295783274159;
double w95 = 2.4923671600494096;
double w99 = 3.8781250216053948;
printf("Test asymptotic cdf using Marsaglia & Marsaglia values:\n");
printf("Pr(W2 < 1.93295783274159) = \%g, the theoretical value is 0.90\n", adinf(w90));
printf("Pr(W2 < 2.4923671600494096) = %g, the theoretical value is 0.95\n", adinf(w95));
printf("Pr(W2 < 3.8781250216053948) = %g, the theoretical value is 0.99\n", adinf(w99));
printf("\n");
printf("Generating a sample of size 100 with Box-Müller (mean 0 and var 1)\n");
gsl_vector * sample = gsl_vector_alloc(100);
for (size_t i=0; i < sample->size; i++)
  gsl_vector_set(sample,i,gsl_ran_gaussian(r,1.0));
double W2 = AndersonDarling_W2(sample,false);
printf("The Anderson-Darling statistics, W2, value is: %g\n", W2);
printf("Prob(W2 \le %g) = %g\n", W2, AD_cdf_P(sample->size, W2));
gsl_vector_free(sample);
printf("Generating a sample of size 750 with the ratio of uniforms (mean 0 and var 1)\n");
sample = gsl_vector_alloc(750);
for (size_t i=0; i < sample->size; i++)
 gsl_vector_set(sample,i,gsl_ran_ugaussian_ratio_method(r));
W2 = AndersonDarling_W2(sample,false);
printf("The Anderson-Darling statistics, W2, value is: %g\n", W2);
printf("Prob(W2 \le %g) = %g\n", W2, AD_cdf_P(sample->size, W2));
gsl_vector_free(sample);
printf("Generating a sample of size 500 with the ziggurat (mean 0 and var 1.2)\n");
sample = gsl_vector_alloc(500);
for (size_t i=0; i < sample->size; i++)
 gsl_vector_set(sample,i,gsl_ran_gaussian_ziggurat(r, 1.2));
W2 = AndersonDarling_W2(sample,false);
printf("The Anderson-Darling statistics, W2, value is: g^n, W2);
printf("Prob(W2 <= %g) = %g\n", W2, AD_cdf_P(sample->size, W2));
printf("\n");
printf("Generating now 10,000 samples of size 100 form a standard normal with the ziggurat\n");
printf("method and computing the cdf of the W2 statistics...\n");
double W2_cdf_sample[10000];
sample = gsl_vector_alloc(100);
for (size_t rep=0; rep < 10000; rep++) {</pre>
  for (size_t i=0; i < sample->size; i++)
   gsl_vector_set(sample,i,gsl_ran_gaussian_ziggurat(r, 1.0));
 W2_cdf_sample[rep] = AD_cdf_P(sample->size,AndersonDarling_W2(sample,false));
gsl_vector_free(sample);
gsl_sort(W2_cdf_sample,1,10000);
double decile[9]:
printf("The theoretical deciles of the cdf of the W2 statistics are:\n");
printf("0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9.\n");
printf("The empirical deciles of the cdf of the W2 statistics are:\n");
for (size_t i=0; i < 9; i++)
 decile[i] = W2\_cdf\_sample[(i+1)*1000-1];
decile[1],decile[2],decile[3],decile[4],decile[5],decile[6],
```

```
decile[7],decile[8]);
printf("\n");
printf("Generating now 10,000 samples of size 100 form a normal(0,1.05) with the ziggurat\n");
printf("method and computing the cdf of the W2 statistics...\n");
sample = gsl_vector_alloc(100);
for (size_t rep=0; rep < 10000; rep++) {</pre>
 for (size_t i=0; i < sample->size; i++)
    gsl_vector_set(sample,i,gsl_ran_gaussian_ziggurat(r, 1.05));
 W2_cdf_sample[rep] = AD_cdf_P(sample->size,AndersonDarling_W2(sample,false));
gsl_vector_free(sample);
gsl_sort(W2_cdf_sample,1,10000);
printf("The deciles of the cdf of the W2 statistics are:\n");
for (size_t i=0; i < 9; i++)
 decile[i] = W2\_cdf\_sample[(i+1)*1000-1];
printf("\%g, \ \%g, \ \%g \backslash n", \ decile[0],
 decile[1],decile[2],decile[3],decile[4],decile[5],decile[6],
 decile[7],decile[8]);
printf("\n");
gsl_rng_free(r);
```

We compile the code with

```
gcc -Wall -g -o code/gof_test code/gof_test.c -lgsl -lgslcblas -lm -std=gnu11
```

We run it with:

```
./code/gof_test
```

```
***************
Test asymptotic cdf using Marsaglia & Marsaglia values:
Pr(W2 < 1.93295783274159) = 0.899989, the theoretical value is 0.90
\mbox{Pr(W2 < 2.4923671600494096) = 0.950008, the theoretical value is 0.95}
Pr(W2 < 3.8781250216053948) = 0.989997, the theoretical value is 0.99
Generating a sample of size 100 with Box-Müller (mean 0 and var 1)
The Anderson-Darling statistics, W2, value is: 0.889134
Prob(W2 \le 0.889134) = 0.579274
Generating a sample of size 750 with the ratio of uniforms (mean 0 and var 1)
The Anderson-Darling statistics, W2, value is: 0.500623
Prob(W2 \le 0.500623) = 0.253873
Generating a sample of size 500 with the ziggurat (mean 0 and var 1.2)
The Anderson-Darling statistics, W2, value is: 6.32691
Prob(W2 \le 6.32691) = 0.999319
Generating now 10,000 samples of size 100 form a standard normal with the ziggurat
method and computing the cdf of the W2 statistics...
The theoretical deciles of the cdf of the W2 statistics are:
0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9.
The empirical deciles of the cdf of the W2 statistics are:
0.104977,\ 0.201766,\ 0.299999,\ 0.401884,\ 0.505917,\ 0.606301,\ 0.701158,\ 0.796981,\ 0.900323.
```

3.3 ratio structure and related functions

Our C code is going to use a structure akin to the adu structure to store its ratiometric estimates. A bunch a functions are going to be associated with this structure.

3.3.1 C code related to ratio structures

```
/** \struct ratio
  * \brief Structure holding arrays of gsl_vectors each vector contains
  * ratiometric estimates.
  */
typedef struct
{
    gsl_vector * RATIO; //!< ratiometric estimator
    gsl_vector * RATIO_SE; //!< standard error of RATIO
    gsl_vector * TIME; //!< time (in s) of measurements
} ratio;</pre>
```

ratio type definition

ratio_alloc definition It will be helpful to have an alloc function for ratio structures:

```
/** \fn ratio * ratio_alloc(size_t n_obs)
   \brief Allocates a [ratio](@ref ratio) structure

The function allocates memory for an [ratio](@ref ratio) structure

\param[in] n_obs the number of measurements / obserations
\returns a pointer to an allocated ratio

*/

ratio * ratio_alloc(size_t n_obs) {
   ratio * res = malloc(sizeof(ratio));
   res->RATIO = gsl_vector_alloc(n_obs);
   res->RATIO_SE = gsl_vector_alloc(n_obs);
   res->TIME = gsl_vector_alloc(n_obs);
   return res;
}
```

ratio_free **definition** It will also be helpful to have a free function for ratio structures:

```
/** \fn int ratio_free(ratio * ratio_ptr)
  \brief Frees a [ratio](@ref ratio) structure

\param ratio_ptr a pointer to an allocated [ratio](@ref ratio) structure
  \returns 0 if everything goes fine

*/
int ratio_free(ratio * ratio_ptr) {
  gsl_vector_free(ratio_ptr->RATIO);
  gsl_vector_free(ratio_ptr->RATIO_SE);
  gsl_vector_free(ratio_ptr->TIME);
  free(ratio_ptr);
  return 0;
}
```

ratio_get_set **macro definitions** We define next macros with arguments giving an easy way to get and set values of specific members of ratio structure:

```
/** \def ratio_get(ratio,member,i)
   \brief A macro that returns value at index \a i of
        member \a member from \a [ratio](@ref ratio) structure

*/
#define ratio_get(ratio,member,i) gsl_vector_get(ratio->member,i)
/** \def ratio_set(ratio,member,i,x)
   \brief A macro that sets value at index \a i of
        member \a member from \a [ratio](@ref ratio) structure at \a x

*/
#define ratio_set(ratio,member,i,x) gsl_vector_set(ratio->member,i,x)
```

ratio_fprintf **definition** We now define a function that prints to the stdout the content of an ratio structure:

```
/** \fn int ratio_fprintf(FILE* fp, ratio * pratio)
    \brief Prints [ratio] (@ref ratio) content to fp
    \param[in] fp file pointer
    \param[in] pratio a pointer to a [ratio](@ref ratio) structure
    \rule \
int ratio_fprintf(FILE* fp, ratio * pratio) {
 size_t nobs=(pratio)->TIME->size;
 fprintf(fp,"# Ratiometric estimator:\n");
  fprintf(fp,"# Time Ca (est) Ca (se)\n");
  for (size_t i=0; i<nobs; i++) {</pre>
   double time = ratio_get((pratio),TIME,i);
   double ratio = ratio_get((pratio), RATIO,i);
   double ratio_se = ratio_get((pratio),RATIO_SE,i);
   fprintf(fp,"%9.9g %9.9g %9.9g\n",
          time, ratio, ratio_se);
  fprintf(fp,"\n\n");
 return 0;
```

ratio_est We now define the only function doing "interesting" work, ratio_est, that does the computations leading to the ratiometric estimation and is standard error.

```
/** \fn ratio * ratio_est(adu * padu, dye * pdye, illumination * plight, ccd * pccd, size_t nrep)
    \brief Computes ratiometric estimator and estimates its standard error
    \param[in] padu a pointer to an [adu](@ref adu) structure
    \param[in] pdye a pointer to a [dye](@ref dye) structure
    \param[in] plight a pointer to an [illumination](@ref illumination) structure
    \param[in] nrep the number of replicates used in the MC estimation of the SE
    \return a pointer to an initialized [ratio](@ref ratio) structure
ratio * ratio_est(adu * padu,
                  dye * pdye,
                  illumination * plight,
                  ccd * pccd,
                  size_t nrep)
  // get the dye parameters
  double Rmin = pdye->R_min_hat;
  double Rmax = pdye->R_max_hat;
  double Keff = pdye->K_eff_hat;
  // get the illumination parameters
  double T340 = plight->T_340;
  double T380 = plight->T_380;
  // get the CCD chip parameters
  double nP = (double) pccd->P;
  double nPB = (double) pccd->P_B;
  // macro that returns the "ratio"
#define R(ADU340, ADU340B, ADU380, ADU380B)
  ((ADU340/nP)-(ADU340B/nPB))*T380/\
  ((ADU380/nP)-(ADU380B/nPB))/T340
  // macro the returns the estimated free [Ca2+]
  // for a given "ratio"
#define Ca(r) Keff*(r-Rmin)/(Rmax-r)
  const gsl_rng_type * T = gsl_rng_default;
  gsl_rng_env_setup();
  gsl_rng * rng = gsl_rng_alloc (T);
  size_t nobs = (padu)->TIME->size;
  ratio * res = ratio_alloc(nobs);
  // do the MC standard error estimation
  for (size_t i=0; i<nobs; i++) {</pre>
    double adu340 = adu_get(padu,ADU340,i);
    double adu340B = adu_get(padu,ADU340B,i);
    double adu380 = adu_get(padu,ADU380,i);
    double adu380B = adu_get(padu,ADU380B,i);
    double r = R(adu340, adu340B, adu380, adu380B);
    ratio_set(res,TIME,i,adu_get(padu,TIME,i));
    ratio_set(res,RATIO,i,Ca(r));
    double g = pccd->gain;
    double s2 = g*g*nP*pccd->s2;
    double s2B = g*g*nPB*pccd->s2;
    double Ca_rep[nrep];
    for (size_t j=0; j<nrep; j++) {</pre>
      double adu340r = adu340+gsl_ran_gaussian_ziggurat(rng,sqrt(g*adu340+s2));
      double adu340Br = adu340B+gsl_ran_gaussian_ziggurat(rng,sqrt(g*adu340B+s2B));
```

```
double adu380r = adu380+gsl_ran_gaussian_ziggurat(rng,sqrt(g*adu380+s2));
    double adu380Br = adu380B+gsl_ran_gaussian_ziggurat(rng,sqrt(g*adu380B+s2B));
    r = R(adu340r,adu340Br,adu380r,adu380Br);
    Ca_rep[j] = Ca(r);
    }
    ratio_set(res,RATIO_SE,i,gsl_stats_sd(Ca_rep,1,nrep));
}
gsl_rng_free (rng);
return res;
}
```

ratio_find_fit_start Function ratio_find_fit_start locates the first point whose amplitude is smaller than the baseline plus a fraction of the stimulation induced jump.

```
/** \fn size_t ratio_find_fit_start(ratio * pratio, double remaining_fraction, size_t baseline)
    \brief Locates the first point of a transient whose amplitude is smaller than the baseline
    plus a fraction of the stimulation induced jump.
    \param[in] pratio a pointer to an initialized [ratio](@ref ratio) structure
    \verb|\param[in]| remaining\_fraction the remaining fraction of the jump amplitude|
    from which to start
    \param[in] baseline the length (in sample points) of the baseline
    \return a `size_t` with the searched location
size_t ratio_find_fit_start(ratio * pratio, double remaining_fraction, size_t baseline)
 double baseline_mean = 0.0;
 for (size_t i=0; i < baseline; i++)</pre>
   baseline_mean += gsl_vector_get(pratio->RATIO,i);
  baseline_mean /= baseline;
  size_t max_idx = gsl_vector_max_index(pratio->RATIO);
  double DeltaCa = gsl_vector_get(pratio->RATIO,max_idx)-baseline_mean;
  double threshold = DeltaCa*remaining_fraction+baseline_mean;
  size t i=max idx+1:
  while ((gsl_vector_get(pratio->RATIO,i) > threshold) & (i < pratio->RATIO->size))
   i++;
 return i;
}
```

mono_exp_fit_res We define a structure holding results of a mono-exponential fit.

```
/** \struct mono_exp_fit_res
  \brief Structure holding result of a mono-exponential
  fit Y = baseline + delta * exp(-(t-t0)/tau)

Depending on the input data the nonlinear least-squares
  can be weighted. That's the case when working with the
  ratiometric estimator.

*/
typedef struct
{
  size_t nobs; //!< number of observation used for the fit
  size_t baseline_length; //!< length of baseline region
  size_t fit_start; //!< first point used for the fit</pre>
```

```
double baseline; //!< fitted baseline value
double baseline_se; //!< standard error of the baseline
double delta; //!< fitted jump amplitude
double delta_se; //!< standard error of delta
double tau; //!< fitted time constant
double tau_se; //!< standard error of tau
double rss; //!< RSS value
int status; //!< solver's status when fit stops
} mono_exp_fit_res;</pre>
```

mono_exp_fit_res_fprintf This function prints the structure content to a file (or the stdout).

```
/** \fn int mono_exp_fit_res_fprintf(FILE * fp, mono_exp_fit_res * str, ratio * pratio)
    \brief Prints content of a [mono_exp_fit_res] (@ref mono_exp_fit_res) structure
    together with the fitted data
    \param[in] fp pointer to the file where printing is performed
    \param[in] str pointer to the [mono_exp_fit_res] (@ref mono_exp_fit_res)
    structure to print
    \param[in] pratio pointer to a [ratio](@ref ratio) structure containing
    the fitted data
    \returns 0 if everything goes fine
int mono_exp_fit_res_fprintf(FILE * fp, mono_exp_fit_res * str, ratio * pratio)
  fprintf(fp,"# Fitted model Ca = baseline+delta*exp(-(t-t0)/tau)\n");
  fprintf(fp,"# nobs = %d\n", (int) str->nobs);
  fprintf(fp,"# number of degrees of freedom = %d\n", ((int) str->nobs)-3);
  fprintf(fp,"# baseline length = %d\n", (int) str->baseline_length);
  fprintf(fp,"# fit started from point %d\n", (int) str->fit_start);
  fprintf(fp,"# estimated baseline %g and standard error %g\n", str->baseline,str->baseline_se);
  fprintf(fp,"# estimated delta %g and standard error %g\n", str->delta,str->delta_se);
  fprintf(fp,"# estimated tau %g and standard error %g\n", str->tau,str->tau_se);
  fprintf(fp,"# residual sum of squares: %g\n", str->rss);
  double dof = (((double) str->nobs)-3.0);
  \label{lem:str} fprintf(fp, "\mbox{\tt \# RSS per degree of freedom: $\mbox{\tt \%g}\n"$, str->rss/dof);}
  double p_larger = gsl_cdf_chisq_Q(str->rss,dof);
  fprintf(fp,"# Probability of observing a larger of equal RSS per DOF under the null hypothesis: %g\n",p_larger);
  if (p_larger < 0.01)
    fprintf(fp,"# WARNING: THE FIT IS NOT GOOD!\n");
  fprintf(fp, "\n");
  fprintf(fp,"# rss per degree of freedom: %g\n\n", str->rss/(((double) str->nobs)-3.0));
  for (size_t i=0; i<str->baseline_length; i++) {
    double time = gsl_vector_get(pratio->TIME,i);
    double y = gsl_vector_get(pratio->RATIO,i);
    double pred = str->baseline;
    double resid = (y-pred)/gsl_vector_get(pratio->RATIO_SE,i);
    fprintf(fp,"%g %g %g %g\n",time,y,pred,resid);
  fprintf(fp,"\n");
  double t0 = gsl_vector_get(pratio->TIME,str->fit_start);
  for (size_t i=str->fit_start; i<pratio->TIME->size; i++) {
    double time = gsl_vector_get(pratio->TIME,i);
    double dt = time-t0;
```

```
double y = gsl_vector_get(pratio->RATIO,i);
double pred = str->baseline;
pred += str->delta*exp(-dt/str->tau);
double resid = (y-pred)/gsl_vector_get(pratio->RATIO_SE,i);
fprintf(fp,"%g %g %g %g\n",time,y,pred,resid);
}
return 0;
}
```

ratio_for_fit We define a specific structure suitable for fitting a mono-exponential decay to ratio metric estimates stored in a ratio structure:

```
/** \struct ratio_for_fit
  \brief Structure suitable for fitting a mono-exponential decay to
    the ratio metric estimates stored in a [ratio](@ref ratio) structure

*/
typedef struct
{
    size_t i0; //!< index at which the decay fit starts
    size_t baseline_length; //!< baseline length
    ratio * pratio; //!< pointer to a ratio structure
} ratio_for_fit;</pre>
```

ratio_residuals We define a function returning the (weighted) residuals of a mono-exponential fit suitable for use with the gsl nonlinear least-squares solver.

```
/** \fn int ratio_residuals (const gsl_vector * x, void *data, gsl_vector * f)
    \brief Returns the (weighted) residuals of a mono-exponential fit suitable
    for use with the `gsl` [nonlinear least-squares solver] (https://www.gnu.org/software/gsl/doc/html/nls.html#providing
    \param[in] x pointer to a [`gsl_vector`](https://www.gnu.org/software/gsl/doc/html/vectors.html#vectors)
    holding the present model parameter values
    \param[in] data pointer to a structure holding the "data" to fit
    \param[out] f pointer to a [`gsl_vector`](https://www.gnu.org/software/gsl/doc/html/vectors.html#vectors)
    where the residuals get stored.
    \returns `GSL_SUCCESS` if everything goes fine
int ratio_residuals (const gsl_vector * x,
                     void *data,
                    gsl_vector * f)
{
  size_t i0 = ((ratio_for_fit *)data)->i0;
  size_t baseline_length = ((ratio_for_fit *)data)->baseline_length;
  ratio *pratio = ((ratio_for_fit *)data)->pratio;
  gsl_vector * time = pratio->TIME;
  gsl_vector * Ca = pratio->RATIO;
  gsl_vector * SE = pratio->RATIO_SE;
  size_t n = time->size;
  double baseline = gsl_vector_get (x, 0);
  double delta = gsl_vector_get (x, 1);
  double tau = gsl_vector_get (x, 2);
```

```
size_t i;

for (i=0; i baseline_length; i++)
    gsl_vector_set (f, i, (baseline - gsl_vector_get(Ca,i))/gsl_vector_get(SE,i));

double t0 = gsl_vector_get(time,i0);
    for (size_t j=i0; j n; j++){
        /* Model Yj = delta * exp(-(tj-t0)/tau) + baseline */
        double dt = gsl_vector_get(time,j) - t0;
        double Yj = delta * exp(-dt/tau) + baseline;
        gsl_vector_set (f, i, (Yj - gsl_vector_get(Ca,j))/gsl_vector_get(SE,j));
        i++;
}

return GSL_SUCCESS;
}
```

ratio_fit_callback We define a function called after each iteration of the nonlinear least-squares solver that prints to the stderr information on the procedure.

```
/** \fn void ratio_fit_callback(const size_t iter, void *params,
    const gsl_multifit_nlinear_workspace *w)
    \brief A callback function printing progress during
    [nonlinear least-squares fitting](https://www.gnu.org/software/gsl/doc/html/nls.html#high-level-driver)
    \param[in] iter the current iteration
    \param[in] params set to `NULL` when used but required by the [solver](https://www.gnu.org/software/gsl/doc/html/nls
    \param[in] w a pointer to the [\gsl_multifit_nlinear_workspace\](https://www.gnu.org/software/gsl/doc/html/nls.html#
void ratio_fit_callback(const size_t iter,
                        void *params,
                        const gsl_multifit_nlinear_workspace *w)
 gsl_vector *f = gsl_multifit_nlinear_residual(w);
  gsl_vector *x = gsl_multifit_nlinear_position(w);
  fprintf(stderr, "iter %2zu: baseline = %.4f, delta = %.4f, tau = %.4f, RSS = %.4f\n",
          gsl_vector_get(x, 0),
         gsl_vector_get(x, 1),
          gsl_vector_get(x, 2),
          gsl_pow_2(gsl_blas_dnrm2(f)));
```

ratio_fit Function ratio_fit fits a mono-exponential to the decaying part of a stimulation. Its skeleton is:

```
/** \fn mono_exp_fit_res ratio_fit(ratio * pratio, size_t baseline,
    size_t start_fit, size_t maxit)
   \brief Fits a mono-exponential to the decaying part of a stimulation

\param[in] pratio a pointer to a [ratio](@ref ratio) structure
   holding the "data"
   \param[in] baseline baseline length
```

```
\param[in] start_fit the sampling point from which we start
   fitting the decay
    \param[in] the maximal number of iterations
    \returns a [mono_exp_fit_res](@ref mono_exp_fit_res) structure
   holding the results
mono_exp_fit_res ratio_fit(ratio * pratio,
                           size_t baseline,
                           size_t start_fit,
                          size_t maxit)
 // nobs: number of observations to fit
 const size_t nobs = baseline+pratio->TIME->size-start_fit;
 // p: number of model parameters
 const size_t p = 3;
 // data: a ratio_for_fit structure with the data and parameters
          required for computing the residuals
 ratio_for_fit data = {.i0=start_fit,
                        .baseline_length=baseline,
                        .pratio=pratio};
 <<ratio_fit_model_par>>
 <<ratio_fit_function_to_minimize_definition>>
 <<ratio_fit_solver_workspace_allocation_initialization>>
 <<ratio_fit_initial_rss_value>>
 <<ratio_fit_run_solver>>
 <<ratio_fit_par_covar>>
 <<ratio_fit_final_rss_value>>
#define FIT(i) gsl_vector_get(w->x, i)
#define ERR(i) sqrt(gsl_matrix_get(covar,i,i))
 <<ratio_fit_print_end_info>>
 // Prepare the output
 mono_exp_fit_res res = {.nobs=nobs,
                         .baseline_length=baseline,
                          .fit_start=start_fit,
                          .baseline=FIT(0),
                          .baseline_se=ERR(0),
                          .delta=FIT(1),
                          .delta_se=ERR(1),
                          .tau=FIT(2),
                          .tau_se=ERR(2),
                          .rss=rss,
                          .status=status};
 // Free allocated memory
 gsl_multifit_nlinear_free (w);
 gsl_matrix_free (covar);
 gsl_vector_free (par);
 return res;
```

```
}
```

Code block <<ratio_fit_model_par>> allocates memory and initializes par a pointer to a gsl vector containing the 3 model parameters:

Code block <<ratio_fit_function_to_minimize_definition>> initializes a gsl_multifit_nlinear_fdf structure containing the residuals function and accessory information required by the solver:

Code block <<ratio_fit_solver_workspace_allocation_initialization>> allocates and initializes w, the solver workspace with default parameters:

```
// allocate solver workspace with default parameters
  const gsl_multifit_nlinear_type *T = gsl_multifit_nlinear_trust;
gsl_multifit_nlinear_parameters fdf_params =
  gsl_multifit_nlinear_default_parameters();
gsl_multifit_nlinear_workspace *w = gsl_multifit_nlinear_alloc (T, &fdf_params, nobs, p);

// initialize solver with starting point and weights
gsl_multifit_nlinear_init (par, &fdf, w);
```

Code block <<ratio_fit_initial_rss_value>> computes the initial value of the residual sum of squares (the criterion we want to minimize), the computed value is stored in variable rss0:

```
// compute initial rss value
gsl_vector *residuals = gsl_multifit_nlinear_residual(w);
double rss0;
gsl_blas_ddot(residuals, residuals, &rss0);
```

Code block <<ratio_fit_run_solver>> does the main job of the function, it runs the solver for a maximal number of iterations (maxit) if the other stopping criteria are not met before. For the significance and values of xtol, gtol and ftol see the gsl manual.

Code block <<ratio_fit_par_covar>> computes the covariance matrix of the model parameters (stored in the gsl_matrix pointed to by covar) once the solver has returned.

```
gsl_matrix *J;
gsl_matrix *covar = gsl_matrix_alloc (p, p);
// compute covariance of best fit parameters
J = gsl_multifit_nlinear_jac(w);
gsl_multifit_nlinear_covar (J, 0.0, covar);
```

Code block <<ratio_fit_final_rss_value>> computes the final RSS value and stores the result in variable rss:

```
// compute final cost
double rss;
gsl_blas_ddot(residuals, residuals, &rss);
```

Code block <<ratio_fit_print_end_info>> prints details on the fitting procedure together with parameter estimations to the stderr:

```
// print end info
fprintf(stderr, "Fitted model Ca = baseline+delta*exp(-(t-t0)/tau)\n");
fprintf(stderr, "Summary from method '%s/%s'\n",
        gsl_multifit_nlinear_name(w),
         gsl_multifit_nlinear_trs_name(w));
fprintf(stderr, "number of iterations: %zu\n",
        gsl_multifit_nlinear_niter(w));
fprintf(stderr, "function evaluations: %zu\n", fdf.nevalf);
fprintf(stderr, "Jacobian evaluations: %zu\n", fdf.nevaldf);
fprintf(stderr, "reason for stopping: %s\n",
         (info == 1) ? "small step size" : "small gradient");
fprintf(stderr, "initial RSS = %f\n", rss0);
fprintf(stderr, "final
                          RSS = f\n", rss);
fprintf(stderr, "\n");
fprintf(stderr,"Number of observation: %d\n", (int) nobs);
fprintf(stderr,"Number of degrees of freedom: %d\n", ((int) nobs)-3);
fprintf(stderr, "Baseline length: %d\n", (int) baseline);
fprintf(stderr,"Fit started from point %d\n", (int) start_fit);
fprintf(stderr,"Estimated baseline %g and standard error %g\n", FIT(0),ERR(0));
fprintf(stderr, "Estimated delta %g and standard error %g\n", FIT(1),ERR(1));
fprintf(stderr, "Estimated \ tau \ \%g \ and \ standard \ error \ \%g\n", \ FIT(2), ERR(2));
double dof = (((double) nobs)-3.0);
fprintf(stderr,"RSS\ per\ degree\ of\ freedom:\ %g\n",\ rss/dof);
double p_larger = gsl_cdf_chisq_Q(rss,dof);
fprintf(stderr, "Probability of observing a larger of equal RSS per DOF under the null hypothesis: %g\n",p_larger);
if (p_larger < 0.01)
  fprintf(stderr,"WARNING: THE FIT IS NOT GOOD!\n");
fprintf(stderr,"\n");
```

```
/** \file ratio_test.c
   \brief Program testing the ratiometric functions
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include <math.h>
#include <hdf5.h>
#include <hdf5_hl.h>
#include <gsl/gsl_math.h>
#include <gsl/gsl_vector.h>
#include <gsl/gsl_rng.h>
#include <gsl/gsl_randist.h>
#include <gsl/gsl_cdf.h>
#include <gsl/gsl_blas.h>
#include <gsl/gsl_multifit_nlinear.h>
#include <gsl/gsl_statistics_double.h>
<<adu-type-definition>>
<<adu_alloc>>
<<adu_free>>
<<adu_get_set>>
<<adu_vector-type-definition>>
<<adu_vector_alloc>>
<<adu_vector_free>>
<<data_get_nelt>>
<<adu_vector_read_from_file>>
<<adu_printf>>
<<adu_vector_printf>>
<<dye-type-definition>>
<<dye_read_from_file>>
<<dye_printf>>
<<il><!re></illumination_read_from_file>>
<\!\!<\!\!\texttt{ccd-type-definition}\!\!>\!\!>
<<ccd_read_from_file>>
<<cd_printf>>
<<\!\! \texttt{aba-type-definition}\!\!>>
<<aba_alloc>>
<<aba_free>>
<<aba_read_from_file>>
<<aba_printf>>
<<ratio-type-definition>>
<<ratio_alloc>>
<<ratio_free>>
<<ratio_get_set>>
<<ratio_fprintf>>
<<ratio_est>>
<<ratio_find_fit_start>>
<<ratio_for_fit>>
<<ratio_residuals>>
<<ratio_fit_callback>>
<<mono_exp_fit_res>>
<<mono_exp_fit_res_fprintf>>
<<ratio_fit>>
#define FNAME "data_paper/data_beta_escin/DA_121219_E1.h5"
int main()
{
```

```
// Open FILE
char fname[] = FNAME;
hid_t fid = H5Fopen (fname, H5F_ACC_RDONLY, H5P_DEFAULT);
aba * paba = aba_read_from_file(fid);
// Close file
H5Fclose (fid);
ratio * pratio = ratio_est(paba->data->adu_v[1],&paba->dye,&paba->light,&paba->ccd,1000);
aba_free(paba);
ratio_fprintf(stdout,pratio);
printf("\n\n");
size_t start_pos = ratio_find_fit_start(pratio,0.5,15);
mono_exp_fit_res res = ratio_fit(pratio,15,start_pos,25);
mono_exp_fit_res_fprintf(stdout,&res,pratio);
ratio_free(pratio);
return 0;
}
```

ratio_test

ratio_test compilation and run We compile the code with:

```
gcc -Wall -g -o code/ratio_test code/ratio_test.c -lgsl -lgslcblas -lhdf5 -lhdf5_hl -lm -std=gnu11
```

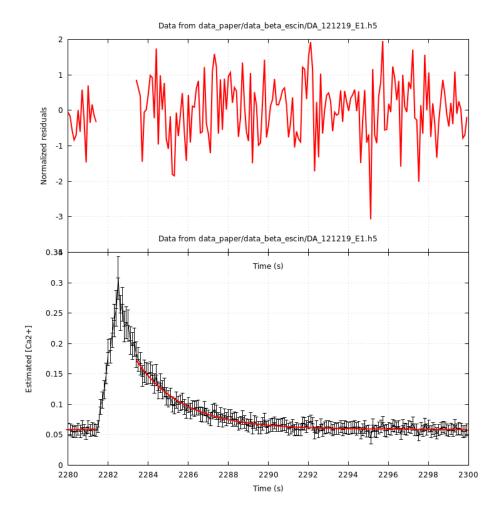
We run it with valgrind:

```
valgrind --leak-check=full ./code/ratio_test > titi
```

```
==15272== Memcheck, a memory error detector
==15272== Copyright (C) 2002-2017, and GNU GPL'd, by Julian Seward et al.
==15272== Using Valgrind-3.14.0 and LibVEX; rerun with -h for copyright info
==15272== Command: ./code/ratio_test
==15272==
iter 0: baseline = 0.0586, delta = 0.1231, tau = 16.5000, RSS = 22664.2848
iter 1: baseline = 0.0597, delta = 0.0565, tau = 5.3161, RSS = 658.4080
iter 2: baseline = 0.0583, delta = 0.0629, tau = 3.8287, RSS = 414.3510
iter 3: baseline = 0.0585, delta = 0.0783, tau = 3.0541, RSS = 258.6214
iter 4: baseline = 0.0587, delta = 0.0971, tau = 2.5991, RSS = 155.1582
     5: baseline = 0.0588, delta = 0.1095, tau = 2.4067, RSS = 129.3976
iter 6: baseline = 0.0589, delta = 0.1132, tau = 2.3526, RSS = 127.7445
iter 7: baseline = 0.0589, delta = 0.1137, tau = 2.3436, RSS = 127.7223
iter 8: baseline = 0.0589, delta = 0.1137, tau = 2.3427, RSS = 127.7222
iter 9: baseline = 0.0589, delta = 0.1137, tau = 2.3427, RSS = 127.7222
iter 10: baseline = 0.0589, delta = 0.1137, tau = 2.3427, RSS = 127.7222
iter 11: baseline = 0.0589, delta = 0.1137, tau = 2.3427, RSS = 127.7222
iter 12: baseline = 0.0589, delta = 0.1137, tau = 2.3427, RSS = 127.7222
iter 13: baseline = 0.0589, delta = 0.1137, tau = 2.3427, RSS = 127.7222
Fitted model Ca = baseline+delta*exp(-(t-t0)/tau)
Summary from method 'trust-region/levenberg-marquardt'
number of iterations: 13
function evaluations: 72
Jacobian evaluations: 0
reason for stopping: small step size
initial RSS = 22664.284799
final RSS = 127.722162
```

```
Number of observation: 181
Number of degrees of freedom: 178
Baseline length: 15
Fit started from point 34
Estimated baseline 0.0588818 and standard error 0.000546884
Estimated delta 0.113685 and standard error 0.00338681
Estimated tau 2.34267 and standard error 0.0946631
RSS per degree of freedom: 0.71754
Probability of observing a larger of equal RSS per DOF under the null hypothesis: 0.998311
==15272==
==15272== HEAP SUMMARY:
==15272== in use at exit: 0 bytes in 0 blocks
==15272== total heap usage: 4,941 allocs, 4,941 frees, 2,441,573 bytes allocated
==15272==
==15272== All heap blocks were freed -- no leaks are possible
==15272== For counts of detected and suppressed errors, rerun with: -v
==15272== ERROR SUMMARY: 0 errors from 0 contexts (suppressed: 0 from 0)
```

We can make a figure showing the ratiometric estimator, the standard error and the fit as follows:



3.3.2 ratio header and source

The header part in code block <<ratio.h>>:

```
<<ratio-type-definition>>
ratio * ratio_alloc(size_t n_obs);
int ratio_free(ratio * ratio_ptr);
<<ratio_get_set>>
int ratio_fprintf(FILE * fp,ratio * pratio);
ratio * ratio_est(adu * padu, dye * pdye,illumination * plight,ccd * pccd,size_t nrep);
size_t ratio_find_fit_start(ratio * pratio, double remaining_fraction, size_t baseline);
<<mono_exp_fit_res>>
int mono_exp_fit_res_fprintf(FILE * fp, mono_exp_fit_res * str, ratio * pratio);
<<ratio_for_fit>>
int ratio_residuals (const gsl_vector * x, void *data, gsl_vector * f);
void ratio_fit_callback(const size_t iter, void *params, const gsl_multifit_nlinear_workspace *w);
mono_exp_fit_res_ratio_fit(ratio * pratio, size_t baseline, size_t start_fit, size_t maxit);
```

The function definitions <<ratio.c>> stored in file code/ratio.c:

```
/** \file ratio.c
   \brief Functions to work with the ratiometric estimator.

*/
#include "abaa.h"

<<ratio_alloc>>

<<ratio_free>>

<<ratio_free>>

<<ratio_est>>

<<ratio_find_fit_start>>

<<ratio_residuals>>

<<ratio_fit_callback>>

<<mono_exp_fit_res_fprintf>>

<<ratio_fit>>
</ratio_fit>>
</ratio_fit>>
```

4 Building the abaa library

We see that the part of ratio_test that precedes the main function is getting pretty large (to say the least)! This is a sign that it is time to define a library that we will call abaa for "Added Buffer Approach Analysis" that will contain all our functions, structures, etc.

4.1 The abaa.h header file

File abaa.h will contain the structures, macros and function prototypes.

```
/** \file abaa.h
* \brief Header file for "added buffer approach analysis"
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include <getopt.h>
#include <math.h>
#include <hdf5.h>
#include <hdf5_hl.h>
#include <gsl/gsl_math.h>
#include <gsl/gsl_vector.h>
#include <gsl/gsl_rng.h>
#include <gsl/gsl_randist.h>
#include <gsl/gsl_cdf.h>
#include <gsl/gsl_blas.h>
#include <gsl/gsl_multifit_nlinear.h>
#include <gsl/gsl_statistics_double.h>
#include <gsl/gsl_fit.h>
#include <gsl/gsl_multifit.h>
#include <gsl/gsl_sort.h>
```

```
#include <gsl/gsl_sort_vector.h>

<<adu.h>>

<<adu_vector.h>>

<<dye.h>>

<<iillumination.h>>

<<ccd.h>>

<<ature color="block">
<<ature color="block">
</aba.h>>

<<ature color="block">
<<ature color="block">
</aba.h>>

<<ature color="block">
<<ature color="block">
<<ature color="block">
<ature color="
```

4.2 The Makefile

```
P=programe_name
OBJECTS=
CFLAGS += -g -Wall -std=gnu11
LDLIBS = -lhdf5 -lhdf5_hl -lgsl -lgslcblas -lm
$(P): $(OBJECTS)
all : libabaa.a adu_test adu_vector_test dye_test illumination_test \
ccd_test aba_test ratio_test ratio_test2
test : adu_test_run dye_test_run illumination_test_run ccd_test_run \
aba_test_run adu_vector_test_run ratio_test2_run
libabaa.a : adu.o adu_vector.o illumination.o dye.o ccd.o aba.o ratio.o \
        ar cr libabaa.a adu.o adu_vector.o illumination.o dye.o ccd.o aba.o ratio.o \
fura.o
adu_test_objects=adu_test.o
adu_test : $(adu_test_objects)
        cc $(adu_test_objects) $(LDLIBS) -o adu_test
adu_test_run : adu_test
        ./adu_test
adu_vector_test_objects=adu_vector_test.o
adu_vector_test : $(adu_vector_test_objects)
        cc $(adu_vector_test_objects) $(LDLIBS) -o adu_vector_test
\verb"adu_vector_test_run": adu_vector_test"
        cd .. && ./code/adu_vector_test > toto && gnuplot -persist code/adu_vector_test_plot_loading_curve.gp
dye_test_objects=dye_test.o
dye_test : $(dye_test_objects)
        cc $(dye_test_objects) $(LDLIBS) -o dye_test
```

```
dye_test_run : dye_test
       cd .. && ./code/dye_test
{\tt illumination\_test\_objects=illumination\_test.o}
illumination_test : $(illumination_test_objects)
        \verb|cc $(illumination_test_objects) $(LDLIBS) - o illumination_test|\\
illumination_test_run : illumination_test
       cd .. && ./code/illumination_test
ccd_test_objects=ccd_test.o
ccd_test : $(ccd_test_objects)
       cc $(ccd_test_objects) $(LDLIBS) -o ccd_test
\verb|ccd_test_run| : \verb|ccd_test|
       cd .. && ./code/ccd_test
aba_test_objects=aba_test.o
aba_test : $(aba_test_objects)
       cc $(aba_test_objects) $(LDLIBS) -o aba_test
aba_test_run : aba_test
       cd .. && ./code/aba_test | head -n 30
ratio_test_objects=ratio_test.o
ratio_test : $(ratio_test_objects)
        cc $(ratio_test_objects) $(LDLIBS) -o ratio_test
ratio_test2.o : abaa.h
ratio_test2_objects=ratio_test2.o
ratio_test2 : $(ratio_test2_objects) libabaa.a
       cc $(ratio_test2_objects) libabaa.a $(LDLIBS) -o ratio_test2
ratio_test2_run : ratio_test2
        cd .. && ./code/ratio_test2 > titi && gnuplot -persist code/ratio_test_fig.gp
fit_ratiometric : fit_ratiometric.o libabaa.a
       cc fit_ratiometric.o libabaa.a $(LDLIBS) -o fit_ratiometric
fura_concentration : fura_concentration.o libabaa.a
       cc fura_concentration.o libabaa.a $(LDLIBS) -o fura_concentration
fura_during_stim : fura_during_stim.o libabaa.a
        cc fura_during_stim.o libabaa.a $(LDLIBS) -o fura_during_stim
aba_ratio : aba_ratio.o libabaa.a
       cc aba_ratio.o libabaa.a $(LDLIBS) -o aba_ratio
.PHONY : clean
clean :
        rm -f libabaa.a adu.o adu_vector.o illumination.o dye.o ccd.o aba.o ratio.o \
        fura.o \
        $(adu_test_objects) adu_test \
        $(adu_vector_test_objects) adu_vector_test \
        $(dye_test_objects) dye_test \
        $(illumination_test_objects) illumination_test \
        $(ccd_test_objects) ccd_test \
```

```
$(aba_test_objects) aba_test \
$(ratio_test_objects) ratio_test \
$(ratio_test2_objects) ratio_test2 \
fit_ratiometric.o fit_ratiometric \
fura_concentration.o fura_concentration \
fura_during_stim.o fura_during_stim \
aba_ratio.o aba_ratio
```

4.2.1 Testing that everything works

We redefine our last test function using the library:

```
/** \file ratio_test2.c
    \brief Test program for the ratiometric estimator functions and
          structures of the abaa library.
#include "abaa.h"
{\tt \#define\ FNAME\ "data\_paper/data\_beta\_escin/DA\_121219\_E1.h5"}
int main()
 // Open FILE
  char fname[] = FNAME;
  hid_t fid = H5Fopen (fname, H5F_ACC_RDONLY, H5P_DEFAULT);
  aba * paba = aba_read_from_file(fid);
  // Close file
  H5Fclose (fid);
  ratio * pratio = ratio_est(paba->data->adu_v[3],&paba->dye,&paba->light,&paba->ccd,1000);
  aba_free(paba);
  ratio_fprintf(stdout,pratio);
  printf("\n\n");
  size_t start_pos = ratio_find_fit_start(pratio,0.5,15);
  mono_exp_fit_res res = ratio_fit(pratio,15,start_pos,25);
  mono_exp_fit_res_fprintf(stdout,&res,pratio);
  ratio_free(pratio);
 return 0;
```

4.3 The SConstruct file

As an alternative to make, we can use SCons that requires Python and the definition of a SConstruct file that we now define (and write in the code folder):

```
LIBS=["hdf5","hdf5_hl","gsl","gslcblas","m"],LIBPATH=".")
env.Program(target="dye_test",
           source="dye_test.c",
           LIBS=["hdf5","hdf5_hl","gsl","gslcblas","m"],LIBPATH=".")
env.Program(target="illumination_test",
           source="illumination_test.c",
           LIBS=["hdf5","hdf5_h1","gsl","gslcblas","m"],LIBPATH=".")
env.Program(target="ccd_test",
           source="ccd_test.c",
           LIBS=["hdf5","hdf5_hl","gsl","gslcblas","m"],LIBPATH=".")
env.Program(target="aba_test",
           source="aba_test.c",
           LIBS=["hdf5","hdf5_hl","gsl","gslcblas","m"],LIBPATH=".")
env.Program(target="ratio_test",
           source="ratio_test.c",
           LIBS=["hdf5","hdf5_hl","gsl","gslcblas","m"],LIBPATH=".")
env.Program(target="ratio_test2",
           source="ratio_test2.c"
           LIBS=["abaa","hdf5","hdf5_hl","gsl","gslcblas","m"],LIBPATH=".")
```

5 Our first "user's" program: fit_ratiometric

We now write, fit_ratiometric, our first user's program fitting a mono-exponential decay to the ratiometric estimator of a single transient.

5.1 Program's task

fit_ratiometric is essentially a user friendly version of ratio_test. It will allow the user to specify:

- an input file name containing the data.
- an output file name prefix where results will get written.
- a stimulation number (what stimulation does the user want to fit?).
- a maximal number of iteration for the nonlinear least-squares solver.
- a baseline length.
- a location of a criteria to select from where the decay should be fitted.
- a Boolean controlling the generation of a gnuplot script for quickly viewing the result.

5.1.1 fit_ratiometric **code**

```
/** \file fit_ratiometric.c
   \brief Fits mono-exponential model to ratiometric estimator
#include "abaa.h"
int main(int argc, char *argv[])
{
 <<fit_ratiometric-usage>>
 <<fit_ratiometric-args>>
 hid_t fid = H5Fopen (filename, H5F_ACC_RDONLY, H5P_DEFAULT);
 aba * paba = aba_read_from_file(fid);
 // Close file
 H5Fclose (fid);
 ratio * pratio = ratio_est(paba->data->adu_v[stim], &paba->dye, &paba->light, &paba->ccd, 1000);
 aba_free(paba);
 char out[512];
 strcpy(out,output);
 strcat(out,"_CaRatio");
 FILE *fp = fopen(out,"w");
 fprintf(fp,"# Data from %s stim %d\n",filename,(int) stim);
 fprintf(fp,"# Ratiometric estimator\n");
 ratio_fprintf(fp,pratio);
 fclose(fp);
 size_t start_pos;
 if (start_fit >= 1)
   start_pos = (size_t) start_fit;
 else
   start_pos = ratio_find_fit_start(pratio,start_fit,baseline_length);
 mono_exp_fit_res res = ratio_fit(pratio,baseline_length,start_pos,maxiter);
 strcpy(out,output);
 strcat(out,"_RatioFit");
 fp = fopen(out,"w");
 fprintf(fp,"# Data from %s stim %d\n",filename,(int) stim);
 fprintf(fp,"# Ratiometric estimator mono-exponential fit\n");
 mono_exp_fit_res_fprintf(fp,&res,pratio);
 fclose(fp);
 ratio_free(pratio);
 if (g_script) {
   <<fit_ratiometric_g_script>>
 return 0;
```

fit_ratiometric skeleton

```
" -o --output <character string>: output file name prefix (e.g. 'DA_121219_E1_s1_ratio')\n"
" -s --stim <positive integer>: the stimulation to fit (default 1)\n"
" -m --max_iter <positive integer>: maximal number of iterations performed by\n"
        the nonlinear least-squares solver (default 50)\n"
" -b --baseline_length <positive integer>: baseline length in samples (default 15)\n"
   -f --start_fit <positive real>: where decay fit starts, if > 1 interpreted as the\n"
        number of samples after the peak, if 0< f < 1 interpreted as the remaining \n"
       fraction of the jump and fitting starts when the transient reaches that level\n"
" -g --graphics: if set, a gnuplot script file named output.gp is generated \n\
" The program opens 'input' file, computes the ratiometric estimator from the raw data\n"
" and fits the following model to it: Ca = baseline + delta * exp (-(t-t0)/tau) n"
" where tO is the time on the decay phase at which the fit starts (set by parameter 'f').\n"
" A constant is also fitted to the baseline region: Ca = baseline.\n"
" Standard errors for the ratiometric estimator are obtained by Monte-Carlo simulation.\n"
"While the program performs the least-squares optimization relevant information get printed\n"
" to the stderr. The ratiometric estimator and its standard error are printed to a \text{text} \setminus n"
" file named 'output_CaRatio'. The fitted parameters, fitted values and residuals are\n"
 printed to a text file named 'output_RatioFit'. If 'g' is selected, a gnuplot script\n"
" file whose name is the 'output' name with the '.gp' suffix is generated. A graphical display\n"
" of the result can then be obtained with: gnuplot -persist 'output.gp'\n";
```

<<fit_ratiometric-usage>>

<<fi>t_ratiometric-args>> This code block reads the program parameters. It assigns (after allocating memory if necessary):

filename pointer to a character string with the name of the data file.

output pointer to a character string with the name of the output file name.

stim, maxiter, baseline_length stim number, maximal number of iterations and baseline length.

start_fit the number used to set from where the decay gets fitted.

g_script indicates if a gnuplot script should be generated.

```
char *filename;
char *output;
size_t stim=1, maxiter=50, baseline_length=15;
double start_fit=0.5;
int g_script=0;
{int opt;
  static struct option long_options[] = {
    {"input", required_argument, NULL, 'i'},
    {"output", required_argument, NULL, 'o'},
    {"stim", optional_argument, NULL, 's'},
    {"graphic", optional_argument, NULL, 'g'},
    {"maxiter", optional_argument, NULL, 'm'},
    {"baseline_length",optional_argument,NULL,'b'},
    {"start_fit", optional_argument, NULL, 'f'},
    {"help",no_argument,NULL,'h'},
    {NULL,0,NULL,0}
  };
```

```
int long_index =0;
while ((opt = getopt_long(argc,argv,
                        "hgi:o:s:m:b:f:",
                         long_options,
                         &long_index)) != -1) {
  switch(opt) {
  case 'i':
  {
   filename = optarg;
  }
  break;
  case 'o':
  {
   output = optarg;
  break;
  case 'g':
  {
   g_script=1;
  break;
  case 's':
   stim = (size_t) atoi(optarg);
  }
  break;
  case 'm':
   maxiter = (size_t) atoi(optarg);
  }
  break;
  case 'b':
   baseline_length = (size_t) atoi(optarg);
  }
  break;
  case 'f':
   start_fit = (double) atof(optarg);
   if (start_fit<=0) {</pre>
     fprintf(stderr,"start_fit should be > 0.\n");
     return -1;
   }
  }
 case 'h': printf(usage,argv[0]);
  return -1;
 default : fprintf(stderr,usage,argv[0]);
   return -1;
}
```

<<fit_ratiometric_g_script>> We write the gnuplot script generating the diagnostic plot:

```
strcpy(out,output);
strcat(out,".gp");
fp = fopen(out,"w");
char RatioFit[512];
strcpy(RatioFit,output);
strcat(RatioFit,"_RatioFit");
char CaRatio[512];
strcpy(CaRatio,output);
strcat(CaRatio,"_CaRatio");
char format[] = "%g";
fprintf(fp,
        "unset key\n"
        "set grid\n"
        "set multiplot title 'Data from %s stim %d' noenhanced layout 2,1 margins 0.1,0.9,0.1,0.95 spacing 0,0\n"
        "set ylabel 'Normalized residuals'\n"
        "set xtics format ''\n"
        "plot '%s' using 1:4 with lines line
color rgb 'red' linewidth 2\n"
        "set format x '%s'\n"
        "set xlabel 'Time (s)'\n"
        "set ylabel 'Estimated [Ca2+]'\n"
        "plot '%s' using 1:2:($3*1.96) with yerrorlines
                                                              \\\n"
            linecolor rgb 'black' linewidth 1,
                                                               \\\n"
              '%s' using 1:3 with lines linecolor rgb 'red'\\n"
             linewidth 2\n"
        "unset multiplot",
        filename, (int) stim, RatioFit, format, CaRatio, RatioFit);
fclose(fp);
```

```
cd code && make fit_ratiometric
```

fit_ratiometric compilation

```
make: fit_ratiometric est à jour.
```

5.2 Using fit_ratiometric

What to do if we forget how to use the program?

```
-b --baseline_length <positive integer>: baseline length in samples (default 15)
 -f --start_fit <positive real>: where decay fit starts, if > 1 interpreted as the
     number of samples after the peak, if 0<f<1 interpreted as the remaining
     fraction of the jump and fitting starts when the transient reaches that level
 -g --graphics: if set, a gnuplot script file named output.gp is generated
The program opens 'input' file, computes the ratiometric estimator from the raw data
and fits the following model to it: Ca = baseline + delta * exp(-(t-t0)/tau)
where t0 is the time on the decay phase at which the fit starts (set by parameter 'f').
A constant is also fitted to the baseline region: Ca = baseline.
Standard errors for the ratiometric estimator are obtained by Monte-Carlo simulation.
While the program performs the least-squares optimization relevant information get printed
to the stderr. The ratiometric estimator and its standard error are printed to a text
file named 'output_CaRatio'. The fitted parameters, fitted values and residuals are
printed to a text file named 'output_RatioFit'. If 'g' is selected, a gnuplot script
file whose name is the 'output' name with the '.gp' suffix is generated. A graphical display
of the result can then be obtained with: gnuplot -persist 'output.gp'
```

Fine so lets fit the second stimulation of our test dataset:

```
./code/fit_ratiometric -i data_paper/data_beta_escin/DA_121219_E1.h5 -o DA_121219_E1_s2 -s 2 -g
```

```
iter 0: baseline = 0.0505, delta = 0.0755, tau = 15.7000, RSS = 17219.2218
iter 1: baseline = 0.0532, delta = 0.0525, tau = 1.2056, RSS = 3257.7394
iter 2: baseline = 0.0563, delta = 0.0633, tau = 3.3014, RSS = 402.2209
iter 3: baseline = 0.0530, delta = 0.0794, tau = 3.0219, RSS = 172.8142
iter 4: baseline = 0.0530, delta = 0.0797, tau = 3.0698, RSS = 171.1807
iter 5: baseline = 0.0530, delta = 0.0797, tau = 3.0718, RSS = 171.1802
iter 6: baseline = 0.0530, delta = 0.0797, tau = 3.0718, RSS = 171.1802
iter 7: baseline = 0.0530, delta = 0.0797, tau = 3.0719, RSS = 171.1802
iter 8: baseline = 0.0530, delta = 0.0797, tau = 3.0719, RSS = 171.1802
iter 9: baseline = 0.0530, delta = 0.0797, tau = 3.0719, RSS = 171.1802
Fitted model Ca = baseline+delta*exp(-(t-t0)/tau)
Summary from method 'trust-region/levenberg-marquardt'
number of iterations: 9
function evaluations: 46
Jacobian evaluations: 0
reason for stopping: small step size
initial RSS = 17219.221778
final RSS = 171.180170
Number of observation: 173
Number of degrees of freedom: 170
Baseline length: 15
Fit started from point 42
Estimated baseline 0.0530184 and standard error 0.000378172
Estimated delta 0.0796949 and standard error 0.00142419
Estimated tau 3.07185 and standard error 0.0901479
RSS per degree of freedom: 1.00694
Probability of observing a larger of equal RSS per DOF under the null hypothesis: 0.460172
```

We can use valgrind to make sure everything is fine:

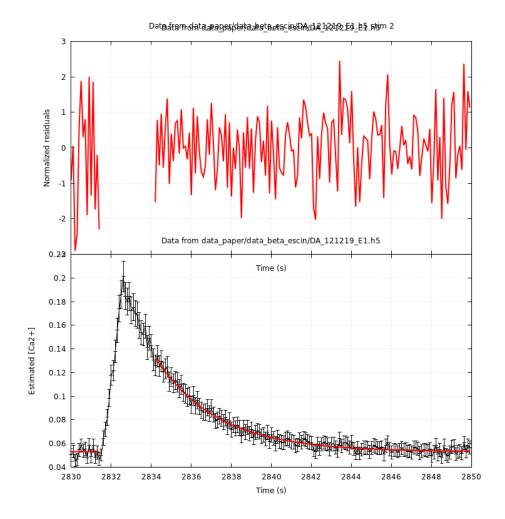
We can look at the top part of file DA_121219_E1_s2_RatioFit with:

```
head DA_121219_E1_s2_RatioFit -n 25
```

```
\verb|# Data from data_paper/data_beta_escin/DA_121219_E1.h5 stim 2|\\
# Ratiometric estimator mono-exponential fit
# Fitted model Ca = baseline+delta*exp(-(t-t0)/tau)
# nobs = 173
# number of degrees of freedom = 170
# baseline length = 15
# fit started from point 42
\# estimated baseline 0.0530184 and standard error 0.000378172
\# estimated delta 0.0796949 and standard error 0.00142419
\mbox{\#} estimated tau 3.07185 and standard error 0.0901479
# residual sum of squares: 171.18
\# RSS per degree of freedom: 1.00694
# Probability of observing a larger of equal RSS per DOF under the null hypothesis: 0.460172
# rss per degree of freedom: 1.00694
        Ca Prediction Residual
# Time
2830.01 0.0504706 0.0530184 -0.913407
2830.11 0.0531824 0.0530184 0.0593775
2830.21 0.0454172 0.0530184 -2.90247
2830.31 0.0466744 0.0530184 -2.42539
2830.41 0.054658 0.0530184 0.581709
2830.51 0.0583309 0.0530184 1.88669
2830.61 0.053892 0.0530184 0.304269
2830.71 0.0554407 0.0530184 0.80927
```

We get the diagnostic plot with:

```
gnuplot -persist DA_121219_E1_s2.gp
```



6 Getting Fura concentration during a stimulation:

fura_concentration

6.1 Motivation

To implement the added buffer approach we need to know (or estimate) the Fura concentration within the cell during a transient. To that end, we write a new program, fura_concentration, that prints to the stdout the estimated [Fura].

6.1.1 fura_concentration **code**

/** \file fura_concentration.c
\brief Program computing the [Fura] and returning it to the stdout

```
#/
#include "abaa.h"
int main(int argc, char *argv[])
{
     <<fura_concentration-usage>>
     </fura_concentration-args>>
     hid_t fid = H5Fopen (filename, H5F_ACC_RDONLY, H5P_DEFAULT);
     aba * paba = aba_read_from_file(fid);
     // Close file
     H5Fclose (fid);
     ts_vector *pfura = fura_est(paba);
     aba_free(paba);
     ts_vector_fprintf(stdout,pfura);
     ts_vector_free(pfura);
     return 0;
}
```

fura_concentration skeleton

```
static char usage[] = \
   "usage: %s -i --input=string\n"
   " -i --input <character string>: data file name (e.g. data_paper/data_beta_escin/DA_121219_E1.h5)\n\n"
   " The program opens 'input' file, estimates the [Fura] within the cell\n"
   " and prints it to the 'stdout'. The loading curve measurements appear first\n"
   " followed by the individual stimalation separated by two blank lines.\n"
   " Results are printed on two columns: Time and [Fura].\n\n"
   " IT IS ASSUMED THAT WHEN THE MAXIMAL BACKGROUND SUBTRACTED FLUORESCENCE AT\n"
   " 360 nm IS OBSERVED, THE FURA CONCENTRATION IN THE CELL AND IN THE PIPETTE\n"
   " ARE IDENTICAL (NO EXTRAPOLATION BASED ON A FIT IS PERFORMED).\n\n";
```

<<fura_concentration-usage>>

This code block reads the program parameters. It assigns (after allocating memory if necessary):

filename pointer to a character string with the name of the data file.

```
case 'i':
    {
      filename = optarg;
    }
    break;
    case 'h': printf(usage,argv[0]);
      return -1;
    default : fprintf(stderr,usage,argv[0]);
      return -1;
    }
}
```

```
cd code && make fura_concentration
```

fura_concentration compilation

```
make: fura_concentration est à jour.
```

6.2 Using fura_concentration

What to do if we forget how to use the program?

```
./code/fura_concentration --help

usage: ./code/fura_concentration -i --input=string
-i --input <character string>: data file name (e.g. data_paper/data_beta_escin/DA_121219_E1.h5)

The program opens 'input' file, estimates the [Fura] within the cell and prints it to the 'stdout'. The loading curve measurements appear first followed by the individual stimalation separated by two blank lines.

Results are printed on two columns: Time and [Fura].

IT IS ASSUMED THAT WHEN THE MAXIMAL BACKGROUND SUBTRACTED FLUORESCENCE AT 360 nm IS OBSERVED, THE FURA CONCENTRATION IN THE CELL AND IN THE PIPETTE ARE IDENTICAL (NO EXTRAPOLATION BASED ON A FIT IS PERFORMED).
```

We run it (at "valgrind" it at the same time) with:

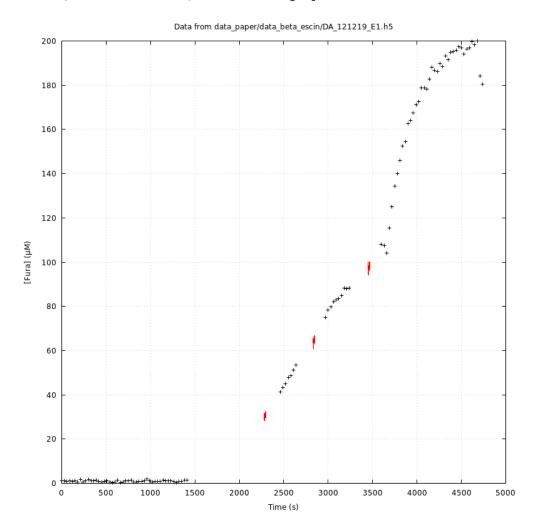
valgrind ./code/fura_concentration -i data_paper/data_beta_escin/DA_121219_E1.h5 > DA_121219_E1_fura

```
==15286== Memcheck, a memory error detector
==15286== Copyright (C) 2002-2017, and GNU GPL'd, by Julian Seward et al.
==15286== Using Valgrind-3.14.0 and LibVEX; rerun with -h for copyright info
==15286== Command: ./code/fura_concentration -i data_paper/data_beta_escin/DA_121219_E1.h5
```

66

```
==15286==
==15286== HEAP SUMMARY:
==15286== in use at exit: 0 bytes in 0 blocks
==15286== total heap usage: 4,864 allocs, 4,864 frees, 2,414,493 bytes allocated
==15286==
==15286== All heap blocks were freed -- no leaks are possible
==15286==
==15286== For counts of detected and suppressed errors, rerun with: -v
==15286== ERROR SUMMARY: 0 errors from 0 contexts (suppressed: 0 from 0)
```

Displaying the output is straightforward with gnuplot:



6.3 fura_during_stim

We now define a program that reads from the stdin fura concentrations having the same format as what fura_concentration prints to the stdout and then get the mean, min and max [Fura] values during a specific part of a stimulation.

6.3.1 fura_during_stim code

```
/** \file fura_during_stim.c
   \brief Use output of fura_concentration to get mean, min and max [Fura]
          during a specific stimulation.
#include "abaa.h"
int main(int argc, char *argv[])
 <<fura_during_stim-usage>>
 <<fura_during_stim-args>>
 char buffer[256];
 int n1,n2;
 int in=0;
  // Read line per line
 while (fgets(buffer, sizeof(buffer), stdin) && in == 0)
   // Look for right pattern in line
   if (2 == sscanf(buffer, "# Stim %d with %d elements", &n1,&n2))
      // Extract relevant value
     if ((size_t) n1 == stim)
       in = 1;
  if (in==0)
   printf("Stim %d not found!\n", (int) stim);
 size_t n_obs = n2;
  // Advance start_fit-1 lines
 size_t i;
 for (i=0; i<start_fit; i++)</pre>
   fgets(buffer, sizeof(buffer), stdin);
  double fura_cum=0.0,fura_min=1e6,fura_max=0.0;
 for (; i<n_obs; i++) {
   float time,fura_val;
   double fura;
   fscanf(stdin,"%f %f",&time,&fura_val);
   fura = (double) fura_val;
   fura_cum += fura;
   if (fura < fura_min)</pre>
     fura_min = fura;
   if (fura > fura_max)
     fura_max=fura;
 printf("%g %g %g\n",
        fura_cum/(n_obs-start_fit),
        fura_min,
        fura_max);
 return 0;
```

${\tt fura_during_stim} \ {\tt skeleton}$

```
static char usage[] = \
"usage: %s [-s --stim=integer] -f --start_fit=integer \n\n"
```

```
" -s --stim <positive integer>: the stimulation to fit (default 1)\n"
" -f --start_fit <positive integer>: sample point where decay fit starts\n\n"
" The program reads [Fura] from the 'stdin', data are assumed organized in 3 columns:\n"
" Index Time and [Fura]\n"
" Several data sets called 'loading curve', 'Stimulation 1', 'Stimulation 2', etc\n"
" are assumed to be present with 2 blank lines (gnuplot style) separating each data\n"
" set. Each set starts with its name following a '#', the next line also starts with a\n"
" '#' and contains '# xxx observations', where 'xxx' is the number of observations in\n"
" the data set. The program goes to stimulation specified by 's' (default 1) and starts\n"
" dealing with data starting from observation specified by parameter 'f'. The value of\n"
" the latter parameter should be set to the value given in line '# fit started from point yy'\n"
" in the file generated by a call to 'fit_ratiometric' ('yy' stands for the value of 'f').\n"
" The program prints to the 'stdout' the mean, min and max [Fura] from point 'f'.\n\n";
```

<<fura_during_stim-usage>>

<<fr><<fura_during_stim-args>> This code block reads the program parameters. It assigns:
stim stim number.

start_fit the sample point from which the decay gets fitted.

```
size_t stim=1;
size_t start_fit;
{int opt;
  static struct option long_options[] = {
    {"stim",optional_argument,NULL,'s'},
    {"start_fit",required_argument,NULL,'f'},
    {"help", no_argument, NULL, 'h'},
    {NULL,0,NULL,0}
  7:
  int long_index =0;
  while ((opt = getopt_long(argc,argv,
                            "hs:f:",
                            long_options,
                            &long_index)) != -1) {
    switch(opt) {
    case 's':
     stim = (size_t) atoi(optarg);
    }
    break;
    case 'f':
    {
     start_fit = (size_t) atof(optarg);
    }
    break:
    case 'h': printf(usage,argv[0]);
     return -1;
    default : fprintf(stderr,usage,argv[0]);
     return -1;
 }
}
```

```
cd code && make fura_during_stim
```

fura_during_stim compilation

```
make: fura_during_stim est à jour.
```

6.4 Using fura_during_stim

What to do if we forget how to use the program?

```
./code/fura_during_stim --help

usage: ./code/fura_during_stim [-s --stim=integer] -f --start_fit=integer

-s --stim <positive integer>: the stimulation to fit (default 1)

-f --start_fit <positive integer>: sample point where decay fit starts

The program reads [Fura] from the 'stdin', data are assumed organized in 3 columns:
    Index Time and [Fura]

Several data sets called 'loading curve', 'Stimulation 1', 'Stimulation 2', etc are assumed to be present with 2 blank lines (gnuplot style) separating each data set. Each set starts with its name following a '#', the next line also starts with a '#' and contains '# xxx observations', where 'xxx' is the number of observations in the data set. The program goes to stimulation specified by 's' (default 1) and starts dealing with data starting from observation specified by parameter 'f'. The value of the latter parameter should be set to the value given in line '# fit started from point yy' in the file generated by a call to 'fit_ratiometric' ('yy' stands for the value of 'f').

The program prints to the 'stdout' the mean, min and max [Fura] from point 'f'.
```

We run it with (we do not need a valgrind test here since the program doesn't perform any memory allocation):

```
./code/fura_during_stim -s 2 -f 42 < DA_121219_E1_fura
```

70

We can do the last call in a more sophisticated and more automatic manner:

```
file_name=DA_121219_E1_s2_RatioFit
stim=`grep "stim " $file_name | sed -e "s/# Data .* stim //g"`
start_fit=`grep "# fit started from point" $file_name | sed -e "s/# fit started from point //g"`
./code/fura_concentration -i data_paper/data_beta_escin/DA_121219_E1.h5 | ./code/fura_during_stim -s $stim -f $start_fit
```

64.3812 61.4134 67.0886

64.3812 61.4134 67.0886

We can now construct a line containing everything we will need for the weighted linear regression leading to the endogenous κ parameter in the added buffer approach with:

```
file_name=DA_121219_E1_s2_RatioFit

stim=`grep "stim " \$file_name | sed -e "s/# Data .* stim //g"`

start_fit=`grep "# fit started from point" \$file_name | sed -e "s/# fit started from point //g"`

fura_conc=`./code/fura_concentration - i data_paper/data_beta_escin/DA_121219_E1.h5 | ./code/fura_during_stim -s \$stim -f

tau_and_se=`grep "# estimated tau" \$file_name | sed -e "s/# estimated tau //g" | sed -e "s/ and standard error//g"`

Ca=`grep "# estimated baseline" \$file_name | sed -e "s/# estimated baseline //g" | sed -e "s/ and standard error .*//g"`

echo \$fura_conc \$Ca \$tau_and_se
```

64.3812 61.4134 67.0886 0.0530184 3.07185 0.0901479

7 Getting the time constant as a function of κ_F

7.1 We start by fitting each of the free transients of data set

DA_121219_E1.h5

7.1.1 First transient

```
./code/fit_ratiometric -i data_paper/data_beta_escin/DA_121219_E1.h5 -o DA_121219_E1_s1 -s 1 -g
```

```
iter 0: baseline = 0.0586, delta = 0.1231, tau = 16.5000, RSS = 22664.2848
iter 1: baseline = 0.0597, delta = 0.0565, tau = 5.3161, RSS = 658.4080
      2: baseline = 0.0583, delta = 0.0629, tau = 3.8287, RSS = 414.3510
iter 3: baseline = 0.0585, delta = 0.0783, tau = 3.0541, RSS = 258.6214
iter 4: baseline = 0.0587, delta = 0.0971, tau = 2.5991, RSS = 155.1582
iter 5: baseline = 0.0588, delta = 0.1095, tau = 2.4067, RSS = 129.3976
iter 6: baseline = 0.0589, delta = 0.1132, tau = 2.3526, RSS = 127.7445
iter 7: baseline = 0.0589, delta = 0.1137, tau = 2.3436, RSS = 127.7223
iter 8: baseline = 0.0589, delta = 0.1137, tau = 2.3427, RSS = 127.7222
iter 9: baseline = 0.0589, delta = 0.1137, tau = 2.3427, RSS = 127.7222
iter 10: baseline = 0.0589, delta = 0.1137, tau = 2.3427, RSS = 127.7222
iter 11: baseline = 0.0589, delta = 0.1137, tau = 2.3427, RSS = 127.7222
iter 12: baseline = 0.0589, delta = 0.1137, tau = 2.3427, RSS = 127.7222
Fitted model Ca = baseline+delta*exp(-(t-t0)/tau)
Summary from method 'trust-region/levenberg-marquardt'
number of iterations: 12
function evaluations: 56
Jacobian evaluations: 0
reason for stopping: small step size
initial RSS = 22664.284799
final RSS = 127.722162
Number of observation: 181
Number of degrees of freedom: 178
Baseline length: 15
Fit started from point 34
Estimated baseline 0.0588818 and standard error 0.000546884
Estimated delta 0.113685 and standard error 0.00338681
```

```
Estimated tau 2.34267 and standard error 0.0946631
RSS per degree of freedom: 0.71754
Probability of observing a larger of equal RSS per DOF under the null hypothesis: 0.998311
```

We then get the first line of our tau versus Fura file:

```
./code/fura_concentration -i data_paper/data_beta_escin/DA_121219_E1.h5 > DA_121219_E1_fura
file_name=DA_121219_E1_s1_RatioFit
stim=`grep "stim " \file_name | sed -e "s/# Data .* stim //g"`
start_fit=`grep "# fit started from point" \file_name | sed -e "s/# fit started from point //g"`
fura_conc=`./code/fura_during_stim -s \file_name | sed -e "s/# estimated tau //g" | sed -e "s/ and standard error//g"`
tau_and_se=`grep "# estimated tau" \file_name | sed -e "s/# estimated tau //g" | sed -e "s/ and standard error .*//g"`
echo \fura_conc \fura_con
```

7.1.2 Second transient

```
./code/fit_ratiometric -i data_paper/data_beta_escin/DA_121219_E1.h5 -o DA_121219_E1_s2 -s 2 -g
```

```
iter 0: baseline = 0.0505, delta = 0.0755, tau = 15.7000, RSS = 17219.2218
iter 1: baseline = 0.0532, delta = 0.0525, tau = 1.2056, RSS = 3257.7394
iter 2: baseline = 0.0563, delta = 0.0633, tau = 3.3014, RSS = 402.2209
iter 3: baseline = 0.0530, delta = 0.0794, tau = 3.0219, RSS = 172.8142
iter 4: baseline = 0.0530, delta = 0.0797, tau = 3.0698, RSS = 171.1807
     5: baseline = 0.0530, delta = 0.0797, tau = 3.0718, RSS = 171.1802
iter 6: baseline = 0.0530, delta = 0.0797, tau = 3.0718, RSS = 171.1802
iter 7: baseline = 0.0530, delta = 0.0797, tau = 3.0719, RSS = 171.1802
iter 8: baseline = 0.0530, delta = 0.0797, tau = 3.0719, RSS = 171.1802
iter 9: baseline = 0.0530, delta = 0.0797, tau = 3.0719, RSS = 171.1802
Fitted model Ca = baseline+delta*exp(-(t-t0)/tau)
Summary from method 'trust-region/levenberg-marquardt'
number of iterations: 9
function evaluations: 46
Jacobian evaluations: 0
reason for stopping: small step size
initial RSS = 17219.221778
final RSS = 171.180170
Number of observation: 173
Number of degrees of freedom: 170
Baseline length: 15
Fit started from point 42
Estimated baseline 0.0530184 and standard error 0.000378172
Estimated delta 0.0796949 and standard error 0.00142419
Estimated tau 3.07185 and standard error 0.0901479
RSS per degree of freedom: 1.00694
Probability of observing a larger of equal RSS per DOF under the null hypothesis: 0.460172
```

We then get the second line of our tau versus Fura file:

```
file_name=DA_121219_E1_s2_RatioFit

stim=`grep "stim " $file_name | sed -e "s/# Data .* stim //g"`

start_fit=`grep "# fit started from point" $file_name | sed -e "s/# fit started from point //g"`

fura_conc=`./code/fura_during_stim -s $stim -f $start_fit < DA_121219_E1_fura`

tau_and_se=`grep "# estimated tau" $file_name | sed -e "s/# estimated tau //g" | sed -e "s/ and standard error//g"`

Ca=`grep "# estimated baseline" $file_name | sed -e "s/# estimated baseline //g" | sed -e "s/ and standard error .*//g"`

echo $fura_conc $Ca $tau_and_se >> DA_121219_E1_tau_vs_fura
```

7.1.3 Third transient

```
./code/fit_ratiometric -i data_paper/data_beta_escin/DA_121219_E1.h5 -o DA_121219_E1_s3 -s 3 -g
iter 0: baseline = 0.0507, delta = 0.0530, tau = 14.7000, RSS = 10888.6212
iter 1: baseline = 0.0494, delta = 0.0467, tau = 1.1453, RSS = 5829.0426
iter 2: baseline = 0.0559, delta = 0.0383, tau = 3.1382, RSS = 963.6889
iter 3: baseline = 0.0508, delta = 0.0549, tau = 4.5807, RSS = 204.7654
iter 4: baseline = 0.0499, delta = 0.0560, tau = 4.3772, RSS = 158.6090
iter 5: baseline = 0.0500, delta = 0.0561, tau = 4.3649, RSS = 158.5868
iter 6: baseline = 0.0500, delta = 0.0561, tau = 4.3638, RSS = 158.5868
iter 7: baseline = 0.0500, delta = 0.0561, tau = 4.3637, RSS = 158.5868
iter 8: baseline = 0.0500, delta = 0.0561, tau = 4.3637, RSS = 158.5868
iter 9: baseline = 0.0500, delta = 0.0561, tau = 4.3637, RSS = 158.5868
iter 10: baseline = 0.0500, delta = 0.0561, tau = 4.3637, RSS = 158.5868
iter 11: baseline = 0.0500, delta = 0.0561, tau = 4.3637, RSS = 158.5868
Fitted model Ca = baseline+delta*exp(-(t-t0)/tau)
Summary from method 'trust-region/levenberg-marquardt'
number of iterations: 11
function evaluations: 48
Jacobian evaluations: 0
reason for stopping: small step size
initial RSS = 10888.621234
final RSS = 158.586760
Number of observation: 163
Number of degrees of freedom: 160
Baseline length: 15
Fit started from point 52
Estimated baseline 0.049958 and standard error 0.000388658
Estimated delta 0.05609 and standard error 0.000821936
Estimated tau 4.36367 and standard error 0.13015
RSS per degree of freedom: 0.991167
```

Probability of observing a larger of equal RSS per DOF under the null hypothesis: 0.516723

We then get the third line of our tau versus Fura file:

```
file_name=DA_121219_E1_s3_RatioFit

stim=`grep "stim " \file_name | sed -e "s/# Data .* stim //g"`

start_fit=`grep "# fit started from point" \file_name | sed -e "s/# fit started from point //g"`

fura_conc=`./code/fura_during_stim -s \file_name | sed -e "s/# fit started from point //g"`

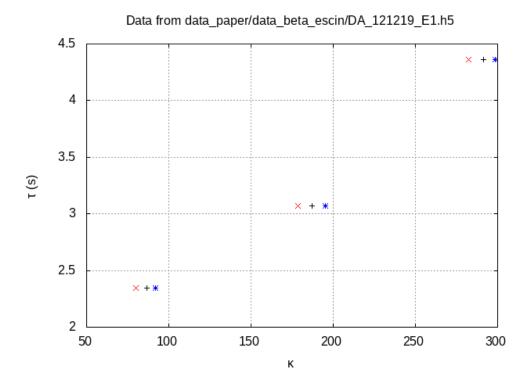
tau_and_se=`grep "# estimated tau" \file_name | sed -e "s/# estimated tau //g" | sed -e "s/ and standard error//g"`

Ca=`grep "# estimated baseline" \file_name | sed -e "s/# estimated baseline //g" | sed -e "s/ and standard error .*//g"`

echo \file_fura_conc \file_fura_conc \file_name | sed -e "s/# estimated baseline //g" | sed -e "s/ and standard error .*//g"`
```

7.2 Plotting τ as a function of κ_F

We plot the results with gnuplot:



8 A program doing all that at once

It can become quit "painful" to repeat the steps of the previous section all other for each new experiment. We therefore write a program that does everything at once:

- 1. Reads the data.
- 2. Get the loading curve.
- 3. Fits a mono-exponential decay to the ratiometric estimators of the user specified stimulations.
- 4. Fits a weighted linear regression to the decay time constant vs κ_F and get the two key parameters: γ/v and κ_S .

A text file (or several ones, like in step 3) is/are generated at each step.

8.1 The aba_ratio program

We will call our aba_ratio since it implements the added buffer approach using the ratiometric estimator.

8.1.1 aba_ratio code

aba_ratio **skeleton** The program <<aba_ratio.c>> gets stored in file code/aba_ratio.c:

```
/** \file aba_ratio.c
    \brief Added buffer approach using the ratiometric estimator
    This program does "everything at once":
    1. Reads the data.
    2. Get the loading curve.
    3. Fits a mono-exponential decay to the ratiometric estimators of the user specified stimulations.
    4. Fits a weighted linear regression to the decay time constant vs \f$\kappa_{F}\f$ and get the two key parameters:
    The last fit, time constant vs f^{\star} is performed in 3 different ways using respectively the mean f^{\star} is
    value during the fitted part of the transient, the minimal or the maximal value.
    A text file (or several ones, like in step 3) is/are generated at each step.
#include "abaa.h"
/** \def NREP 10000
    \brief Number of replicates in MC/Bootstrap simulations
#define NREP 10000
int wls_fit(const gsl_vector * kappa,
            mono_exp_fit_res * fit_res,
            size_t n_stim,
            char * filename,
            char * output,
            gsl_rng * rng,
            int what,
            size_t *stim);
int robust_fit(const gsl_vector * kappa,
               mono_exp_fit_res * fit_res,
               size_t n_stim,
               char * filename,
               char * output,
               gsl_rng * rng,
               int what,
               size_t *stim);
int main(int argc, char *argv[])
{
    This code block defines a character strings containing the
   help of the program.
  <<aba_ratio-usage>>
    This code block reads the program parameters. It assigns (after allocating memory if necessary):
     - filename: pointer to a character string with the name of the data file.
     - output: pointer to a character string with the name of the output file name.
     - stim: an array with the numbers of the stimulations to use.
    - maxiter, baseline_length: maximal number of iterations and baseline length.
```

```
- start_fit: the number used to set from where the decay gets fitted.
  - g_script: indicates if a gnuplot script should be generated.
<<aba_ratio-args>>
  This code block opens HDF5 file `filename`.
   `paba` is a pointer to an aba structure that gets
   allocated and initialized.
  Do not forget to free the memory pointed to by `paba` before
program exit.
*/
<<aba_ratio-read-data>>
  This code block allocates and initializes a ts_vector
  structure pointed to by `pfura`.
  A char array, `out`, with 512 elements is declared.
  A file pointer, `fp`, is declared.
  The loading curve is printed to a file named `output_loading_curve`.
  Do not forget to free `pfura` before program exit.
<<aba_ratio-get-loading-curve>>
if (g_script) {
   This code block generated a gnuplot script
   making the loading curve figure.
   A char array, `file4gp`, with 512 elements is declared.
 <<aba_ratio_loading_curve_g_script>>
}
The next code blocks get the ratiometric estimator
and to the mono-exponential fit for each selected
stimulation.
mono_exp_fit_res fit_res[n_stim];
for (size_t s_idx=0; s_idx<n_stim; s_idx++) {</pre>
 <<aba_ratio_ratiometric_estimator>>
 <<aba_ratio_mono_exp_fit>>
 if (g_script) {
   <<aba_ratio_mono_exp_g_script>>
}
The next block gets the mean, min and max kappa_Fura
values at each stimulation. The result is stored
in three gsl_vector called kappa_mu, kappa_inf and kappa_sup.
These vectors must be freed before exiting the program.
*/
<<aba_ratio_kappa_Fura>>
The next code block does 3 linear regressions
of tau on mean / min / max kappa_Fura
```

```
<<aba_ratio_tau_vs_kappa>>
 if (g_script) {
   <<aba_ratio_tau_vs_kappa_g_script>>
 gsl_vector_free(kappa_mu);
 gsl_vector_free(kappa_inf);
 gsl_vector_free(kappa_sup);
 aba_free(paba);
 ts_vector_free(pfura);
 free(stim);
 return 0;
#define BETAO(c) gsl_vector_get((c),0)
#define BETAO_SE(cov) sqrt(gsl_matrix_get((cov),0,0))
#define BETAO_VAR(cov) gsl_matrix_get((cov),0,0)
#define BETA1(c) gsl_vector_get((c),1)
#define BETA1_SE(cov) sqrt(gsl_matrix_get((cov),1,1))
#define BETA1_VAR(cov) gsl_matrix_get((cov),1,1)
#define gamma_over_v_hat(c) 1.0/BETA1((c))
#define gamma_over_v_se(c,cov) BETA1_SE((cov))/
 gsl_pow_2(BETA1((c)))
#define kappa_s(c) BETAO((c))/BETA1((c))-1.0
#define kappa_s_se(c,cov) sqrt(BETAO_VAR((cov))/gsl_pow_2(BETA1((c)))+\
                               BETA1_VAR((cov))*gsl_pow_2(BETA0((c)))/gsl_pow_4(BETA1((c))))
<<wls_fit>>
<<robust fit>>
```

```
" -b --baseline_length <positive integer>: baseline length in samples (default 15).\n"
   -f --start_fit <positive real>: where decay fit starts, if > 1 interpreted as the \n''
        number of samples after the peak, if 0< f< 1 interpreted as the remaining n"
        fraction of the jump and fitting starts when the transient reaches that level. \n
        Default value: 0.5.\n"
" -r --robust: if set, a robust linear regression of tau vs kappa_Fura is performed\n"
       using a bi-square weight function.\n"
" -g --graphics: if set, gnuplot script files are generated.\n\"
" The program opens 'input' file, get the loading curve and prints the result to a file \ensuremath{\text{n}} "
" named output_loading_curve; then for every stimulation specified in the 'stim' list \n"
" it computes the ratiometric estimator from the raw data\n"
" and fits the following model to it: Ca = baseline + delta * exp (-(t-t0)/tau)n"
" where t0 is the time on the decay phase at which the fit starts (set by parameter 'f').\n"
" A constant is also fitted to the baseline region: Ca = baseline.\n"
" Standard errors for the ratiometric estimator are obtained by Monte-Carlo simulation.\n"
"While the program performs the least-squares optimization relevant information get printed\n"
" to the stderr. The ratiometric estimator and its standard error are printed to a text\n"
" file named 'output_CaRatio_sX' (where 'X' stands for the stimulation number. The fitted\n'
  parameters, fitted values and residuals are printed to a text file named 'output_RatioFit_sX'.\n"
" If 'g' is selected, a gnuplot script file whose name is the 'output_YY_sX.gp' where 'YY' is\n"
" either 'loading_curve' or 'RatioFit' 'is generated. A graphical display\n"
" of the result can then be obtained with: gnuplot -persist 'output_YY_sX.gp'\n\n"
"Once each specified stimulation has been fitted, a regression of tau vs kappa is performed\n"
" using three different values for kappa: the mean value during the fitted part of the transient, \n"
" the minimal and the maximal values. Information and fit results get printed to the 'stderr' as\n"
"well as to files named 'output_aba_tau_vs_mean/min/max_kappa', if option '-g' is set, gnuplot\n"
"script files are also generated with names 'output_aba_tau_vs_mean/min/max_kappa.gp'\n\n"
"When a robust linear regression is requested (by using optional argument '-r' or '--robust'\n"
" when calling the program), a bi-square weight function is used (see:\n"
" https://www.gnu.org/software/gsl/doc/html/lls.html#robust-linear-regression). Since\n"
" the robust methods implemented in the GSL do not allow for the use of the standard errors on\n"
" the dependent variable, we multiply the observations in order to have approximately the\n"
" right standard error ratio: that is, if an observation has a standard error of 0.13 and\n"
" another one has 0.091, we will include two identical copies of the second since (0.13/0.091)^2\n"
" is approximately 2. This use of multiple copies is reported to the user.\n\";
```

<<aba_ratio-usage>>

```
char *filename;
char output[512];
size_t maxiter=50, baseline_length=15;
double start_fit=0.5;
int g_script=0;
size_t n_stim = 0; // initialize the stimulation counter
size_t *stim;
int do_robust = 0;
int out_unset=1; // Indicator of output specification
  static struct option long_options[] = {
    {"input", required_argument, NULL, 'i'},
    {"output", optional_argument, NULL, 'o'},
    {"stim", optional_argument, NULL, 's'},
    {"graphic", optional_argument, NULL, 'g'},
    {"maxiter", optional_argument, NULL, 'm'},
    {"baseline_length",optional_argument,NULL,'b'},
```

```
{"start_fit", optional_argument, NULL, 'f'},
  {"robust", optional_argument, NULL, 'r'},
  {"help", no_argument, NULL, 'h'},
  {NULL,0,NULL,0}
};
int long_index =0;
while ((opt = getopt_long(argc,argv,
                         "hgri:o:s:m:b:f:",
                          long_options,
                          &long_index)) != -1) {
 switch(opt) {
 case 'i':
  {
   filename = optarg;
 break;
  case 'o':
  {
   out_unset = 0;
   strcpy(output,optarg);
 }
 break;
  case 'g':
   g_script=1;
 break;
  case 'r':
   do_robust=1;
 }
 break;
  case 's':
   char *start = strdup(optarg); // duplicate optarg content
   char *running;
    running = start;
   char *token = strsep(&running, ",");
    while (token != NULL) {
     token = strsep (&running, ","); // split optarg at each ","
     n_stim++;
   free(start);
    // The number of stimulation is now known
    // Allocate memory for the vector of stim indexes
    stim=malloc(n_stim*sizeof(size_t));
   start = strdup(optarg); // duplicate optarg content again
   running = start;
   // Get the index of each stimulation
   for (size_t i=0; i<n_stim; i++) {</pre>
     token = strsep (&running, ",");
     stim[i] = (size_t) atoi(token);
   }
   free(start);
 }
 break;
  case 'm':
  {
```

```
maxiter = (size_t) atoi(optarg);
   }
   break;
   case 'b':
     baseline_length = (size_t) atoi(optarg);
    }
    break;
    case 'f':
     start_fit = (double) atof(optarg);
     if (start_fit<=0) {</pre>
       fprintf(stderr, "start_fit should be > 0.\n");
       return -1;
     }
   }
   break;
   case 'h': printf(usage,argv[0]);
     return -1;
   default : fprintf(stderr,usage,argv[0]);
     return -1;
   }
 }
}
// Set output prefix name if not given
if (out_unset) {
 char *start = strdup(filename); // duplicate filename content
 char *p = strtok(start,"."); // stop at ".h5"
 strcpy(output,p);
 strcat(output,"_aba");
 free(start);
```

<<aba_ratio-args>>

```
hid_t fid = H5Fopen (filename, H5F_ACC_RDONLY, H5P_DEFAULT);
aba * paba = aba_read_from_file(fid);
// Close file
H5Fclose (fid);
// Take care of the default for stim
if (n_stim == 0) {
    n_stim = paba->data->nelt-1;
    stim = malloc(n_stim*sizeof(size_t));
    for (size_t s_idx=0; s_idx<n_stim; s_idx++)
        stim[s_idx]=s_idx+1;
}</pre>
```

<<aba_ratio-read-data>>

```
ts_vector *pfura = fura_est(paba);
char out[512];
strcpy(out,output);
```

```
strcat(out,"_loading_curve");
FILE *fp = fopen(out,"w");
fprintf(fp,"# Cellular [Fura] for dataset %s\n\n",filename);
ts_vector_fprintf(fp,pfura);
fclose(fp);
```

<<aba_ratio-get-loading-curve>>

<<aba_ratio_loading_curve_g_script>> We write the gnuplot script generating the diagnostic plot:

```
char file4gp[512];
strcpy(file4gp,output);
strcat(file4gp,"_loading_curve");
strcpy(out,output);
strcat(out,"_loading_curve.gp");
fp = fopen(out,"w");
fprintf(fp,
       "unset key\n"
       "set grid\n"
       "set ylabel '[Fura] (\muM)'\n"
       "set xlabel 'Time (s)'\n"
       "plot '%s' index 0 using 1:2 linecolor rgb 'black',\\\n",  
       file4gp);
for (size_t i=0; i<n_stim; i++)</pre>
 fclose(fp);
```

```
fprintf(stderr,
       "* Doing now stimulation %d\n"
      (int) stim[s_idx]);
ratio * pratio = ratio_est(paba->data->adu_v[stim[s_idx]],
                      &paba->dye,&paba->light,
                       &paba->ccd,NREP);
strcpy(out,output);
strcat(out,"_CaRatio_s");
char stim_nb[99];
sprintf(stim_nb,"%d", (int) stim[s_idx]);
strcat(out,stim_nb);
FILE *fp = fopen(out,"w");
fprintf(fp,"# Data from %s stim %d\n",filename,(int) stim[s_idx]);
fprintf(fp,"# Ratiometric estimator\n");
ratio_fprintf(fp,pratio);
fclose(fp);
```

<<aba_ratio_ratiometric_estimator>>

```
size_t start_pos;
if (start_fit >= 1)
 start_pos = (size_t) start_fit;
else
 start_pos = ratio_find_fit_start(pratio,start_fit,baseline_length);
fit_res[s_idx] = ratio_fit(pratio,baseline_length,start_pos,maxiter);
strcpy(out,output);
strcat(out,"_RatioFit_s");
strcat(out,stim_nb);
fp = fopen(out,"w");
fprintf(fp,"# Data from %s stim %d\n",filename,(int) stim[s_idx]);
fprintf(fp,"# Ratiometric estimator mono-exponential fit\n");
mono_exp_fit_res_fprintf(fp,&fit_res[s_idx],pratio);
fclose(fp);
ratio_free(pratio);
fprintf(stderr,
       "* Stimulation %d done\n"
       "*********\n\n",
       (int) stim[s_idx]);
```

<<aba_ratio_mono_exp_fit>>

```
strcpy(out,output);
strcat(out,"_RatioFit_s");
strcat(out,stim_nb);
strcat(out,".gp");
fp = fopen(out,"w");
char RatioFit[512];
strcpy(RatioFit,output);
strcat(RatioFit,"_RatioFit_s");
strcat(RatioFit,stim_nb);
char CaRatio[512];
strcpy(CaRatio,output);
strcat(CaRatio,"_CaRatio_s");
strcat(CaRatio,stim_nb);
char format[] = "%g";
fprintf(fp,
        "unset key\n"
        "set grid\n"
        "set multiplot title 'Data from %s stim %d' noenhanced layout 2,1 margins 0.1,0.9,0.1,0.95 spacing 0,0\n"
        "set ylabel 'Normalized residuals'\n"
        "set xtics format ''\n"
        "plot '%s' using 1:4 with lines line
color rgb 'red' linewidth 2\n"
        "set format x '%s'\n"
        "set xlabel 'Time (s)'\n"
        "set ylabel 'Estimated [Ca2+]'\n"
        "plot '%s' using 1:2:($3*1.96) with yerrorlines \\\n"
             linecolor rgb 'black' linewidth 1,
                                                                \\\n"
              '%s' using 1:3 with lines linecolor rgb 'red'\\n"
             linewidth 2\n"
        "unset multiplot",
        filename, (int) stim[s_idx], RatioFit, format, CaRatio, RatioFit);
fclose(fp);
```

```
gsl_vector * kappa_mu = gsl_vector_alloc(n_stim);
gsl_vector * kappa_inf = gsl_vector_alloc(n_stim);
gsl_vector * kappa_sup = gsl_vector_alloc(n_stim);
for (size_t s_idx=0; s_idx<n_stim; s_idx++) {</pre>
 double K_d=paba->dye.K_d_hat;
 double Ca = (fit_res[s_idx]).baseline;
 double res=K_d/gsl_pow_2(K_d+Ca);
 double res_inf,res_sup;
 gsl_vector * fura_conc=pfura->ts_v[stim[s_idx]]->AMPLITUDE;
 {\tt gsl\_vector\_const\_view~Fura=gsl\_vector\_const\_subvector(fura\_conc,}
                                                          (fit_res[s_idx]).fit_start,
                                                          fura_conc->size-(fit_res[s_idx]).fit_start);
 // We take as [Fura] the mean [Fura] over the fitted decay period
 res *= gsl_stats_mean(Fura.vector.data,1,Fura.vector.size);
 gsl_stats_minmax(&res_inf,&res_sup,Fura.vector.data,1,Fura.vector.size);
 gsl_vector_set(kappa_mu, s_idx, res);
 {\tt gsl\_vector\_set(kappa\_inf, s\_idx, res\_inf*K\_d/gsl\_pow\_2(K\_d+Ca));}
 gsl_vector_set(kappa_sup, s_idx, res_sup*K_d/gsl_pow_2(K_d+Ca));
```

<<aba_ratio_kappa_Fura>>

```
// Set up RNG for MC
const gsl_rng_type * T = gsl_rng_default;
gsl_rng_env_setup();
gsl_rng * rng = gsl_rng_alloc (T);
if (do_robust) {
  // Fit and print tau vs mean kappa value
  robust_fit(kappa_mu,fit_res,n_stim,filename,output,rng,0,stim);
  // Fit and print tau vs min kappa value
  robust_fit(kappa_inf,fit_res,n_stim,filename,output,rng,1,stim);
  // Fit and print tau vs max kappa value
  robust_fit(kappa_sup,fit_res,n_stim,filename,output,rng,2,stim);
} else {
  // Fit and print tau vs mean kappa value
  {\tt wls\_fit(kappa\_mu,fit\_res,n\_stim,filename,output,rng,0,stim);}
  // Fit and print tau vs min kappa value
  wls_fit(kappa_inf,fit_res,n_stim,filename,output,rng,1,stim);
  // Fit and print tau vs max kappa value
  wls_fit(kappa_sup,fit_res,n_stim,filename,output,rng,2,stim);
// Free RNG
gsl_rng_free (rng);
```

<<aba_ratio_tau_vs_kappa>>

```
char file4gp[512];
//define a macro generating the gnuplot script
{\tt \#define\ mk\_gp\_script(p\_name)} \setminus
 strcpy(file4gp,output);\
 strcat(file4gp,"_tau_vs_" #p_name "_kappa");\
 strcpy(out,output);\
 strcat(out,"_tau_vs_" #p_name "_kappa.gp");\
  fp = fopen(out, "w");\
  fprintf(fp,\
    "unset key\n"\
    "set grid\n"
    "set ylabel ' (s)'\n"\
    "set title 'Data from %s' noenhanced\n"\
    "set xrange [-1000<*:*]\n"\
    "plot '%s' index 0 using 1:2:(1.96*$3) linecolor rgb 'red' with yerrorbars,\\\n",\
         filename,file4gp);\
  fprintf(fp,\
         "'' index 1 using 1:2 with lines linecolor rgb 'black', \\\n");\
  fprintf(fp,\
          "'' index 1 using 1:3 with lines linecolor rgb 'blue' lt 'dotted', \\\n");\
  fprintf(fp,\
          "'' index 1 using 1:4 with lines linecolor rgb 'blue' lt 'dotted'");\
  fclose(fp);\
#define mk_gp_script_robust(p_name)\
  strcpy(file4gp,output);\
 strcat(file4gp,"_tau_vs_" #p_name "_kappa_robust");\
  strcpy(out,output);\
  strcat(out,"_tau_vs_" #p_name "_kappa_robust.gp");\
  fp = fopen(out,"w");\
  fprintf(fp,\
    "unset key\n"\
    "set grid\n"
    "set ylabel ' (s)'\n"\
    "set xlabel '" #p_name " _Fura' noenhanced\n"\
   "set title 'Data from %s' noenhanced\n"\
    "plot '%s' index 0 using 1:2:(1.96*$3) linecolor rgb 'red' with yerrorbars,\\\n",\
         filename,file4gp);\
  fprintf(fp,\
          "'' index 1 using 1:2 with lines linecolor rgb 'black', \\\n");\
  fprintf(fp,\
          "'' index 1 using 1:3 with lines linecolor rgb 'black' lt 'dotted', \\\n");
  fprintf(fp,\
         "'' index 1 using 1:4 with lines line
color rgb 'black' lt 'dotted',\\\n");\
  fprintf(fp,\
          "'' index 1 using 1:5 with lines linecolor rgb 'blue', \\\n"); \
  fprintf(fp,\
         "'' index 1 using 1:6 with lines linecolor rgb 'blue' lt 'dotted', \\\n");\
  fprintf(fp,\
          "'' index 1 using 1:7 with lines linecolor rgb 'blue' lt 'dotted'");
  fclose(fp);\
if (do_robust) {
mk_gp_script_robust(mean)
mk_gp_script_robust(min)
```

```
mk_gp_script_robust(max)
} else {
mk_gp_script(mean)

mk_gp_script(min)

mk_gp_script(max)
}
```

<<aba_ratio_tau_vs_kappa_g_script>>

```
/// Obrief Performs a weighted linear regression and prints results
/// to `stderr` and to a file whose prefix is built from
111
          `output`.
111
/// @returns 0 if everything is fine
int wls_fit(const gsl_vector * kappa, ///< [in] vector of kappa values.</pre>
           mono_exp_fit_res * fit_res, ///< [in] vector of mono_exp_fit_res.</pre>
           {\tt size\_t} n_stim, ///< [in] the number of stimulation.
           char * filename, ///< Name of file containing the data</pre>
           char * output, ///< Prefix of file name where results are written</pre>
           gsl_rng * rng, ///< Pointer to a gsl_rng</pre>
           int what, ///< What is processed? 0 = mean, 1 = min, 2 = max</pre>
           size_t *stim ///< [in] Vector of indexes of used stimulation</pre>
 )
{
 if (what==0)
   fprintf(stderr,"* Doing tau vs mean kappa_Fura regression *\n");
  if (what == 1)
   fprintf(stderr,"* Doing tau vs min kappa_Fura regression *\n");
  if (what==2)
   fprintf(stderr,"* Doing tau vs max kappa_Fura regression *\n");
  gsl_vector * c = gsl_vector_alloc(2);
 gsl_matrix * cov = gsl_matrix_alloc(2,2);
  double chisq,tss;
  // Prepare data for fit
 gsl_vector * tau = gsl_vector_alloc(n_stim); // The dependent variable
 gsl\_vector * w = gsl\_vector\_alloc(n\_stim); // The weight of the above
 for (size_t s_idx=0; s_idx<n_stim; s_idx++) {
   gsl_vector_set(tau, s_idx, (fit_res[s_idx]).tau);
   gsl_vector_set(w, s_idx, 1.0/gsl_pow_2((fit_res[s_idx]).tau_se));
  // Get total sum of squares (TSS)
 tss = gsl_stats_wtss(w->data,1,tau->data,1,tau->size);
  // Allocate design matrix
 gsl_matrix * X = gsl_matrix_alloc(n_stim,2);
  // Fill design matrix
 for (size_t s_idx=0; s_idx<n_stim; s_idx++) {
   gsl_matrix_set(X,s_idx,0,1.0);
   {\tt gsl\_matrix\_set(X,s\_idx,1,gsl\_vector\_get(kappa,s\_idx));}
 gsl_multifit_linear_workspace * work = gsl_multifit_linear_alloc (n_stim, 2);
```

```
gsl_multifit_wlinear (X, w, tau, c, cov, &chisq, work);
gsl_multifit_linear_free (work);
double kappa_S_MC[NREP];
double beta0 = BETAO(c);
double beta1 = BETA1(c);
double cov00 = BETAO_VAR(cov);
double cov11 = BETA1_VAR(cov);
double beta0_se = BETA0_SE(cov);
double kappa_S = kappa_s(c);
double kappa_S_se = kappa_s_se(c,cov);
double se11=BETA1_SE(cov);
double rho=gsl_matrix_get(cov,0,1)/beta0_se/se11;
for (size_t rep_idx=0; rep_idx<NREP; rep_idx++) {</pre>
 double num, denom;
 gsl_ran_bivariate_gaussian(rng,beta0_se,se11,rho,&num,&denom);
 num+=beta0:
 denom+=beta1;
  //double num=(beta0+gsl_ran_gaussian_ziggurat(rng,beta0_se));
  //double denom=(beta1+gsl_ran_gaussian_ziggurat(rng,se11));
 kappa_S_MC[rep_idx] = num/denom-1.0;
gsl_sort(kappa_S_MC,1,NREP);
double kappa_S_195=kappa_S_MC[(size_t)(0.025*NREP-1)];
double kappa_S_u95=kappa_S_MC[(size_t)(0.975*NREP-1)];
double kappa_S_199=kappa_S_MC[(size_t)(0.005*NREP-1)];
double kappa_S_u99=kappa_S_MC[(size_t)(0.995*NREP-1)];
fprintf(stderr, "Best fit: tau = %g + %g kappa_Fura\n", beta0 , beta1 );
fprintf(stderr, "Covariance matrix:\n");
fprintf(stderr, "Total sum of squares (TSS) = %g\n", tss);
fprintf(stderr,"chisq (Residual sum of squares, RSS) = %g\n", chisq);
double p_larger = gsl_cdf_chisq_Q(chisq,n_stim-2);
fprintf(stderr, "Probability of observing a larger of equal RSS per DOF under the null hypothesis: %g\n",p_larger);
fprintf(stderr,"R squared (1-RSS/TSS) = %g\n", 1 - chisq / tss);
fprintf(stderr,"Estimated gamma/v with standard error: g +- g\n",
      gamma_over_v_hat(c), gamma_over_v_se(c,cov));
fprintf(stderr, "Estimated kappa_S with standard error (using error propagation): %g +/- %g\n",
       kappa_S, kappa_S_se);
fprintf(stderr, "kappa_S confidence intervals based on parametric bootstrap\n");
fprintf(stderr, \verb|"0.95 CI for kappa_S: [\|\|g,\|\|g] \| n \| , kappa_S_195, kappa_S_u95);
fprintf(stderr,"0.99 CI for kappa_S: [%g,%g]\n",kappa_S_199,kappa_S_u99);
if (what==0)
 fprintf(stderr,"* tau vs mean kappa_Fura regression done *\n");
if (what==1)
 fprintf(stderr,"* tau vs min kappa_Fura regression done *\n");
if (what==2)
 fprintf(stderr,"* tau vs max kappa_Fura regression done *\n");
// Print to file
char out[512];
strcpy(out,output);
if (what==0)
```

```
strcat(out,"_tau_vs_mean_kappa");
if (what==1)
 strcat(out,"_tau_vs_min_kappa");
if (what==2)
 strcat(out,"_tau_vs_max_kappa");
FILE *fp = fopen(out,"w");
if (what==0)
 fprintf(fp,"# vs mean linear regression for data set %s\n",filename);
if (what==1)
 fprintf(fp,"# vs min linear regression for data set %s\n",filename);
if (what==2)
 fprintf(fp,"# vs max linear regression for data set %s\n",filename);
fprintf(fp,"# Using stimulation: %d",(int) stim[0]);
for (size_t s_idx=1; s_idx<n_stim; s_idx++)</pre>
 fprintf(fp,", %d", (int) stim[s_idx]);
fprintf(fp, "\n");
fprintf(fp,"# Covariance matrix:\n");
fprintf(fp,"# [ %+.5e, %+.5e \n", cov00, gsl_matrix_get(cov,0,1));
fprintf(fp,"# %+.5e, %+.5e ]\n", gsl_matrix_get(cov,1,0), cov11);
fprintf(fp,"# Total sum of squares (TSS) = %g\n", tss);
fprintf(fp,"# chisq (Residual sum of squares, RSS) = %g\n", chisq);
fprintf(fp,"# Probability of observing a larger of equal RSS per DOF under the null hypothesis: %g\n",p_larger);
fprintf(fp,"# R squared (1-RSS/TSS) = %g\n", 1 - chisq / tss);
fprintf(fp,"# Estimated gamma/v with standard error: %g +/- %g\n",
       gamma_over_v_hat(c), gamma_over_v_se(c,cov));
fprintf(fp,"\#\ Estimates\ kappa\_S\ with\ standard\ error\ (using\ error\ propagation)\colon \ \%g\ +/-\ \%g\n",
       kappa_S, kappa_S_se);
fprintf(fp, \verb|"# kappa_S confidence intervals based on parametric bootstrap|n");\\
fprintf(fp,"# 0.95 CI for kappa_S: [%g,%g]\n",kappa_S_195,kappa_S_u95);
fprintf(fp,"\n\n");
fprintf(fp,"# The data\n"
       "# _Fura
                 _SE\n");
for (size_t s_idx=0; s_idx<n_stim; s_idx++)</pre>
  fprintf(fp,"%g %g %g\n",
         gsl_vector_get(kappa,s_idx),
         gsl_vector_get(tau,s_idx),
         (fit_res[s_idx]).tau_se);
fprintf(fp, "\n");
fprintf(fp,
       "# The fitted data\n"
       "# Preticted values with lower and upper bounds of 0.95 \text{ CI}\n"
       "# _Fura _lwr _upr\n");
double kappa_bd = 0.0;
if (kappa_S > 0.0)
 kappa_bd = 1.25*kappa_S+1;
// double kappa_range = 1.05*gsl_vector_get(kappa,n_stim-1)+kappa_S_u99+1;
double kappa_range = 1.05*gsl_vector_get(kappa,n_stim-1)+kappa_bd;
double delta_kappa = kappa_range/250;
gsl_vector * kappa_v = gsl_vector_alloc(2);
gsl_vector_set(kappa_v,0,1.0);
for (size_t i=0; i<250; i++) {
  double kappaP = -kappa_bd+delta_kappa*i;
 gsl_vector_set(kappa_v,1,kappaP);
 double tauP,tauP_err;
  gsl_multifit_linear_est(kappa_v, c, cov, &tauP, &tauP_err);
```

<<wls_fit>>

```
/// Obrief Performs a robust linear regression and prints results
/// to `stderr` and to a file whose prefix is built from
///
         `output`.
///
/// @returns 0 if everything is fine
int robust_fit(const gsl_vector * kappa, ///< [in] vector of kappa values.</pre>
             mono_exp_fit_res * fit_res, ///< [in] vector of mono_exp_fit_res.</pre>
              size_t n_stim, ///< [in] the number of stimulation.</pre>
              char * filename, ///< Name of file containing the data</pre>
              char * output, ///< Prefix of file name where results are written</pre>
              gsl_rng * rng, ///< Pointer to a gsl_rng
              int what, ///< What is processed? 0 = mean, 1 = min, 2 = max
             size_t *stim ///< [in] Vector of indexes of used stimulation</pre>
 )
 if (what==0)
   fprintf(stderr,"* Doing tau vs mean kappa_Fura robust bi-square regression *\n");
 if (what==1)
   fprintf(stderr,"* Doing tau vs min kappa_Fura robust bi-square regression *\n");
 if (what==2)
   fprintf(stderr,"* Doing tau vs max kappa_Fura robust bi-square regression *\n");
  gsl_vector * c = gsl_vector_alloc(2);
 gsl_vector * c_ols = gsl_vector_alloc(2);
 gsl_matrix * cov = gsl_matrix_alloc(2,2);
gsl_matrix * cov_ols = gsl_matrix_alloc(2,2);
 double tss;
  // Find out tau estimation with largest variance
  double max_var = 0.0;
 for (size_t s_idx=0; s_idx<n_stim; s_idx++) {
   double var = gsl_pow_2((fit_res[s_idx]).tau_se);
   if (var > max_var)
   max_var = var;
```

```
// Get the number of pseudo observations
size_t pseudo_n_stim = 0;
for (size_t s_idx=0; s_idx<n_stim; s_idx++) {</pre>
 double var = gsl_pow_2((fit_res[s_idx]).tau_se);
 pseudo_n_stim += (size_t) round(max_var/var);
// Prepare pseudo data for fit
// Pseudo data are obtained from actual data by
// replicating some observations in order to have
// the right standard error ratio
gsl_vector * tau = gsl_vector_alloc(pseudo_n_stim);
gsl_vector * pkappa = gsl_vector_alloc(pseudo_n_stim);
size_t p_idx = 0;
for (size_t s_idx=0; s_idx<n_stim; s_idx++) {
  double var = gsl_pow_2((fit_res[s_idx]).tau_se);
  size_t ncp = (size_t) round(max_var/var);
  double tau_value = (fit_res[s_idx]).tau;
  double kappa_value = gsl_vector_get(kappa,s_idx);
  for (size_t c_idx=0; c_idx < ncp; c_idx++) {</pre>
    gsl_vector_set(tau,p_idx,tau_value);
    gsl_vector_set(pkappa,p_idx,kappa_value);
   p_idx += 1;
 }
// Get total sum of squares (TSS)
tss = gsl_stats_tss(tau->data,1,tau->size);
// Allocate design matrix
gsl_matrix * X = gsl_matrix_alloc(pseudo_n_stim,2);
// Fill design matrix
for (size_t s_idx=0; s_idx<pseudo_n_stim; s_idx++) {</pre>
  gsl_matrix_set(X,s_idx,0,1.0);
  gsl_matrix_set(X,s_idx,1,gsl_vector_get(pkappa,s_idx));
// Do robust with bi-square weight function
gsl_multifit_robust_workspace * work = gsl_multifit_robust_alloc (gsl_multifit_robust_bisquare,
                                                                   pseudo_n_stim, 2);
gsl_multifit_robust (X, tau, c, cov, work);
gsl_multifit_robust_stats rstats = gsl_multifit_robust_statistics(work);
double chisq = rstats.sse;
double Rsq = rstats.Rsq;
gsl_multifit_robust_free (work);
// Do OLS fit
gsl_multifit_robust_workspace * work_ols = gsl_multifit_robust_alloc (gsl_multifit_robust_ols,
                                                                       pseudo_n_stim, 2);
gsl_multifit_robust (X, tau, c_ols, cov_ols, work_ols);
gsl_multifit_robust_stats rstats_ols = gsl_multifit_robust_statistics(work_ols);
double chisq_ols = rstats_ols.sse;
double Rsq_ols = rstats_ols.Rsq;
gsl_multifit_robust_free (work_ols);
double kappa_S_MC[NREP];
double beta0 = BETAO(c);
double beta1 = BETA1(c);
double cov00 = BETAO_VAR(cov);
double cov11 = BETA1_VAR(cov);
```

```
double beta0_se = BETA0_SE(cov);
double kappa_S = kappa_s(c);
double kappa_S_se = kappa_s_se(c,cov);
double se11=BETA1_SE(cov);
for (size_t rep_idx=0; rep_idx<NREP; rep_idx++) {</pre>
  double num=(beta0+gsl_ran_gaussian_ziggurat(rng,beta0_se));
 double denom=(beta1+gsl_ran_gaussian_ziggurat(rng,se11));
 kappa_S_MC[rep_idx] = num/denom-1.0;
gsl_sort(kappa_S_MC,1,NREP);
double kappa_S_195=kappa_S_MC[(size_t)(0.025*NREP-1)];
double kappa_S_u95=kappa_S_MC[(size_t)(0.975*NREP-1)];
double kappa_S_199=kappa_S_MC[(size_t)(0.005*NREP-1)];
double kappa_S_u99=kappa_S_MC[(size_t)(0.995*NREP-1)];
fprintf(stderr,"Best\ fit:\ tau\ =\ \%g\ +\ \%g\ kappa\_Fura\n",beta0\ ,\ beta1\ );
fprintf(stderr, "Covariance matrix:\n");
fprintf(stderr,"[ %+.5e, %+.5e \n", cov00, gsl_matrix_get(cov,0,1));
fprintf(stderr," %+.5e, %+.5e ]\n", gsl_matrix_get(cov,1,0), cov11);
fprintf(stderr, "Total sum of squares (TSS) = %g\n", tss);
fprintf(stderr,"chisq (Residual sum of squares, RSS) = %g\n", chisq);
fprintf(stderr,"R squared (1-RSS/TSS) = %g\n", Rsq);
fprintf(stderr, "Estimated gamma/v with standard error: %g +/- %g\n",
       gamma_over_v_hat(c), gamma_over_v_se(c,cov));
fprintf(stderr, "Estimated kappa_S with standard error (using error propagation): %g +/- %g\n",
       kappa_S, kappa_S_se);
fprintf(stderr, "kappa\_S \ confidence \ intervals \ based \ on \ parametric \ bootstrap \verb|\|n"|);
fprintf(stderr,"0.95 CI for kappa_S: [%g,%g]\n",kappa_S_195,kappa_S_u95);
fprintf(stderr, "0.99 \ CI \ for \ kappa\_S: \ [\%g,\%g]\n", kappa\_S\_199, kappa\_S\_u99);
if (what==0)
 fprintf(stderr,"* tau vs mean kappa_Fura robust bi-square regression done *\n");
if (what==1)
 fprintf(stderr,"* tau vs min kappa_Fura robust bi-square regression done *\n");
if (what==2)
 fprintf(stderr,"* tau vs max kappa_Fura robust bi-square regression done *\n");
// Print OLS results to stderr
if (what==0)
 fprintf(stderr,"* Doing tau vs mean kappa_Fura ordinary regression *\n");
if (what==1)
 fprintf(stderr,"* Doing tau vs min kappa_Fura ordinary regression *\n");
if (what==2)
  fprintf(stderr,"* Doing tau vs max kappa_Fura ordinary regression *\n");
double beta0_ols = BETA0(c_ols);
double beta1_ols = BETA1(c_ols);
double cov00_ols = BETAO_VAR(cov_ols);
double cov11_ols = BETA1_VAR(cov_ols);
double beta0_ols_se = BETA0_SE(cov_ols);
double kappa_S_ols = kappa_s(c_ols);
double kappa_S_ols_se = kappa_s_se(c_ols,cov_ols);
double se11_ols=sqrt(cov11_ols);
for (size_t rep_idx=0; rep_idx<NREP; rep_idx++) {</pre>
 double num=(beta0_ols+gsl_ran_gaussian_ziggurat(rng,beta0_ols_se));
```

```
double denom=(beta1_ols+gsl_ran_gaussian_ziggurat(rng,se11_ols));
 kappa_S_MC[rep_idx] = num/denom-1.0;
gsl_sort(kappa_S_MC,1,NREP);
double kappa_S_ols_195=kappa_S_MC[(size_t)(0.025*NREP-1)];
double kappa_S_ols_u95=kappa_S_MC[(size_t)(0.975*NREP-1)];
double kappa_S_ols_199=kappa_S_MC[(size_t)(0.005*NREP-1)];
double kappa_S_ols_u99=kappa_S_MC[(size_t)(0.995*NREP-1)];
fprintf(stderr, "Best fit: tau = %g + %g kappa_Fura\n", beta0_ols , beta1_ols );
fprintf(stderr, "Covariance matrix:\n");
fprintf(stderr,"[ %+.5e, %+.5e \n", cov00_ols, gsl_matrix_get(cov_ols,0,1));
fprintf(stderr, "Total sum of squares (TSS) = %g\n", tss);
fprintf(stderr, "chisq (Residual sum of squares, RSS) = %g\n", chisq_ols);
fprintf(stderr,"R squared (1-RSS/TSS) = %g\n", Rsq_ols);
fprintf(stderr,"Estimated gamma/v with standard error: g +- g\n'',
       gamma_over_v_hat(c_ols), gamma_over_v_se(c_ols,cov_ols));
fprintf(stderr, "Estimated kappa_S with standard error (using error propagation): %g +/- %g\n",
       kappa_S_ols, kappa_S_ols_se);
fprintf(stderr,"kappa_S confidence intervals based on parametric bootstrap\n");
fprintf(stderr,"0.99 CI for kappa_S: [%g,%g]\n",kappa_S_ols_199,kappa_S_ols_u99);
if (what==0)
 fprintf(stderr,"* tau vs mean kappa_Fura ordinary regression done *\n");
if (what==1)
 fprintf(stderr,"* tau vs min kappa_Fura ordinary regression done *\n");
if (what==2)
 fprintf(stderr,"* tau vs max kappa_Fura ordinary regression done *\n");
// Print to file
char out[512];
strcpy(out,output);
if (what==0)
  strcat(out,"_tau_vs_mean_kappa_robust");
if (what==1)
 strcat(out,"_tau_vs_min_kappa_robust");
if (what == 2)
 strcat(out,"_tau_vs_max_kappa_robust");
FILE *fp = fopen(out,"w");
if (what==0)
 fprintf(fp,"# vs mean robust regression for data set %s\n",filename);
if (what==1)
 fprintf(fp,"# vs min robust regression for data set %s\n",filename);
if (what==2)
 fprintf(fp,"# vs max robust regression for data set %s\n",filename);
fprintf(fp,"# Using stimulation: %d",(int) stim[0]);
for (size_t s_idx=1; s_idx<n_stim; s_idx++)</pre>
 fprintf(fp,", %d", (int) stim[s_idx]);
fprintf(fp,"\n");
fprintf(fp,"# Results obtained with robust bi-square regression:");
fprintf(fp,"# Best fit: tau = %g + %g kappa_Fura\n",beta0 , beta1 );
fprintf(fp,"# Covariance matrix:\n");
fprintf(fp,"# [ %+.5e, %+.5e \n", cov00, gsl_matrix_get(cov,0,1));
fprintf(fp,"# %+.5e, %+.5e ]\n", gsl_matrix_get(cov,1,0),cov11);
fprintf(fp,"# Total sum of squares (TSS) = %g\n", tss);
```

```
fprintf(fp,"# chisq (Residual sum of squares, RSS) = %g\n", chisq);
fprintf(fp,"# R squared (1-RSS/TSS) = %g\n", Rsq);
fprintf(fp,"# Estimated gamma/v with standard error: %g +/- %g\n",
     gamma_over_v_hat(c), gamma_over_v_se(c,cov));
fprintf(fp,"# Estimates kappa_S with standard error (using error propagation): %g +/- %g\n",
       kappa_S, kappa_S_se);
fprintf(fp,"# kappa_S confidence intervals based on parametric bootstrap\n");
fprintf(fp,"# 0.95 CI for kappa_S: [%g,%g]\n",kappa_S_195,kappa_S_u95);
fprintf(fp, "\# 0.99 \ CI \ for \ kappa\_S: \ [\%g,\%g]\n", kappa\_S\_199, kappa\_S\_u99);
fprintf(fp,"\n\n");
fprintf(fp,"# Results obtained with ordinary regression:\n");
fprintf(fp,"# Best fit: tau = %g + %g kappa_Fura\n",beta0_ols , beta1_ols );
fprintf(fp,"# Covariance matrix:\n");
fprintf(fp,"# Total sum of squares (TSS) = %g\n", tss);
fprintf(fp,"\# chisq (Residual sum of squares, RSS) = %g\n", chisq_ols);
fprintf(fp,"# R squared (1-RSS/TSS) = %g\n", Rsq_ols);
fprintf(fp,"# Estimated gamma/v with standard error: %g +/- %g\n",
       gamma_over_v_hat(c_ols), gamma_over_v_se(c_ols,cov_ols));
fprintf(fp,"# Estimates kappa_S with standard error (using error propagation): %g +/- %g\n",
       kappa_S_ols, kappa_S_ols_se);
fprintf(fp,"# kappa_S confidence intervals based on parametric bootstrap\n");
fprintf(fp,"# 0.99 CI for kappa_S: [%g,%g]\n",kappa_S_ols_199,kappa_S_ols_u99);
fprintf(fp,"\n\n");
fprintf(fp,"# The data\n"
       "# _Fura
                  _SE\n");
for (size_t s_idx=0; s_idx<n_stim; s_idx++)</pre>
  fprintf(fp,"%g %g %g\n",
         gsl_vector_get(kappa,s_idx),
         (fit_res[s_idx]).tau,
         (fit_res[s_idx]).tau_se);
fprintf(fp,"\n\n");
fprintf(fp,
        "# The fitted data\n"
       "# Preticted values with lower and upper bounds of 0.95 CI and the two fitting methods\n"
       "# _Fura _lwr _upr _ols _ols_lwr _ols_upr\n");
double kappa_range = 1.05*gsl_vector_get(pkappa,pseudo_n_stim-1)+kappa_S_u99+1;
double delta_kappa = kappa_range/250;
gsl_vector * kappa_v = gsl_vector_alloc(2);
gsl_vector_set(kappa_v,0,1.0);
for (size_t i=0; i<250; i++) {
  double kappaP = -kappa_S_u99-1+delta_kappa*i;
  gsl_vector_set(kappa_v,1,kappaP);
 double tauP,tauP_err;
  gsl_multifit_robust_est(kappa_v, c, cov, &tauP, &tauP_err);
  double tauP_ols,tauP_ols_err;
  gsl_multifit_robust_est(kappa_v, c_ols, cov_ols, &tauP_ols, &tauP_ols_err);
  fprintf(fp,
         "%g %g %g %g %g %g\n",
         kappaP, tauP,
         tauP-1.96*tauP_err,
         tauP+1.96*tauP_err,
         tauP_ols,
         tauP ols-1.96*tauP ols err.
```

```
tauP_ols+1.96*tauP_ols_err);
}
gsl_vector_free(kappa_v);
fclose(fp);

gsl_vector_free(tau);
gsl_vector_free(pkappa);
gsl_vector_free(c);
gsl_vector_free(c_ols);
gsl_matrix_free(X);
gsl_matrix_free(cov);
gsl_matrix_free(cov_ols);

return 0;
}
```

<<robust_fit>>

```
cd code && make aba_ratio
```

aba_ratio compilation

```
make: aba_ratio est à jour.
```

8.2 Using aba_ratio

8.2.1 Getting help

What to do if we forget how to use the program?

```
./code/aba_ratio --help
```

```
usage: ./code/aba_ratio -i --input=string [-o --output=string] ...
         ... [-s --stim=integer,integer,integer] ..
          ... [-m --maxiter=integer] [-b --baseline_length=integer] ...
          ... [-f --start_fit=real] [-r --robust] [-g --graphic]
 -i --input <character string>: data file name (e.g. data_paper/data_beta_escin/DA_121219_E1.h5)
  -o --output <character string>: output file name prefix (e.g. 'DA_121219_E1_s1_ratio');
       if not specificied, the '.h5' is stripped from 'input' and '_aba' is added
  -s --stim <positive integer>: coma separated list of stimulations to fit
      (default all stimulation considered).
  -m --max_iter <positive integer>: maximal number of iterations performed by
       the nonlinear least-squares solver (default 50).
  -b --baseline_length <positive integer>: baseline length in samples (default 15).
  -f --start_fit <positive real>: where decay fit starts, if > 1 interpreted as the
      number of samples after the peak, if 0<f<1 interpreted as the remaining
      fraction of the jump and fitting starts when the transient reaches that level.
      Default value: 0.5.
```

```
-r --robust: if set, a robust linear regression of tau vs kappa_Fura is performed using a bi-square weight function.-g --graphics: if set, gnuplot script files are generated.
```

The program opens 'input' file, get the loading curve and prints the result to a file named output_loading_curve; then for every stimulation specified in the 'stim' list it computes the ratiometric estimator from the raw data and fits the following model to it: Ca = baseline + delta * exp (-(t-t0)/tau) where t0 is the time on the decay phase at which the fit starts (set by parameter 'f'). A constant is also fitted to the baseline region: Ca = baseline.

Standard errors for the ratiometric estimator are obtained by Monte-Carlo simulation. While the program performs the least-squares optimization relevant information get printed to the stderr. The ratiometric estimator and its standard error are printed to a text file named 'output_CaRatio_sX' (where 'X' stands for the stimulation number. The fitted parameters, fitted values and residuals are printed to a text file named 'output_RatioFit_sX'. If 'g' is selected, a gnuplot script file whose name is the 'output_YY_sX.gp' where 'YY' is either 'loading_curve' or 'RatioFit' 'is generated. A graphical display of the result can then be obtained with: gnuplot -persist 'output_YY_sX.gp'

Once each specified stimulation has been fitted, a regression of tau vs kappa is performed using three different values for kappa: the mean value during the fitted part of the transient, the minimal and the maximal values. Information and fit results get printed to the 'stderr' as well as to files named 'output_aba_tau_vs_mean/min/max_kappa', if option '-g' is set, gnuplot script files are also generated with names 'output_aba_tau_vs_mean/min/max_kappa.gp'

When a robust linear regression is requested (by using optional argument '-r' or '--robust' when calling the program), a bi-square weight function is used (see: https://www.gnu.org/software/gsl/doc/html/lls.html#robust-linear-regression). Since the robust methods implemented in the GSL do not allow for the use of the standard errors on the dependent variable, we multiply the observations in order to have approximately the right standard error ratio: that is, if an observation has a standard error of 0.13 and another one has 0.091, we will include two identical copies of the second since (0.13/0.091)^2 is approximately 2. This use of multiple copies is reported to the user.

8.2.2 Running aba_ratio

We run the program on data set DA/DA_121219_E1.h5 with:

./code/aba_ratio -i data_paper/data_beta_escin/DA_121219_E1.h5 -g

```
iter 10: baseline = 0.0589, delta = 0.1138, tau = 2.3392, RSS = 127.5713
iter 11: baseline = 0.0589, delta = 0.1138, tau = 2.3392, RSS = 127.5713
iter 12: baseline = 0.0589, delta = 0.1138, tau = 2.3392, RSS = 127.5713
Fitted model Ca = baseline+delta*exp(-(t-t0)/tau)
Summary from method 'trust-region/levenberg-marquardt'
number of iterations: 12
function evaluations: 56
Jacobian evaluations: 0
reason for stopping: small step size
initial RSS = 22560.772065
final RSS = 127.571349
Number of observation: 181
Number of degrees of freedom: 178
Baseline length: 15
Fit started from point 34
Estimated baseline 0.058857 and standard error 0.000547938
Estimated delta 0.113819 and standard error 0.00339631
Estimated tau 2.33918 and standard error 0.0947737
RSS per degree of freedom: 0.716693
Probability of observing a larger of equal RSS per DOF under the null hypothesis: 0.998365
* Stimulation 1 done
**********
**********
* Doing now stimulation 2
**********
iter 0: baseline = 0.0505, delta = 0.0755, tau = 15.7000, RSS = 17127.2911
iter 1: baseline = 0.0532, delta = 0.0524, tau = 1.1877, RSS = 3258.8071
iter 2: baseline = 0.0563, delta = 0.0627, tau = 3.2968, RSS = 410.4336
iter 3: baseline = 0.0530, delta = 0.0795, tau = 3.0225, RSS = 169.9101
iter 4: baseline = 0.0530, delta = 0.0798, tau = 3.0718, RSS = 168.2218
iter 5: baseline = 0.0530, delta = 0.0798, tau = 3.0738, RSS = 168.2212
iter 6: baseline = 0.0530, delta = 0.0797, tau = 3.0739, RSS = 168.2212
iter 7: baseline = 0.0530, delta = 0.0797, tau = 3.0739, RSS = 168.2212
iter 8: baseline = 0.0530, delta = 0.0797, tau = 3.0739, RSS = 168.2212
iter 9: baseline = 0.0530, delta = 0.0797, tau = 3.0739, RSS = 168.2212
Fitted model Ca = baseline+delta*exp(-(t-t0)/tau)
Summary from method 'trust-region/levenberg-marquardt'
number of iterations: 9
function evaluations: 43
Jacobian evaluations: 0
reason for stopping: small step size
initial RSS = 17127.291078
final RSS = 168.221246
Number of observation: 173
Number of degrees of freedom: 170
Baseline length: 15
Fit started from point 42
Estimated baseline 0.0530034 and standard error 0.000379632
Estimated delta 0.0797495 and standard error 0.00143484
Estimated tau 3.07388 and standard error 0.0906272
RSS per degree of freedom: 0.989537
Probability of observing a larger of equal RSS per DOF under the null hypothesis: 0.524164
```

```
* Stimulation 2 done
***********
**********
* Doing now stimulation 3
**********
iter 0: baseline = 0.0507, delta = 0.0530, tau = 14.7000, RSS = 10847.6780
iter 1: baseline = 0.0494, delta = 0.0466, tau = 1.1167, RSS = 5844.7928
iter 2: baseline = 0.0560, delta = 0.0376, tau = 3.1071, RSS = 1007.7739
iter 3: baseline = 0.0508, delta = 0.0548, tau = 4.6014, RSS = 210.8745
iter 4: baseline = 0.0499, delta = 0.0560, tau = 4.3709, RSS = 157.6289
iter 5: baseline = 0.0500, delta = 0.0561, tau = 4.3581, RSS = 157.5996
iter 6: baseline = 0.0500, delta = 0.0561, tau = 4.3569, RSS = 157.5996
iter 7: baseline = 0.0500, delta = 0.0561, tau = 4.3568, RSS = 157.5996
iter 8: baseline = 0.0500, delta = 0.0561, tau = 4.3568, RSS = 157.5996
iter 9: baseline = 0.0500, delta = 0.0561, tau = 4.3568, RSS = 157.5996
iter 10: baseline = 0.0500, delta = 0.0561, tau = 4.3568, RSS = 157.5996
iter 11: baseline = 0.0500, delta = 0.0561, tau = 4.3568, RSS = 157.5996
Fitted model Ca = baseline+delta*exp(-(t-t0)/tau)
Summary from method 'trust-region/levenberg-marquardt'
number of iterations: 11
function evaluations: 50
Jacobian evaluations: 0
reason for stopping: small step size
initial RSS = 10847.678001
final RSS = 157.599555
Number of observation: 163
Number of degrees of freedom: 160
Baseline length: 15
Fit started from point 52
Estimated baseline 0.0499656 and standard error 0.000388917
Estimated delta 0.0561071 and standard error 0.000826757
Estimated tau 4.35681 and standard error 0.130141
RSS per degree of freedom: 0.984997
Probability of observing a larger of equal RSS per DOF under the null hypothesis: 0.538851
**********
* Stimulation 3 done
***********
***********
* Doing tau vs mean kappa_Fura regression *
************
Best fit: tau = 1.43541 + 0.00951986 kappa_Fura
Covariance matrix:
[ +2.05752e-02, -1.00932e-04
  -1.00932e-04, +5.93942e-07
Total sum of squares (TSS) = 157.149
chisq (Residual sum of squares, RSS) = 4.56232
Probability of observing a larger of equal RSS per DOF under the null hypothesis: 0.0326828
R \text{ squared } (1-RSS/TSS) = 0.970968
Estimated gamma/v with standard error: 105.044 +/- 8.50376
Estimated kappa_S with standard error (using error propagation): 149.78 +/- 19.3914
kappa_S confidence intervals based on parametric bootstrap
0.95 CI for kappa_S: [104.373,211.581]
0.99 CI for kappa_S: [93.8481,239.592]
************
* tau vs mean kappa_Fura regression done *
```

```
************
*************
* Doing tau vs min kappa_Fura regression *
************
Best fit: tau = 1.49012 + 0.00965061 kappa_Fura
Covariance matrix:
[ +1.94068e-02, -9.86866e-05
 -9.86866e-05, +6.09311e-07
Total sum of squares (TSS) = 157.149
chisq (Residual sum of squares, RSS) = 4.2975
Probability of observing a larger of equal RSS per DOF under the null hypothesis: 0.0381685
R squared (1-RSS/TSS) = 0.972653
Estimated gamma/v with standard error: 103.62 +/- 8.38128
Estimated kappa_S with standard error (using error propagation): 153.407 +/- 19.088
{\tt kappa\_S} \ {\tt confidence} \ {\tt intervals} \ {\tt based} \ {\tt on} \ {\tt parametric} \ {\tt bootstrap}
0.95 CI for kappa_S: [108.414,214.659]
0.99 CI for kappa_S: [95.0422,238.853]
*************
* tau vs min kappa_Fura regression done *
************
************
* Doing tau vs max kappa_Fura regression *
************
Best fit: tau = 1.39244 + 0.0094002 kappa_Fura
Covariance matrix:
[ +2.15679e-02, -1.02704e-04
 -1.02704e-04, +5.81330e-07 ]
Total sum of squares (TSS) = 157.149
chisq (Residual sum of squares, RSS) = 5.14649
Probability of observing a larger of equal RSS per DOF under the null hypothesis: 0.0232934
R squared (1-RSS/TSS) = 0.967251
Estimated gamma/v with standard error: 106.381 +/- 8.62854
Estimated kappa_S with standard error (using error propagation): 147.128 +/- 19.7087
kappa_S confidence intervals based on parametric bootstrap
0.95 CI for kappa_S: [100.924,208.224]
0.99 CI for kappa_S: [88.7097,232.675]
************
* tau vs max kappa_Fura regression done *
*************
```

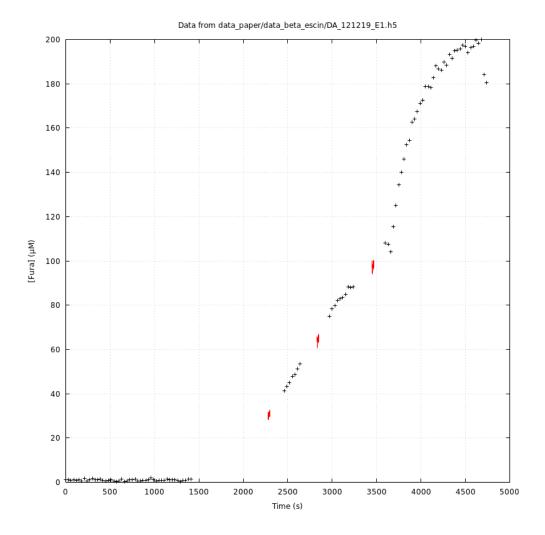
We can test it with valgrind as follows (result not shown but its fine):

```
valgrind ./code/aba_ratio -i data_paper/data_beta_escin/DA_121219_E1.h5
```

8.2.3 Looking at the results

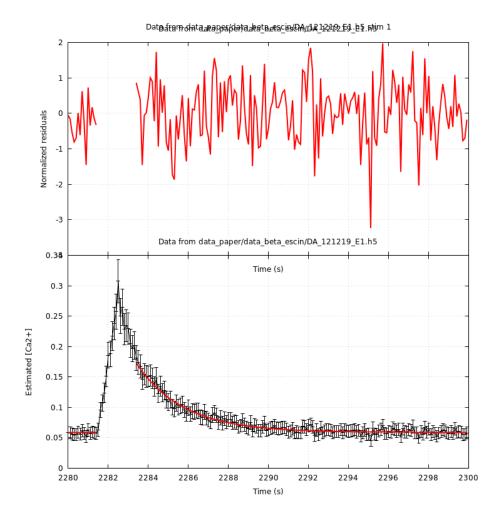
loading curve The quickest way to get the loading curve is to type:

```
gnuplot -persist data_paper/data_beta_escin/DA_121219_E1_aba_loading_curve.gp
```



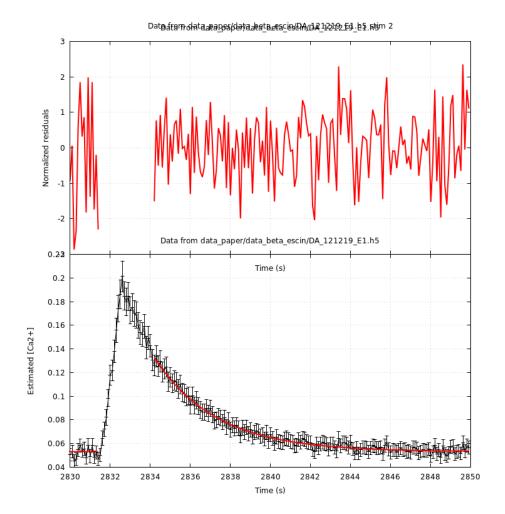
First stimulation fit The quickest way to get the diagnostic figure is:

gnuplot -persist data_paper/data_beta_escin/DA_121219_E1_aba_RatioFit_s1.gp



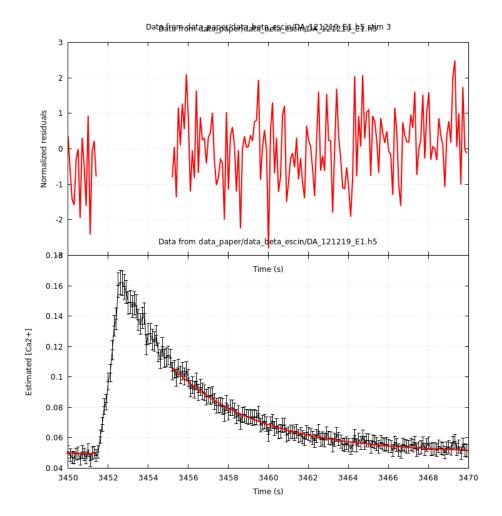
Second stimulation fit The quickest way to get the diagnostic figure is:

gnuplot -persist data_paper/data_beta_escin/DA_121219_E1_aba_RatioFit_s2.gp



Third stimulation fit The quickest way to get the diagnostic figure is:

gnuplot -persist data_paper/data_beta_escin/DA_121219_E1_aba_RatioFit_s3.gp



 τ **vs** κ_{Fura} **regression** We get a written summary of the linear regression performed with the mean κ_F value with:

head -n 15 data_paper/data_beta_escin/DA_121219_E1_aba_tau_vs_mean_kappa

```
# kappa_S confidence intervals based on parametric bootstrap
# 0.95 CI for kappa_S: [104.373,211.581]
# 0.99 CI for kappa_S: [93.8481,239.592]
```

We get the figure with:

gnuplot -persist data_paper/data_beta_escin/DA_121219_E1_aba_tau_vs_mean_kappa.gp

