Solving the Schrödinger Equation Using the 2D Crank-Nicolson Method

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REFRENCES

Github link: $https://github.com/christopheblomsen/fys4150_pro5$

I. INTRODUCTION

II. THEORY

III. METHODS

The bare Schrödinger equation can be written as

$$i\frac{\partial u}{\partial t} = -\frac{\partial^2 u}{\partial x^2} - \frac{\partial^2 u}{\partial y^2} + v(x, y)u. \tag{1}$$

We will solve this equation by discretizing it according to the Crank-Nicolson approach. The Crank-Nicolson

5cmodinger equation can be written as

approach is given by

$$\frac{u^{n+1} - u^n}{\Delta t} = \frac{1}{2} \left(F_i^{n+1} + F_i^n \right), \tag{2}$$

where u^n is the dimentionless wavefunction, in two dimentions, at time step n. u^{n+1} is then the wavefunction at time step n+1.

IV. RESULTS

V. CONCLUSION