CSE 250B: Section 4 - Sharad Vikram

1. Nearest Neighbor Practice

You're given the following (X, y) pairs: (1.5, 1), (2.5, 1), (1, 0), (2, 0), (3, 0)

- (a) What is the 1-nearest neighbor decision rule?
- (b) **True/False**: The 1-nearest neighbor algorithm is consistent.
- (b) Name two methods that can speed up nearest neighbor queries.
- 2. Statistical Learning Theory

Let
$$\eta(x) = \begin{cases} 0.4 & \text{if } x < 0 \\ 0.9 & \text{if } x \ge 0 \end{cases}$$
, and $\mu(x) = \begin{cases} 0 & \text{if } x < -1 \\ 0.2 & \text{if } -1 \le x < 0 \\ 0.8 & \text{if } 0 \le x \le 1 \\ 0 & \text{if } x > 1 \end{cases}$.

- (a) What is the decision rule h(x)?
- (b) What is the Bayes risk?
- (c) We define a cost sensitive risk function: $R(h) = 5 \times Pr(Y = 0, h(X) = 1) + P(Y = 1, h(X) = 0)$. What is our decision rule with this cost function?
- 3. Distance Function

Under what conditions of S is the following function a valid distance metric?

$$d(x,y) = (x-y)^T S(x-y)$$

4. Covariance

Let X and Y be random variables.

- (a) Show that if X is of independent Y, Cov(X, Y) = 0.
- (b) Show that if Cov(X, Y) = 0, X is not necessarily independent of Y.
- 5. Find the spectral decomposition of the following matrices.
 - (a) $\begin{bmatrix} 1 & 2 \\ 2 & 4 \end{bmatrix}$
 - (b) $\begin{bmatrix} 3 & 2 \\ 2 & 3 \end{bmatrix}$