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In the following sections we will measure the fit characteristics of reweighting EFT to SM data. To do so we need to select some observables to perform fits with. In addition to a handful of phase-space observables, we will also examine optimal observables. We also need to select for each observable, the range and bin sizes, in as objective a way as possible, as these will affect the fit results to some degree.

We will continue to use the SM and EFT data samples used previously. Both samples contain 1M events, which we will scale to a luminosity of 10 fb–1.

## Data range

Most of our observables have long tails approaching a sparse distribution of single events separated by areas with no events. Once binned, these sparse areas will result in bins with low statistics and empty bins. When fitting, all bins are treated equally and if we have a relatively high number of low statistic bins, these can dominate the fit results. With some fit objectives, such as minimizing χ2, empty data bins are skipped, reducing the degrees of freedom for the fit.

One can solve such problems, by using different bin sizes across the data range to ensure that no bins have low statistics. This is discussed in the next section. For simplicity though, we have chosen to use equal-width bins for our histograms, thus sparse data tails remain an issue, and the data range must be carefully chosen.

To set the data range in a somewhat objective manner, we have chosen ranges that exclude less than 10 events on either end, after scaling to the test luminosity of 10 fb–1. Thus the underflow and overflow bins will have less than 10 events. Why use 10 events as the criteria? Simply because, a bin with 10 events and thus an error of has more than a 3 sigma probability of not having a true value of zero. Bins with less than 10 events have a small but significant probability of being zero.

In addition, we have set the range based solely upon the SM data sample, that is the data sample that we are fitting to and not the EFT data sample that we are reweighting. A common range and bin size must be used to perform binned fits. Normally one bins one’s data (the SM sample) according to its characteristics, and then bins the model (the reweighted EFT sample) equivalently.

## Binning for binned fits

All choices in binning affect fit results to some degree, and unfortunately it is not easy to gauge these effects. We desire that fit results remain fairly stable as a function of binning near our binning choice.

We have several choices when binning our data. The **first choice** is whether a single bin-width should be used across the entire range, equivalent to dividing the data range equally into a specified number of bins, or whether different bin-widths should be used through the data range.

The choice of a single bin-width is obviously the simplest. However, as mentioned in the previous section, our observables often have areas of sparse events at one or both ends of their data range. These areas will contain bins that are empty or with low statistics. One cannot reweight an empty bin, and bins with low statistics have larger relative errors. When fitting, all bins are treated equally and if we have a relatively high number of low statistic bins, these can dominate the fit results. Also with some fit objectives, such as minimizing χ2, empty data bins are skipped, reducing the degrees of freedom for the fit.

One can solve such problems, by using different bin sizes across the data range to ensure that no bins have low statistics. Thus there will be more bins in areas of high density and fewer in areas of low density. One can divide each bin’s height by its bin width, to create a density distribution, but this is not necessary for fitting, and will cannot be used with a likelihood fit objective that compares event counts. However, gauging the binning effects of a specific choice of variable bin-widths on a fit result is not an easy task.

For this project, we have chosen for simplicity to use equal-width bins for our histograms, despite the potential benefits of variable bin-widths. This means that we must be aware of the sparse regions in our data, and take care to handle empty and low-statistic bins appropriately. This is discussed further in the sections describing the fits performed.

One potential compromise between variable and fixed bin-widths, is to use fixed bin-widths, and then to fill in empty bins with events from adjacent non-empty bins, spreading the events evenly across the empty areas. This has the same affect of creating wider pseudo-bins locally where the density is lower, without actually changing the binning scheme. This obviously can only be done on model histograms and not data histograms, as data should never be modified. This technique is used where appropriate, and discussed further in sections describing the fits performed.

One can also obviously avoid low-statistic and empty bins by using more events.

The **second choice**, in the case of using fixed bin-widths, is the number of bins to use across the data range. There are widely different suggestions on how to determine the optimal number of bins for a given data set. For

Table of selected observables. Description of range definition.

# Fitting EFT to SM for parton-level WZ-production

Confident that we have the reweighting tools to construct the observable plots for any defined set of EFT model parameters, we will now measure the fit characteristics of reweighting EFT to SM data at the parton-level. Specifically, we measure how well reweighted EFT data fits the SM data for each selected observable, using a fit algorithm to determine the EFT model parameters that fit best. This is done using the same parton-level WZ-production pseudo-data generated by Sherpa used previously.

The SM and EFT data samples both have 1M events. Their total cross-sections are 18.554 ± 0.016 pb for SM and 42.805 ± 0.038 pb for EFT. The data samples are scaled to a luminosity of 10 fb–1, and Asimov bin errors are used as discussed in 4.2.1.

Log-likelihood minimization is used to fit to event counted observables, and -minimization is used to fit to mean-observables. The results are shown in Table XXX.

Observables

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| **Observable** | **Type** | **Bin Range** | **Bins** | **Fit Bins a** | **Underflow**  **Count b** | **Overflow**  **Count b** |
| **PT(Z)** | count | 0 to 750 GeV/c | 150 | 150 | 0 | 8.2 |
| **M(WZ) =** | count | 0 to 3000 GeV/c2 | 150 | 142 | 0 | 6.3 |
| **y(Z)** | count | −5 to +5 | 100 | 98 | 0 | 0 |
| **O1(cWWW)** | count | −60000 to 7000 | 1000 | 1000 | 6.7 | 3.4 |
| **O2(cWWW)** | count | 0 to 2×1012 | 1000 | 1000 | 0 | 5.9 |
| **O1(cW)** | count | (−200 to 2)×104 | 1000 | 997 | 2.7 | 0 |
| **O2(cW)** | count | 0 to 6×1011 | 1000 | 1000 | 0 | 7.6 |
| **O1(cB)** | count | −800 to 5000 | 1000 | 996 | 1.5 | 8.2 |
| **O2(cB)** | count | 0 to 2×108 | 1000 | 1000 | 0 | 3.7 |
| **O1(cWWW) vs** | mean | 0 to 3000 GeV | 100 | 76 | 0 | 6.3 |
| **O2(cWWW) vs** | mean | 0 to 3000 GeV | 100 | 76 | 0 | 6.3 |
| **O1(cW) vs** | mean | 0 to 3000 GeV | 100 | 76 | 0 | 6.3 |
| **O2(cW) vs** | mean | 0 to 3000 GeV | 100 | 76 | 0 | 6.3 |
| **O1(cB) vs** | mean | 0 to 3000 GeV | 100 | 76 | 0 | 6.3 |
| **O2(cB) vs** | mean | 0 to 3000 GeV | 100 | 76 | 0 | 6.3 |

1. Fit skips bins with a zero error value. For mean observables, fit also skips bins with less than 10 effective events in either the SM or EFT sample prior to any luminosity scaling.
2. SM sample at 10 fb−1.

Fit Results

| Observable | EFT Parameter | Fit Single | | | Fit All | | |
| --- | --- | --- | --- | --- | --- | --- | --- |
| Value  [10−6] | Error  [10−6] |  | Value  [10−6] | Error  [10−6] |  |
| PT(Z) | cWWW | −0.25 | 0.33 | 0.27 | 0.053 | 0.58 | 0.27 |
| cW | −0.11 | 0.13 | 0.27 | −0.16 | 0.20 |
| cB | 2.4 | 5.3 | 0.26 | −2.3 | 10 |
| M(WZ) | cWWW | −1.2 | 0.19 | 0.52 | 0.23 | 2.4 | 0.50 |
| cW | −1.1 | 0.25 | 0.48 | −1.42 | 0.71 |
| cB | 23.0 | 12.0 | 0.49 | −27 | 41 |
| y(Z) | cWWW | −0.98 | 0.73 | 0.61 | 0.60 | 3.2 | 0.62 |
| cW | −0.41 | 0.37 | 0.61 | −1.6 | 3.2 |
| cB | 12 | 11 | 0.61 | −39 | 140 |
| O1(cWWW) | cWWW | −0.29 | 0.28 | 0.36 | 0.37 | 0.89 | 0.36 |
| cW | −0.10 | 0.11 | 0.36 | 0.020 | 0.39 |
| cB | 3.8 | 3.8 | 0.36 | 7.3 | 17 |
| O2(cWWW) | cWWW | −0.30 | 0.25 | 0.058 | 0.42 | 0.48 | 0.057 |
| cW | −0.10 | 0.12 | 0.059 | 0.18 | 0.50 |
| cB | 7.0 | 6.4 | 0.058 | 17 | 22 |
| O1(cW) | cWWW | −0.21 | 0.23 | 0.099 | 0.16 | 0.69 | 0.099 |
| cW | −0.069 | 0.095 | 0.099 | 0.0081 | 0.24 |
| cB | 3.4 | 3.9 | 0.099 | 5.0 | 13 |
| O2(cW) | cWWW | −0.35 | 0.23 | 0.076 | 0.51 | 0.44 | 0.074 |
| cW | −0.12 | 0.11 | 0.077 | 0.23 | 0.50 |
| cB | 7.3 | 5.5 | 0.075 | 19 | 20 |
| O1(cB) | cWWW | −0.28 | 0.28 | 0.40 | 0.32 | 0.98 | 0.40 |
| cW | −0.095 | 0.11 | 0.40 | −0.0091 | 0.36 |
| cB | 3.4 | 3.8 | 0.40 | 5.7 | 17 |
| O2(cB) | cWWW | −0.24 | 0.24 | 0.086 | 0.17 | 0.67 | 0.087 |
| cW | −0.086 | 0.10 | 0.087 | −0.012 | 0.25 |
| cB | 4.1 | 4.4 | 0.086 | 5.1 | 13 |
| O1(cWWW) vs | cWWW | 0.0028 | 0.077 | 0.19 | −0.00027 | 0.11 | 0.065 |
| cW | 0.44 | 0.17 | 0.063 | 0.44 | 0.17 |
| cB | −6.2 | 12 | 0.19 | −0.97 | 17 |
| O2(cWWW) vs | cWWW | 0.0029 | 0.018 | 3.3 | −0.00024 | 0.026 | 0.87 |
| cW | 0.46 | 0.041 | 0.85 | 0.46 | 0.041 |
| cB | −6.3 | 2.9 | 3.2 | −0.94 | 4 |
| O1(cW) vs | cWWW | 0.0028 | 0.021 | 2.5 | −0.00024 | 0.029 | 0.69 |
| cW | 0.46 | 0.046 | 0.67 | 0.45 | 0.047 |
| cB | −6.3 | 3.3 | 2.5 | −0.94 | 4.5 |
| O2(cW) vs | cWWW | 0.0028 | 0.020 | 2.7 | −0.00024 | 0.028 | 0.74 |
| cW | 0.46 | 0.045 | 0.72 | 0.46 | 0.045 |
| cB | −6.3 | 3.1 | 2.7 | −0.94 | 4.3 |
| O1(cB) vs | cWWW | 0.0029 | 0.13 | 0.080 | −0.00032 | 0.17 | 0.035 |
| cW | 0.43 | 0.27 | 0.034 | 0.43 | 0.28 |
| cB | −6.2 | 20 | 0.035 | −0.91 | 27 |
| O2(cB) vs | cWWW | 0.0028 | 0.12 | 0.091 | −0.00030 | 0.16 | 0.037 |
| cW | 0.43 | 0.25 | 0.036 | 0.43 | 0.25 |
| cB | −6.2 | 18 | 0.090 | −0.92 | 25 |

cWWW

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| **Observable** | **Fit cWWW** | | | **Fit All** | | |
| **Value**  **[10−6]** | **Error**  **[10−6]** |  | **Value**  **[10−6]** | **Error**  **[10−6]** |  |
| **PT(Z)** | −0.25 | 0.33 | 0.27 | 0.053 | 0.58 | 0.27 |
| **M(WZ)** | −1.18 | 0.18 | 0.50 | 0.10 | 2.1 | 0.47 |
| **y(Z)** | −0.98 | 0.73 | 0.61 | 0.60 | 3.2 | 0.62 |
| **O1(cWWW)** | −0.29 | 0.28 | 0.36 | 0.37 | 0.89 | 0.36 |
| **O2(cWWW)** | −0.30 | 0.25 | 0.058 | 0.42 | 0.48 | 0.057 |
| **O1(cW)** | −0.21 | 0.23 | 0.099 | 0.16 | 0.69 | 0.099 |
| **O2(cW)** | −0.35 | 0.23 | 0.076 | 0.51 | 0.44 | 0.074 |
| **O1(cB)** | −0.28 | 0.28 | 0.40 | 0.32 | 0.98 | 0.40 |
| **O2(cB)** | −0.24 | 0.24 | 0.086 | 0.17 | 0.67 | 0.087 |
| **O1(cWWW) vs** | 0.0028 | 0.077 | 0.19 | −0.00027 | 0.11 | 0.065 |
| **O2(cWWW) vs** | 0.0029 | 0.018 | 3.3 | −0.00024 | 0.026 | 0.87 |
| **O1(cW) vs** | 0.0028 | 0.021 | 2.5 | −0.00024 | 0.029 | 0.69 |
| **O2(cW) vs** | 0.0028 | 0.020 | 2.7 | −0.00024 | 0.028 | 0.74 |
| **O1(cB) vs** | 0.0029 | 0.13 | 0.080 | −0.00032 | 0.17 | 0.035 |
| **O2(cB) vs** | 0.0028 | 0.12 | 0.091 | −0.00030 | 0.16 | 0.037 |

cW

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| **Observable** | **Fit cW** | | | **Fit All** | | |
| **Value**  **[10−6]** | **Error**  **[10−6]** |  | **Value**  **[10−6]** | **Error**  **[10−6]** |  |
| **PT(Z)** | −0.11 | 0.13 | 0.27 | −0.16 | 0.20 | 0.27 |
| **M(WZ)** | −1.1 | 0.24 | 0.46 | −1.42 | 0.37 | 0.47 |
| **y(Z)** | −0.41 | 0.37 | 0.61 | −1.6 | 3.2 | 0.62 |
| **O1(cWWW)** | −0.10 | 0.11 | 0.36 | 0.020 | 0.39 | 0.36 |
| **O2(cWWW)** | −0.10 | 0.12 | 0.059 | 0.18 | 0.50 | 0.057 |
| **O1(cW)** | −0.069 | 0.095 | 0.099 | 0.0081 | 0.24 | 0.099 |
| **O2(cW)** | −0.12 | 0.11 | 0.077 | 0.23 | 0.50 | 0.074 |
| **O1(cB)** | −0.095 | 0.11 | 0.40 | −0.0091 | 0.36 | 0.40 |
| **O2(cB)** | −0.086 | 0.10 | 0.087 | −0.012 | 0.25 | 0.087 |
| **O1(cWWW) vs** | 0.44 | 0.17 | 0.063 | 0.44 | 0.17 | 0.065 |
| **O2(cWWW) vs** | 0.457 | 0.041 | 0.85 | 0.456 | 0.041 | 0.87 |
| **O1(cW) vs** | 0.456 | 0.046 | 0.67 | 0.455 | 0.047 | 0.69 |
| **O2(cW) vs** | 0.456 | 0.045 | 0.72 | 0.455 | 0.045 | 0.74 |
| **O1(cB) vs** | 0.43 | 0.27 | 0.034 | 0.43 | 0.28 | 0.035 |
| **O2(cB) vs** | 0.43 | 0.25 | 0.036 | 0.43 | 0.25 | 0.037 |

cB

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| **Observable** | **Fit cB** | | | **Fit All** | | |
| **Value**  **[10−6]** | **Error**  **[10−6]** |  | **Value**  **[10−6]** | **Error**  **[10−6]** |  |
| **PT(Z)** | 2.4 | 5.3 | 0.26 | −2.3 | 10 | 0.27 |
| **M(WZ)** | 23 | 12 | 0.47 | −27 | 29 | 0.47 |
| **y(Z)** | 12 | 11 | 0.61 | −39 | 140 | 0.62 |
| **O1(cWWW)** | 3.8 | 3.8 | 0.36 | 7.3 | 17 | 0.36 |
| **O2(cWWW)** | 7.0 | 6.4 | 0.058 | 17 | 22 | 0.057 |
| **O1(cW)** | 3.4 | 3.9 | 0.099 | 5.0 | 13 | 0.099 |
| **O2(cW)** | 7.3 | 5.5 | 0.075 | 19 | 20 | 0.074 |
| **O1(cB)** | 3.4 | 3.8 | 0.40 | 5.7 | 17 | 0.40 |
| **O2(cB)** | 4.1 | 4.4 | 0.086 | 5.1 | 13 | 0.087 |
| **O1(cWWW) vs** | −6.2 | 12 | 0.19 | −0.97 | 17 | 0.065 |
| **O2(cWWW) vs** | −6.3 | 2.9 | 3.2 | −0.94 | 4 | 0.87 |
| **O1(cW) vs** | −6.3 | 3.3 | 2.5 | −0.94 | 4.5 | 0.69 |
| **O2(cW) vs** | −6.3 | 3.1 | 2.7 | −0.94 | 4.3 | 0.74 |
| **O1(cB) vs** | −6.2 | 20 | 0.079 | −0.91 | 27 | 0.035 |
| **O2(cB) vs** | −6.2 | 18 | 0.090 | −0.92 | 25 | 0.037 |

# Fitting EFT to SM for simulated measurement of WZ-production

# Conclusion

# Bibliography