

Midterm #6

a) 51.1875₁₀

$$51/2 = 25 \text{ R } 1$$

$$25/2 = 12 \text{ R } 1$$

$$12/2 = 6 \text{ R } 0$$

$$6/2 = 3 \text{ R } 0$$

$$3/2 = 1 \text{ R } 1$$

$$1/2 = 0 \text{ R } 1$$

$$0.1875 \times 2 = 0.375$$

$$0.375 \times 2 = 0.75$$

$$0.75 \times 2 = 1.5$$

$$.5 \times 2 = 1.0$$

$$51.1875_{10} = 110011.0011_2$$

$$= 0.1100110011 \times 2^6$$

$$11001100 | 0000000 | 00000000 | 00000010$$

$$C \quad C \quad C \quad 0 \quad 0 \quad 0 \quad 0 \quad 6$$

$$CCC00006$$

$$110011.0011_2 = 33.3_{10}$$

$$= 63.14_8$$

② 3.19921875₁₀

$$3/2 = 1 \text{ R } 1$$

$$1/2 = 0 \text{ R } 1$$

$$0.19921875 \times 2 = 0.3984375$$

$$0.3984375 \times 2 = 0.796875$$

$$0.796875 \times 2 = 1.59375$$

$$0.59375 \times 2 = 1.1875$$

$$0.1875 \times 2 = 0.375$$

$$0.375 \times 2 = 0.75$$

$$0.75 \times 2 = 1.5$$

$$.5 \times 2 = 1.0$$

$$3.19921875_{10} = 11.00110011_2$$

$$= 3.196_8$$

$$= 3.33_{16}$$

② 0011 0011 | 00111111 | 11111111 | 00000000

3 3 3 F F F 0 0 2

3 3 0 4 0 0 0 0 2

33400002₁₆

11500000

③ 0011 0011 | 00110011 | 00110011 | 11111110

3 3 3 3 3 3 F E

3 3 3 3 3 4 F E

33334FE₁₆

c) 069999902

01101001 | 10011001 | 10011001 | 00000010

0.01101001×2^2
 $= 1.101001_2$

$1.101001_2 = (1 \times 2^0) + (1 \times 2^{-1}) + (1 \times 2^{-3}) + (1 \times 2^{-6})$

$= 1 + 0.5 + 0.125 + 0.015625$
 $= 1.640625_{10}$

$$\textcircled{2} 69999903_{16}$$

$$= 0.01101001 \times 2^3$$

$$= 11.01001_2$$

$$\begin{aligned} 11.01001_2 &= (1 \times 2^1) + (1 \times 2^0) + (1 \times 2^{-2}) + (1 \times 2^{-5}) \\ &= 2 + 1 + 0.25 + 0.03125 \\ &= 3.28125_{10} \end{aligned}$$

$$\textcircled{3} 966667FF_{16}$$

$$10010110 | 01100110 | 01100111 | 11111111$$

$$= 0.100101100110011001100111 \times 2^1$$

$$= 1.0010110011001100110011$$

$$\begin{aligned} &= (1 \times 2^0) + (1 \times 2^{-3}) + (1 \times 2^{-5}) + (1 \times 2^{-6}) + (1 \times 2^{-9}) + (1 \times 2^{-10}) \\ &\quad + (1 \times 2^{-13}) + (1 \times 2^{-14}) + (1 \times 2^{-17}) + (1 \times 2^{-18}) + (1 \times 2^{-21}) \\ &\quad + (1 \times 2^{-22}) + (1 \times 2^{-23}) \end{aligned}$$

$$= 0.125 + 0.03125 + 0.015625 + 0.0078125 + 0.0009765625 + \dots$$

$$= 1.1750007152557373047_{10}$$