# A Table of Commutation Relations

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# 1 A table of commutation relations for operators of a single particle.

#### 1.1 Operators to use.

- Observables (Hermitian):  $x, p_x, H = \frac{p_x^2}{2m}, N = a^{\dagger}a, J_x, J_y, J_z, J, \Pi$
- Non-observables:  $a, a^{\dagger}, T$ ,

#### 1.2 The table.

## 1.3 Operator definitions.

- $p_x = \frac{\hbar}{i} \frac{\partial}{\partial x}$  in the x-basis. Townsend p.158.
- $\Pi |x\rangle = |-x\rangle$  Townsend p.213.
- $H = \frac{p^2}{2m} + V(x)$  Sakurai p.97, (2.4.2).

#### 1.4 References.

- 0 Any operator commutes with itself.
- $-i\hbar$  See Townsend eq. 6.31, p. 155 or Griffiths eq. 2.51, p.55. This leads to the uncertainty principle  $\Delta x \Delta p_x \geq \frac{\hbar}{2}$ .
- $-a\,$  See Sakurai p.90, (2.3.10).
- $-a^{\dagger}$  See Sakurai p.90, (2.3.11).
  - 0 H and  $p_x$  commute since  $H = \frac{p_x^2}{2m}$ .
- 2 A table of commutation relations for operators of two particles.