

Topological Data Analysis of Treasury Yield Curve Rates

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Abstract

We explore the use of Topological Data Analysis (TDA) to study the evolution of US Treasury Yield Curve Rates from 2015 - 2020. We particularly focus on the use of TDA to understand the shape and structure of our multidimensional rates series and whether useful economic inference can be derived from topological tools.

1 Introduction

Topological Data Analysis (TDA) is an emerging multidisciplinary field that uses tools from topology, statistics, and scientific computing to extract insights about complex data. Many existing papers introduce the technique to an unfamiliar reader [7, 9, 14, 19]. From a practical perspective, TDA can be used primarily to explore the structure of multidimensional data with regard to shape and connectivity.

TDA has shown significant promise in a variety of fields, including cosmology [10, 17, 18, 16], image analysis [6, 13, 8, 15, 1], finance [12, 11], and neuroscience [2, 3, 4, 5], among many others. This paper does not attempt to present a comprehensive overview of all existing applications of TDA in the scientific literature. However, across all examined papers, the primary theme involves the extraction of insights about the shape and structure of complex multidimensional datasets.

With this paper, I aim to demonstrate the utility of TDA for exploring economic and financial questions, with a specific focus on treasury yield curve rates. A similar exploration takes place in [12] with attention to the equity markets, and we follow their example in our study of rates. Their findings are particularly interesting as they present one of few existing analyses utilizing TDA to explore economic and financial research. Gidea and Katz find a strong rising trend for trading days prior to financial downturns, which implies that TDA may be useful as a new econometric analysis to complement traditional methods.

This analysis is meaningful for two main reasons. First, it is (to our knowledge) the first implementation of TDA to examine the shape and structure of treasury yield curve rates. Second, it provides an introduction of TDA to the economics community, who may not have been previously exposed. Based on our survey of the literature, applications of TDA are common in finance, but not much was found in the economics space. Given its utilization across a wide number of fields and the increasing complexity of economic data, TDA has the potential to add significant value to researchers in economics and finance.

To complete our analysis, we utilize daily treasury yield curve rates data from 2015 - 2020 across multiple maturity periods. *description of method here.* *description of results here.* *description of why this matters here.*

The remainder of this paper is structured as follows: section 2 describes the mathematical and theoretical details of TDA, including a detailed view of some existing applications; section 3 provides a summary of the existing literature on yield curve rates and the methodologies that have been used to date. Sections 4 and 5 explore our methodology and dataset, respectively, providing a detailed outline of the analysis we undertake and the nuances of the underlying dataset. Finally, sections 6 and 7 present our results, conclusions, and thoughts on future research.

- 2 Topological Data Analysis**
- 3 Treasury Yield Curve Rates**
- 4 Methodology**
- 5 Data**
- 6 Results**
- 7 Conclusion**

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