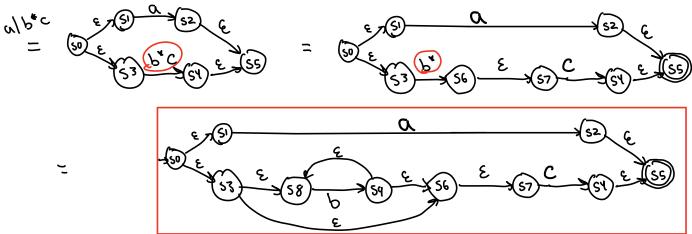
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## Midterm Make-up Exam CS 314, Fall 2024 Section 01-04

(20 pts) RE to NFA, and NFA to DFA Give credit for matching the a, the OR, or the b\*  $a \mid b^*c$ 

(a) Use Thompson's construction to construct an NFA for the regular expression above.



(b) Convert the NFA to a DFA using subset construction.

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istruction.		ı	
	8	Ь	C
D1 \{ 50,51,53, \\ 58,56,57\}	{52,55}	03 {59,58,56 57}	£54,55}
D3	$\times$	559,58,56 D3 573	584 ,543 D4

(c) Minimize the DFA. If the DFA is already minimal, justify it.

a pultition lead

"The DFA is already minimized o

## $\mathbf{2}$ (20 pts) Context Free Grammars

(a) Write a grammar for  $a^x b^y$  where y = x + 2 and  $x \ge 0$  (i.e., exactly 2 more b's than a's).

$$\langle S \rangle = \langle A \rangle b$$

$$\langle A \rangle = \alpha \langle A \rangle b \rangle \epsilon$$

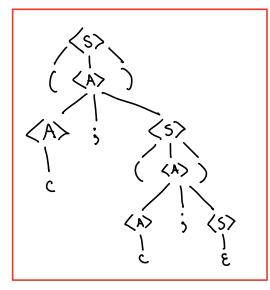
(b) Consider the following grammar (where  $\langle S \rangle = \text{start symbol}$ ):

$$\langle S \rangle \rightarrow (\langle A \rangle) \mid \epsilon$$

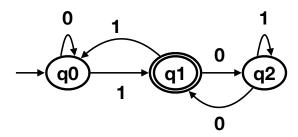
$$\langle A \rangle \rightarrow \langle A \rangle; \langle S \rangle \mid c$$

Present a derivation for the string (c;(c;)) and give the parse tree.

$$\begin{array}{cccc}
\langle S \rangle \\
\overrightarrow{R} & (C; (\langle A \rangle)) \\
\overrightarrow{R} & (\langle A \rangle; \langle S \rangle) \\
\overrightarrow{R} & (\langle A \rangle; \langle S \rangle) \\
\overrightarrow{R} & (C; (C; \langle S \rangle)) \\
\overrightarrow{R} & (C; (C; \langle S \rangle)) \\
\overrightarrow{R} & (C; (C; \langle S \rangle))
\end{array}$$
3 (20 pts) Simulating DFA



Consider the DFA below, determine whether the given strings can be accepted or rejected. q0 is the start state, and q1 is the accepting state.



- (a) 10 (Accept or Reject)
- (b) 111 (Accept or Reject?)

Describe in English what the strings accepted by this DFA have in common.

- · Binary numbers starting at I
  · All binary multiples of 3 plus I and incrementing by

## 4 (40 pts) Unambiguous Grammar

Consider the following grammar that attempts to describe a regular expression:

- 1.  $\langle e \rangle$  ::=  $\langle x \rangle | \epsilon$
- 2. < e > ::= < e > < e >
- 3. < e > ::= < e > \*
- 4.  $\langle e \rangle$  ::=  $\langle e \rangle$  "| "  $\langle e \rangle$
- 5. < e > ::= (< e >)
- 6.  $\langle x \rangle$  ::= a | b | c ... y | z
- (a) Show that the above grammar is ambiguous.

(b) Recall that Kleen Closure (\*) has highest precedence, followed by concatenation, and then alternation ("|"). Let's assume concatenation, alternation and Kleen closure are all left associative. Rewrite the grammar such that it is unambiguous and the precedence/associativity rules are enforced. Note that double quotes are added for the actual alternation operator to distinguish from the | sign that separates production rules.

There precedence operations are nested deeper in grammar

brecengence: () > Kleenc > concat > Mujon

lowest precedence:

(5) ::= 
$$\langle A \rangle$$

(c) | $\langle C \rangle$ 

Con cat  $\langle C \rangle$  ::=  $\langle C \rangle \langle K \rangle$  | $\langle K \rangle$ 

Kleene  $\langle K \rangle$  ::=  $\langle K \rangle$  | $\langle K \rangle$ 

highest precedence:

 $\langle S \rangle$  ::=  $\langle K \rangle$  | $\langle K \rangle$ 
 $\langle K \rangle$  ::=  $\langle K \rangle$  | $\langle K \rangle$ 
 $\langle K \rangle$  ::=  $\langle K \rangle$  | $\langle K \rangle$