

Fundamentals of Data Science

Semester B 20-21

Tutorial 8

1a.(i) The first cluster is $\{6,12,18,24,30\}$, and its centroid is given by $\frac{6+12+18+24+30}{5} = 18$

The second cluster is $\{42,48\}$, and its centroid is given by $\frac{42+48}{2} = 45$

The sum squared error is

$$(6-18)^2 + (12-18)^2 + (18-18)^2 + (24-18)^2 + (30-18)^2 + (42-45)^2 + (48-45)^2 = 378$$

(ii) The first cluster is $\{6,12,18,24\}$, and its centroid is given by $\frac{6+12+18+24}{4} = 15$

The second cluster is $\{30,42,48\}$, and its centroid is given by $\frac{30+42+48}{3} = 40$

The sum squared error is

$$(6-15)^2 + (12-15)^2 + (18-15)^2 + (24-15)^2 + (30-40)^2 + (42-40)^2 + (48-40)^2 = 348$$

b. There will be no change to the clusters generated in both cases (i) and (ii).

2 The first cluster is $\{A\}$, and its centroid is $(2,10)$.

The second cluster is $\{C,D,E,F,H\}$, and its centroid is $\left(\frac{8+5+7+6+4}{5}, \frac{4+8+5+4+9}{5}\right) = (6,6)$.

The third cluster is $\{B,G\}$, and its centroid is $\left(\frac{2+1}{2}, \frac{5+2}{2}\right) = (1.5, 3.5)$.