## Policy Learning V: Reinforcement Learning V

- 1. The Advantage Function (A2C)
  - a. What happened to using the Bellman equation?
  - b. We can include it for  $G_{\theta'}$ 
    - i.  $G_{\theta'}$  just estimates the "value" of the current choice
    - ii. But we know choices are related!
      - 1. How good is a choice?

$$_{2} \quad A(s_{t}, a_{t}) = Q_{\theta'}(s_{t}, a_{t}) - V_{\theta''}(s_{t})$$

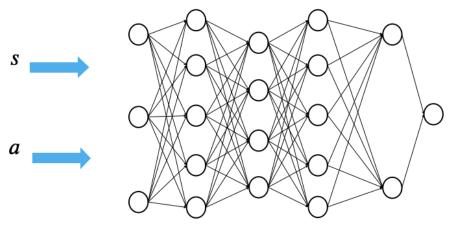
- iii. This is called the advantage function
  - 1. Do we need two function-approximations, one for and one for
  - 2. No!

$$Q(s_t, a_t) = \mathbb{E}\Big[R(s_{t+1}) + \gamma V(s_{t+1})\Big]$$

v. Therefore

$$A(s_t, a_t) = R(s_{t+1}) + \gamma V_{\theta''}(s_{t+1}) - V_{\theta''}(s_t)$$

- c. We only need  $V_{\theta''}$  and  $\pi_{\theta}$ !
- 2. Offline Actor-Critic RL
  - a. Could also do this offline
    - i. Sample N trajectories (i.e. play N games) and record trajectories
    - ii. Build supervised learning datasets
    - iii. For k training iterations:
      - 1. Update  $\pi_{\theta}$  and  $G_{\theta'}$
    - iv. Repeat
  - b. Useful for scaling:
    - i. A3C (Async A2C) = play lots of games in parallel (in eplore step), update after
- 3. NN Q-Function



- a.
- b. NN takes place of tabular Q-function
- c. How to apply updates?
  - i. If we had a table:

$$Q(s,a) \leftarrow Q(s,a) + \alpha \left( R(s) + \gamma \max_{a'} Q(s',a') - Q(s,a) \right)$$

ii. Since we have a NN...cannot adjust Q value directly (like in above equation):

$$\theta_i \leftarrow \theta_i + \alpha \left( R(s) + \gamma \max_{a'} \hat{Q}_{\theta}(s', a') - \hat{Q}_{\theta}(s, a) \right) \frac{\partial \hat{Q}_{\theta}(s, a)}{\partial \theta_i}$$

- d. Gradient descent!
  - i. Error (loss function) =

$$R(s) + \gamma \max_{a'} \hat{Q}_{\theta}(s', a') - \hat{Q}_{\theta}(s, a)$$

- 4. Training a NN Q-function
  - a. For now, let us assume exporation function f is randomized impl.
    - i. With some probability p, ignore policy and choose random action
    - ii. With remaining probability 1-p, follow policy
  - b. Let us observe the transition (s, a, s') where we have recorded R(s) and R(s')
    - i. Fix the policy (i.e. just use the NN):
      - 1. Calculate TD error by iterating over possible actions a' in s'

$$e = R(s) + \gamma \max_{a'} \hat{Q}_{\theta}(s', a') - \hat{Q}_{\theta}(s, a)$$

ii. Backprop e through the network treating e like it is any other error function