References (Array) & Lazy

1. Concepts

- a. Functional programming takes advantage of using immutable values
- b. In python, def foo():

res = [] def bar():

res = res.append(1)

Here, res in res.append(1) refers to the res on the bar function, but res is not defined there, implying that an error will occur

res is mutable data structure (makes program harder to reason)

c. In ML, that is not the case (error does not occur and refers to the right variable, res refers to the correct res

2. References

a. Reference is an array of size 1 (singleton array) (reference is pointer and value)

```
    val A = ref(5)
    val x = !A (get the value of referred value)
    val () = !A:= !A + 1 (update the value of A)
```

c. fun fact(x) =

let

```
val res = ref(1)
val i = ref(0)
fun loop(): unit =
    if !i < x then
        i := !i + 1
        res := !res * !i
        loop()
    else ()</pre>
```

in

loop(); !res

end

- d. Two kinds of arrays
 - i. Mutable (array)
 - ii. Immutable (vector)
- e. val A =

```
val x = Array.sub(A,i) (*subscripting*)
```

```
val = Array.update(A,i,v) (*update i with v *)
       f. Effectful programming features \rightarrow features that cause effect (example \rightarrow print(x)
           \rightarrow it prints value of x which is an effect)
       g. Exceptions \rightarrow one of effectful programming features
       h. Pure programming features \rightarrow (example \rightarrow 1 + 2 \rightarrow does not produce any effect
           to the programmer)
       i. Foreach to iforeach (iforeach is the index, enumerate in python)
       j. fun array foreach(A: 'a array, work: 'a -> unit): unit =
                    int1 foreach(Array.length(A), fn i \Rightarrow work(Array.sub(A,i))
       k. fun array iforeach(A: 'a array, iwork: (int * 'a) -> unit): unit =
                    foreach to iforeach(array foreach)(A, iwork)
3. Lazy
        a. fun from(n: int): int list =
                    n::from(n+1) (* will cause stack overflow \rightarrow maximum recursion reached
                    *)
       b. fun from(n: int) = int list =>
                    n::from(n+1) (* will cause stack overflow \rightarrow maximum recursion reached
                    (* when lambda is seen, evaluation stops and it will be a value *) \rightarrow never
                    go into the body of lambda, use lambda to stop evaluation
       c. datatype 'a strmcon =
                    strmcon nil
                   | strmcon cons of ('a * (unit -> 'a strmcon))
           type 'a stream = unit -> 'a strmcon(stream is a function that returns a
            stream constructor)
           (*stream constructor*) (*stream is a lazy list*)
       d. fun from(n: int) = fn() = >
                    strmcon cons(n,from(n+1))
                    (* when lambda is seen, evaluation stops and it will be a value *) \rightarrow never
                    go into the body of lambda, use lambda to stop evaluation
           OR
           fun from(n: int): int stream = fn() =>
                    strmcon cons(n,from(n+1))
           val the Nats = from(0)
           val fxs = theNats
           val strmcon cons(x0, fxs) = fxs() \rightarrow x0 is 0
           val strmcon cons(x1, fxs) = fxs() \rightarrow x1 is 1
           val strmcon cons(x2, fxs) = fxs() \rightarrow x2 is 2
           val strmcon cons(x3, fxs) = fxs() \rightarrow x3 is 3
           (*presents an illusion of infinite list*)
```