

$$\textcircled{1} (a) G(a, b) \stackrel{\text{def}}{=} \exists x (P(a, x) \wedge P(x, b))$$

$$(b) S(a, b) \stackrel{\text{def}}{=} \exists x (P(x, a) \wedge P(x, b)) \text{ where } a \neq b$$

$$(c) A(a, b) \stackrel{\text{def}}{=} \exists x (S(a, x) \wedge P(x, b))$$

$$(d) C(a, b) \stackrel{\text{def}}{=} \exists x (A(x, a) \wedge P(x, b))$$

$$(e) R(a, b) \stackrel{\text{def}}{=} \exists x (C(x, a) \wedge P(x, b))$$

$$(f) I(a, b) \stackrel{\text{def}}{=} G(a, b) \vee P(a, b) \vee G(b, a) \vee P(b, a) \vee S(a, b) \vee A(a, b) \\ \vee A(b, a)$$

$\textcircled{2} \exists x (x \in A)$: existential quantifier

$\forall x (\neg (x \in A))$: universal quantifier