

**Theorem 1.1.** *Every rank 2 orbit closure of genus 3 translation surfaces is one of*

$$\tilde{\mathcal{Q}}(3, -1^3) \subset \mathcal{H}^{\text{odd}}(4), \quad \tilde{\mathcal{H}}^{\text{hyp}}(2) \subset \mathcal{H}^{\text{hyp}}(2, 2), \quad \tilde{\mathcal{H}}^{\text{odd}}(2) \subset \mathcal{H}^{\text{odd}}(2, 2),$$

*which have dimension 4, or*

$$\tilde{\mathcal{Q}}(4, -1^4) \subset \mathcal{H}^{\text{odd}}(2, 2), \quad \tilde{\mathcal{Q}}(2, 1, -1^3) \subset \mathcal{H}(2, 1, 1), \quad \tilde{\mathcal{H}}(1, 1) \subset \mathcal{H}(1^4),$$

*which have dimension 5, or  $\tilde{\mathcal{Q}}(2, 2, -1^4) \subset \mathcal{H}(1^4)$ , which has dimension 6.*

Note  $\tilde{\mathcal{H}}^{\text{hyp}}(2) = \tilde{\mathcal{Q}}(1, 1, -1^2)$ ,  $\tilde{\mathcal{H}}^{\text{odd}}(2) \subset \tilde{\mathcal{Q}}(4, -1^4)$ , and  $\tilde{\mathcal{H}}(1, 1) \subset \tilde{\mathcal{Q}}(2, 2, -1^4)$ .