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MCStylistic: A Lisp package  
for modelling aspects of  
music cognition and  
stylistic composition

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Tom Collins,  
Nottingham, home of Robin Hood,  
August 2011.



## RELATED PUBLICATIONS

If making use of Secs. 3.1 or 4.3, please cite the following journal paper.

Tom Collins, Robin Laney, Alistair Willis, and Paul H. Garthwaite. Modelling pattern importance in Chopin's mazurkas. *Music Perception*, 28(4):387-414, 2011.

If making use of Secs. 3.1 or 4.4, please cite the following conference paper.

Tom Collins, Jeremy Thurlow, Robin Laney, Alistair Willis, and Paul H. Garthwaite. A comparative evaluation of algorithms for discovering translational patterns in Baroque keyboard works. In J. Stephen Downie and Remco Veltkamp, editors, *Proceedings of the International Symposium on Music Information Retrieval*, pages 3-8, Utrecht, 2010. International Society for Music Information Retrieval.

If making use of anything else, please cite my thesis.

Tom Collins. *Improved methods for pattern discovery in music, with applications in automated stylistic composition*. PhD thesis, Faculty of Mathematics, Computing and Technology, The Open University, 2011.



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MCStylistic is a Lisp package for modelling aspects of **M**usic **C**ognition and **S**tylistic composition.

My guess is most people will be reading this because they wish to check out some aspect of my work on algorithms for pattern discovery in music or automated stylistic composition, or they want to try the code with a view to writing some code themselves. Either way, great! This documentation is written with the above activities in mind. Chapter 1 gets you the user setup with *Common Lisp* (short for list processing), which is my programming language of choice for the work on pattern discovery and automated stylistic composition. If you are already running a version of Lisp, please jump straight to Sec. 1.2.

Chapter 2 gives examples for importing and exporting files of various formats. (It is difficult to do much of any substance until you can import a file, work on it in the Lisp environment, and then export it to another file, so as to save the work.)

Chapter 3 is split into three sections. Section 3.1 contains code for discovering and rating musical patterns, along with an explanation. Sections 3.2 and 3.3 exemplify two models for generating stylistic compositions. The models are called Racchman-Oct2010 and Racchmaninof-Oct2010, standing for RAndom Constrained CHain of Markovian Nodes with INheritance Of Form.

The longest chapter by far is Chapter 4. It contains documentation for each individual function that I have included in the package MCStylistic-Oct2010.



# CHAPTER 1 SETUP

## 1.1 Installing Clozure Common Lisp

There are many versions of Common Lisp, of which Clozure Common Lisp (CCL) is one. Information about CCL can be found at

<http://www.clozure.com/clozurecl.html>,

as well as a link to the CCL Wiki:

<http://trac.clozure.com/ccl>.

On the latter page there is a link to download information:

<http://ccl.clozure.com/download.html>.

This page recommends getting CCL via Subversion, but I have found the archive files (below the comments about Subversion) to work just as well.

If you require more information on installing CCL, please consult the online documentation:

<http://ccl.clozure.com/manual/index.html>.

## 1.2 Loading MCStylistic

The recommended location for the MCStylistic-Oct2010 folder is in a new folder (which you need to create) called *MCStylistic*, in CCL's (or your preferred Lisp implementation's) application folder. If you wish to locate MCStylistic-Oct2010 elsewhere (or separate the locations of data, example files, and functions) then do so, carry on reading, and see the next footnote.

The folder MCStylistic-Oct2010 contains a file called *setup.lisp*. To load the MCStylistic package, open up CCL (or your preferred Lisp implementa-

tion) and open *setup.lisp*.<sup>1</sup> Open a Listener window as well if not already open (File → New Listener). Copy the line of code *between* ‘#|’ and ‘|#’ from *setup.lisp* and paste it at the prompt of the Listener (the prompt is a question mark in CCL). Then hit Return.

Lastly, back in the window containing *setup.lisp*, select all of the text (Edit → Select All) and execute the selection (Lisp → Execute Selection). After about ten seconds, you should see a message in the Listener that reads ‘Welcome to MCStylistic-Oct2010’. This means we are ready to begin.

Each time you wish to use the MCStylistic package, the ritual of copying and pasting the line of code between ‘#|’ and ‘|#’ and then executing the remainder of the text in *setup.lisp* must be observed.

## 1.3 Lisp tips

In CCL it is possible to highlight code between parentheses by double-clicking either the opening or closing parenthesis.

*Rest to be written.*

---

<sup>1</sup>To use the MCStylistic package from a location other than ‘/Applications/CCL/MCStylistic/MCStylistic-Oct2010’, go to lines 12-14 of *setup.lisp* (just below the line that reads `*MCStylistic-Oct2010-path*`) and change the string to specify your preferred location. Following the definition of `*MCStylistic-Oct2010-path*` are definitions for the locations of data, example files, and functions, which can also be changed if you wish. When finished making changes, check that your pathnames are not missing any forward slashes and save *setup.lisp*.

## CHAPTER 2

## IMPORTING AND EXPORTING FILES

The examples in this chapter assume that the Lisp package MCStylistic has been loaded (cf. Sec. 1.2).

### 2.1 Lists stored as text

The function `read-from-file` can be used to import lists that are stored as text files (.txt) into the Lisp environment. For instance, the folder called *Example files* that comes with MCStylistic contains a text file called *short-list.txt*, which can be imported into the Lisp environment using the following code.

```
1 (read-from-file
2   (concatenate
3     'string
4     *MCStylistic-Oct2010-example-files-path*
5     "/short-list.txt"))
6 --> ((9 23 1 19) (14 9 14 5 20 25) (16 5 18 3 5 14 20)
7      ("sure" 9 4) (13 9 19 8 5 1 18 4) (8 5 18))
```

Not setting the path in line 4 correctly (cf. Sec. 1.2) may result in an error message.

To be able to make use of the above list, it is necessary to give it a name as it is imported. For instance the following code names an imported list, and then accesses its second element.

```
1 (setq
2   *little-list*
3   (read-from-file
4     (concatenate
```

```

5      'string
6      *MCStylistic-Oct2010-example-files-path*
7      "/short-list.txt")))
8 --> ((9 23 1 19) (14 9 14 5 20 25) (16 5 18 3 5 14 20)
9      ("sure" 9 4) (13 9 19 8 5 1 18 4) (8 5 18))
10 (nth 1 *little-list*)
11 --> (14 9 14 5 20 25)

```

Sometimes we want to import and name a list (or other data types for that matter), but do not want to see the entire list output (which is what happened in both of the above examples), perhaps because the list is very long. One way of suppressing output is as follows.

```

1 (progn
2   (setq
3     *little-list*
4     (read-from-file
5       (concatenate
6         'string
7         *MCStylistic-Oct2010-example-files-path*
8         "/short-list.txt"))))
9   "*little-list* imported")
10 --> "*little-list* imported"

```

The function `write-to-file` enables lists that are defined within the Lisp environment to be stored as text files. For instance, at present the *Example files* folder that comes with MCStylistic does not contain any file called *another-list.txt*, but we are going to create one. The following code assumes that the variable `*little-list*` has been defined as per lines 1-10 above. Elements of this list are combined with other variables and values to form a new list, which is stored as a text file using the function `write-to-file`.

```

1 (setq *A* (list 0 60 60 1 0))
2 --> (0 60 60 1 0)
3 (setq *B* "middle C")
4 --> "middle C"
5 (setq
6   *new-list*
7   (list
8     (nth 3 *little-list*) *A* (nth 4 *little-list*) *B*
9     4 2))

```

```

10 --> (("sure" 9 4) (0 60 60 1 0) (13 9 19 8 5 1 18 4)
11     "middle C" 4 2)
12 (write-to-file
13  *new-list*
14  (concatenate
15   'string
16   *MCStylistic-Oct2010-example-files-path*
17   "/another-list.txt"))
18 --> T

```

The *Example files* folder should now contain a file called *another-list.txt*. If you open up this text file in a text editor, it should contain elements of the list shown in lines 10-11 above.<sup>1</sup> If you are using a different version of Lisp to CCL, it is worth checking two things. First, importing a file and then exporting it with a new name results in two text files with exactly the same format. This should be the case as *\*print-length\** and *\*print-pretty\** are both set to *nil* (cf. Sec. 1.2). Second, if the location specified in the call to *write-to-file* does not already exist, Lisp creates the location and writes the file.

## 2.2 Musical Instrument Digital Interface (MIDI)

The function *load-midi-file* can be used to import a Standard MIDI File into the Lisp environment. Musical instrument digital interface (MIDI) is a means by which an electronic instrument (such as a synthesiser, electronic piano, drum kit, even a customised guitar, etc.) can connect to a computer and hence communicate with music software (Roads, 1996). When a MIDI file is imported into the Lisp environment using the function *load-midi-file*, a list of five-element lists is defined, where the first element is the *ontime* of a MIDI event, the second element is the *MIDI note number* (MNN, with ‘middle C’ = C4 = 60, C#4 = 61, etc.), the third element is the *duration* (arbitrary timescale), the fourth element is the *channel* (between 1 and 16), and the fifth element is the *velocity* (between 0 for silence and 127 for maximal loudness). These five-element lists are shown in lines 12-15 of the following code, which imports a MIDI representation of the second movement of the Concerto in G minor op.6 no.3 by Antonio Vivaldi (1678-1741).

<sup>1</sup>The function *write-to-file* and other export functions exemplified in this chapter *overwrite* existing files, as opposed to using *supersede* or *append* (for details, see Seibel, 2005).

```

1 (progn
2   (setq
3     *vivaldi-movement*
4     (load-midi-file
5       (concatenate
6         'string
7         *MCStylistic-Oct2010-example-files-path*
8         "/vivaldi-op6-no3-2.mid")))
9     "*vivaldi-movement* imported")
10 --> "*vivaldi-movement* imported"
11 (firstn 10 *vivaldi-movement*)
12 --> ((0 79 1 6 64) (0 69 1 4 64) (0 49 1 1 64)
13      (0 49 1 3 64) (0 76 1 5 64) (1 79 1 6 64)
14      (1 69 1 4 64) (1 76 1 5 64) (1 49 1 1 64)
15      (1 49 1 3 64))

```

The function `saveit` can be used to export an appropriate list defined in the Lisp environment to a Standard MIDI File. The term *appropriate* means that each element of the list is a five-element list (as in lines 12-15 above), with permissible values for ontime (positive float), MNN (integer between 0 and 127), duration (positive float), channel (integer between 1 and 16), and velocity (integer between 0 and 127). Trying to export an inappropriate list as a MIDI file may result in an error message. As an example, the folder called *Example files* that comes with MCStylistic does not contain any file called *two-arpeggios.mid*, but we can create one using the following code.

```

1 (progn
2   (setq
3     *arpeggios*
4     '((0 49 8000 1 64) (1000 69 7000 1 69)
5       (2000 76 6000 1 74) (3000 79 5000 7 79)
6       (8000 50 8000 1 84) (9000 69 7000 1 89)
7       (10000 74 6000 1 94) (11000 77 5000 7 99)))
8   (saveit
9     (concatenate
10      'string
11      *MCStylistic-Oct2010-example-files-path*
12      "/two-arpeggios.mid")
13      *arpeggios*))
14 --> (concatenate

```



```
15     'string
16     *MCStylistic-Oct2010-example-files-path*
17     "/two-arpeggios.mid")
```

MIDI files can be opened and played using programs such as QuickTime Player, RealPlayer, and Windows Media Player. They can also be embedded in web pages. Playing the file created above, you may notice that ontimes and durations are specified in milliseconds. If you have used MCStylistic to discover some repeated patterns (cf. Sec. 3.1) or to generate a dataset representation of music (cf. Sec. 3.2), then the function `saveit` is a convenient way to audition (hear) the results.

## 2.3 Kern

*To be written.*

## 2.4 Other

*To be written.*



## CHAPTER 3

## EXAMPLE CODE

### 3.1 Discovering and rating musical patterns

The folder called *Example files* that comes with MCStylistic contains a Lisp file called *Discovering and rating musical patterns.lisp*. This section will reproduce and discuss chunks of code from this file. The idea is to discover and rate some repeated patterns occurring in bars 1-19 of the Sonata in C minor L10 by Domenico Scarlatti (1685-1757). The algorithm is the Structure Induction Algorithm with Compactness Trawling (SIACT), as defined by Collins, Thurlow, Laney, Willis, and Garthwaite (2010). It combines the Structure Induction Algorithm (SIA) with the concept of compactness (Meredith, Lemström, and Wiggins, 2002, 2003). The formula for rating discovered patterns was developed by Collins, Laney, Willis, and Garthwaite (2011).

Figure 3.1 shows the Scarlatti excerpt annotated with four patterns *A-D* discovered by a music analyst, Dr Jeremy Thurlow.<sup>1</sup> As an example, we will determine which of the four patterns are discovered by SIACT. It is assumed that the package MCStylistic has been loaded, and that the variable `*MCStylistic-Oct2010-example-files-path*` has been defined appropriately. Files are imported from the location specified by this variable, and several new files exported to this location.

```
57 #| Step 1 - Set the parameters. |#  
58 (setq *compact-thresh* 2/3)  
59 (setq *cardina-thresh* 3)  
60 (setq *region-type* "lexicographic")
```

<sup>1</sup>The analyst's complete annotations and a parallel commentary can be found at <http://www.tomcollinsresearch.net>

**Allegro** [ $\text{♩} = 152$ ]

The musical score consists of five systems of staves. The first system (bars 1-4) has two blue circles labeled 'A' highlighting the first and last measures. The second system (bars 5-8) has four orange circles labeled 'B' highlighting specific chords. The third system (bars 9-11) has two black circles labeled 'C' highlighting a complex passage. The fourth system (bars 12-15) has three orange circles labeled 'B' and one purple circle labeled 'D' highlighting specific chords. The fifth system (bars 16-19) has two orange circles labeled 'B' and one purple circle labeled 'D' highlighting specific chords.

Figure 3.1: Bars 1-19 from the Sonata in C minor L10 by D. Scarlatti. Bounding lines indicate some of the analyst's annotations for this excerpt.

The Structure Induction Algorithm with Compactness Trawling (SIACT) has two parameters; a compactness threshold and a points (or cardinality) threshold (Collins et al., 2010). The default version of *compactness* uses a lexicographic region type.

```

62 #| Step 2 - Load dataset and create projections. |#
63 (progn
64   (setq
65     *dataset*
66     (read-from-file
67       (concatenate
68         'string
69         *MCStylistic-Oct2010-example-files-path*
70         "/scarlatti-L10-bars1-19.txt")))
71   (setq
72     *dataset-1-1-0-1-0*
73     (orthogonal-projection-unique-equalp
74       *dataset* '(1 1 0 1 0)))
75   (setq
76     *dataset-1-0-1-0-0*
77     (orthogonal-projection-unique-equalp
78       *dataset* '(1 0 1 0 0)))
79   "Dataset loaded and projections created")

```

The full dataset representation of the excerpt by D. Scarlatti contains dimensions for ontime, MIDI note number (MNN), morphetic pitch number (MPN, for details see Sec. 2.25 of Collins, 2011), duration, and staff. In general, we will want to look at lots of different projections for this dataset, but for this example we consider just two: first, the projection on to ontime, MNN, and duration; second, the projection on to ontime and MPN. These projections are defined using the function `orthogonal-projection-unique-equalp`.

```

81 #| Step 3 - Run SIA on projection (1 1 0 1 0). |#
82 (time
83   (SIA-reflected-merge-sort
84     *dataset-1-1-0-1-0*
85     (concatenate
86       'string
87       *MCStylistic-Oct2010-example-files-path*
88       "/L 10 (1 1 0 1 0) SIA")))
89 ; 0.506381 seconds.

```

This code runs an implementation of the Structure Induction Algorithm (SIA) on the dataset projection for ontime, MNN, and duration, and exports the output to a text file called *L 10 (1 1 0 1 0) SIA.txt* in the *Example files* folder. On a 2.33 GHz machine with 3 GB RAM, this code takes just over half a second to run (line 89).

```

91  #| Step 4 - Run SIACT on projection (1 1 0 1 0). |#
92  (progn
93    (setq
94      *SIA-1-1-0-1-0*
95      (read-from-file
96        (concatenate
97          'string
98          *MCStylistic-Oct2010-example-files-path*
99          "/L 10 (1 1 0 1 0) SIA.txt")))
100    (time
101      (compactness-trawler
102        *SIA-1-1-0-1-0* *dataset-1-1-0-1-0*
103        (concatenate
104          'string
105          *MCStylistic-Oct2010-example-files-path*
106          "/L 10 (1 1 0 1 0) SIACT.txt")
107        *compact-thresh* *cardina-thresh* *region-type*)))
108  ; 0.531744 seconds.

```

Lines 93-99 of the above code import the output of SIA from the file *L 10 (1 1 0 1 0) SIA.txt* just created in the *Example files* folder. Then, in lines 101-107, the compactness trawler (CT) is run, using the parameter values defined earlier. The output of the function compactness-trawler is exported to a text file called *L 10 (1 1 0 1 0) SIACT.txt* in the *Example files* folder. Taking steps 3 (SIA) and 4 (CT) together, SIACT has been applied to the excerpt by D. Scarlatti.

```

110 #| Step 5 - Rate discovered patterns for projection
111 (1 1 0 1 0). |#
112 (progn
113   (setq
114     *SIACT-1-1-0-1-0*
115     (read-from-file
116       (concatenate
117         'string

```

```

118      *MCStylistic-Oct2010-example-files-path*
119      "/L 10 (1 1 0 1 0) SIACT.txt"))))
120  (time
121    (setq
122      *hash-1-1-0-1-0*
123      (evaluate-variables-of-patterns2hash
124        *SIACT-1-1-0-1-0* *dataset-1-1-0-1-0*)))
125  (write-to-file-balanced-hash-table
126    *hash-1-1-0-1-0*
127    (concatenate
128      'string
129      *MCStylistic-Oct2010-example-files-path*
130      "/L 10 (1 1 0 1 0) hash.txt"))
131  (concatenate
132    'string
133    "Discovered patterns have been rated and placed in"
134    " in the hash table *hash-1-1-0-1-0*. They have"
135    " also been written to a text file for future"
136    " reference."))
137  ; 2.376775 seconds.

```

Lines 115-119 of the above code import the output of SIACT from the file just created in the *Example files* folder, *L 10 (1 1 0 1 0) SIACT.txt*. Each discovered pattern is given a rating for musical importance in lines 121-124, using the function `evaluate-variables-of-patterns2hash`. The hash table (cf. Sec. 2.4) created by this function is exported to a text file called *L 10 (1 1 0 1 0) hash.txt* in the *Example files* folder.

```

139  #| Here are the details for pattern A, as annotated in
140  the Documentation, Fig. 3.1. |#
141  (disp-ht-el (nth 13 *hash-1-1-0-1-0*))
142  --> (("name" . "pattern 24") ("compactness" . 1)
143      ("expected occurrences" . 35.375904)
144      ("rating" . 7.539052)
145      ("pattern"
146        (1/2 60 1/2) (1 63 1/2) (3/2 67 1/2) (2 72 1/2)
147        (5/2 75 1/2) (3 79 1/2) (7/2 84 1/2) (4 79 1/2)
148        (9/2 75 1/2) (5 72 1/2) (11/2 67 1/2) (6 60 1))
149      ("translators" (0 0 0) (6 -12 0)) ("index" . 24)
150      ("cardinality" . 12) ("MTP vectors" (6 -12 0))
151      ("compression ratio" . 24/13))

```

```

152     ("region"
153      (1/2 60 1/2) (1 63 1/2) (3/2 67 1/2) (2 72 1/2)
154      (5/2 75 1/2) (3 79 1/2) (7/2 84 1/2) (4 79 1/2)
155      (9/2 75 1/2) (5 72 1/2) (11/2 67 1/2) (6 60 1))
156     ("occurrences" . 2))

```

Above we see details for pattern *A*, as annotated in Fig. 3.1. It has been rated as approximately 7.5 out of 10, using a weighted combination of *compactness*, *expected occurrences*, and *compression ratio*.

Lines 158-214 of the Lisp file *Discovering and rating musical patterns.lisp* will not be reproduced here. Steps 6, 7, and 8 are analogous to steps 3, 4, and 5, applying SIACT and the rating formula to the projection for ontime and MPN. Among the output, we pick out the following result.

```

216  #| Here are the details for pattern B, as annotated in
217  the Documentation, Fig. 3.1. |#
218  (disp-ht-el (nth 2 *hash-1-0-1-0-0*))
219  --> (("name" . "pattern 40") ("compactness" . 13/15)
220      ("expected occurrences" . 44.16958)
221      ("rating" . 8.927441)
222      ("pattern"
223       (73/4 71) (37/2 72) (75/4 73) (19 69) (19 74)
224       (39/2 68) (39/2 73) (20 69) (20 74) (41/2 68)
225       (41/2 73) (21 69) (21 74))
226      ("translators"
227       (-6 0) (-3 -7) (0 0) (3 -7) (15 -10) (18 -17)
228       (24 -11) (30 -12))
229      ("index" . 40) ("cardinality" . 13)
230      ("MTP vectors"
231       (36 -12) (30 -11) (30 -12) (24 -11) (24 -17)
232       (18 -17) (15 -2) (12 -3) (9 -1) (9 -7) (3 -7)
233       (3 -7))
234      ("compression ratio" . 26/5)
235      ("region"
236       (73/4 71) (37/2 72) (75/4 73) (19 64) (19 69)
237       (19 74) (39/2 68) (39/2 73) (20 64) (20 69)
238       (20 74) (41/2 68) (41/2 73) (21 69) (21 74))
239      ("occurrences" . 8))

```

Above we see details for pattern *B*, as annotated in Fig. 3.1. It has been rated as approximately 8.9 out of 10. Pattern *C*, as annotated in the Fig. 3.1,



is not discovered by SIACT. Close inspection of the music reveals that  $C$  is not a translational pattern for either of the projections considered above. Pattern  $D$  is not discovered by SIACT either, but a pattern that contains  $D$  is discovered. The containing pattern begins where  $D$  does, in bar 14, and continues into bar 16. We are prompted to consider why the first occurrence of  $D$  is annotated as finishing earlier, in bar 15. It may be that the rests in bar 15 suggest a boundary to the analyst; an appropriate point for demarcating the first occurrence of pattern  $D$ . When the sonata is played at full pace, however, these rests can be difficult to perceive.

More information about functions for pattern discovery and rating can be found in Secs. 4.4 and 4.3.

## 3.2 Stylistic composition with Racchman-Oct2010

The folder called *Example files* that comes with MCStylistic contains a Lisp file called *Stylistic composition with Racchman-Oct2010.lisp*. This section will reproduce and discuss chunks of code from this file. The idea is to demonstrate Racchman-Oct2010 (standing for RAndom Constrained CHain of MArkovian Nodes), which is a model for automated stylistic composition. A date stamp is added to Racchman in case it is superseded by future work. Chapters 8 and 9 of Collins (2011) provide a full explanation of the model. It is similar in spirit to the databases and programs referred to collectively as Experiments in Musical Intelligence (EMI), as outlined by Cope (1996, 2001, 2005).

Here I will exemplify the building of initial states lists and transition lists, and the use of these lists by Racchman-Oct2010 to generate an opening passage of a mazurka in the style of Frédéric Chopin (1810-1849). This very passage was used in an evaluation of the model (excerpt 19 in Chapter 10 of Collins, 2011); the user may wish to experiment with different random seeds, resulting in different generated passages. The building of the initial states lists and transition lists takes about two hours on a 2.33 GHz machine with 3 GB RAM, so for users not wishing to wait that long, the resulting files have been placed in the *Example files* folder, in a folder called *Racchman-Oct2010 example*. The passage generation takes about 260 seconds.

Step 1 of the code involves creating one list called `*variable-names*`, creating another list called `*catalogue*`, and then importing dataset representations for thirty-nine mazurkas into the Lisp environment. The code is not reproduced here; it is verbose but relatively straightforward to under-

stand.

```

345 #| Step 2 - Create lists of initial/final state-
346 context pairs, and transition lists. |#
347 (progn
348   (setq
349     *initial-states*
350     (construct-initial-states
351       *variable-names* *catalogue* "beat-spacing-states"
352       10 3 3 1))
353   (write-to-file
354     *initial-states*
355     (concatenate
356       'string
357       *MCStylistic-Oct2010-example-files-path*
358       "/Racchman-Oct2010 example/initial-states.txt"))
359   (setq
360     *final-states*
361     (construct-final-states
362       *variable-names* *catalogue* "beat-spacing-states"
363       10 3 3 1))
364   (write-to-file
365     *final-states*
366     (concatenate
367       'string
368       *MCStylistic-Oct2010-example-files-path*
369       "/Racchman-Oct2010 example/final-states.txt"))
370   "Initial/final state-context pairs exported.")
371
372 (progn
373   (setq *transition-matrix* nil)
374   (construct-stm
375     *variable-names* *catalogue* "beat-spacing-states"
376     3 3 1)
377   (write-to-file
378     *transition-matrix*
379     (concatenate
380       'string
381       *MCStylistic-Oct2010-example-files-path*
382       "/Racchman-Oct2010 example"
383       "/transition-matrix.txt"))

```

```

384 (setq *transition-matrix* nil)
385 (construct-stm<-
386   *variable-names* *catalogue* "beat-spacing-states"
387   3 3 1)
388 (write-to-file
389   *transition-matrix*
390   (concatenate
391     'string
392     *MCStylistic-Oct2010-example-files-path*
393     "/Racchman-Oct2010 example"
394     "/transition-matrix<-.txt"))
395 "Transition lists exported.")

```

The function `construct-initial-states` is called in line 350 to construct a list of initial state-context pairs, which are then exported to a text file (lines 353-358). In lines 359-394 there are analogous calls to (and file exports for) the functions `construct-final-states`, `construct-stm`, and `construct-stm<-`. As mentioned, users not wishing to create these lists themselves will find them in the folder called *Racchman-Oct2010 example*.<sup>2</sup>

```

397 #| Step 3 - Define parameter values for
398 Racchman-Oct2010. |#
399 (progn
400   (setq *beats-in-bar* 3) (setq *c-absrb* 10)
401   (setq *c-src* 4) (setq *c-bar* 19) (setq *c-min* 19)
402   (setq *c-max* 19) (setq *c-beat* 12)
403   (setq *c-prob* 0.2) (setq *c-for* 3)
404   (setq *c-back* 3)
405   (setq
406     *checklist*
407     (list "originalp" "mean&range" "likelihoodp"))
408 "Racchmann-Oct2010 parameters defined.")

```

The above parameter values for Racchman-Oct2010 are explained fully in Chapters 8 and 9 of Collins (2011). In brief, they control the number of

<sup>2</sup>It should be noted that the internal initial states and internal final states are defined by hand (but completely algorithmically). The list of internal initial states, for instance, contains three beat-spacing states (where these exist) from each of the thirty-nine mazurkas, taken from the time points at which the rst three phrases are marked as ending in the score, according to Paderewski's (1953) edition.

absorptions permitted at each stage of the generating process ( $c_{\text{absb}} = 10$ ), the number of consecutive states heralding from the same source ( $c_{\text{src}} = 4$ ), the range ( $c_{\text{min}} = c_{\text{max}} = \bar{c} = 19$ ), low-likelihood chords ( $c_{\text{prob}} = .2$  and  $c_{\text{beat}} = 12$ ), and a sense of departure/arrival ( $c_{\text{for}} = c_{\text{back}} = 3$ ).

```

410  #| Step 4 - Import lists of initial/final state-
411  context pairs, and transition lists. It should be
412  noted that some variables, such as
413  *internal-initial-states*, are not required for this
414  example, so their import code is commented out. |#
415  (progn
416    (setq
417      *initial-states*
418      (read-from-file
419        (concatenate
420          'string
421          *MCStylistic-Oct2010-example-files-path*
422          "/Racchman-Oct2010 example/initial-states.txt")))
423    #|
424    (setq
425      *internal-initial-states*
426      (read-from-file
427        (concatenate
428          'string
429          *MCStylistic-Oct2010-example-files-path*
430          "/Racchman-Oct2010 example"
431          "/internal-initial-states.txt")))
432    |#
433    (setq
434      *internal-final-states*
435      (read-from-file
436        (concatenate
437          'string
438          *MCStylistic-Oct2010-example-files-path*
439          "/Racchman-Oct2010 example"
440          "/internal-final-states.txt")))
441    #|
442    (setq
443      *final-states*
444      (read-from-file
445        (concatenate

```

```

446     'string
447     *MCStylistic-Oct2010-example-files-path*
448     "/Racchman-Oct2010 example/final-states.txt"))
449 |#
450 (setq
451   *stm->*
452   (read-from-file
453     (concatenate
454       'string
455       *MCStylistic-Oct2010-example-files-path*
456       "/Racchman-Oct2010 example"
457       "/transition-matrix.txt")))
458 (setq
459   *stm<-*
460   (read-from-file
461     (concatenate
462       'string
463       *MCStylistic-Oct2010-example-files-path*
464       "/Racchman-Oct2010 example"
465       "/transition-matrix<-.txt")))
466 (concatenate
467   'string
468   "Initial state/context pairs and transition lists"
469   " imported."))

```

The above code imports initial states lists and transition lists, some of which were created in step 1. As the idea is to generate the opening passage of a mazurka, it is not necessary to import the external final states list, nor the internal initial states list, which is why lines 424-431 and 442-448 are commented out.

```

471 #| Step 5 - Import the dataset of an existing Chopin
472 mazurka to be used as a template (op.56 no.2). A
473 template (cf. Def. 9.1 in Collins, 2011) consists of
474 basic information, such as tempo and the pitch of the
475 lowest-sounding note of the first chord, which is
476 transferred to the generated passage. |#
477 (progn
478   (setq
479     *dataset-all*
480     (read-from-file

```

```

481     (concatenate
482       'string
483       *MCStylistic-Oct2010-data-path*
484       "/Dataset/C-56-2-ed.txt"))
485   (setq
486     *dataset-template*
487     (subseq *dataset-all* 0 135))
488   "Template imported.")

```

The above code imports an existing Chopin mazurka to be used as a template. The opening section of this mazurka is defined as the `*dataset-template*`, as the idea is to generate an opening passage.

```

490  #| Step 6 - Generate candidate passages using
491  Racchman-Oct2010 and select one. |#
492  (progn
493    (setq
494      *rs* #.(CCL::INITIALIZE-RANDOM-STATE 46803 5306))
495    (setq time-a (get-internal-real-time))
496    (setq
497      *output*
498      (generate-beat-MNN-spacing<->
499        *initial-states* *stm->* *internal-final-states*
500        *stm<-* *dataset-template* *checklist*
501        *beats-in-bar* *c-absrb* *c-src* *c-min* *c-max*
502        *c-bar* *c-beat* *c-prob* *c-for* *c-back*))
503    (setq time-b (get-internal-real-time))
504    (float
505      (/
506        (- time-b time-a)
507        internal-time-units-per-second)))
508  ; 266.0195 seconds.
509  (most-plausible-join
510    (third *output*) 23 *dataset-template* *stm->* 3 3 1
511    *c-beat*)
512  ; "united,3,3,backwards-dominant"

```

The above code is at the heart of the Racchman-Oct2010 model, as it is responsible for generating a passage. In lines 493-494 a random seed is defined called `*rs*`. If users wish to experiment with different random seeds,

they can alter the numbers in line 494 manually, or use the built-in function `make-random-state`. Lines 496-502 of the code generates several candidate passages, which takes about 260 seconds. It is worth pointing out that different random seeds will result in different passage generation times. Of all the generated candidates, the output of Racchman-Oct2010 is the passage whose states are all members of the transition list and whose likelihood profile is, on average, closest to that of the template piece. This is determined in lines 509-511.

```

514 #| Step 7 - Export the generated passage to MIDI and
515 text files. |#
516 (progn
517   (setq
518     *output-datapoints*
519     (gethash
520       "united,3,3,backwards-dominant"
521       (third *output*)))
522   (saveit
523     (concatenate
524       'string
525       *MCStylistic-Oct2010-example-files-path*
526       "/Racchman-Oct2010 example/generated-passage.mid")
527     (modify-to-check-dataset
528       (translation
529         *output-datapoints*
530         (list
531           (- 0 (first (first *output-datapoints*)))
532             0 0 0 0)) 950))
533   (write-to-file
534     *output-datapoints*
535     (concatenate
536       'string
537       *MCStylistic-Oct2010-example-files-path*
538       "/Racchman-Oct2010 example"
539       "/generated-passage.txt"))
540   (concatenate
541     'string
542     "Generated passage exported to MIDI and text"
543     " files."))

```

The generated passage is exported to a MIDI file, as well as to a text file.

When this code is executed, the files *generated-passage.mid* and *generated-passage.txt* should appear in the folder called *Racchman-Oct2010 example* (which is in the *Example files* folder).

The above code and functions invoked (cf. Sec. 4.5 for additional documentation) represent something of an achievement: this code accompanies the first full description (in Chapters 8 and 9 of Collins, 2011) of a model for generating passages in the style of Chopin mazurkas. There is still much to be achieved, however. Models for automated stylistic composition ought to be evaluated thoroughly in order to gauge stylistic success and identify weaknesses. Evaluation of the passages generated by Racchman-Oct2010 suggests that there are stylistically successful aspects, with room for future improvements (see Chapter 11 of Collins, 2011 for more details).

### 3.3 Stylistic composition with Racchmaninof-Oct2010

The folder called *Example files* that comes with MCStylistic contains a Lisp file called *Stylistic composition with Racchmaninof-Oct2010.lisp*. This section will reproduce and discuss chunks of code from this file. The code is very similar to that discussed in Sec. 3.2, so in the following we will focus on the parts that differ. The idea is to demonstrate Racchmaninof-Oct2010 (standing for RAndom ConstrAined CHain of MArkovian Nodes with INheritance Of Form), which is a model for automated stylistic composition. A date stamp is added to Racchmaninof in case it is superseded by future work. Chapters 8 and 9 of Collins (2011) provide a full explanation of the model. The main difference between Racchman-Oct2010 and Racchmaninof-Oct2010 is that the latter includes pattern inheritance. This means the temporal and registral positions of discovered repeated patterns from an existing piece are used as a template to guide the generation of a new passage of music. Both models are similar in spirit to the databases and programs referred to collectively as Experiments in Musical Intelligence (EMI), as outlined by Cope (1996, 2001, 2005).

Here I will exemplify the building of initial states lists and transition lists, and the use of these lists by Racchmaninof-Oct2010 to generate an opening passage of a mazurka in the style of Chopin. This very passage was used in an evaluation of the model (excerpt 28 in Chapter 10 of Collins, 2011); the user may wish to experiment with different random seeds, resulting in different generated passages. The building of the initial states lists and transition lists takes about two hours on a 2.33 GHz machine with 3 GB RAM, so for



users not wishing to wait that long, the resulting files have been placed in the *Example files* folder, in a folder called *Racchman-Oct2010 example*. The passage generation takes about 5 seconds.

Steps 1-4 of the code will not reproduced here; it is analogous to the code in Sec. 3.2.

```

477 #| Step 5 - Import the dataset of an existing Chopin
478 mazurka (op.68 no.1) to be used as a template with
479 patterns. A template with patterns (cf. Def. 9.3 in
480 Collins, 2011) consists of basic information, such as
481 tempo and the pitch of the lowest-sounding note of the
482 first chord, but also information to do with
483 discovered patterns, such as the ontimes of first and
484 last datapoints, translators, and subset scores. The
485 second chunk of code here runs SIACT, rates the
486 discovered patterns, and performs some filtering as
487 described in Sec. 7.3.1 of Collins (2011). |#
488 (progn
489   (setq
490     *dataset-all*
491     (read-from-file
492       (concatenate
493         'string
494         *MCStylistic-Oct2010-data-path*
495         "/Dataset/C-68-1-ed.txt")))
496   (setq
497     *dataset-template*
498     (subseq *dataset-all* 0 231))
499   (setq
500     *dataset-projected*
501     (orthogonal-projection-unique-equalp
502       *dataset-template* '(1 1 1 0 0)))
503   "Template imported and projected.")
504
505 (progn
506   (setq time-a (get-internal-real-time))
507   (setq *compact-thresh* 4/5)
508   (setq *cardina-thresh* 3)
509   (setq *region-type* "lexicographic")
510   (setq *duration-thresh* 3)
511   (SIA-reflected-merge-sort

```

```

512     *dataset-projected*
513     (concatenate
514       'string
515       *MCStylistic-Oct2010-example-files-path*
516       "/Racchmaninof-Oct2010 example"
517       "/C-68-1 (1 1 1 0 0) SIA"))
518   (setq
519     *SIA-output*
520     (read-from-file
521       (concatenate
522         'string
523         *MCStylistic-Oct2010-example-files-path*
524         "/Racchmaninof-Oct2010 example"
525         "/C-68-1 (1 1 1 0 0) SIA.txt")))
526   (compactness-trawler
527     *SIA-output* *dataset-projected*
528     (concatenate
529       'string
530       *MCStylistic-Oct2010-example-files-path*
531       "/Racchmaninof-Oct2010 example"
532       "/C-68-1 (1 1 1 0 0) CT.txt")
533     *compact-thresh* *cardina-thresh*
534     *region-type*)
535   (setq
536     *SIACT-output*
537     (read-from-file
538       (concatenate
539         'string
540         *MCStylistic-Oct2010-example-files-path*
541         "/Racchmaninof-Oct2010 example"
542         "/C-68-1 (1 1 1 0 0) CT.txt")))
543   (setq
544     *patterns-hash*
545     (prepare-for-pattern-inheritance
546       *SIACT-output* *dataset-projected*
547       *duration-thresh*))
548   (write-to-file-balanced-hash-table
549     *patterns-hash*
550     (concatenate
551       'string
552       *MCStylistic-Oct2010-example-files-path*

```

```

553   "/Racchmaninof-Oct2010 example"
554   "/C-68-1 (1 1 1 0 0) PH.txt"))
555 (setq time-b (get-internal-real-time))
556 (float
557   (/
558     (- time-b time-a)
559     internal-time-units-per-second)))
560 ; 1.500049 sec. Patterns discovered, rated, filtered.

```

In lines 488-503 a dataset representation of Chopin's Mazurka in C major op.68 no.1 is imported, and attention restricted to the first 231 datapoints (line 498). A projection on to the dimensions of ontime, MNN, and MPN is defined in lines 499-502. The second chunk of code (lines 505-565) runs SIACT (an example run of the pattern discovery algorithm SIACT was discussed in Sec. 3.1). Parameters are set in lines 507-510. The parameters *\*compact-thresh\**, *\*cardina-thresh\**, and *\*region-type\** were met before (cf. Sec. 3.1). The parameter *\*duration-thresh\** ensures that only discovered patterns of at least this duration (last ontime minus first ontime) are inherited. SIA is run and the results imported in lines 511-525. The compactness trawler (CT) is run and the results imported in lines 526-542. The patterns are rated, filtered, and exported in lines 543-554. The filters include the duration threshold mentioned above, as well as removal of overlapping occurrences of the same pattern, and removal of a pattern  $Q$  and its occurrences when  $Q$  is the lower-rated of two patterns  $P$  and  $Q$ , they have the same translators, and  $Q$  is a subset of  $P$ . For further discussion of these filters, see Sec. 7.3.1 in Collins (2011).

```

562 #| Step 6 - Generate candidate passages using
563 Racchmaninof-Oct2010 and select one. |#
564 (progn
565   (setq
566     *rs* #.(CCL::INITIALIZE-RANDOM-STATE 56837 36574))
567   (setq
568     *whole-piece-interval*
569     (list
570       (floor (first (first *dataset-all*)))
571       (ceiling (first (my-last *dataset-all*)))))
572   (setq time-a (get-internal-real-time))
573   (setq
574     *interval-output-pairs*
575     (generate-beat-spacing<->pattern-inheritance

```

```

576      *external-initial-states*
577      *internal-initial-states* *stm->*
578      *external-final-states* *internal-final-states*
579      *stm<-* *dataset-template* *patterns-hash*
580      *whole-piece-interval* *checklist* *beats-in-bar*
581      *c-absrb* *c-src* *c-bar* *c-min* *c-max* *c-beat*
582      *c-prob* *c-for* *c-back*))
583  (setq time-b (get-internal-real-time))
584  (float
585    (/
586      (- time-b time-a)
587      internal-time-units-per-second)))
588  ; 5.126742 seconds.

```

The above code is at the heart of the Racchmaninof-Oct2010 model, as it is responsible for generating a passage. In lines 565-566 a random seed is defined called *\*rs\**. If users wish to experiment with different random seeds, they can alter the numbers in line 566 manually, or use the built-in function `make-random-state`. The time interval for which a new passage will be generated is defined in lines 567-571 of the code defines *t*. The order in which different portions of this time interval are addressed depends on the subset scores and ratings of discovered patterns. Lines 573-582 generate and select from several candidate passages, which takes about 5 seconds. It is worth pointing out that different random seeds will result in different passage generation times. The way in which discovered patterns are inherited by the generated passage is exemplified in Sec. 9.6 of Collins (2011), but not discussed further here.

```

590  #| Step 7 - Export the generated passage to MIDI and
591  text files. |#
592  (progn
593    (setq
594      *output-datapoints*
595      (interval-output-pairs2dataset
596        *interval-output-pairs*))
597    (saveit
598      (concatenate
599        'string
600        *MCStylistic-Oct2010-example-files-path*
601        "/Racchmaninof-Oct2010 example"
602        "/generated-passage.mid")
603    (modify-to-check-dataset

```

```
604     (translation
605       *output-datapoints*
606       (list
607         (- 0 (first (first *output-datapoints*)))
608         0 0 0 0)) 850))
609 (write-to-file
610   *output-datapoints*
611   (concatenate
612     'string
613     *MCStylistic-Oct2010-example-files-path*
614     "/Racchmaninof-Oct2010 example"
615     "/generated-passage.txt"))
616 (concatenate
617   'string
618   "Generated passage exported to MIDI and text"
619   " files."))
```

The generated passage is exported to a MIDI file, as well as to a text file. When this code is executed, the files *generated-passage.mid* and *generated-passage.txt* should appear in the folder called *Racchmaninof-Oct2010 example* (which is in the *Example files* folder).

As with Sec. 3.2, the above code and functions invoked (cf. Sec. 4.5 for additional documentation) represent something of an achievement: this code accompanies the first full description (in Chapters 8 and 9 of Collins, 2011) of a model for pattern inheritance. There is still much to be achieved, however. Models for automated stylistic composition ought to be evaluated thoroughly in order to gauge stylistic success and identify weaknesses. Evaluation of the passages generated by Racchmaninof-Oct2010 suggests that there are stylistically successful aspects, with room for future improvements (Chapter 11 of Collins, 2011). In particular, the prize remains unclaimed for demonstrating experimentally that pattern inheritance alone can lead to improved ratings of stylistic success.



# CHAPTER 4

---

## DOCUMENTATION FOR INDIVIDUAL FUNCTIONS

### 4.1 Maths foundation

#### 4.1.1 List processing

These functions do simple but important things with lists. For example, the function `add-to-list` adds the first argument (a number) to each element of the second argument (a list). A slightly more complicated function called `remove-nth` removes the `nth` element from a given list.

#### **add-to-list**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	
Comments/see also	

Example:

```
(add-to-list 5 '(1 2 3))  
--> (6 7 8).
```

This function adds a constant to each element of a list.

**add-to-nth**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	firstn
Called by	
Comments/see also	

Example:

```
(add-to-nth 1 3 '(1 2 3 5 9))
--> (1 2 4 5 9).
```

This function adds a constant to the  $n$ th element of a list.

**choose**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	factorial, factorial-j
Called by	
Comments/see also	

Example:

```
(choose 9 5)
--> 126.
```

This function returns ' $n$  choose  $r$ ', that is  $n!/(r!(n-r)!)$ , where  $n$  and  $r$  are natural numbers or zero.

**constant-vector**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	
Comments/see also	

Example:

```
(constant-vector 2.4 6)
--> (2.4 2.4 2.4 2.4 2.4 2.4).
```

This function gives a constant vector of prescribed length.



**factorial**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	choose
Comments/see also	

Example:

```
(factorial 5)
--> 120.
```

This function returns  $n(n-1)(n-2)\cdots 3\cdot 2\cdot 1$ , where  $n$  is a natural number or zero.

**factorial-j**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	choose
Comments/see also	

Example:

```
(factorial-j 9 3)
--> 3024.
```

The arguments of this function are  $n > j$ , both natural numbers or zero. The answer  $n(n-1)(n-2)\cdots(n-j)$  is returned. If  $j \geq n$  or  $j < 0$ , 1 is returned. This function makes the function choose more efficient by avoiding direct calculation of  $n!/r!$ .

**first-n-naturals**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	
Comments/see also	

Example:

```
(first-n-naturals 5)
--> (5 4 3 2 1).
```

This function returns the first n natural numbers as a list.

## **firstn**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	add-to-nth, remove-nth
Comments/see also	

Example:

```
(firstn 3 '(3 4 (5 2) 2 0))
--> (3 4 (5 2)).
```

This function returns the first n items of a list.

## **index-item-1st-occurs**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	
Comments/see also	

Example:

```
(index-item-1st-occurs 2 '(1 0 0 2 4 2))
--> 3.
```

Taking an item and a list of items as its arguments, this function returns the index at which the given item first occurs, counting from zero. If the item does not occur at all then the function returns NIL.

## **last-first**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	lastn
Comments/see also	

Example:

```
(last-first 3 '(3 4 (5 2) 2 0))
--> (0 2 (5 2)).
```

This function returns the last *n* items of a list, but in reverse order. NB the function `last` returns a list rather than a list element.

## lastn

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	last-first
Called by	add-to-nth, remove-nth
Comments/see also	

Example:

```
(lastn 3 '(3 4 (5 2) 2 0))
--> ((5 2) 2 0).
```

This function returns the last *n* items of a list.

## multiply-list-by-constant

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	
Comments/see also	

Example:

```
(multiply-list-by-constant '(2 0) 5)
--> (10 0).
```

Two arguments are supplied to this function: a list and a constant. A list is returned, containing the result of multiplying each element of the list by the constant.

**my-last**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	
Comments/see also	

Example:

```
(my-last '(1 3 6 7))
--> 7.
```

Returns the last element of a list as an element, not as a list.

**nth-list**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	
Comments/see also	

Example:

```
(nth-list '(1 3 0) '(6 -3 -88 0 4 44))
--> (-3 0 6).
```

This function applies the function `nth` recursively to the second list argument, according to the items of the first list argument.

**nth-list-of-lists**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	
Comments/see also	Could be rewritten using the function <code>map-car</code> .

Example:

```
(nth-list-of-lists 0 '((48 2) (-50 0) (-5 5)))
--> (48 -50 5).
```

This function takes two arguments; an item `n` and a list of sub-lists. It returns the `nth` item of each sub-list as a list.

### remove-nth

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	remove-nth-list, sort-by-col-asc, sort-by-col-desc
Comments/see also	

Example:

```
(remove-nth 4 '(6 4 5 5 2 3 1))
--> (6 4 5 5 3 1).
```

This code removes the `nth` item of a list, counting from zero.

### remove-nth-list

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	remove-nth
Called by	
Comments/see also	

Example:

```
(remove-nth-list '(3 5 0) '(1 2 3 4 5 6 7))
--> (2 3 5 7).
```

The function `remove-nth-list` applies the function `remove-nth` recursively to the second argument, according to the indices in the first argument, which do not have to be ordered or distinct.

**test-equalp-nth-to-x**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	
Comments/see also	Deprecated.

Example:

```
(test-equalp-nth-to-x '(3 5 0) 1 5)
--> T.
```

The first argument to this function is a list of numbers, the second argument is an index that refers to one of these numbers. If this number is equalp to the third argument, T is returned, and nil otherwise.

**test-equalp-nth-to-xs**

Started, last checked	19/1/2010, 19/1/2010
Location	List processing
Calls	
Called by	
Comments/see also	Deprecated.

Example:

```
(test-equalp-nth-to-xs '(3 5 0) 1 '(2 4 5 6))
--> T.
```

The first argument to this function is a list of numbers, the second argument is an index that refers to one of these numbers. This number is tested for membership in the third argument, and the output is the result of this test. Note it will not recognise 1.0 as 1.

**4.1.2 Set operations**

These functions enable the formation of unions and intersections over lists that represent finite sets in  $n$ -dimensional space. It is also possible to find translators of a pattern in a dataset.

**add-two-lists**

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	
Called by	test-equal<potential-translator, translation
Comments/see also	add-two-lists-mod-2nd-n

Example:

```
(add-two-lists '(4 7 -3) '(8 -2 -3))
--> (12 5 -6)
```

Adds two lists element-by-element. It is assumed that elements of list arguments are numbers, and the list arguments are of the same length. An empty first (but not second) argument will be tolerated.

**check-potential-translators**

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	test-equal<potential-translator
Called by	translators-of-pattern-in-dataset
Comments/see also	check-potential-translators-mod-2nd-n

Example:

```
(check-potential-translators
 '(3 52) '((0 0) (1 2) (1 5) (2 7))
 '((0 60) (3 52) (4 57) (5 59)))
--> ((0 0) (1 5) (2 7))
```

Checks whether the first argument, when translated by each member of the second argument, is a member of the third argument. Members of the second argument that satisfy this property are returned.

**insert-retaining-sorted-asc**

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	vector<vector
Called by	union-multidimensional-sorted-asc
Comments/see also	

Example:

```
(insert-retaining-sorted-asc
 '(5 0) '((-6 2) (-4 1) (8 0)))
--> ((-6 2) (-4 1) (5 0) (8 0))
```

Two arguments are supplied to this function: a (real) vector and a strictly-ascending list of (real) vectors (of the same dimension). The first argument is included in the second and output, so that it remains a strictly-ascending list of vectors. (Note this means that if the first argument is already in the list, then this list is output unchanged.)

## intersection-multidimensional

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	test-equal<list-elements
Called by	intersections-multidimensional
Comments/see also	

Example:

```
(intersection-multidimensional
 '((4 8 8) (4 7 6) (5 -1 0) (2 0 0))
 '((4 6 7) (2 0 0) (4 7 6)))
--> ((4 7 6) (2 0 0))
```

Like the built-in Lisp function `intersection`, this function returns the intersection of two lists. Unlike the built-in Lisp function, this function handles lists of lists.

## intersections-multidimensional

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	intersection-multidimensional, null-list-of-lists
Called by	
Comments/see also	

Example:



```
(intersections-multidimensional
 '(((4 8 8) (4 7 6) (5 -1 0) (2 0 0))
   ((4 6 7) (2 0 0) (4 7 6))
   ((4 7 6) (2 1 0) (5 -1 0) (5 0 5))))
--> ((4 7 6))
```

The single argument to this function consists of  $n$  lists of lists (of varying length). Their intersection is calculated and returned.

### null-list-of-lists

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	
Called by	intersections-multidimensional
Comments/see also	

Example:

```
(null-list-of-lists
 '(((4 8 8) (4 7 6) (5 -1 0) (2 0 0))
   ()
   ((4 7 6) (2 1 0) (5 -1 0) (5 0 5))))
--> T
```

The single argument to this function consists of  $n$  lists of lists (of varying length). If any one of these lists is empty then the value T is returned. Otherwise the value NIL is returned. Note that a null argument gives the output NIL.

### set-difference-multidimensional-sorted-asc

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	test-equal<list-elements
Called by	
Comments/see also	

Example:

```
(set-difference-multidimensional-sorted-asc
 '((-1 1) (0 1) (1 1) (2 3) (4 -4) (4 3))
```

```
'((-1 1) (0 1) (2 3) (3 2) (4 3)))
--> ((1 1) (4 -4))
```

This function computes the set difference  $A \setminus B = \{a \in A \mid a \notin B\}$  for point sets.

### sort-dataset-asc

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	union-multidimensional-sorted-asc
Called by	union-multidimensional-sorted-asc, unions-multidimensional-sorted-asc
Comments/see also	Deprecated.

Example:

```
(sort-dataset-asc
 '((1 1) (0 1) (4 4) (0 1) (1 1) (-2 3) (4 4) (4 3)))
--> ((-2 3) (0 1) (0 1) (1 1)
      (1 1) (4 3) (4 4) (4 4))
```

This function takes one argument: a dataset. It sorts the dataset ascending by each dimension in turn. By the definition of *dataset*, the dataset should not contain repeated values. If it does these will be removed.

### subset-multidimensional

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	test-equal<list-elements
Called by	subset-score-of-pattern
Comments/see also	

Example:

```
(subset-multidimensional
 '((2 56) (6 60)) '((0 62) (2 56) (6 60) (6 72)))
--> T
```

This function returns T if and only if the first argument is a subset of the second, and it is assumed that the second list is sorted ascending.

**subtract-list-from-each-list**

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	subtract-two-lists
Called by	translators-of-pattern-in-dataset
Comments/see also	subtract-list-from-each-list-mod-2nd-n

Example:

```
(subtract-list-from-each-list
 '( (8 -2 -3) (4 6 6) (0 0 0) (4 7 -3)) '(4 7 -3))
--> ((4 -9 0) (0 -1 9) (-4 -7 3) (0 0 0))
```

The function `subtract-two-lists` is applied recursively to each sublist in the first list argument, and the second argument.

**subtract-two-lists**

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	
Called by	subtract-list-from-each-list, test-translation-no-length-check
Comments/see also	subtract-two-lists-mod-2nd-n

Example:

```
(subtract-two-lists '(4 7 -3) '(8 -2 -3))
--> (-4 9 0)
```

Subtracts the second list from the first, element-by-element. It is assumed that elements of list arguments are numbers, and the list arguments are of the same length. An empty first (but not second) argument will be tolerated.

**test-equal<list-elements**

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	
Called by	intersection-multidimensional, set-difference-multidimensional-sorted-asc
Comments/see also	

Example:

```
(test-equal<list-elements
  '((0 1) (0 2) (1 1) (3 1/4)) '(1 1))
--> T
```

The first argument is a list of sublists, assumed to be sorted ascending by each of its elements in turn. We imagine it as a set of vectors (all members of the same  $n$ -dimensional vector space). The second argument  $\mathbf{v}$  (another list) is also an  $n$ -dimensional vector. If  $v_1$  is less than  $v_2$ , the first element of the first element of the first argument then NIL is returned, since we know the list is sorted ascending. Otherwise each item is checked for equality.

### test-equal<potential-translator

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	add-two-lists
Called by	check-potential-translators
Comments/see also	test-equal<potential-translator-mod-2nd-n

Example:

```
(test-equal<potential-translator
  '((0 1) (0 2) (1 2) (3 1/4)) '(0 1) '(1 1))
--> ((1 1))
```

This function is very similar in spirit to test-equal<list-elements. The first argument here is a dataset, the second is a member of some pattern (so also a member of the dataset), and the third is a potential translator of the patternpoint. If the potential translator is really a translator, it is returned, and NIL otherwise.

### test-translation

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	test-translation-no-length-check
Called by	check-potential-translators
Comments/see also	test-translation-mod-2nd-n

Example:

```
(test-translation
  '((2 2) (4 5)) '((11 6) (13 9)))
--> T
```

If the first argument to this function, a list, consists of vectors of uniform dimension that are the pairwise translation of vectors in another list (the function's second argument), then T is returned, and nil otherwise. The length of the vectors is checked first for equality, then passed to the function `test-translation-no-length-check` if equal.

### test-translation-no-length-check

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	subtract-two-lists
Called by	test-translation
Comments/see also	test-translation-mod-2nd-n-no-length-check

Example:

```
(test-translation-no-length-check
  '((2 2) (4 5)) '((11 6) (13 9)))
--> T
```

If the first argument to this function, a list, consists of vectors of uniform dimension that are the pairwise translation of vectors in another list (the function's second argument), then T is returned, and nil otherwise. The length of the vectors is not checked for equality. (At present the function returns T if two empty lists are provided as arguments.)

### translation

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	add-two-lists
Called by	translational-equivalence-class
Comments/see also	translation-mod-2nd-n

Example:

```
(translation '((8 -2 -3) (4 6 6) (4 7 -3)) '(3 1 0))
--> ((11 -1 -3) (7 7 6) (7 8 -3))
```

The first argument is a list of sublists, but we imagine it as a set of vectors (all members of the same  $n$ -dimensional vector space). The second argument—another list—is also an  $n$ -dimensional vector, and this is added to each of the members of the first argument. ‘Added’ means vector addition, that is element-wise, so the resulting set is a translation of the first argument by the second.

## translation

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	add-two-lists
Called by	translational-equivalence-class
Comments/see also	translation-mod-2nd-n

Example:

```
(translation '((8 -2 -3) (4 6 6) (4 7 -3)) '(3 1 0))
--> ((11 -1 -3) (7 7 6) (7 8 -3))
```

The first argument is a list of sublists, but we imagine it as a set of vectors (all members of the same  $n$ -dimensional vector space). The second argument—another list—is also an  $n$ -dimensional vector, and this is added to each of the members of the first argument. ‘Added’ means vector addition, that is element-wise, so the resulting set is a translation of the first argument by the second.

## translational-equivalence-class

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	translation
Called by	
Comments/see also	

Example:

```
(translational-equivalence-class
 '( (6 2) (7 1/2) (15/2 1/4) (31/4 1/4) (8 1) (9 1) )
 '( (0 1) (0 4/3) (0 2) (1 1) (4/3 1/3) (5/3 1/3)
   (2 1/2) (2 1) (5/2 1/2) (3 1/2) (3 2) (7/2 1/2) )
```

```

(4 1/2) (4 1) (9/2 1/2) (5 1) (6 1) (6 2)
(7 1/2) (7 1) (15/2 1/4) (31/4 1/4) (8 1) (9 1)
(9 2) (10 1/2) (10 1) (21/2 1/4) (43/4 1/4)
(11 1) (12 1) (12 2) (13 1/2) (13 2) (27/2 1/4)
(55/4 1/4) (14 1) (14 2) (15 1) (16 1/3) (16 2)
(49/3 1/3) (50/3 1/3) (17 1)))
--> (((6 2) (7 1/2) (15/2 1/4)
      (31/4 1/4) (8 1) (9 1))
      ((9 2) (10 1/2) (21/2 1/4)
      (43/4 1/4) (11 1) (12 1))
      ((12 2) (13 1/2) (27/2 1/4)
      (55/4 1/4) (14 1) (15 1)))

```

The function takes two arguments: a pattern  $P$  and a dataset  $D$ . It returns the translational equivalence class of  $P$  in  $D$ .

## translations

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	translation
Called by	
Comments/see also	translations-mod-2nd-n

Example:

```

(translations
 '((1 2) (2 4)) '((0 0) (1 2)))
--> (((1 2) (2 4)) ((2 4) (3 6)))

```

There are two arguments to this function, a pattern and some translators. The pattern is translated by each translator and the results returned.

## translators-of-pattern-in-dataset

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	check-potential-translators, subtract-list-from-each-list
Called by	translational-equivalence-class
Comments/see also	Should be deprecated by implementing the version in Ukkonen, Lemström, and Mäkinen (2003). See also translators-of-pattern-in- dataset-mod-2nd-n.

Example:

```
(translators-of-pattern-in-dataset
'((8 3) (8 7))
'((4 7) (8 -3) (8 3) (8 7) (9 -3) (10 7) (11 -3)
(13 -3) (13 1)))
--> ((0 0) (5 -6))
```

A pattern and dataset are provided. The translators of the pattern in the dataset are returned.

## union-multidimensional-sorted-asc

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	insert-retaining-sorted-asc, sort-dataset-asc
Called by	sort-dataset-asc, union-multidimensional- sorted-asc
Comments/see also	

Example:

```
(union-multidimensional-sorted-asc
'((-5 0 4) (-4 3 1) (8 5 3) (8 6 0))
'((-4 3 1) (-6 2 2) (8 5 0) (8 6 0))
T)
--> ((-6 2 2) (-5 0 4) (-4 3 1) (8 5 0)
(8 5 3) (8 6 0))
```



Two lists of (real) vectors of the same dimension are supplied to this function. If the first is sorted strictly ascending already, a third argument of T should be supplied to prevent it being sorted so. The union of these lists is output and remains strictly ascending.

### unions-multidimensional-sorted-asc

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	sort-dataset-asc, union-multidimensional-sorted-asc
Called by	
Comments/see also	

Example:

```
(unions-multidimensional-sorted-asc
 '( ((12 10) (0 0) (1 2)) ((0 0) (1 5)) ((6 6))) )
--> ((0 0) (1 2) (1 5) (6 6) (12 10))
```

The function union-multidimensional-sorted- asc is applied recursively to a list of  $k$ -dimensional vector sets.

### vector<vector

Started, last checked	13/1/2010, 13/1/2010
Location	Set operations
Calls	
Called by	insert-retaining-sorted-asc
Comments/see also	

Example:

```
(vector<vector '(4 6 7) '(4 6 7.1))
--> T
```

For  $\mathbf{d} = (d_1, d_2, \dots, d_k)$ ,  $\mathbf{e} = (e_1, e_2, \dots, e_k)$ , we say that  $\mathbf{d}$  is less than  $\mathbf{e}$ , denoted  $\mathbf{d} \prec \mathbf{e}$ , if and only if there exists an integer  $1 \leq j \leq k$  such that  $d_j < e_j$ , and  $d_i = e_i$  for  $1 \leq i < j$ . This function returns true if its first argument is 'less than' its second argument, "equal" if the two arguments are equal, and nil otherwise.

### 4.1.3 Sort by

These functions culminate in the function `sort-by`, and were written when I was new to Lisp. As such, there are faster, more robust, in-built alternatives for some of the functions.

#### **break-fixed-with-sort-by-col**

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	lastn, rows-with-fixed-same-as-1st-row, sort-by-col
Called by	sort-by
Comments/see also	

Example:

```
(break-fixed-with-sort-by-col '(1 2)
  '((3 4 0 0) (3 4 5 2) (0 4 5 -3)
    (-1 4 5 9) (1 3 6 1) (-1 2 7 0))
  3 "desc")
--> '((3 4 0 0) (-1 4 5 9) (3 4 5 2)
      (0 4 5 -3) (1 3 6 1) (-1 2 7 0))
```

This function has as its second argument a list whose items are themselves lists of `m` items, and it is assumed that this list has already been sorted by certain 'columns' (ascending or descending) specified in the first argument; a list called `fixed`. In these specified 'columns', any ties which persist between consecutive 'rows' are (potentially) broken, with a sort by the argument `col` (default direction is ascending).

We see in the example above that a sort has already been conducted by 'columns' one and two, hence the argument `fixed` is `'(1 2)`. The function breaks the specified ties in the given list with a descending sort by column three.

#### **index-item-1st-doesnt-occur**

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	
Called by	
Comments/see also	index-item-1st-occurs

Example:

```
(index-item-1st-doesnt-occur 0 '(0 0 0 -2 4 2))
--> 3
```

Taking an item and a list of items as its arguments, this function returns the index at which the given item first does not occur, counting from zero. If the list is constant and equal to the item then the function returns NIL.

### index-equalps-for-pair-list

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	
Called by	nos-consecutives-with-nonempty-fixed
Comments/see also	

Example:

```
(index-equalps-for-pair-list
 '(1 3 4) '((1 7 9 2 1 1) (0 7 9 9 1 0)))
--> (T NIL T)
```

This function looks for equality (using the function equalp) in a pair of lists at those indices specified by a second variable index.

### max-argmax

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	
Called by	sort-by-col-desc, sort-items-desc
Comments/see also	min-argmin

Example:

```
(max-argmax '(2 4 -2 7/2 4))
--> (4 1)
```

This function returns the maximum item in a nonempty list (assuming all items are of the same type), as well as the index of that maximum item, counting from zero.

**max-item**

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	
Called by	
Comments/see also	min-item

Example:

```
(max-item '(2/3 -3 15 2))
--> 15
```

This function finds the maximum item in a nonempty list. It assumes all items are of the same type; otherwise nonsense output can be produced.

**max-nth**

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	
Called by	max-nth-argmax
Comments/see also	min-nth

Example:

```
(max-nth 0 '((0 3 10) (1 5 2) (0 4 9)))
--> (1 5 2)
```

This function returns the maximum item in a list where all items are themselves lists of  $m$  items. In order to find the maximum therefore, it is necessary to specify the ‘column’ (counting from zero) by which the search ought to be conducted.

**max-nth-argmax**

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	index-item-1st-occurs, max-nth
Called by	
Comments/see also	min-nth-argmin

Example:

```
(max-nth-argmax 2 '((0 3 2) (0 4 8) (0 5 -2) (9 9 2)))
--> ((0 4 8) 1)
```

Here we return the maximum item in a list where all items are themselves lists of  $m$  items, searching by the  $n$ th ‘column’ counting from zero. Also returned is the index of the maximum item.

### min-argmin

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	index-item-1st-occurs, min-item
Called by	sort-by-col-asc, sort-items-asc
Comments/see also	max-argmax

Example:

```
(min-argmin '(0 4 -2 7/2 -2))
--> (-2 2)
```

This function returns the minimum item in a nonempty list (assuming all items are of the same type), as well as the index of that minimum item, counting from zero.

### min-item

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	
Called by	min-argmin
Comments/see also	max-item

Example:

```
(min-item '(2/3 -3 15 2))
--> -3
```

This function finds the minimum item in a nonempty list. It assumes all items are of the same type; otherwise nonsense output can be produced.

**min-nth**

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	
Called by	min-nth-argmin
Comments/see also	max-nth

Example:

```
(min-nth 2 '((0 3 10) (1 5 7) (0 4 9)))
--> (1 5 7)
```

This function returns the minimum item in a list where all items are themselves lists of  $m$  items. In order to find the minimum therefore, it is necessary to specify the ‘column’ (counting from zero) by which the search ought to be conducted.

**min-nth-argmin**

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	index-item-1st-occurs, min-nth
Called by	
Comments/see also	max-nth-argmax

Example:

```
(min-nth-argmin 1 '((0 3 2) (0 5 -2) (0 0 8) (9 9 2)))
--> ((0 0 8) 2)
```

Here we return the minimum item in a list where all items are themselves lists of  $m$  items, searching by the  $n$ th ‘column’ counting from zero. Also returned is the index of the minimum item.

**nos-consecutives-with-fixed**

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	nos-consecutives-with-nonempty-fixed
Called by	rows-with-fixed-same-as-1st-row
Comments/see also	

Example:

```
(nos-consecutives-with-fixed
 '(1 3)
 '((7 4 0 2 1) (1 4 -1 2 -9) (3 4 4 1 1)
   (2 -5 0 3 -9) (2 4 5 2 -2) (3 4 4 2 1)
   (1 1 1 1 1)))
--> 2
```

Suppose that the items indexed by  $I = (i_1, i_2, \dots, i_m)$  in a list are  $x_1, x_2, \dots, x_m$ , and that this is the case for several such lists, appearing as the first  $n$  entries in some list of lists. Then this function will return the value  $n$ . If index is empty, then the length of the list is returned. This has a bearing on higher-level functions.

### **nos-consecutives-with-nonempty-fixed**

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	firstn, index-equals-for-pair-list, test-all-true
Called by	nos-consecutives-with-fixed
Comments/see also	

Example:

```
(nos-consecutives-with-nonempty-fixed
 '(1 3)
 '((7 4 0 2 1) (1 4 -1 2 -9) (3 4 4 2 1)
   (2 -5 0 2 -9) (2 4 5 2 -2) (3 4 4 2 1)
   (1 1 1 1 1)))
--> 2
```

Here the function assumes a nonempty  $I = (i_1, i_2, \dots, i_m)$ , indexing items  $x_1, x_2, \dots, x_m$  in some list. This is supposed to be the case for several such lists, appearing as the first  $n$  entries in some list of lists. This function will return the value  $n$ . It may seem unnecessary to have both the functions `nos-consecutives-with-fixed` and `nos-consecutives-with-nonempty-fixed`, but writing the two as a single function results in a less efficient algorithm.

**rows-with-fixed-same-as-1st-row**

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	firstn, nos-consecutives-with-fixed
Called by	break-fixed-with-sort-by-col
Comments/see also	

Example:

```
(rows-with-fixed-same-as-1st-row
 '(1 3)
 '((7 4 0 2 1) (1 4 -1 2 -9) (3 4 4 1 1)
   (2 -5 0 3 -9) (2 4 5 2 -2) (3 4 4 2 1)
   (1 1 1 1 1)))
--> ((7 4 0 2 1) (1 4 -1 2 -9))
```

Suppose that the  $i_1$ th,  $i_2$ th, ...,  $i_m$ th items in a list are  $x_1, x_2, \dots, x_m$ , and that this is the case for several such lists appearing as the first  $n$  entries in some list of lists. Then this function will return those first  $n$  entries.

**sort-by**

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	break-fixed-with-sort-by-col
Called by	
Comments/see also	

Example:

```
(sort-by
 '((5 "asc") (0 "asc") (1 "asc") (3 "desc")))
 '((1000 41 500 1 84 1500) (1000 36 500 1 84 1500)
   (1000 41 500 2 84 1500) (0 60 1000 1 84 1000)
   (2500 61 500 1 84 3000) (3000 62 1000 1 84 4000)
   (1500 60 1500 1 84 3000)))
--> ((0 60 1000 1 84 1000) (1000 36 500 1 84 1500)
   (1000 41 500 2 84 1500) (1000 41 500 1 84 1500)
   (1500 60 1500 1 84 3000) (2500 61 500 1 84 3000)
   (3000 62 1000 1 84 4000))
```



This code sorts a list of items (where each item is itself a list of  $m$  items). It does so according to an index (of arbitrary length) consisting of ‘column’ numbers and the direction in which each column ought to be sorted. If for example, (0 "asc") appears before (3 "desc") in the index, then the list is sorted first by ‘column’ 0 ascending. And then any ties which emerge might be broken by sorting among tied sets according to ‘column’ 3 descending.

### sort-by-col

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	sort-by-col-asc, sort-by-col-desc
Called by	break-fixed-with-sort-by-col
Comments/see also	

Example:

```
(sort-by-col
 2 '((3 -2 5 0) (4 1 -8 1) (4 1 0 -2) (3 0 0 -1))
"desc")
--> ((3 -2 5 0) (4 1 0 -2) (3 0 0 -1) (4 1 -8 1))
(sort-by-col
 2 '((3 -2 5 0) (4 1 -8 1) (4 1 0 -2) (3 0 0 -1)))
--> ((4 1 -8 1) (4 1 0 -2) (3 0 0 -1) (3 -2 5 0))
```

This code sorts a list of items (where each item is itself a list of  $m$  items) in a specified direction (e.g. ‘desc’). If this direction is not provided, the function sorts in an ascending order. It assumes all items are of the same type; otherwise nonsense output can be produced.

### sort-by-col-asc

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	min-nth-argmin, remove-nth
Called by	sort-by-col
Comments/see also	

Example:

```
(sort-by-col-asc
```

```
2 '((3 -2 5 0) (4 1 -8 1) (4 1 0 -2) (3 0 0 -1)))
--> ((4 1 -8 1) (4 1 0 -2) (3 0 0 -1) (3 -2 5 0))
```

This function returns a list (where each item is itself a list of  $m$  items) which is ordered ascending by a particular ‘column’. It assumes all items are of the same type; otherwise nonsense output can be produced.

### sort-by-col-desc

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	max-nth-argmax, remove-nth
Called by	sort-by-col
Comments/see also	

Example:

```
(sort-by-col-desc
 2 '((3 -2 -5 0) (4 1 8 1) (4 1 0 -2) (3 0 0 -1)))
--> ((4 1 8 1) (4 1 0 -2) (3 0 0 -1) (3 -2 -5 0))
```

This function returns a list (where each item is itself a list of  $m$  items) which is ordered descending by a particular ‘column’. It assumes all items are of the same type; otherwise nonsense output can be produced.

### sort-items

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	
Called by	
Comments/see also	Non-destructive use of built-in function called sort.

Example:

```
(sort-items '(8 2 5 0 -6 2) "desc")
--> (8 5 2 2 0 -6)
(sort-items '(8 2 5 0 -6 2))
--> (-6 0 2 2 5 8)
```

This code sorts a list of items (non- destructively) in a specified direction (e.g. 'desc'). If this direction is not provided, the function sorts in an ascending order. It assumes all items are of the same type; otherwise nonsense output can be produced.

### sort-items-asc

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	
Called by	
Comments/see also	Deprecated.

Example:

```
(sort-items-asc '(0 2 4 6 -1 2))
--> (-1 0 2 2 4 6)
```

This code sorts a list of items (non- destructively) in ascending order. It assumes all items are of the same type; otherwise nonsense output can be produced.

### sort-items-desc

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	
Called by	
Comments/see also	Deprecated.

Example:

```
(sort-items-desc '(0 2 4 6 -1 2))
--> (6 4 2 2 0 -1)
```

This code sorts a list of items (non- destructively) in descending order. It assumes all items are of the same type; otherwise nonsense output can be produced.

**test-all-true**

Started, last checked	8/8/2008, 8/8/2008
Location	Sort by
Calls	
Called by	nos-consecutives-with-nonempty-fixed
Comments/see also	

Example:

```
(test-all-true '(T NIL T T NIL))
--> NIL
```

This code tests whether all of the items in a list (of Ts and NILs) are in fact Ts.

**4.1.4 Vector operations**

These functions allow common vector operations, such as taking norms, calculating dot products and distance functions.

**fibonacci-list**

Started, last checked	29/1/2010, 29/1/2010
Location	Vector operations
Calls	
Called by	
Comments/see also	

Example:

```
(fibonacci-list '(0 1 2 4 8))
-->
'(0 1 3 7 15).
```

The  $n$ th element of the list returned is the sum of the previous  $n - 1$  elements, with the convention that a sum over an empty set is zero.

**multiply-two-lists**

Started, last checked	29/1/2010, 29/1/2010
Location	Vector operations
Calls	
Called by	
Comments/see also	

Example:

```
(multiply-two-lists '(4 7 -3) '(8 -2 -3))
--> (32 -14 9).
```

Multiplies two lists element-by-element. It is assumed that elements of list arguments are numbers, and the list arguments are of the same length. An empty first (but not second) argument will be tolerated.

**normalise-0-1**

Started, last checked	29/1/2010, 29/1/2010
Location	Vector operations
Calls	normalise-0-1-checks-done
Called by	
Comments/see also	

Example:

```
(normalise-0-1 '(4 7 -3 2))
--> (7/10 1 0 1/2).
```

Normalises data (linearly) to  $[0, 1]$ .

**normalise-0-1-checks-done**

Started, last checked	29/1/2010, 29/1/2010
Location	Vector operations
Calls	
Called by	normalise-0-1
Comments/see also	

Example:

```
(normalise-0-1-checks-done '(4 7 -3 2))
--> (7/10 1 0 1/2).
```

Normalises data (linearly) to  $[0, 1]$ , assuming that the data is not constant and that the min and max are not already 0, 1 respectively.

### 4.1.5 Stats sampling

The functions below are for finding summary statistics, and for taking random samples from data.

#### **choose-one**

Started, last checked	6/10/2010, 6/10/2010
Location	Vector operations
Calls	
Called by	
Comments/see also	

Example:

```
(choose-one '(1 2 4))
--> 4
```

A random, equiprobable choice is made between elements of a list.

#### **mean**

Started, last checked	6/10/2010, 6/10/2010
Location	Vector operations
Calls	fibonacci-list, my-last
Called by	
Comments/see also	

Example:

```
(mean '(6 7 4))
--> 17/3
```

The mean of a list of numbers is returned.

**random-permutation**

Started, last checked	6/10/2010, 6/10/2010
Location	Vector operations
Calls	nth-list, sample-integers-no-replacement
Called by	
Comments/see also	

Example:

```
(random-permutation '("A" "B" "C" "D" "E"))
--> ("C" "A" "E" "D" "B")
```

The output of this function is a random permutation of an input list.

**range**

Started, last checked	6/10/2010, 6/10/2010
Location	Stats sampling
Calls	max-item, min-item
Called by	pitch-range
Comments/see also	

Example:

```
(range '(60 61 62))
--> 2
```

Range is the maximum member of a list, minus the minimum member.

**sample-integers-no-replacement**

Started, last checked	6/10/2010, 6/10/2010
Location	Vector operations
Calls	add-to-list, choose-one first-n-naturals
Called by	random-permutation
Comments/see also	

Example:

```
(sample-integers-no-replacement 10 7)
--> (5 4 8 2 0 3 9)
```

The first argument to this function,  $n$ , is an integer, as is the second  $m \leq n$ . The output is a random sample (without replacement) from the integers  $0, \dots, n-1$  of size  $m$ . If  $m > n$ , we set  $m = n$ .

## sd

Started, last checked	6/10/2010, 6/10/2010
Location	Stats sampling
Calls	fibonacci-list, mean, my-last
Called by	rhythmic-variability
Comments/see also	

Example:

```
(sd '(64 55 65 55 72 55 55 55 60 59 67))
--> 5.7178855
```

The standard deviation of the sample (using a denominator of  $n$ , where  $n$  is the sample size).

## 4.1.6 Geometric operations

The functions below are for finding summary statistics, and for taking random samples from data.

### convex-hull

Started, last checked	11/5/2010, 11/5/2010
Location	Geometric operations
Calls	
Called by	
Comments/see also	

Example:

```
(setq a-list '((-4 4) (-2 -2) (-2 2) (0 0) (1 1)
               (2 -2) (2 4) (6 2)))
(convex-hull a-list)
--> ((-2 -2) (2 -2) (6 2) (2 4) (-4 4))
```



For a set of points in the plane, this function returns those points that lie on the convex hull, using the Graham scan algorithm. Passing an empty set of points to this function will result in an error.

### counter-clockwise

Started, last checked	11/5/2010, 11/5/2010
Location	Geometric operations
Calls	
Called by	convex-hull
Comments/see also	

Example:

```
(counter-clockwise '((-2 -2) (2 -2) (1 1)))
--> -1
```

This function takes three points in the plane as its argument,  $p_1, p_2$ , and  $p_3$ , arranged in a single list. If travelling along the line from  $p_1$  to  $p_2$ , turning next to  $p_3$  means turning counter-clockwise, then 1 is the value returned. If clockwise then  $-1$  is returned, and if collinear then 0 is returned.

### dot-adjacent-points

Started, last checked	11/5/2010, 11/5/2010
Location	Geometric operations
Calls	
Called by	in-polygon
Comments/see also	

Example:

```
(dot-adjacent-points
 '((-1 -3) (1 1) (-2 -1) (-1 -3)))
--> (-4 -3 5)
```

This function takes adjacent pairs from the argument list and computes their dot product.

**in-polygonp**

Started, last checked	11/5/2010, 11/5/2010
Location	Geometric operations
Calls	dot-adjacent-points, fibonacci-list, multiply-list-by-constant, multiply-two-lists, my-last, quadrant-number, signum-adjacent-determinants, spacing-items, substitute-index-by-index-abs-x, translation
Called by	points-in-convex-hull
Comments/see also	

Example:

```
(setq closed-vertices
      '((-2 -2) (2 -2) (6 2) (2 4) (-4 4) (-2 -2)))
(in-polygonp '(1 1) closed-vertices)
--> T
```

A point in the plane and a list of closed, adjacent vertices are supplied as arguments. T is returned if the point is inside or on the polygon, and nil otherwise.

**min-y-coord**

Started, last checked	11/5/2010, 11/5/2010
Location	Geometric operations
Calls	
Called by	convex-hull
Comments/see also	

Example:

```
(min-y-coord '((-4 4) (-2 -2) (-2 2) (2 -2) (6 2)))
--> (-2 -2)
```

This function returns the point with the minimum  $y$ -coordinate, where the argument is assumed to be in the form  $((x_1, y_1), (x_2, y_2), \dots, (x_n, y_n))$ . Ties are broken using the  $x$ -coordinate.

**points-in-convex-hull**

Started, last checked	11/5/2010, 11/5/2010
Location	Geometric operations
Calls	
Called by	
Comments/see also	

Example:

```
(points-in-convex-hull
 '((-1.71 -1.13) (1.27 -3.95) (3.66 -2.05)
   (-2.65 -3.48) (1.4 -2.94) (1.53 0.51) (-2.67 0.32))
 '((-1.33 0.3) (-1.3 -4.0) (0.83 1.41) (1.83 2.89)
   (1.85 -0.94) (2.22 -2.93) (2.34 2.81) (2.4 -0.15)
   (2.49 -2.71)))
--> ((-1.33 0.3) (1.85 -0.94) (2.22 -2.93)
      (2.49 -2.71))
```

This function takes two sets of points in the plane as its arguments. The convex hull is found for the first set. It is then determined for each member of the second set whether or not that member is inside (or on) the convex hull or not. The points in the convex hull are returned. There is a plot for the above example in the *Example files* folder, entitled *convex-hull.pdf*.

**quadrant-number**

Started, last checked	11/5/2010, 11/5/2010
Location	Geometric operations
Calls	
Called by	in-polygonp
Comments/see also	

Example:

```
(quadrant-number '(-4 4))
--> 2
```

This function returns the quadrant number of the plane point  $(x, y)$  supplied as argument.

**signum-adjacent-determinants**

Started, last checked	11/5/2010, 11/5/2010
Location	Geometric operations
Calls	
Called by	in-polygonp
Comments/see also	

Example:

```
(signum-adjacent-determinants
 '((-1 -3) (1 1) (-2 -1) (-1 -3)))
--> (1 1 1)
```

This function takes adjacent pairs from the argument list and computes the sign of the determinant, as though the pairs were in a  $2 \times 2$  matrix.

**spacing-items**

Started, last checked	11/5/2010, 11/5/2010
Location	Geometric operations
Calls	
Called by	in-polygonp
Comments/see also	

Example:

```
(spacing-items '(0 12 1 7 4))
--> '(12 -11 6 -3)
```

A list of numbers is the only argument. The intervals between adjacent numbers are returned. It is possible to produce nonsense output if null values are interspersed with non-null values.

**substitute-index-by-index-abs-x**

Started, last checked	11/5/2010, 11/5/2010
Location	Geometric operations
Calls	
Called by	in-polygonp
Comments/see also	

Example:

```
(substitute-index-by-index-abs-x
 '(-4 4 -2 2 6 2) '(3 5 10 12 7 13) 2)
--> (-4 4 10 12 6 13)
```

This function is very specific. When the absolute value of the  $i$ th item of the first argument is equal to the third argument, that item is replaced in the output with the  $i$ th item of the second argument.

### 4.1.7 Interpolation

These functions are for interpolating step functions given by pairs of  $x$ - and  $y$ -values at specified values.

#### abs-differences-for-curves-at-points

Started, last checked	1/10/2010, 1/10/2010
Location	Interpolation
Calls	linearly-interpolate
Called by	
Comments/see also	

Example:

```
(setq knot-value-pairs1 '((0 0) (1.5 1) (2 3) (4 2)))
(setq knot-value-pairs2 '((0 0) (1 1) (2 3) (4 3)))
(abs-differences-for-curves-at-points
 knot-value-pairs1 knot-value-pairs2)
--> (0 1.0 0 1)
```

Two lists of knot-value pairs are provided as arguments. The  $x$ -values of the first argument are interpolated using the second argument. The absolute difference between these interpolated values and the actual  $y$ -values of the first argument is returned.

#### index-1st-sublist-item<

Started, last checked	1/10/2010, 1/10/2010
Location	Interpolation
Calls	
Called by	
Comments/see also	

Example:

```
(index-1st-sublist-item<
 0 '(14 14 14 11 0 0 -1 -2 -2))
--> 6
```

This function takes two arguments: a real number  $x$  and a list  $L$  of real numbers. It returns the index of the first element of  $L$  which is less than  $x$ .

### **index-1st-sublist-item>**

Started, last checked	1/10/2010, 1/10/2010
Location	Interpolation
Calls	
Called by	linearly-interpolate
Comments/see also	

Example:

```
(index-1st-sublist-item>
 0 '(-2 -2 -1 0 0 11 14 14 14))
--> 5
```

This function takes two arguments: a real number  $x$  and a list  $L$  of real numbers. It returns the index of the first element of  $L$  which is greater than  $x$ .

### **linearly-interpolate**

Started, last checked	1/10/2010, 1/10/2010
Location	Interpolation
Calls	index-1st-sublist-item>, my-last, nth-list-of-lists
Called by	abs-differences-for-curves-at-points, linearly- interpolate-x-values
Comments/see also	

Example:

```
(setq knot-value-pairs '((0 0) (1 1) (2 3) (4 3)))
(linearly-interpolate 1.5 knot-value-pairs)
--> 2.0
```

The second argument is a list of knot-value pairs. The  $x$ -value of the first argument is interpolated to give a  $y$ -value using the knot-value pairs. If the first argument exceeds the endpoints, the appropriate endpoint value is returned.

### linearly-interpolate-x-values

Started, last checked	1/10/2010, 1/10/2010
Location	Interpolation
Calls	linearly-interpolate
Called by	
Comments/see also	

Example:

```
(setq knot-value-pairs '((0 0) (1 1) (2 3) (4 3)))
(linearly-interpolate-x-values
 '(1.5 2 1.75) knot-value-pairs)
--> (2.0 3 2.5)
```

The second argument is a list of knot-value pairs. The first argument is a list of  $x$ -values that are interpolated to give  $y$ -values using the knot-value pairs. If any members of the first argument exceeds the endpoints, the appropriate endpoint value is returned.

## 4.2 File conversion

### 4.2.1 Text files

The functions below will export a list to a text file, and import such text into the Lisp environment as lists.

#### read-from-file

Started, last checked	15/1/2010, 15/1/2010
Location	Text files
Calls	
Called by	
Comments/see also	

Example:

```
(read-from-file
  (concatenate
    'string
    *MCStylistic-Oct2010-example-files-path*
    "/short-list.txt"))
--> ((9 23 1 19) (14 9 14 5 20 25) (16 5 18 3 5 14 20)
      ("sure" 9 4) (13 9 19 8 5 1 18 4) (8 5 18))
```

This function returns the contents of a file specified by the variable path&name. It returns each row of the file as a list, in a list of lists.

### read-from-file-arbitrary

Started, last checked	15/1/2010, 15/1/2010
Location	Text files
Calls	
Called by	
Comments/see also	

Example:

```
(read-from-file-arbitrary
  (concatenate
    'string
    *MCStylistic-Oct2010-example-files-path*
    "/short-list 2.txt"))
--> ("first line consisting of anything"
      "sure 9 4" "second line consisting of &~%$")
```

This function is similar to the function read-from-file. The difference is that read-from-file- arbitrary will parse any file, converting each line to a string for further processing.

### update-written-file

Started, last checked	15/1/2010, 15/1/2010
Location	Text files
Calls	read-from-file, write-to-file
Called by	
Comments/see also	

Example:



```

(read-from-file
  (concatenate
    'string
    *MCStylistic-Oct2010-example-files-path*
    "/short-list 3.txt"))
--> (((0 7) (0 60) (2 63))
      ((2 2) (2 72))
      ((3 -1) (0 60) (3 67))
      ((6 0) (3 67) (5 66)))
(update-written-file
  (concatenate
    'string
    *MCStylistic-Oct2010-example-files-path*
    "/short-list")
  3 '(6 60) '((2 2) . ((2 72))))
--> T
(read-from-file
  (concatenate
    'string
    *MCStylistic-Oct2010-example-files-path*
    "/short-list 3.txt"))
--> (((0 7) . ((0 60) (2 63)))
      ((2 2) . ((2 72) (6 60)))
      ((3 -1) . ((0 60) (3 67)))
      ((6 0) . ((3 67) (5 66))))

```

This function updates the contents of a specified file by removing the row associated with the variable `updatee`, and replacing it with `updater` appended within `updatee`. It should overwrite the existing file. The position of the row is preserved.

### write-to-file

Started, last checked	15/1/2010, 15/1/2010
Location	Text files
Calls	
Called by	update-written-file
Comments/see also	

Example:

```
(write-to-file
```

```
'(5 7 8 "hello" 9)
(concatenate
 'string
 *MCStylistic-Oct2010-example-files-path*
 "/short-list 4.txt"))
--> T
```

This function writes the data provided in the first list to a file with the path and name provided in the second list. The s in the format argument is essential for retaining strings as they appear in the data.

### **write-to-file-append**

Started, last checked	15/1/2010, 15/1/2010
Location	Text files
Calls	
Called by	
Comments/see also	

Example:

```
(write-to-file-append
 '(10 "goodbye")
 (concatenate
 'string
 *MCStylistic-Oct2010-example-files-path*
 "/short-list 4.txt"))
--> T
```

The only difference between this and the function write-to-file is that an existing file will be opened and new data appended, rather than overwritten.

### **write-to-file-supersede**

Started, last checked	15/1/2010, 15/1/2010
Location	Text files
Calls	write-to-file
Called by	
Comments/see also	

Example:

```

(write-to-file
  '(5 7 8 "hello" 9)
  (concatenate
    'string
    *MCStylistic-Oct2010-example-files-path*
    "/short-list 5.txt"))
--> T
(write-to-file-supersede
  '(10 "goodbye")
  (concatenate
    'string
    *MCStylistic-Oct2010-example-files-path*
    "/short-list 5.txt"))
--> T

```

The only difference between this and the function `write-to-file` is that an existing file will be superseded, rather than overwritten.

### write-to-file-with-open-file

Started, last checked	15/1/2010, 15/1/2010
Location	Text files
Calls	
Called by	
Comments/see also	

Example:

```

(write-to-file-with-open-file
  "hello"
  (concatenate
    'string
    *MCStylistic-Oct2010-example-files-path*
    "/New folder/short-list.txt"))
--> T

```

There was a problem with the function `write-to-file` in Emacs, because it would not export to a directory that did not already exist. This was remedied using the functions `with-open-file` and `ensure-directories-exist`. However, this function only works with a single (i.e. non-list) variable. Once you have used it to create the directory, use the function `write-to-file` as per usual.

### 4.2.2 MIDI import

The main function here is `load-midi-file`, for importing a MIDI (Musical Instrument Digital Interface) file into the Lisp environment as a list of lists.

#### **add-tempo**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	
Comments/see also	Deprecated.

Example:

```
(add-tempo '(5012 5012 5012))
--> 2
```

As tempo and granularity are needed to convert ticks to ms, this function is invoked when the number 81 is parsed (which indicates a tempo change). The format of each entry here is (time-in-ticks time-in-ms usec/qn). Storing the time of the tempo change in both formats simplifies the calculations.

#### **convert-granularity**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	get-header
Comments/see also	

Example: within `get-header` example,

```
(convert-granularity (get-short input-stream))
--> 120
```

The treatment of division is unusual. Granularity is in ticks per beat (crotchet).

**convert-vlq**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	set-track-time
Comments/see also	get-vlq

Example:

```
(setq
  fstring
  (concatenate
    'string *MCStylistic-Oct2010-example-files-path*
    "/vivaldi-op6-no3-2.mid"))
(with-open-file
  (input-stream
    fstring :element-type '(unsigned-byte 8)
    :if-does-not-exist nil)
  (convert-vlq (get-vlq input-stream)))
--> 77
```

This function converts an integer represented using variable-length quantity (VLQ) into the digit representation. In MIDI files, time is listed as ticks in VLQs.

**earlier**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	load-midi-file
Comments/see also	

Example:

```
(earlier '(5 60) '(6.5 61))
--> T
```

This function returns T if the first element of the first argument is less than the first element of the second argument, and NIL otherwise.

**first>=**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	ticks-ms
Comments/see also	

Example:

```
(first>= 60 '(59 64 67))
--> T
```

This is a test function for tempo searches.

**gather-bytes**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	get-metadata, read-track
Comments/see also	

Example:

```
(with-open-file
  (s
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/temp-bytes")
    :direction :output :element-type 'unsigned-byte)
  (write-byte 101 s) (write-byte 111 s))
--> 111
(with-open-file
  (s
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/temp-bytes") :element-type 'unsigned-byte)
  (gather-bytes s 2))
--> (101 111)
```

This function reads arbitrary bytes into a list.

### get-header

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	get-metadata, read-track
Comments/see also	

Example:

```
(setq
  fstring
  (concatenate
    'string *MCStylistic-Oct2010-example-files-path*
    "/vivaldi-op6-no3-2.mid"))
(with-open-file
  (input-stream
    fstring :element-type '(unsigned-byte 8)
    :if-does-not-exist nil)
  (setup)
  (get-header input-stream))
--> 120
```

This function reads the file header.

### get-metadata

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	gather-bytes
Called by	parse-events, read-track
Comments/see also	

Example:

```
(setq
  fstring
  (concatenate
    'string *MCStylistic-Oct2010-example-files-path*
```

```

    "/vivaldi-op6-no3-2.mid"))
(with-open-file
  (input-stream
    fstring :element-type '(unsigned-byte 8)
    :if-does-not-exist nil)
  (get-metadata input-stream))
--> (84 104 100 0 0 0 6 0 1 0 12 0 120 77 84 114 107 0
      0 0 12 0 255 81 3 15 66 64 196 56 255 47 0 77 84
      114 107 0 0 1 196 0 192 6 0 144 49 64 0 255 3 11
      104 97 114 112 115 105 99 104 111 114 100 0 255 4
      11 104 97 114 112 115 105 99 104 111 114)

```

This function reads a length, then gathers that many bytes together (representing metadata).

### get-short

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	get-header
Comments/see also	get-word

Example: within get-header example,

```

(get-short input-stream)
--> 1

```

This function is a 16-bit retriever.

### get-track-header

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	get-type, get-word
Called by	read-track
Comments/see also	

Example:

```

(setq

```



```
fstring
(concatenate
 'string *MCStylistic-Oct2010-example-files-path*
 "/vivaldi-op6-no3-2.mid"))
(with-open-file
 (input-stream
  fstring :element-type '(unsigned-byte 8)
  :if-does-not-exist nil)
 (setup)
 (get-header input-stream)
 (get-track-header input-stream))
--> 12
```

This function reads a track header.

### get-type

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	get-header, get-track-header
Comments/see also	

Example: within get-header example,

```
(get-type input-stream)
--> "MThd"
```

Helps to read header.

### get-word

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	get-header, get-track-header
Comments/see also	get-short

Example: within get-header example,

```
(get-word input-stream)
--> 6
```

This function is a 32-bit retriever.

## get-vlq

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	set-track-time
Comments/see also	convert-vlq

Example:

```
(setq
  fstring
  (concatenate
    'string *MCStylistic-Oct2010-example-files-path*
    "/vivaldi-op6-no3-2.mid"))
(with-open-file
  (input-stream
    fstring :element-type '(unsigned-byte 8)
    :if-does-not-exist nil)
  (get-vlq input-stream))
--> (77)
```

All events are separated by a delta time, so this function gets the VLQ.

## handle-bend

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	parse-events
Comments/see also	

Example:

```
(handle-bend #XA0 60 3)
--> (160 60 3)
```

This function discards bend data.

**handle-control**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	parse-events
Comments/see also	

Example:

```
(handle-control #XA0 60 84)
--> (160 60 84)
```

This function discards control data.

**handle-note**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	ticks-ms
Called by	parse-events
Comments/see also	

Example:

```
(handle-note #XA0 60 84)
--> 0
```

This function parses a note-on event.

**handle-off**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	match-note, ticks-ms
Called by	parse-events
Comments/see also	

Example:

```
(handle-off #XA0 60 84)
--> 0
```

This function searches for the note-on event to which a note-off event belongs and sets the duration accordingly. This does not handle overlapping notes of the same pitch.

### **handle-pressure**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	parse-events
Comments/see also	

Example:

```
(handle-pressure #XA0 60)
--> (160 60)
```

This function discards pressure data.

### **handle-program**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	parse-events
Comments/see also	

Example:

```
(handle-program #XA0 60)
--> (160 60)
```

This function discards program data.

### **handle-touch**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	parse-events
Comments/see also	

Example:

```
(handle-touch #XA0 60 84)
--> (160 60 84)
```

This function discards touch data.

## list-to-string

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	parse-metadata
Comments/see also	

Example:

```
(list-to-string '(84 104 111 109 97 115))
--> "Thomas."
```

This function converts ASCII to strings. Note that most metadata is text.

## load-midi-file

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	earlier, get-header, read-track, setup
Called by	
Comments/see also	

Example:

```
(setq
 imported-midi
 (load-midi-file
 (concatenate
 'string *MCStylistic-Oct2010-example-files-path*
 "/vivaldi-op6-no3-2.mid"))))
(subseq imported-midi 0 10)
--> ((0 79 1 6 64) (0 69 1 4 64) (0 49 1 1 64)
      (0 49 1 3 64) (0 76 1 5 64) (1 79 1 6 64)
      (1 69 1 4 64) (1 76 1 5 64) (1 49 1 1 64)
      (1 49 1 3 64))
```

This main function imports a MIDI file into the Lisp environment.

### **match-note**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	handle-off
Comments/see also	

Example:

```
(match-note '(#XA0 62) '(4 62 0 #XA0))
--> T
```

This function tests for a note-off event.

### **parse-events**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	handle-bend, handle-control, handle-note, handle-off, handle-pressure, handle-program, handle-touch, parse-metadata, strip-sysex
Called by	read-and-parse-event
Comments/see also	

Example:

```
(setq
  fstring
  (concatenate
    'string *MCStylistic-Oct2010-example-files-path*
    "/vivaldi-op6-no3-2.mid"))
(with-open-file
  (input-stream
    fstring :element-type '(unsigned-byte 8)
    :if-does-not-exist nil)
  (parse-events #XA0 60 input-stream))
--> (160 60 77)
```

This function handles track data.

**parse-metadata**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	list-to-string
Called by	parse-events
Comments/see also	

Example:

```
(parse-metadata '(9 104))
--> 1
```

This function extracts tempo and end-of- track information from the meta-data.

**re-time**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	my-last
Called by	
Comments/see also	Deprecated.

Example:

```
(re-time
 '( ( (1 69 1 4 64) (0 79 1 6 64) (2 49 1 3 64)
      (0 69 1 4 64) )
 '( ( (1 69 1 4 64) (0 79 1 6 64) (2 49 1 3 64)
      (0 69 1 4 64) ) )
--> ( ( (1 69 1 4 64) (0 79 1 6 64) (2 49 1 3 64)
      (0 69 1 4 64) (2 69 1 4 64) (1 79 1 6 64)
      (3 49 1 3 64) (1 69 1 4 64) )
```

This function appends some events (the second argument) to other events (the first argument) by translating them by the ontime of the last event from the first argument.

**read-and-parse-event**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	parse-events
Called by	read-track
Comments/see also	

Example:

```
(setq
  fstring
  (concatenate
    'string *MCStylistic-Oct2010-example-files-path*
    "/vivaldi-op6-no3-2.mid"))
(with-open-file
  (input-stream
    fstring :element-type '(unsigned-byte 8)
    :if-does-not-exist nil)
  (read-and-parse-event input-stream))
--> NIL
```

This function deals with running status.

**read-track**

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	gather-bytes, get-track-header, read-and-parse-event, set-track-time
Called by	load-midi-file
Comments/see also	

Example:

```
(setq
  fstring
  (concatenate
    'string *MCStylistic-Oct2010-example-files-path*
    "/vivaldi-op6-no3-2.mid"))
(with-open-file
  (input-stream
```



```

    fstring :element-type '(unsigned-byte 8)
    :if-does-not-exist nil)
  (setup)
  (get-header input-stream)
  (read-track input-stream))
--> NIL

```

This function is called once per track, and reads track data.

### set-track-time

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	convert-vlq, get-vlq
Called by	read-track
Comments/see also	

Example:

```

(setq
  fstring
  (concatenate
    'string *MCStylistic-Oct2010-example-files-path*
    "/vivaldi-op6-no3-2.mid"))
(with-open-file
  (input-stream
    fstring :element-type '(unsigned-byte 8)
    :if-does-not-exist nil)
  (set-track-time input-stream))
--> 77

```

There are times between events, so `*track-time*` must be accumulated across each track.

### setup

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	load-midi-file
Comments/see also	Consider giving more specific name.

Example:

```
(setup)
--> #()
```

This function sets the values of three variables.

## strip-sysex

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	parse-events
Comments/see also	

Example:

```
(setq
  fstring
  (concatenate
    'string *MCStylistic-Oct2010-example-files-path*
    "/vivaldi-op6-no3-2.mid"))
(with-open-file
  (input-stream
    fstring :element-type '(unsigned-byte 8)
    :if-does-not-exist nil)
  (strip-sysex input-stream))
--> "Error: Unexpected end of file"
```

This function deletes sysex data. The example gives an error because the imported MIDI file does not contain any sysex.

## ticks-ms

Started, last checked	26/1/2009, 26/1/2009
Location	MIDI import
Calls	
Called by	handle-note, handle-off
Comments/see also	

Example:

```
(ticks-ms 50)
--> 5/12
```

The time conversion function searches the tempo map from the end to find tempo in effect at the time.

### 4.2.3 MIDI export

The functions below are for exporting datapoints (dimensions for ontime in milliseconds, MIDI note number, duration in milliseconds, channel, and velocity) to a MIDI file. The main function is saveit.

#### convert-ontime-to-deltatime

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	
Called by	create-midi-events
Comments/see also	

Example:

```
(convert-ontime-to-deltatime 500)
--> 24
    0
```

This function converts an ontime to a deltatime.

#### create-midi-events

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	convert-ontime-to-deltatime, make-midi-note-msg, make-midi-pc-msg
Called by	create-MTrk
Comments/see also	

Example:

```
(create-midi-events
 '((0 36 1000 1 35) (0 48 1000 1 35) (500 60 500 7 40)
   (0 1 0 1 255)))
```

```
--> ((0 (144 36 35)) (48 (128 36 35)) (0 (144 48 35))
      (48 (128 48 35)) (24 (150 60 40))
      (48 (134 60 40)) (0 (192 0)))
```

This function converts datapoints into the format required for the function `create-midi-track-data`.

## **create-midi-file**

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	
Called by	save-as-midi, saveit
Comments/see also	

Example:

```
(setq
  outfilename
  (concatenate
    'string *MCStylistic-Oct2010-example-files-path*
    "/midi-export-test.mid"))
(create-midi-file outfilename)
--> #<BASIC-FILE-BINARY-OUTPUT-STREAM
      ((concatenate
        'string *MCStylistic-Oct2010-example-files-path*
        "/midi-export-test.mid")/13 ISO-8859-1)
      #x3000419BC3FD>
```

This function creates an output stream.

## **create-midi-track-data**

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	make-var-len
Called by	create-MTrk
Comments/see also	

Example:

```
(create-midi-track-data '((0 (193 1)) (2 (193 1))))
--> (0 193 1 2 193 1)
```

Each element of the variable `midiEvents` is of the format `((deltaTime (byte3 byte2 byte1))`. They should be sorted in the order for the file and their `deltaTimes` are relative to each other (each relative to the previous). This function creates an integer-stream representation.

### create-midi-tracks

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	create-tempo-track, create-MTrk
Called by	save-as-midi, saveit
Comments/see also	

Example:

```
(create-midi-tracks
'((0 1 0 1 255) (0 2 0 2 255) (0 3 0 3 255)
  (0 4 0 4 255) (0 5 0 5 255) (0 6 0 6 255)
  (0 7 0 7 255) (0 8 0 8 255) (0 9 0 9 255)
  (0 10 0 10 255) (0 11 0 11 255) (0 12 0 12 255)
  (0 13 0 13 255) (0 14 0 14 255) (0 15 0 15 255)
  (0 16 0 16 255) (0 60 1000 1 127))))
--> ((77 84 114 107 0 0 0 4 0 255 47 0)
      (77 84 114 107 0 0 0 15 0 192 0 0 144 60 127 48
       128 60 127 0 255 47 0)
      (77 84 114 107 0 0 0 7 0 193 1 0 255 47 0)
      (77 84 114 107 0 0 0 7 0 194 2 0 255 47 0)
      (77 84 114 107 0 0 0 7 0 195 3 0 255 47 0)
      (77 84 114 107 0 0 0 7 0 196 4 0 255 47 0)
      (77 84 114 107 0 0 0 7 0 197 5 0 255 47 0)
      (77 84 114 107 0 0 0 7 0 198 6 0 255 47 0)
      (77 84 114 107 0 0 0 7 0 199 7 0 255 47 0)
      (77 84 114 107 0 0 0 7 0 200 8 0 255 47 0)
      (77 84 114 107 0 0 0 7 0 201 9 0 255 47 0)
      (77 84 114 107 0 0 0 7 0 202 10 0 255 47 0)
      (77 84 114 107 0 0 0 7 0 203 11 0 255 47 0)
      (77 84 114 107 0 0 0 7 0 204 12 0 255 47 0)
      (77 84 114 107 0 0 0 7 0 205 13 0 255 47 0))
```

```
(77 84 114 107 0 0 0 7 0 206 14 0 255 47 0)
(77 84 114 107 0 0 0 7 0 207 15 0 255 47 0))
```

This function takes datapoints and lists representing the ends of tracks, and converts them into the integer streams in preparation for the function write-to-midi-file.

### **create-MThd**

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	
Called by	save-as-midi, saveit
Comments/see also	

Example:

```
(create-MThd 17)
--> (77 84 104 100 0 0 0 6 0 1 0 17 0 48)
```

This function creates the integer stream representing a MIDI file's header data.

### **create-MTrk**

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	create-midi-events, create-midi-track-data, fix-deltatime, sort-by-deltatime, split-bytes
Called by	create-midi-tracks
Comments/see also	

Example:

```
(create-MTrk '((0 1 0 1 255) (0 60 1000 1 127)))
--> (77 84 104 100 0 0 0 6 0 1 0 17 0 48)
```

This function creates the integer stream representing one track in a MIDI file.

**create-tempo-track**

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	split-bytes
Called by	create-midi-tracks
Comments/see also	

Example:

```
(create-tempo-track)
--> ((77 84 114 107 0 0 0 4 0 255 47 0))
```

This function creates the integer representation for a MIDI file's tempo track.

**fix-deltatime**

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	
Called by	create-MTrk
Comments/see also	

Example:

```
(fix-deltatime 40 '((0 (207 15))))
--> ((-40 (207 15)))
```

This function shifts all of the deltatimes back by the first argument.

**get-channel-events**

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	
Called by	create-midi-tracks
Comments/see also	

Example:

```
(get-channel-events
1
```

```
'((0 1 0 1 255) (0 2 0 2 255) (0 3 0 3 255)
  (0 4 0 4 255) (0 5 0 5 255) (0 6 0 6 255)
  (0 7 0 7 255) (0 8 0 8 255) (0 9 0 9 255)
  (0 10 0 10 255) (0 11 0 11 255) (0 12 0 12 255)
  (0 13 0 13 255) (0 14 0 14 255) (0 15 0 15 255)
  (0 16 0 16 255) (0 60 1000 1 127)))
--> ((0 1 0 1 255) (0 60 1000 1 127))
```

This function takes an integer between 1 and 16 (inclusive) as its first argument, and a list of datapoints as its second argument. It returns elements of this list whose fourth element is equal to the first argument.

## get-byte

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	
Called by	split-bytes
Comments/see also	

Example:

```
(get-byte 3 7)
--> 0
```

This function converts an integer to bytes, starting at the rightmost index.

## insert-program-changes

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	
Called by	save-as-midi, saveit
Comments/see also	

Example:

```
(insert-program-changes '((0 60 1000 1 127)))
--> ((0 1 0 1 255) (0 2 0 2 255) (0 3 0 3 255)
  (0 4 0 4 255) (0 5 0 5 255) (0 6 0 6 255)
  (0 7 0 7 255) (0 8 0 8 255) (0 9 0 9 255)
```



```
(0 10 0 10 255) (0 11 0 11 255) (0 12 0 12 255)
(0 13 0 13 255) (0 14 0 14 255) (0 15 0 15 255)
(0 16 0 16 255) (0 60 1000 1 127))
```

This function inserts MIDI track headers as datapoints (signified by 255).

### make-midi-note-msg

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	
Called by	create-midi-events
Comments/see also	

Example:

```
(make-midi-note-msg '(0 60 1000 1 127) 144)
--> (144 60 127)
```

This function creates MIDI note messages of the type processed by the function `create-midi-track-data`. It should be pointed out that `#x90` is for a note-on and `#x80` for a note-off.

### make-midi-pc-msg

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	
Called by	create-midi-events
Comments/see also	

Example:

```
(make-midi-pc-msg '(0 16 0 16 255))
--> (207 15)
```

This function creates MIDI PC messages of the type processed by the function `create-midi-track-data`. It should be pointed out that `#xC0` is for a program change.

**make-var-len**

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	
Called by	create-midi-track-data
Comments/see also	

Example:

```
(make-var-len 1241)
--> (137 89)
```

This function converts integers to a binary- like representation. Adapted from <http://www.blitter.com/~russtopia/MIDI/~jglatt/>.

**save-as-midi**

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	create-midi-file, create-midi-tracks, create-MThd, insert-program-changes, write-to-midi-file
Called by	
Comments/see also	saveit

Example:

```
(save-as-midi
 "midi-export-test.mid"
 '((0 36 1000 1 35) (0 48 1000 1 35) (500 60 500 7 40)
 (1000 63 500 7 45) (1500 67 500 7 50)
 (2000 72 500 7 55) (2500 75 500 7 60)
 (3000 79 500 12 65) (3500 84 500 12 70)
 (4000 79 500 12 75) (4500 75 500 12 80)
 (5000 72 500 12 84) (5500 67 500 12 84)))
--> (concatenate
 'string
 *MCStylistic-Oct2010-example-files-path*
 "/midi-export-test.mid")
```

This function exports datapoints (dimensions for ontime in milliseconds, MIDI note number, duration in milliseconds, channel, and velocity) to a

MIDI file. It can clip the end of the file, so to avoid this, use the function `saveit`.

## **saveit**

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	create-midi-file, create-midi-tracks, create-MThd, insert-program-changes, write-to-midi-file
Called by	
Comments/see also	save-as-midi

Example:

```
(saveit
  (concatenate
    'string
    *MCStylistic-Oct2010-example-files-path*
    "/midi-export-test.mid")
  '((0 36 1000 1 35) (0 48 1000 1 35) (500 60 500 7 40)
    (1000 63 500 7 45) (1500 67 500 7 50)
    (2000 72 500 7 55) (2500 75 500 7 60)
    (3000 79 500 12 65) (3500 84 500 12 70)
    (4000 79 500 12 75) (4500 75 500 12 80)
    (5000 72 500 12 84) (5500 67 500 12 84)))
--> (concatenate
  'string
  *MCStylistic-Oct2010-example-files-path*
  "/midi-export-test.mid")
```

This function is very similar to the function `save-as-midi` (exporting data-points with dimensions for ontime in milliseconds, MIDI note number, duration in milliseconds, channel, and velocity, to a MIDI file). The difference is that this function does not clip the end of the file.

**sort-by-deltatime**

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	
Called by	create-MTrk
Comments/see also	

Example:

```
(sort-by-deltatime '((24 (207 15)) (0 (207 15))))
--> ((0 (207 15)) (24 (207 15)))
```

This function sorts a list of lists ascending by the car of each list.

**split-bytes**

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	get-byte
Called by	create-MTrk, create-tempo-track
Comments/see also	

Example:

```
(split-bytes 7 4)
--> (0 0 0 7)
```

This function splits a long integer into its high byte and low byte.

**write-to-midi-file**

Started, last checked	27/1/2009, 27/1/2009
Location	MIDI export
Calls	
Called by	save-as-midi, saveit
Comments/see also	

Example:

```
(setq
 outfilename
```

```

(concatenate
  'string *MCStylistic-Oct2010-example-files-path*
  "/midi-export-test.mid"))
(write-to-midi-file
  (create-midi-file outfilename)
  '((77 84 104 100 0 0 0 6 0 1 0 17 0 48)
    (77 84 114 107 0 0 0 4 0 255 47 0)
    (77 84 114 107 0 0 0 15 0 192 0 0 144 60 127 48 128
      60 127 0 255 47 0)
    (77 84 114 107 0 0 0 7 0 193 1 0 255 47 0)
    (77 84 114 107 0 0 0 7 0 194 2 0 255 47 0)))
--> NIL

```

This function will convert MIDI track events to bytes and write them to a specified file.

#### 4.2.4 Hash tables

The functions below are for saving, reading, displaying and querying hash-tables. It can be convenient to work with lists, each of whose elements is a hash table.

##### copy-hash-table

Started, last checked	25/1/2010, 25/1/2010
Location	Hash tables
Calls	
Called by	disp-ht-el, disp-ht-key
Comments/see also	

Example:

```

(setq A (make-hash-table :test #'equal))
(setf (gethash "hair colour" A) "brown")
(setq B (copy-hash-table A))
(list A B)
--> (#<HASH-TABLE
      :TEST EQUAL size 1/60 #x300041A694FD>
     #<HASH-TABLE
      :TEST EQUAL size 1/60 #x300041A683DD>)

```

This function returns a copy of hash table, with the same keys and values. The copy has the same properties as the original, unless overridden by the keyword arguments.

Before each of the original values is set into the new hash-table, key is invoked on the value. As key defaults to `cl:identity`, a shallow copy is returned by default. Adapted from <http://common-lisp.net/project/alexandria/darcs/alexandria/hash-tables.lisp>.

## disp-ht-el

Started, last checked	25/1/2010, 25/1/2010
Location	Hash tables
Calls	
Called by	write-to-file-balanced-hash-table
Comments/see also	

Example:

```
(setq A (make-list-of-hash-tables 2))
(setf (gethash "hair colour" (first A)) "brown")
(setf (gethash "eye colour" (first A)) "brown")
(setf (gethash "hair colour" (second A)) "blond")
(setf (gethash "gender" (second A)) "male")
(dispatch-ht-el (first A))
--> (("hair colour" . "brown")
      ("eye colour" . "brown"))
```

This function displays the contents of a hash table.

## disp-ht-key

Started, last checked	25/1/2010, 25/1/2010
Location	Hash tables
Calls	
Called by	write-to-file-balanced-hash-table
Comments/see also	

Example:

```
(setq A (make-hash-table :test #'equalp))
(setf (gethash "hair colour" A) "brown")
```

```
(setf (gethash ' "eye colour" A) "brown")
(setf (gethash ' "gender" A) "male")
(dispatch-key A)
--> ("hair colour" "eye colour" "gender")
```

This function displays the keys of a hash table.

## hash-tables-with-key-value-pairs

Started, last checked	25/1/2010, 25/1/2010
Location	Hash tables
Calls	constant-vector
Called by	
Comments/see also	

Example:

```
(setq A (make-list-of-hash-tables 2))
(setf (gethash ' "hair colour" (first A)) "brown")
(setf (gethash ' "eye colour" (first A)) "brown")
(setf (gethash ' "name" (first A)) "Chris")
(setf (gethash ' "hair colour" (second A)) "blond")
(setf (gethash ' "gender" (second A)) "male")
(setf (gethash ' "name" (second A)) "Chris")
(setq
  B
  (hash-tables-with-key-value-pairs
    A '(("name" . "Chris") ("hair colour" . "brown"))))
--> (#<HASH-TABLE
      :TEST EQUAL size 3/60 #x3000417DF6FD>)
```

This function returns those hash tables in a list that have key-value pairs equalp to those specified in the second argument. The example returns a list of one hash table because only the first hash table contains information for somebody called Chris with brown hair.

**index-target-translation-in-hash-tables**

Started, last checked	25/1/2010, 25/1/2010
Location	Hash tables
Calls	test-translation
Called by	
Comments/see also	

Example:

```
(setq
  A
  (read-from-file-balanced-hash-table
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/patterns-hash.txt")))
(dispatch-el (fourth A))
(index-target-translation-in-hash-tables
  '((4 38 47) (9/2 38 47) (5 38 47)) A "pattern")
--> 3
```

The hash tables each contain a value specified by the third argument (a key). We think of these as patterns, and want to know if any of the patterns are translations of the first argument, the target. The index of the first extant translation is returned, and nil otherwise.

**index-target-translation-mod-in-hash-tables**

Started, last checked	25/1/2010, 25/1/2010
Location	Hash tables
Calls	test-translation-mod-2nd-n
Called by	number-of-targets-trans-mod-in-hash-tables
Comments/see also	

Example:

```
(setq
  A
  (read-from-file-balanced-hash-table
    (concatenate
```



```

' string
*MCStylistic-Oct2010-example-files-path*
"/patterns-hash.txt"))))
(dispatch (fourth A))
(index-target-translation-mod-in-hash-tables
'((0 36 46) (1/2 48 46) (1 36 46)) A 12 "pattern")
--> 3

```

This function is very similar to the function `index-target-translation-in-hash-tables`, except that in the second dimension translations are carried out modulo the third argument.

### make-list-of-hash-tables

Started, last checked	25/1/2010, 25/1/2010
Location	Hash tables
Calls	
Called by	read-from-file-balanced-hash-table
Comments/see also	

Example:

```

(make-list-of-hash-tables 3)
--> (#<HASH-TABLE
      :TEST EQUAL size 0/60 #x300041BB8A5D>
    #<HASH-TABLE
      :TEST EQUAL size 0/60 #x300041BB84AD>
    #<HASH-TABLE
      :TEST EQUAL size 0/60 #x300041BB7EFD>)

```

This function returns a list, each of whose elements is an empty hash table of type 'equal'.

### number-of-targets-trans-mod-in-hash-tables

Started, last checked	25/1/2010, 25/1/2010
Location	Hash tables
Calls	index-target-translation-mod-in-hash-tables
Called by	
Comments/see also	

Example:

```
(setq
A
(read-from-file-balanced-hash-table
(concatenate
'string
*MCStylistic-Oct2010-example-files-path*
"/patterns-hash.txt")))
(number-of-targets-trans-mod-in-hash-tables
'(((0 36 46) (1/2 60 46) (1 36 46))
((0 60 46) (0 48 53) (0 55 57) (0 60 60) (0 64 62)
(1/2 36 46) (1/2 48 53) (1/2 55 57) (1/2 62 61)
(1/2 65 63) (1 36 46) (1 48 53) (1 55 57)
(1 64 62) (1 67 64) (2 48 53) (2 65 63) (2 69 65)
(3 36 46) (3 48 53) (3 55 57) (3 64 62) (3 67 64)
(7/2 36 46) (7/2 48 53) (7/2 55 57) (7/2 60 60)
(7/2 64 62) (4 36 46) (4 48 53) (4 55 57))))
A 12 "pattern")
--> 2
```

This function is very similar to the function `number-of-targets-translation-in-hash-tables`, except that in the second dimension translation is performed modulo the third argument.

## number-of-targets-translation-in-hash-tables

Started, last checked	25/1/2010, 25/1/2010
Location	Hash tables
Calls	test-target-translation-in-hash-tables
Called by	
Comments/see also	

Example:

```
(setq
A
(read-from-file-balanced-hash-table
(concatenate
'string
*MCStylistic-Oct2010-example-files-path*
"/patterns-hash.txt")))
(number-of-targets-translation-in-hash-tables
```

```
'(((6 48 53) (13/2 48 53) (7 48 53))
  ((24 29 42) (24 41 49) (24 48 53) (24 53 56)
   (24 57 58) (49/2 29 42) (49/2 41 49) (49/2 48 53)
   (49/2 55 57) (49/2 58 59) (25 29 42) (25 41 49)
   (25 48 53) (25 57 58) (25 60 60) (26 41 49)
   (26 58 59) (26 62 61) (27 29 42) (27 41 49)
   (27 48 53) (27 57 58) (27 60 60) (55/2 29 42)
   (55/2 41 49) (55/2 48 53) (55/2 53 56)
   (55/2 57 58) (28 29 42) (28 41 49) (28 48 53)))
A "pattern")
--> 2
```

The function `test-target-translation-in- hash-tables` is applied recursively to each member of the first argument of this function. This argument is a list of targets. Each time a translation of a target is detected, the output (initially set to zero) is incremented by one.

### re-index-list-of-hash-tables

Started, last checked	25/1/2010, 25/1/2010
Location	Hash tables
Calls	
Called by	
Comments/see also	

Example:

```
(setq
A
(read-from-file-balanced-hash-table
(concatenate
'string
*MCStylistic-Oct2010-example-files-path*
"/small-hash-table.txt")))
(setq A (re-index-list-of-hash-tables A 780))
(gethash "index" (first A))
--> 780
T
```

This function re-indexes a list of hash tables beginning from an optional second argument.

## read-from-file-balanced-hash-table

Started, last checked	25/1/2010, 25/1/2010
Location	Hash tables
Calls	make-list-of-hash-tables, read-from-file
Called by	
Comments/see also	

Example:

```
(setq
 A
 (read-from-file-balanced-hash-table
  (concatenate
   'string
   *MCStylistic-Oct2010-example-files-path*
   "/small-hash-table.txt")))
(dispatch (second A))
--> (("height" . "6ft") ("name" . "Justin")
      ("index" . 77))
```

This function reads a balanced list of hash tables that have been written to a file, by the function write-to-file-balanced-hash-table. It is assumed that the hash tables are homogeneous or balanced in the sense that they contain exactly the same keys.

## set-each-hash-table-element

Started, last checked	25/1/2010, 25/1/2010
Location	Hash tables
Calls	
Called by	
Comments/see also	

Example:

```
(setq A (make-list-of-hash-tables 2))
(setf (gethash "hair colour" (first A)) "brown")
(setf (gethash "eye colour" (first A)) "brown")
(setf (gethash "hair colour" (second A)) "blond")
(setf (gethash "gender" (second A)) "male")
(set-each-hash-table-element A "height" "tall")
```

```
(list
  (gethash "height" (first A))
  (gethash "height" (second A)))
--> ("tall" "tall")
```

This function is useful if you have a list of hash tables and you want to set each hash table to have an identical key-value pair.

### test-target-translation-in-hash-tables

Started, last checked	25/1/2010, 25/1/2010
Location	Hash tables
Calls	test-translation
Called by	number-of-targets-translation-in-hash-tables
Comments/see also	Implementation could call index-target-translation-in-hash-tables instead.

Example:

```
(setq
  A
  (read-from-file-balanced-hash-table
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/patterns-hash.txt")))
(dispatch (fourth A))
(test-target-translation-in-hash-tables
  '((6 48 53) (13/2 48 53) (7 48 53)) A "pattern")
--> T
```

The hash tables each contain a value specified by the third argument (a key). We think of these as patterns, and want to know if any of the patterns are translations of the first argument, the target. T is returned if a translation does exist among the hash tables, and nil otherwise.

**write-to-file-balanced-hash-table**

Started, last checked	25/1/2010, 25/1/2010
Location	Hash tables
Calls	disp-ht-el, write-to-file
Called by	
Comments/see also	

Example:

```
(setq A (make-list-of-hash-tables 2))
(setf (gethash "hair colour" (first A)) "brown")
(setf (gethash "eye colour" (first A)) "brown")
(setf (gethash "height" (first A)) 187)
(setf (gethash "hair colour" (second A)) "blond")
(setf (gethash "gender" (second A)) "male")
(write-to-file-balanced-hash-table
 A
 (concatenate
  'string
  *MCStylistic-Oct2010-example-files-path*
  "/small-hash-table 2.txt"))
--> T
```

This function takes as its first argument a list, each of whose elements is a hash table. It applies the function `disp-ht-el` to each element, collects the output and writes it to a text file. At the top of the file are two integers  $n$  and  $m$ , referring to the length of the list and the number of elements in a hash table respectively. It is assumed that the hash tables are homogeneous or balanced in the sense that they contain exactly the same keys, but as the example demonstrates, this does not have to be the case. (Balanced hash tables are easier to read back in.)

**4.2.5 CSV files**

These functions enable the conversion of csv files into lists of lists, and vice versa. Despite using terms like dataset below, neither representation has to be balanced, that is, rows/lists can contain different numbers of elements.

**comma-positions**

Started, last checked	30/7/2010, 30/7/2010
Location	Hash tables
Calls	
Called by	comma-separated-string2list
Comments/see also	space-bar-positions, tab-positions

Example:

```
(comma-positions "uh,ktr,3,4")
--> (2 6 8)
```

This function returns the positions at which commas occur in a string.

**comma-separated-integers2list**

Started, last checked	30/7/2010, 30/7/2010
Location	Hash tables
Calls	comma-separated-string2list
Called by	csv2dataset
Comments/see also	

Example:

```
(comma-separated-integers2list "1.00, 3.00")
--> (1 3)
```

This function applies the function `parse-integer` recursively, once the string supplied as an argument has had the function `comma-separated-string2list` applied.

**comma-separated-string2list**

Started, last checked	30/7/2010, 30/7/2010
Location	Hash tables
Calls	comma-positions
Called by	comma-separated-integers2list
Comments/see also	space-bar-separated-string2list, tab-separated-string2list

Example:

```
(comma-separated-string2list "uh,ktr,3,4")
--> ("uh" "ktr" "3" "4")
```

This function turns a comma-separated string into a list, where formerly each item was preceded or proceeded by a comma.

## csv2dataset

Started, last checked	30/7/2010, 30/7/2010
Location	Hash tables
Calls	comma-separated-integers2list, read-from-file-arbitrary
Called by	comma-separated-integers2list
Comments/see also	

Example:

```
(csv2dataset
 (concatenate
  'string
  *MCStylistic-Oct2010-example-files-path*
  "/short-list.csv"))
--> ((1 3) (2 6) (5 2 2) (6 2))
```

This function converts a file in comma-separated-value (CSV) format to a dataset. At present it is assumed each value is an integer, but it would be worth making this more robust. It item was preceded or proceeded by a comma.

## dataset2csv

Started, last checked	30/7/2010, 30/7/2010
Location	Hash tables
Calls	read-from-file
Called by	
Comments/see also	list-of-lists2csv

Example:

```
(dataset2csv
 '( (1/3 3) (2/6 6) (5 2 2) (6 2) )
 (concatenate
```



```

'string
*MCStylistic-Oct2010-example-files-path*
"/csv-export-test.csv"))
--> T

```

This function converts a dataset (a list of lists of equal length) to a csv file. The first argument is either the path where the dataset resides or the dataset itself. The example causes a file to be created in the specified location.

### list-of-lists2csv

Started, last checked	30/7/2010, 30/7/2010
Location	Hash tables
Calls	read-from-file
Called by	comma-separated-integers2list
Comments/see also	dataset2csv

Example:

```

(list-of-lists2csv
'((1/3 3) (2/6 6) (5 2 2) (6 2))
(concatenate
'string
*MCStylistic-Oct2010-example-files-path*
"/csv-export-test 2.csv"))
--> T

```

This function converts a balanced list of lists to a csv file. The first argument is either the path where the dataset resides or the dataset itself. The example causes a file to be created in the specified location. The function list-of-lists2csv is very similar to the function dataset2csv, the difference being that the former does not round fractions to decimal places.

#### 4.2.6 Director musices

Director musices is a music file format. It is not as common as kern or musicXML, but it uses a list format, which makes it amenable to Lisp import using only a few functions. As far as I can tell, the director musices format does not handle multiple voices on one staff. Some of the functions here, like MIDI-morphetic-pair2pitch&octave, are called by music-import and export functions for different formats.

**check-pitch&octave**

Started, last checked	17/11/2009, 17/11/2009
Location	Director musices
Calls	
Called by	
Comments/see also	

Example:

```
(check-pitch&octave "C3")
--> "C3"
```

This function tests whether a supplied pitch&octave is in an acceptable format and range. I was intending to allow pitches from C0 to C8 (MNNs 12 to 108) but this function will not allow C8, so could be adjusted in future. If acceptable the pitch&octave is returned, and nil otherwise.

**director-musice2datapoint**

Started, last checked	17/11/2009, 17/11/2009
Location	Director musices
Calls	pitch&octave2MIDI-morphetic-pair
Called by	director-musices2dataset-chunked
Comments/see also	

Example:

```
(director-musice2datapoint
 7 1
 '(bar 1 n ("C3" 1/2) key "C" modus "maj" mm 192
  meter (2 2))
 3 "C3" 1/2)
--> (7 48 53 1/2 1 nil)
```

This function converts one line of a director musices file into a datapoint consisting of ontime, MIDI note number, morphetic pitch number, duration, stave, and T if the note is tied over.

**director-musices2dataset**

Started, last checked	17/11/2009, 17/11/2009
Location	Director musices
Calls	director-musices2dataset-chunked, resolve-ties
Called by	
Comments/see also	

Example:

```
(director-musices2dataset
 (concatenate
  'string
  *MCStylistic-Oct2010-example-files-path*
  "/scarlatti-L1-bars11-13.dm"))
--> ((0 79 71 1 1) (0 86 75 7/3 0) (1 43 50 1 1)
      (2 38 47 2 1) (7/3 84 74 1/3 0) (8/3 83 73 1/3 0)
      (3 81 72 1/3 0) (10/3 83 73 1/3 0)
      (11/3 84 74 1/3 0) (4 79 71 1 1) (4 83 73 1/3 0)
      (13/3 84 74 1/3 0) (14/3 86 75 1/3 0)
      (5 43 50 1 1) (5 86 75 4/3 0) (6 38 47 2 1)
      (19/3 84 74 1/3 0) (20/3 83 73 1/3 0)
      (7 81 72 1/3 0) (22/3 83 73 1/3 0)
      (23/3 84 74 1/3 0) (8 79 71 1 1) (8 83 73 1/3 0))
```

This function converts a piece of music represented in the director-musices format into a dataset where each datapoint consists of an ontime, MIDI note number, morphetic pitch number, duration and stave.

**director-musices2dataset-chunked**

Started, last checked	17/11/2009, 17/11/2009
Location	Director musices
Calls	director-musice2datapoint, read-from-file
Called by	director-musices2dataset
Comments/see also	

Example:

```
(director-musices2dataset-chunked
 (concatenate
```

```

'string
*MCStylistic-Oct2010-example-files-path*
"/scarlatti-L1-bars11-13.dm"))
--> ((0 86 75 2 0 T) (2 86 75 1/3 0 NIL)
      (7/3 84 74 1/3 0 NIL) (8/3 83 73 1/3 0 NIL)
      (3 81 72 1/3 0 NIL) (10/3 83 73 1/3 0 NIL)
      (11/3 84 74 1/3 0 NIL) (4 83 73 1/3 0 NIL)
      (13/3 84 74 1/3 0 NIL) (14/3 86 75 1/3 0 NIL)
      (5 86 75 1 0 T) (6 86 75 1/3 0 NIL)
      (19/3 84 74 1/3 0 NIL) (20/3 83 73 1/3 0 NIL)
      (7 81 72 1/3 0 NIL) (22/3 83 73 1/3 0 NIL)
      (23/3 84 74 1/3 0 NIL) (8 83 73 1/3 0 NIL)
      (0 79 71 1 1 NIL) (1 43 50 1 1 NIL)
      (2 38 47 2 1 NIL) (4 79 71 1 1 NIL)
      (5 43 50 1 1 NIL) (6 38 47 2 1 NIL)
      (8 79 71 1 1 NIL))

```

This function converts a piece of music represented in the director-musices format into a chunked dataset, chunked in the sense that ties still have to be resolved.

### guess-morphetic-in-C-major

Started, last checked	17/11/2009, 17/11/2009
Location	Director musices
Calls	
Called by	
Comments/see also	

Example:

```

(guess-morphetic-in-C-major 68)
--> 65

```

This function takes a MIDI note number as its only argument. It attempts to guess (very naively) the corresponding morphetic pitch number, assuming a key of or close to C major.

**index-of-1st-tie**

Started, last checked	17/11/2009, 17/11/2009
Location	Director musices
Calls	my-last
Called by	resolve-tie
Comments/see also	

Example:

```
(index-of-1st-tie
'((4 62 61 1 0 T) (5 62 61 1/4 0 NIL)
(21/4 64 62 1/8 0 NIL) (43/8 66 63 1/8 0 NIL)
(11/2 67 64 1/8 0 NIL) (45/8 69 65 1/8 0 NIL)
(23/4 71 66 1/8 0 NIL) (47/8 73 67 1/8 0 NIL)))
--> 0
```

This function returns the index of the first element of a list of lists whose last value (indicating a tie) is T.

**indices-of-ties**

Started, last checked	17/11/2009, 17/11/2009
Location	Director musices
Calls	
Called by	resolve-tie
Comments/see also	

Example:

```
(indices-of-ties
'((4 62 61 1 0 T) (5 62 61 1 0 T)
(21/4 64 62 1/8 0 NIL) (43/8 66 63 1/8 0 NIL)
(11/2 67 64 1/8 0 NIL) (45/8 69 65 1/8 0 NIL)
(23/4 71 66 1/8 0 NIL) (47/8 73 67 1/8 0 NIL)
(6 62 61 1/4 0 NIL)) 0)
--> (1 8)
```

This function returns the indices of elements that have the same MIDI-morphetic pairs as the element indicated by the second argument, so long as these elements continue to be tied. This function may not be robust enough: replacing the last MNN by 63 results in an infinite loop.

## MIDI-morphetic-pair2pitch&octave

Started, last checked	17/11/2009, 17/11/2009
Location	Director musices
Calls	
Called by	
Comments/see also	

Example:

```
(MIDI-morphetic-pair2pitch&octave '(70 65))
--> "A#4"
```

This function returns the pitch and octave of an input MIDI note number and morphetic pitch number.

## modify-to-check-dataset

Started, last checked	17/11/2009, 17/11/2009
Location	Director musices
Calls	
Called by	
Comments/see also	

Example:

```
(modify-to-check-dataset
 '( ( (0 50 54 5/4 1) (5/4 52 55 1/8 1)
      (11/8 54 56 1/8 1) (3/2 55 57 1/8 1)
      (13/8 57 58 1/8 1) (7/4 59 59 1/8 1)))
--> ((0 50 1250 1 90) (1250 52 125 1 90)
     (1375 54 125 1 90) (1500 55 125 1 90)
     (1625 57 125 1 90) (1750 59 125 1 90))
```

This function converts standard vector representation to events for saving as a MIDI file.

**pitch&octave2MIDI-morphetic-pair**

Started, last checked	17/11/2009, 17/11/2009
Location	Director musices
Calls	
Called by	director-musice2datapoint
Comments/see also	

Example:

```
(pitch&octave2MIDI-morphetic-pair "A#4")
--> (70 65)
```

This function returns the MIDI note number and morphetic pitch number of an input pitch and octave.

**resolve-tie**

Started, last checked	17/11/2009, 17/11/2009
Location	Director musices
Calls	firstn, index-of-1st-tie, indices-of-ties, my-last, remove-nth-list
Called by	resolve-ties
Comments/see also	resolve-ties-kern

Example:

```
(resolve-tie
'((4 62 61 1 0 T) (5 62 61 1/4 0 NIL)
(21/4 64 62 1/8 0 NIL) (43/8 66 63 1/8 0 NIL)
(11/2 67 64 1/8 0 NIL) (45/8 69 65 1/8 0 NIL)
(23/4 71 66 1/8 0 NIL) (47/8 73 67 1/8 0 NIL)))
--> ((4 62 61 5/4 0 NIL) (21/4 64 62 1/8 0 NIL)
(43/8 66 63 1/8 0 NIL) (11/2 67 64 1/8 0 NIL)
(45/8 69 65 1/8 0 NIL) (23/4 71 66 1/8 0 NIL)
(47/8 73 67 1/8 0 NIL))
```

This function locates notes relevant to a tie, creates a single appropriately defined note, and removes the redundant notes.

**resolve-ties**

Started, last checked	17/11/2009, 17/11/2009
Location	Director musices
Calls	orthogonal-projection-unique-equalp, resolve-tie
Called by	resolve-ties
Comments/see also	

Example:

```
(resolve-ties
'((4 62 61 1 0 T) (5 62 61 1/4 0 NIL)
(5 74 68 1 0 T)
(21/4 64 62 1/8 0 NIL) (43/8 66 63 1/8 0 NIL)
(11/2 67 64 1/8 0 NIL) (45/8 69 65 1/8 0 NIL)
(23/4 71 66 1/8 0 NIL) (47/8 73 67 1/8 0 NIL)
(6 74 68 1 0 T) (7 74 68 1/4 0 NIL)))
--> ((4 62 61 5/4 0) (5 74 68 9/4 0)
(21/4 64 62 1/8 0) (43/8 66 63 1/8 0)
(11/2 67 64 1/8 0) (45/8 69 65 1/8 0)
(23/4 71 66 1/8 0) (47/8 73 67 1/8 0))
```

This function applies the function `resolve-tie` recursively until all ties have been resolved. At this point the input dataset is projected to remove the tie dimension.

**4.2.7 Kern**

The functions below will parse a kern file (<http://kern.ccarh.org>) and convert it to a dataset. The main function is `kern-file2dataset`. Occasionally there are conflicts between kern's relative encoding and the timewise parsing function. These could be resolved by writing a partwise parsing function.

**accidental-char-p**

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	
Called by	kern-pitch-chars2pitch&octave
Comments/see also	



Example:

```
(accidental-char-p #\a)
--> nil
```

This function returns true if the input character is associated with kern's representation of accidentals.

### index-of-backward-tie

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	
Called by	resolve-ties-kern
Comments/see also	

Example:

```
(index-of-backward-tie
 '( (4 62 61 1 0 "[") (5 63 61 1 0 "[")
   (21/4 64 62 1/8 0 "[") (43/8 63 61 1/8 0 "]")
   (45/8 64 62 1/8 0 "]") (23/4 62 61 1/8 0 "]")
   (47/8 64 62 1/8 0 "]") (6 63 61 1/4 0 "]")) 2)
--> 5
```

This function returns the index of the element that has the same MIDI-morphetic pairs as the element indicated by the second argument, so long as this element is tied backward.

### kern-dur-pitch2pitch&octave-dur

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	kern-pitch-chars2pitch&octave
Called by	kern-tie-dur-pitch2list
Comments/see also	

Example:

```
(kern-dur-pitch2pitch&octave-dur "8e#")
--> ("E#4" 1/2)
```

This function converts a kern note into pitch-and-octave-number and a duration. It is assumed that any irrelevant symbols have already been removed via the function `remove-if` in combination with the test function `not-tie-dur-pitch-char-p` as applied to `*kern-note*`. Non-notes should then result in `nil` being returned.

## kern-file2dataset

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	<code>parse-kern-row</code> , <code>read-from-file-arbitrary</code> , <code>resolve-ties-kern</code> , <code>staves-info2staves-variable</code>
Called by	
Comments/see also	

Example:

```
(firstn
  10
  (kern-file2dataset
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/vivaldi-op6-no3-2.txt"))))
--> ((0 49 53 1 3) (0 49 53 1 5) (0 69 65 1 2)
      (0 76 69 1 1) (0 79 71 1 0) (1 49 53 1 3)
      (1 49 53 1 5) (1 69 65 1 2) (1 76 69 1 1)
      (1 79 71 1 0))
```

This function converts a text file in the kern format into a dataset, where each datapoint consists of an ontime, MIDI note number, morphetic pitch number, duration, and staff number.

## kern-pitch-chars2pitch&octave

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	<code>accidental-char-p</code> , <code>upcase-p</code>
Called by	<code>kern-dur-pitch2pitch&amp;octave-dur</code>
Comments/see also	

Example:

```
(kern-pitch-chars2pitch&octave "e#")
--> "E#4"
```

This function converts kern pitch characters into the pitch-and-octave-number representation. It can accept junk input, but may produce junk output. For example, try ‘.’ or ‘\*’ as input.

### kern-tie-dur-pitch2list

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	kern-dur-pitch2pitch&octave-dur, number-chars-p, upcase-p
Called by	parse-kern-spaced-notes
Comments/see also	

Example:

```
(kern-tie-dur-pitch2list "[8e#]")
--> ("E#4" 1/2 " ")
```

This function converts a kern note into a list consisting of pitch-and-octave, duration, and tie type. It is assumed that any irrelevant symbols have already been removed via the function remove-if in combination with the test function not-tie-dur-pitch-char-p as applied to *\*kern-note\**. Non-notes should then result in nil being returned.

### not-tie-dur-pitch-char-p

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	
Called by	parse-kern-row
Comments/see also	

Example:

```
(not-tie-dur-pitch-char-p #\h)
--> T
```

This function returns true if the input character is not associated with kern’s representation of pitch.

**number-chars-p**

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	
Called by	kern-tie-dur-pitch2list
Comments/see also	

Example:

```
(number-chars-p #\2)
--> nil
```

This function returns true if the input character is 0-9.

**parse-kern-row**

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	not-tie-dur-pitch-char-p, parse-kern-row-as-notes, space-bar-separated-string2list, tab-separated-string2list, update-staves-variable
Called by	kern-file2dataset
Comments/see also	

Example:

```
(parse-kern-row
 "2d#/ 2f#/      ↗4A\      ↗12cc#\L]      ↗."
 '((1 2) (0 1) (1/2 1)) 15)
--> (((1 2) (0 1) (1/2 1))
      46/3
      ((15 63 61 2 1) (15 66 63 2 1) (15 57 58 1 1))
      ((15 73 67 1/3 0 "]""))))
(parse-kern-row
 "*"      ↗*v      ↗*v      ↗*"
 '((1 1) (0 2) (1/2 1)) 15)
--> (((1 1) (0 1) (1/2 1)) 15)
(parse-kern-row
```

```
" .      ↗.      ↗16r      ↗. "
'((1 2) (0 1) (1/2 1)) 15)
--> (((1 2) (0 1) (1/2 1)) 61/4)
```

This function parses a kern row, consisting of notes/rests, changes to the staves variable, or irrelevant information for our purposes. The output is the staves variable, the new ontime, new datapoints, and new tied datapoints.

### parse-kern-row-as-notes

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	parse-kern-spaced-notes
Called by	parse-kern-row
Comments/see also	

Example:

```
(parse-kern-row-as-notes
'(("2d#" "2f#") ("4A") ("12cc#"]") (""))
'((1 2) (0 1) (1/2 1)) 15)
--> (1/3
      ((15 63 61 2 1) (15 66 63 2 1) (15 57 58 1 1)
       (15 73 67 1/3 0 "]")))
```

This function converts a kern row consisting of tabbed notes into a list of datapoints, and also returns the minimum duration of those notes. It recurses over the staves-variable to ensure that each note is labelled correctly according to staff. It is assumed that any irrelevant symbols have already been removed via the the function `remove-if` in combination with the test function `not-tie-dur-pitch-char-p` as applied to `*kern-note*`. Non-notes/rests should then result in `'(0 NIL)` being returned. A lone crotchet rest should result in `'(1 NIL)` being returned, etc.

### parse-kern-spaced-notes

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	kern-tie-dur-pitch2list, pitch&octave2MIDI-morphetic-pair
Called by	parse-kern-row-as-notes
Comments/see also	

Example:

```
(parse-kern-spaced-notes
 '(("[4C#" "4E#" "4B" "8g#") 0 3 0)
 --> (1/2
      ((3 49 53 1 0 "[") (3 53 55 1 0) (3 59 59 1 0)
       (3 68 64 1/2 0)))
```

This function converts a kern row consisting of spaced notes into a list of datapoints, and also returns the minimum duration of those notes. It is assumed that any irrelevant symbols have already been removed via the function `remove-if` in combination with the test function `not-tie-dur-pitch-char-p` as applied to `*kern-note*`. Non-notes/rests should then result in `'(0 NIL)` being returned. A lone crotchet rest should result in `'(1 NIL)` being returned, etc.

## resolve-ties-kern

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	<code>index-of-backward-tie</code>
Called by	<code>kern-file2dataset</code>
Comments/see also	<code>resolve-ties</code>

Example:

```
(resolve-ties-kern
 '((4 62 61 1 0 "[") (5 63 61 1 0 "[")
   (21/4 64 62 1/8 0 "[") (43/8 63 61 1/8 0 "]")
   (45/8 64 62 1/8 0 "]") (23/4 62 61 1/8 0 "]")
   (47/8 64 62 1/8 0 "]") (6 63 61 1/4 0 "]"))
 '((0 60 60 1 0)))
--> ((0 60 60 1 0) (4 62 61 15/8 0) (5 63 61 1/2 0)
      (21/4 64 62 3/4 0))
```

This function resolves tied datapoints by applying the function `index-of-backward-tie` recursively. It is quite similar to the function `resolve-ties`, which was defined for reading director- musices files.

**return-lists-of-length-n**

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	
Called by	parse-kern-row
Comments/see also	Consider changing location.

Example:

```
(return-lists-of-length-n
 '( (1 0) (0) (2 -1) nil (1 2 3) (7 -2)) 2)
--> ((1 0) (2 -1) (7 -2))
```

Returns all lists in a list of lists that are of length n.

**space-bar-positions**

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	
Called by	space-bar-separated-string2list
Comments/see also	comma-positions, tab-positions

Example:

```
(space-bar-positions
 "4C#\ 4G#\ 4B\          ♯8e#/L          ♯<")
--> (3 7)
```

This function returns the positions at which space-bar symbols occur in a string.

**space-bar-separated-string2list**

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	space-bar-positions
Called by	parse-kern-row
Comments/see also	comma-separated-string2list, tab-separated-string2list

Example:

```
(space-bar-separated-string2list
 "4C#\ 4G#\ 4B\      ♯8e#/L      ♯<")
--> ("4C#" "4G#" "4B"      ♯8e#/L      ♯<")
```

This function turns a space-bar-separated string into a list, where formerly each item was preceded or proceeded by a space.

## split-or-collapse-index

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	
Called by	update-staves-variable
Comments/see also	

Example:

```
(split-or-collapse-index 6 '(2 3 5 7 8))
--> 3
(split-or-collapse-index nil '(2 3 5 7 8))
--> nil
(split-or-collapse-index 8 '(2 3 5 7 8))
--> nil
```

Returns the index of the second argument at which the first argument is exceeded. Deals with degenerate cases as indicated.

## staff-char-p

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	
Called by	staves-info2staves-variable
Comments/see also	

Example:

```
(staff-char-p #\2)
--> nil
```

This function returns true if the input character is ‘\*’, ‘s’, ‘t’, ‘a’, or ‘f’.



**staves-info2staves-variable**

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	staff-char-p, tab-separated-string2list
Called by	kern-file2dataset
Comments/see also	

Example:

```
(staves-info2staves-variable
'("!!!COM: Chopin, Frederic"
  "!!!CDT: 1810///-1849///"
  "!!!OTL: Mazurka in F-sharp Minor, Op. 6, No. 1"
  "!!!OPS: Op. 6" "!!!ONM: No. 1"
  "!!!ODT: 1830///-1832///"
  "!!!PDT: 1832///-1833///"
  "!!!PPP: Leipzig (1832); Paris (1833) and London"
  "!!!ODE: Pauline Plater"
  "**kern      ↗**kern      ↗**dynam"
  "*thru      ↗*thru      ↗*thru"
  "*staff2    ↗*staff1    ↗*staff1/2"
  "*Ipiano    ↗*Ipiano    ↗*Ipiano"
  ">A      ↗>A      ↗>A"))
--> ((1 1) (0 1) (-1/2 1))
```

This function looks through the first few rows of a parsed kern file and determines how many staves there are, leading to the definition of the staves variable.

**tab-positions**

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	
Called by	tab-separated-string2list
Comments/see also	comma-positions, space-bar-positions

Example:

```
(tab-positions "4C#\ 4G#\ 4B\      ↗8e#/L      ↗<")
--> (10 16)
```

This function returns the positions at which tabs occur in a string.

## tab-separated-string2list

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	tab-positions
Called by	parse-kern-row, staves-info2staves-variable, update-staves-variable
Comments/see also	comma-separated-string2list, space-bar-separated-string2list

Example:

```
(tab-separated-string2list
 "4C#\ 4G#\ 4B\      ♯8e#/L      ♯<")
--> ("4C#\ 4G#\ 4B\" "8e#/L" "<")
```

This function turns a tab-separated string into a list, where formerly each item was preceded or proceeded by a tab.

## tied-kern-note-p

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	
Called by	
Comments/see also	

Example:

```
(tied-kern-note-p "12f#/L]")
--> T
```

This function returns true if the input kern note is tied over, from or both.

**upcase-p**

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	
Called by	kern-pitch-chars2pitch&octave
Comments/see also	

Example:

```
(upcase-p #\a)
--> nil
```

This function returns true if the input character is upper case, and nil otherwise.

**update-staves-variable**

Started, last checked	30/6/2010, 30/6/2010
Location	Director musices
Calls	fibonacci-list, index-item-1st-occurs, split-or-collapse-index, tab-separated-string2list
Called by	parse-kern-row
Comments/see also	

Example:

```
(update-staves-variable
 '( (1 1) (0 1) (1/2 1)) "*"      ↗*^      ↗*")
--> ((1 1) (0 2) (1/2 1))
(update-staves-variable
 '( (1 1) (0 2) (1/2 1)) "*"      ↗*v      ↗*v      ↗*")
--> ((1 1) (0 1) (1/2 1))
(update-staves-variable
 '( (1 2) (0 1) (1/2 1)) "*"      ↗*      ↗*^      ↗*")
--> ((1 2) (0 2) (1/2 1))
```

The staves-variable is a list of pairs. The first of each pair gives the staff to which a note belongs. The second of each pair indicates whether that stave is split into multiple voices. The symbol ‘\*’ means leave this staff as it is, the symbol ‘^’ means this staff is splitting into an extra voice, and the symbol ‘v’ means this staff is collapsing into one less voice.

## 4.3 Pattern rating

### 4.3.1 Projection

The main functions of use here are for creating projections of datasets (Meredith et al., 2002), which is a precursor to pattern discovery.

#### **difference-list**

Started, last checked	23/7/2009, 23/7/2009
Location	Projection
Calls	remove-nth, subtract-list-from-each-list
Called by	
Comments/see also	Deprecated.

Example:

```
(difference-list '((8 -2 -3) (4 6 6) (4 7 -3)))
--> ((-4 8 9) (-4 9 0) (4 -8 -9) (0 1 -9) (4 -9 0)
      (0 -1 9))
```

The argument to this function is a list consisting of sublists of equal lengths. For  $i = 1, 2, \dots, n$ , the  $i$ th sublist  $S$  is removed from the argument to give a list  $L$ , and the function `subtract-list-from-each-list` is applied.

#### **index-1st-sublist-item<=**

Started, last checked	23/7/2009, 23/7/2009
Location	Projection
Calls	
Called by	test-equal<subset
Comments/see also	index-1st-sublist-item>=, index-1st-sublist-item>

Example:

```
(index-1st-sublist-item<=
 6 '(14 14 14 11 7 7 6 6 4 1 1 0 0))
--> 6
```

This function takes two arguments: a real number  $x$  and a list  $L$  of real numbers. It returns the index of the first element of  $L$  which is less than or equal to  $x$ .

**index-1st-sublist-item>=**

Started, last checked	23/7/2009, 23/7/2009
Location	Projection
Calls	
Called by	test-equal<subset
Comments/see also	index-1st-sublist-item<=, index-1st-sublist-item>

Example:

```
(index-1st-sublist-item>=
 4 '(0 0 0 1 1 4 6 6 7 7 11 14 14 14))
--> 5
```

This function takes two arguments: a real number  $x$  and a list  $L$  of real numbers. It returns the index of the first element of  $L$  which is greater than or equal to  $x$ .

**is-maximal-translatable-pattern**

Started, last checked	23/7/2009, 23/7/2009
Location	Projection
Calls	difference-list, maximal-translatable-pattern
Called by	
Comments/see also	A more efficient implementation is required.

Example:

```
(is-maximal-translatable-pattern
 '((0 1/2) (1/2 1/2))
 '((0 1/2) (1/2 1/2) (1 1/2) (1 1) (2 3) (5 1/2)
  (11/2 1/2)))
--> (5 0)
```

Two arguments are supplied to this function: a pattern  $P$  and a dataset  $D$ . If  $P$  is a maximal translatable pattern in  $D$  for some vector  $\mathbf{u}$ , then  $\mathbf{u}$  is returned. NIL is returned otherwise.

## maximal-translatable-pattern

Started, last checked	23/7/2009, 23/7/2009
Location	Projection
Calls	add-two-lists, subtract-two-lists, vector<vector
Called by	is-maximal-translatable-pattern
Comments/see also	Should be deprecated by implementing a version analogous to translators-of-pattern-in-dataset from Ukkonen et al. (2003). See also maximal-translatable-pattern-mod-2nd-n.

Example:

```
(maximal-translatable-pattern
 '(2 0)
 '((0 1/2) (0 1) (1 1) (2 1/2) (2 1) (3 2)))
--> ((0 1) (0 1/2))
```

This function assumes that the dataset is sorted ascending. This enables a more efficient search for the maximal translatable pattern of an arbitrary vector  $\mathbf{u}$ , searching in some dataset  $D$ , defined by  $\text{MTP}(\mathbf{u}, D) = \{\mathbf{d} \in D : \mathbf{d} + \mathbf{u} \in D\}$ .

## nth-list-index

Started, last checked	23/7/2009, 23/7/2009
Location	Projection
Calls	
Called by	orthogonal-projection-not-unique-equalp
Comments/see also	

Example:

```
(nth-list-index '(1 1 0 1 0))
--> (0 1 3)
```

This function returns the value of the increment  $i$  if the  $i$ th element of the input list is equal to 1.

**orthogonal-projection-not-unique-equalp**

Started, last checked	23/7/2009, 23/7/2009
Location	Projection
Calls	nth-list, nth-list-index
Called by	orthogonal-projection-unique-equalp
Comments/see also	

Example:

```
(orthogonal-projection-not-unique-equalp
 '( (2 4 -1 6 9) (0 0 4 2 -7) (-3 -2 -1 -1 1)
   (12 0 -7 5 3) (1 2 3 4 3) (1 2 5 4 5))
 '(1 1 0 1 0))
--> ((2 4 6) (0 0 2) (-3 -2 -1) (12 0 5) (1 2 4)
      (1 2 4))
```

Given a set of vectors (all members of the same  $n$ -dimensional vector space), and an  $n$ -tuple of zeros and ones indicating a particular orthogonal projection, this function returns the projected set of vectors.

**orthogonal-projection-unique-equalp**

Started, last checked	23/7/2009, 23/7/2009
Location	Projection
Calls	orthogonal-projection-not-unique-equalp, sort-dataset-asc
Called by	
Comments/see also	

Example:

```
(orthogonal-projection-unique-equalp
 '( (2 4 -1 6 9) (0 0 4 2 -7) (-3 -2 -1 -1 1)
   (12 0 -7 5 3) (1 2 3 4 3) (1 2 5 4 5)
   (12 0 -6 5 4) (-3 -2 1 -1 0) (12 0 -7 5 4))
 '(1 1 0 1 0))
--> ((2 4 6) (0 0 2) (-3 -2 -1) (12 0 5) (1 2 4))
```

Given a set of vectors (all members of the same  $n$ -dimensional vector space), and an  $n$ -tuple of zeros and ones indicating a particular orthogonal projection, this function returns the projected set of vectors. Coincidences are reduced to single vectors.

**pair-off-lists**

Started, last checked	23/7/2009, 23/7/2009
Location	Projection
Calls	
Called by	
Comments/see also	

Example:

```
(pair-off-lists '("asc" "asc" "asc") '(0 1 2))
--> (("asc" 0) ("asc" 1) ("asc" 2))
```

Two lists  $A$  and  $B$  of equal length are provided as arguments to this function. The first element  $a_1$  of  $A$  is paired off with the first element  $b_1$  of  $B$  to become the first sublist of a new list, and so on for  $a_2$  and  $b_2$ ,  $a_3$  and  $b_3$ .

**test-equal<subset**

Started, last checked	23/7/2009, 23/7/2009
Location	Projection
Calls	index-1st-sublist-item<=, index-1st-sublist-item>=, my-last, nth-list-of-lists, test-equal<list-elements
Called by	
Comments/see also	

Example:

```
(test-equal<subset '((4 6) (6 5) (6 5) (6 7))
'((0 1) (0 2) (1 3) (1 4) (4 6) (6 5) (6 7)
(7 9) (7 10) (11 11) (14 1) (14 3) (14 14)))
--> T
```

There are two arguments to this function, both lists of  $n$ -tuples. If when written as sets, the first argument is a subset of the second, then T is returned. Otherwise NIL is returned (and an empty first argument is permissible). The < in the function name indicates that a subfunction, test-equal<list-elements, assumes an argument has been sorted ascending by each of its elements.



### 4.3.2 Musical properties

These functions aid the calculation musical attributes, such as the number of intervallic leaps in a melody. Some of the attributes are implementations of definitions from Pearce and Wiggins (2007); von Hippel (2000); Eerola and North (2000).

#### **cons-ith-while-floor-jth-constantp**

Started, last checked	19/10/2009, 19/10/2009
Location	Musical properties
Calls	
Called by	density
Comments/see also	cons-ith-while-jth-constantp

Example:

```
(cons-ith-while-floor-jth-constantp
 '((13 55) (13 60) (13 64) (27/2 63) (14 55) (15 55)
   (15 59) (15 65) (16 55) (17 72) (18 55) (19 55)
   (22 55) (23 60) (24 55) (24 59) (25 55)) 1 0)
--> (55 60 64 63)
```

This function makes a list from the *i*th item of each list in a list of lists, so long as the floor of the *j*th item is constant.

#### **cons-ith-while-jth-constantp**

Started, last checked	19/10/2009, 19/10/2009
Location	Musical properties
Calls	
Called by	top-line
Comments/see also	cons-ith-while-floor-jth-constantp

Example:

```
(cons-ith-while-jth-constantp
 '((13 55) (13 60) (13 64) (14 55) (15 55) (15 59)
   (15 65) (16 55) (17 72) (18 55) (19 55) (22 55)
   (23 60) (24 55) (24 59) (25 55) (25 67)) 1 0)
--> (55 60 64)
```

This function makes a list from the  $i$ th item of each list in a list of lists, so long as the  $j$ th item is constant.

## density

Started, last checked	19/10/2009, 19/10/2009
Location	Musical properties
Calls	cons-ith-while-floor-jth-constantp
Called by	rhythmic-density
Comments/see also	

Example:

```
(density
 '((13 55) (13 60) (13 64) (27/2 63) (14 55)) 13)
--> 4
```

In a pattern  $P = \{\mathbf{p}_1, \mathbf{p}_2, \dots, \mathbf{p}_l\}$ , let  $\mathbf{p}_i$  have ontime  $x_i$ ,  $i = 1, 2, \dots, l$ . The tactus beats are then the integers from  $a = \lfloor x_1 \rfloor$  to  $b = \lfloor x_l \rfloor$ , assuming that beats coincide with integer ontimes and that the bottom number in the time signature does not change over the course of the pattern. The rhythmic density of the pattern at beat  $c \in [a, b]$ , denoted  $\rho(P, c)$ , is given by the cardinality of the set of all pattern points such that  $\lfloor x_i \rfloor = c$ .

## intervallic-leaps

Started, last checked	19/10/2009, 19/10/2009
Location	Musical properties
Calls	spacing-items, top-line
Called by	
Comments/see also	small-intervals

Example:

```
(intervallic-leaps
 '((13 57) (13 60) (13 62) (14 57) (15 57) (15 59)
   (15 63) (16 57) (17 67) (18 57) (19 57) (22 57)
   (23 60) (24 57) (24 59) (25 57) (25 64)))
--> 7
```

This variable counts the number of intervallic leaps present in the melody line of a pattern, the intuition being that leaping melodies may be rated as

more noticeable or important. Any interval larger than a major third counts, and the same ‘top- line’ rule as in the function `small-intervals` is observed.

### max-pitch-centre

Started, last checked	19/10/2009, 19/10/2009
Location	Musical properties
Calls	mean, nth-list-of-lists
Called by	
Comments/see also	

Example:

```
(max-pitch-centre
 '( ((0 60) (1 61)) ((3 48) (4 49))) 1
 '( ((0 60) (1 61) (2 62) (3 48) (3 57) (4 49)))
--> 23/3
```

Pitch centre is defined as ‘the absolute distance, in semitones, of the mean pitch of a [pattern]...from the mean pitch of the dataset’ (Pearce and Wiggins, 2007, p. 78). By taking the maximum pitch centre over all occurrences of a pattern, I hope to isolate either unusually high, or unusually low occurrences.

### pitch-centre

Started, last checked	19/10/2009, 19/10/2009
Location	Musical properties
Calls	mean, nth-list-of-lists
Called by	
Comments/see also	

Example:

```
(pitch-centre
 '(60 61 62) '( ((0 60) (1 61) (2 62) (3 48) (3 57)))
--> 17/5
```

Pitch centre is defined as ‘the absolute distance, in semitones, of the mean pitch of a [pattern]...from the mean pitch of the dataset’ (Pearce and Wiggins, 2007, p. 78). By taking the maximum pitch centre over all occurrences of a pattern, I hope to isolate either unusually high, or unusually low occurrences.

**pitch-range**

Started, last checked	19/10/2009, 19/10/2009
Location	Musical properties
Calls	nth-list-of-lists, range
Called by	
Comments/see also	

Example:

```
(pitch-range '((0 60) (1 61) (3 62)) 1)
--> 2
```

Pitch range is the range in semitones of a pattern.

**restn**

Started, last checked	19/10/2009, 19/10/2009
Location	Musical properties
Calls	
Called by	rhythmic-density, top-line
Comments/see also	

Example:

```
(restn '((13 55) (13 60) (13 64) (14 55) (15 55)) 3)
--> ((14 55) (15 55))
```

Applies the function rest  $n$  times.

**rhythmic-density**

Started, last checked	19/10/2009, 19/10/2009
Location	Musical properties
Calls	density, my-last, restn
Called by	
Comments/see also	

Example:

```
(rhythmic-density
 '((13 55) (13 60) (13 64) (27/2 63) (14 55) (17 48)))
--> 6/5
```

The rhythmic density of a pattern is defined as ‘the mean number of events per tactus beat’ (Pearce and Wiggins, 2007, p. 78). See the function density for further definitions.

### rhythmic-variability

Started, last checked	19/10/2009, 19/10/2009
Location	Musical properties
Calls	nth-list-of-lists, sd
Called by	
Comments/see also	

Example:

```
(rhythmic-variability
 '((0 64 1) (1 55 1/2) (1 65 1) (2 55 1/2) (2 72 1/3)
   (3 55 1) (4 55 2) (5 55 1/2) (5 60 1)
   (6 59 1/3) (6 67 1/2)) 2)
--> 0.5354223
```

The rhythmic variability of a pattern is defined as ‘the degree of change in note duration (i.e., the standard deviation of the log of the event durations)’ (Pearce and Wiggins, 2007, p. 78). The intuition is that patterns with much rhythmic variation are likely to be noticeable.

### small-intervals

Started, last checked	19/10/2009, 19/10/2009
Location	Musical properties
Calls	spacing-items, top-line
Called by	
Comments/see also	intervallic-leaps

Example:

```
(small-intervals
 '((13 57) (13 60) (13 62) (14 57) (15 57) (15 59)
   (15 63) (16 57) (17 67) (18 57) (19 57) (22 57))
```

```
(23 60) (24 57) (24 59) (25 57) (25 64)))
--> 3
```

The `small-intervals` variable counts the number of such intervals present in the melody line of a pattern, the intuition being that scalar, static or stepwise melodies may be rated as more noticeable or important. As sometimes the melody is not obvious in polyphonic music, I use a ‘top-line’ rule: at each of the pattern’s distinct ontimes there will be at least one datapoint present. At this ontime the melody takes the value of the maximum morphetic pitch number present.

### top-line

Started, last checked	19/10/2009, 19/10/2009
Location	Musical properties
Calls	cons-ith-while-jth-constantp, max-item, restn
Called by	intervallic-leaps, small-intervals
Comments/see also	

Example:

```
(top-line
'((13 55) (13 60) (13 64) (14 55) (15 55) (15 59)
  (15 65) (16 55) (17 72) (18 55) (19 55) (22 55)
  (23 60) (24 55) (24 59) (25 55) (25 67)) 1)
--> (64 55 65 55 72 55 55 55 60 59 67)
```

For each distinct ontime, this function returns the maximum pitch as a member of a list.

### 4.3.3 Empirical preliminaries

These functions make it possible to form empirical  $n$ -dimensional distributions. One of the applications of these empirical distributions is to adapt pattern interest (Conklin and Bergeron, 2008) for polyphonic music.

**accumulate-to-mass**

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	
Called by	present-to-mass
Comments/see also	add-to-mass

Example:

```
(accumulate-to-mass
 '(6 72) '((6 72) 1/4)
 '(((6 72) 1/4) ((4 0.1) 1/2)) 1/4)
--> (((6 72) 1/2) ((4 0.1) 1/2))
```

This function takes four arguments: a datapoint **d**; an element (to be updated) of the emerging empirical probability mass function  $L$ ;  $L$  itself is the third argument; and the fourth argument is  $\mu$ , the reciprocal of the number of datapoints that have been observed. This function has been called because **d** is new to the empirical mass—it is added with mass  $\mu$ .

**add-to-mass**

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	
Called by	present-to-mass
Comments/see also	accumulate-to-mass

Example:

```
(add-to-mass '(6 72) '(((4 0.1) 2/3)) 1/3)
--> (((6 72) 1/3) ((4 0.1) 2/3))
```

This function takes three arguments: a datapoint **d**; an emerging empirical probability mass function  $L$ ; and the third argument is  $\mu$ , the reciprocal of the number of datapoints that have been observed. This function has been called because **d** already forms part  $\lambda$  of the mass. This element is increased to  $\lambda + \mu$ .

## direct-product-of-n-sets

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	direct-product-of-two-sets
Called by	likelihood-of-pattern-or-translation, likelihood-of-translations-geometric-mean
Comments/see also	

Example:

```
(direct-product-of-n-sets
 '( (1 2) ((59) (60)) (-4 -2)))
--> ((1 59 -4) (1 59 -2) (1 60 -4) (1 60 -2) (2 59 -4)
      (2 59 -2) (2 60 -4) (2 60 -2)).
```

This function takes a single argument (assumed to be a list of sets of numbers or sets of sets), and returns the direct product of these sets.

## direct-product-of-two-sets

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	
Called by	direct-product-of-n-sets
Comments/see also	

Example:

```
(direct-product-of-two-sets '(1/3 1 2) '(59 60))
--> ((1/3 59) (1/3 60) (1 59) (1 60) (2 59) (2 60))
```

This function takes two arguments (assumed to be sets of numbers or sets of sets), and returns the direct product of these sets.

## empirical-mass

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	present-to-mass
Called by	likelihood-of-pattern-or-translation, likelihood-of-translations-geometric-mean
Comments/see also	



Example:

```
(empirical-mass '((4 0) (4 0) (0 4)) '())
--> (((0 4) 1/3) ((4 0) 2/3))
```

This function returns the empirical probability mass function  $L$  for a dataset listed  $\mathbf{d}_1^*, \mathbf{d}_2^*, \dots, \mathbf{d}_n^*$ .

### events-with-these-ontime-others

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	events-with-this-ontime-other, index-1st-sublist-item>=, nth-list-of-lists, my-last
Called by	
Comments/see also	

Example:

```
(events-with-these-ontime-others
 '((6 63) (7 96) (9 112))
 '((23/4 86 1/4 2 46) (6 55 1/2 1 37)
 (6 63 1/3 1 37) (6 63 1/2 2 34) (7 91 1 1 56)
 (7 96 1/2 1 73) (7 96 1 1 95) (7 108 3/2 2 50)
 (17/2 109 1/2 2 49) (9 95 1 1 71)
 (9 98 1 1 71) (9 102 1 1 71) (9 112 3/4 2 73)) 1 2)
--> ((6 1/3) (6 1/2) (7 1/2) (7 1) (9 3/4))
```

The first argument to this function is a pattern, under the projection of ontime and MIDI note number (in which case the variable other-index is 1) or morphetic pitch (in which case other-index is 2). The corresponding members of the full dataset are sought out and returned as ontime-other pairs.

### events-with-this-ontime-other

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	
Called by	events-with-these-ontime-others
Comments/see also	

Example:

```
(events-with-this-ontime-other
 '(7 96)
 '((23/4 86 1/4 2 46) (6 55 1/2 1 37)
   (6 63 1/3 1 37) (6 63 1/2 2 34) (7 91 1 1 56)
   (7 96 1/2 1 73) (7 96 1 1 95) (7 108 3/2 2 50)
   (17/2 109 1/2 2 49) (9 95 1 1 71)
   (9 98 1 1 71) (9 102 1 1 71) (9 112 3/4 2 73)) 1 2)
--> ((7 1/2) (7 1))
```

The first argument to this function is a datapoint, under the projection of ontime and MIDI note number (in which case the variable other-index is 1) or morphetic pitch (in which case other-index is 2). The corresponding members of the full dataset are sought out and returned as ontime-other pairs.

## likelihood-of-pattern-or-translation

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	constant-vector, direct-product-of-n-sets, empirical-mass, likelihood-of-subset, orthogonal-projection-not-unique-equalp, potential-n-dim-translations
Called by	
Comments/see also	likelihood-of-translations-geometric-mean

Example:

```
(likelihood-of-pattern-or-translation
 '((0 60 60 1) (1 62 61 1/2) (2 64 62 1/3)
   (3 60 60 1))
 '((0 60 60 1) (1 62 61 1/2) (2 64 62 1/3) (3 60 60 1)
   (4 62 61 1) (5 64 62 1/2) (6 66 63 1/3) (7 62 61 1)
   (8 69 65 3) (11 59 59 1) (12 60 60 1)))
--> 9/14641 + 4/14641 = 13/14641
```

```
(likelihood-of-pattern-or-translation
 '((0 60 1) (1 61 1) (2 62 1) (3 60 1)))
```

```
'((0 60 1) (1 61 1) (1 66 1/2) (3/2 67 1/2) (2 62 1)
  (2 68 1) (5/2 66 1/2) (3 60 1)))
--> 1/4*1/8*1/8*1/4 = 1/1024
```

```
(likelihood-of-pattern-or-translation
'((0 60) (1 61) (2 62) (3 60))
'((0 60) (1 61) (1 66) (3/2 67) (2 62)
  (2 68) (5/2 66) (3 60)))
--> 1/4*1/8*1/8*1/4 + 1/4*1/8*1/8*1/4 = 1/512
```

```
(likelihood-of-pattern-or-translation
'((0 1) (1 1) (2 1) (3 1))
'((0 1) (1 1) (1 1/2) (3/2 1/2) (2 1)
  (2 1/2) (5/2 1/2) (3 1)))
--> 1/16 + 1/16 = 1/8
```

This function takes a pattern and the dataset in which the pattern occurs. It calculates the potential translations of the pattern in the dataset and returns the sum of their likelihoods.

### likelihood-of-subset

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	
Called by	likelihood-of-pattern-or-translation
Comments/see also	likelihood-of-subset-geometric-mean

Example:

```
(likelihood-of-subset
'((60 60 1) (62 61 1/2) (64 62 1/3) (60 60 1))
'(((60 60 1) 3/11) ((62 61 1/2) 1/11)
  ((64 62 1/3) 1/11) ((62 61 1) 2/11)
  ((64 62 1/2) 1/11) ((66 63 1/3) 1/11)
  ((69 65 3) 1/11) ((59 59 1) 1/11)))
--> 9/14641
```

This function takes a pattern-palette and the empirical mass for the dataset-palette in which the pattern occurs. The product of the individual masses is returned, and reverts to zero if any pattern points do not occur in the empirical mass.

**likelihood-of-subset-geometric-mean**

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	
Called by	likelihood-of-translations-geometric-mean
Comments/see also	likelihood-of-subset

Example:

```
(likelihood-of-subset-geometric-mean
'((60 60 1) (62 61 1/2) (64 62 1/3) (60 60 1)) 1/4
'(((60 60 1) 3/11) ((62 61 1/2) 1/11)
((64 62 1/3) 1/11) ((62 61 1) 2/11)
((64 62 1/2) 1/11) ((66 63 1/3) 1/11)
((69 65 3) 1/11) ((59 59 1) 1/11)))
--> 0.1574592
```

This function takes a pattern-palette, the reciprocal length of that pattern, and the empirical mass for the dataset-palette in which the pattern occurs. The geometric mean of the individual masses is returned, and reverts to zero if any pattern points do not occur in the empirical mass.

**likelihood-of-translations-geometric-mean**

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	constant-vector, direct-product-of-n-sets, empirical-mass, likelihood-of-subset-geometric-mean, orthogonal-projection-not-unique-equalp, potential-n-dim-translations, translation
Called by	
Comments/see also	

Example:

```
(likelihood-of-translations-geometric-mean
'((0 60 60 1) (1 62 61 1/2) (2 64 62 1/3)
(3 60 60 1))
'((0 60 60 1) (1 62 61 1/2) (2 64 62 1/3) (3 60 60 1))
```

```
(4 62 61 1) (5 64 62 1/2) (6 66 63 1/3) (7 62 61 1)
(8 69 65 3) (11 59 59 1) (12 60 60 1)))
--> (9/14641)^(1/4) + (4/14641)^(1/4) = 0.2860241
```

```
(likelihood-of-translations-geometric-mean
'((0 60 1) (1 61 1) (2 62 1) (3 60 1))
'((0 60 1) (1 61 1) (1 66 1/2) (3/2 67 1/2) (2 62 1)
(2 68 1) (5/2 66 1/2) (3 60 1)))
--> (1/4*1/8*1/8*1/4)^(1/4) = 0.17677668
```

```
(likelihood-of-translations-geometric-mean
'((0 60) (1 61) (2 62) (3 60))
'((0 60) (1 61) (1 66) (3/2 67) (2 62)
(2 68) (5/2 66) (3 60)))
--> (1/4*1/8*1/8*1/4)^(1/4) + (1/4*1/8*1/8*1/4)^(1/4)
= 0.35355335
```

```
(likelihood-of-translations-geometric-mean
'((0 1) (1 1) (2 1) (3 1))
'((0 1) (1 1) (1 1/2) (3/2 1/2) (2 1)
(2 1/2) (5/2 1/2) (3 1)))
--> (1/16)^(1/4) + (1/16)^(1/4) = 1.
```

This function takes a pattern and the dataset in which the pattern occurs. It calculates the potential translations of the pattern in the dataset and returns the sum of the geometric means of their likelihoods.

Note that this is not really a likelihood, as it is possible for probabilities to be greater than 1.

## likelihood-of-translations-reordered

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	constant-vector, direct-product-of-n-sets, likelihood-of-subset, orthogonal-projection-not-unique-equalp, potential-n-dim-translations, translation
Called by	evaluate-variables-of-pattern2hash
Comments/see also	

Example:

```
(likelihood-of-translations-reordered
'((0 60 60 1) (1 62 61 1/2) (2 64 62 1/3)
  (3 60 60 1))
'((60 60 1) (62 61 1/2) (64 62 1/3) (60 60 1)
  (62 61 1) (64 62 1/2) (66 63 1/3) (62 61 1)
  (69 65 3) (59 59 1) (60 60 1))
'(((60 60 1) 3/11) ((59 59 1) 1/11) ((69 65 3) 1/11)
  ((62 61 1) 2/11) ((66 63 1/3) 1/11)
  ((64 62 1/2) 1/11) ((64 62 1/3) 1/11)
  ((62 61 1/2) 1/11)))
--> 9/14641 + 4/14641 = 13/14641
```

This function takes a pattern and the dataset in which the pattern occurs. It calculates the potential translations of the pattern in the dataset and returns the sum of their likelihoods. Note the order (and mandate) of the arguments is different to the original version of this function, which is called `likelihood-of-pattern-or-translation`.

## potential-1-dim-translations

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	constant-vector, nth-list-of-lists, orthogonal-projection-unique-equalp
Called by	potential-n-dim-translations
Comments/see also	

Example:

```
(potential-1-dim-translations
'(60 60 1)
'((60 60 1) (62 61 1/2) (64 62 1/3) (60 60 1)
  (62 61 1) (64 62 1/2) (66 63 1/3) (62 61 1)
  (69 65 3) (59 59 1) (60 60 1)) 0)
--> (-1 0 2 4 6 9)
```

This function takes three arguments, the first member of a pattern palette, the dataset palette and an index  $i$ . First of all, the dataset is projected uniquely along the dimension of index, creating a vector  $\mathbf{u}$ . Then the  $i$ th member of the first-pattern-palette is subtracted from each member of  $\mathbf{u}$ , giving a list of potential translations along this dimension.

**potential-n-dim-translations**

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	add-to-list, first-n-naturals, potential-1-dim-translations
Called by	likelihood-of-pattern-or-translation, likelihood-of-translations-geometric-mean
Comments/see also	

Example:

```
(potential-n-dim-translations
 '(60 60 1)
 '((60 60 1) (62 61 1/2) (64 62 1/3) (60 60 1)
   (62 61 1) (64 62 1/2) (66 63 1/3) (62 61 1)
   (69 65 3) (59 59 1) (60 60 1)))
--> ((-1 0 2 4 6 9) (-1 0 1 2 3 5) (-2/3 -1/2 0 2))
```

This function takes two arguments, the first member of a pattern palette, the dataset palette and an index. The function `potential-n-dim-translations` is applied recursively to an increment.

**present-to-mass**

Started, last checked	20/10/2009, 20/10/2009
Location	Empirical preliminaries
Calls	accumulate-to-mass, add-to-mass
Called by	empirical-mass
Comments/see also	

Example:

```
(present-to-mass '(0 4) '(((4 0) 2/3)) 1/3)
--> (((0 4) 1/3) ((4 0) 2/3))
```

This function takes three arguments: a datapoint  $\mathbf{d}$ , an empirical probability mass function  $L$  which is in the process of being calculated, and  $\mu$ , the reciprocal of the number of datapoints that have been observed. If  $\mathbf{d}$  is new to the empirical mass, it is added with mass  $\mu$ , and if it already forms part  $\lambda$  of the mass, then this component is increased to  $\lambda + \mu$ .

### 4.3.4 Evaluation heuristics

These functions implement definitions of coverage, compactness, and compression ratio (Meredith et al., 2003; Forth and Wiggins, 2009).

#### compactness

Started, last checked	13/1/2010, 13/1/2010
Location	Evaluation heuristics
Calls	index-item-1st-occurs, my-last, points-in-convex-hull, set-difference-multidimensional-sorted-asc
Called by	compact-subpatterns-more-output
Comments/see also	??

Example:

```
(compactness
 '( (1 2) (2 4) ) '( (1 2) (2 -1) (2 4) (3 6) (5 2) )
 "lexicographic")
--> 2/3

(setq
 dataset-sorted
 '((-4.13 -2.62) (-3.89 -4.13) (-3.82 2.71)
 (-2.67 0.32) (-2.65 -3.48) (-1.71 -1.13)
 (-1.33 0.3) (-1.3 -4.0) (0.83 1.41) (1.27 -3.95)
 (1.4 -2.94) (1.53 0.51) (1.83 2.89) (1.85 -0.94)
 (2.22 -2.93) (2.34 2.81) (2.4 -0.15) (2.49 -2.71)
 (3.66 -2.05) (4.7 -3.99)))
(setq
 pattern-sorted
 '((-2.67 0.32) (-2.65 -3.48) (-1.71 -1.13)
 (1.27 -3.95) (1.4 -2.94) (1.53 0.51) (3.66 -2.05)))
(compactness
 pattern-sorted dataset-sorted "lexicographic")
--> 7/16

(compactness
 pattern-sorted dataset-sorted "convex hull")
--> 7/11
```



The ratio of the number of points in the pattern to the number of points in the region spanned by the pattern. Both pattern and dataset are assumed to be sorted ascending. At present two definitions of region ("lexicographic" and "convex hull") are admissible.

There is a plot for the above example in the Example Files folder, entitled `convex_hull.pdf`. NB we define region as the lexicographic region first, as a point is in the convex hull of the pattern only if it is in its lexicographic region (ought to prove this assertion). This avoids determining in-polygon for each point in the dataset, which would require more time.

### **compactness-min-max**

Started, last checked	13/1/2010, 13/1/2010
Location	Evaluation heuristics
Calls	index-item-1st-occurs, my-last
Called by	compactness-max
Comments/see also	compactness

Example:

```
(compactness-min-max
'((1 2) (2 4)) '((1 2) (2 -1) (2 4) (3 6) (5 2))
0.2 1 "straight down")
--> 2/3
```

The ratio of the number of points in the pattern to the number of points in the region spanned by the pattern. Both pattern and dataset are assumed to be sorted ascending. At present the only admissible definition of region is 'straight down' (which means 'lexicographic', cf. Def. 2.10 in Collins, 2011).

### **compactness-max**

Started, last checked	13/1/2010, 13/1/2010
Location	Evaluation heuristics
Calls	compactness-min-max, translation
Called by	heuristics-pattern-translators-pair
Comments/see also	

Example:

```
(compactness-max
```

```
'((1 2) (2 4)) '((0 0) (1 2) (3 -2))
'((1 2) (2 -1) (2 0) (2 4) (3 0) (3 1) (3 3) (3 6)
  (4 0) (5 1) (5 2))
0.2 1 "straight down" 2)
--> 2/3
```

The function compactness-min-max is applied to each occurrence of a pattern and the maximum compactness returned.

### compression-ratio

Started, last checked	13/1/2010, 13/1/2010
Location	Evaluation heuristics
Calls	coverage
Called by	heuristics-pattern-translators-pair
Comments/see also	

Example:

```
(compression-ratio
'((1 2) (2 4)) '((0 0) (1 2) (3 -2))
'((1 2) (2 -1) (2 0) (2 4) (3 0) (3 1) (3 3) (3 6)
  (4 0) (5 1) (5 2))
0.2 1 5)
--> 1
```

The compression ratio that can be achieved by representing the set of points covered by all occurrences of a pattern by specifying just one occurrence of the pattern together with all the non- zero vectors by which the pattern is translatable within the dataset.

### cover-ratio

Started, last checked	13/1/2010, 13/1/2010
Location	Evaluation heuristics
Calls	coverage
Called by	heuristics-pattern-translators-pair
Comments/see also	

Example:

```
(cover-ratio
'((1 2) (2 4)) '((0 0) (1 2))
'((1 2) (2 4) (3 6) (5 2) (6 1)) 0.2 t t)
--> 3/5
```

The ratio between the number of uncovered datapoints in the dataset that are members of occurrences of the pattern, to the total number of uncovered datapoints in the dataset.

### coverage

Started, last checked	13/1/2010, 13/1/2010
Location	Evaluation heuristics
Calls	intersection-multidimensional, translations, unions-multidimensional-sorted-asc
Called by	compression-ratio, cover-ratio, heuristics-pattern-translators-pair
Comments/see also	coverage-mod-2nd-n

Example:

```
(coverage
'((1 2) (2 4)) '((0 0) (1 2))
'((1 2) (2 4) (3 6) (5 2) (6 1)) t t)
--> 3
```

The number of datapoints in the dataset that are members of occurrences of the pattern.

### coverage-mod-2nd-n

Started, last checked	13/1/2010, 13/1/2010
Location	Evaluation heuristics
Calls	intersection-multidimensional, translations-mod-2nd-n, unions-multidimensional-sorted-asc
Called by	compression-ratio, cover-ratio, heuristics-pattern-translators-pair
Comments/see also	coverage

Example:

```
(coverage-mod-2nd-n
  '((1 2) (2 4)) '((0 0) (1 2))
  '((1 2) (2 4) (3 6) (5 2) (6 1)) 12 t t)
--> 3
```

The number of datapoints in the dataset that are members of occurrences of the pattern. Translations are carried out modulo the fourth argument.

### heuristics-pattern-translators-pair

Started, last checked	13/1/2010, 13/1/2010
Location	Evaluation heuristics
Calls	compactness-max, compression-ratio, cover-ratio, coverage
Called by	heuristics-pattern-translators-pairs
Comments/see also	

Example:

```
(heuristics-pattern-translators-pair
  '((1 2) (2 4)) '((0 0) (1 2) (3 -2))
  '((1 2) (2 -1) (2 0) (2 4) (3 0) (3 1) (3 3) (3 6)
    (4 0) (5 1) (5 2)) '(t t t t t t)
  0.2 0.25 1 0.25 1 "straight down" 11)
--> (5 5/11 1 2/3 2 3)
```

A pattern and its translators in a projected dataset are supplied as arguments to this function, along with an indicator vector that indicates which heuristics out of coverage, cover ratio, compression ratio, compactness,  $|P|$  and  $|T(P, D)|$  should be calculated.

### heuristics-pattern-translators-pairs

Started, last checked	13/1/2010, 13/1/2010
Location	Evaluation heuristics
Calls	heuristics-pattern-translators-pair
Called by	musicological-heuristics
Comments/see also	

Example:

```
(heuristics-pattern-translators-pairs
 '( (((1 2) (2 4)) ((0 0) (1 2) (3 -2)))
   (((1 2) (2 0)) ((0 0) (2 0))) )
 '( ((1 2) (2 -1) (2 0) (2 4) (3 0) (3 1) (3 2) (3 6)
     (4 0) (5 1) (5 2)) '(t t t t t t)
   0.25 0.25 1 0.25 1 "straight down" 11)
--> ((5 5/11 1 2/3 2 3) (4 4/11 1 2/3 2 2))
```

The function `heuristics-pattern-translators-pair` is applied recursively to pairs of pattern-translators.

### musicological-heuristics

Started, last checked	13/1/2010, 13/1/2010
Location	Evaluation heuristics
Calls	heuristics-pattern-translators-pairs, normalise-0-1
Called by	
Comments/see also	

Example:

```
(musicological-heuristics
 '( (((1 2) (2 4)) ((0 0) (1 2) (3 -2)))
   (((1 2) (2 0)) ((0 0) (2 0)))
   (((1 2) (2 4) (4 0)) ((0 0) (1 2) (2 -4))) )
 '( ((1 2) (2 -1) (2 0) (2 4) (3 -2) (3 0) (3 1)
     (3 2) (3 6) (4 0) (5 1) (5 2) (6 -4))
   0.25 1 0.25 1 "straight down" 11)
--> ((1 1 1) (1 1 0))
```

The function `heuristics-pattern-translators-pairs` is applied to pattern-translator pairs with the heuristics indicator set to compression ratio and compactness (max). The values are normalised (linearly) to  $[0, 1]$  and returned as two lists.

## 4.4 Pattern discovery

### 4.4.1 Structural induction mod

The functions below include two early implementations of SIA (Structural induction algorithm, Meredith et al., 2002), the second version working modulo  $n$ .

#### **add-two-lists-mod-2nd-n**

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	add-two-lists
Called by	maximal-translatable-pattern-mod-2nd-n, test-equal<potential-translator-mod-2nd-n, translation-mod-2nd-n
Comments/see also	

Example:

```
(add-two-lists-mod-2nd-n '(4 2 -3) '(8 60 -3) 12)
--> (12 2 -6)
```

Adds two lists element-by-element, treating the second elements of each list modulo  $n$ .

#### **assoc-files**

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	read-from-file
Called by	SIA-reflected, SIA-reflected-mod-2nd-n
Comments/see also	

Example:

```
(assoc-files
 '(2 (2 6)) nil 1 1
 (concatenate
  'string
  *MCStylistic-Oct2010-example-files-path*
  "/Racchman-Oct2010 example/initial-states.txt"))
```

```
--> (1
      ((2 (2 6))
        (NIL NIL "C-17-4"
          ((1 57 58 1 1 2 0) (1 59 59 1 1 2 1)
            (1 65 63 1 1 2 2))))))
```

The arguments to this function are a probe, a path&name, and a positive integer. The integer indicates how many files there are with the specified path&name. Each one, assumed to contain an assoc- list, is read in turn and probed for the presence of the argument in probe. If it is present the relevant row is returned.

### check-potential-translators-mod-2nd-n

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	read-from-file
Called by	translators-of-pattern-in-dataset-mod-2nd-n
Comments/see also	check-potential-translators

Example:

```
(check-potential-translators-mod-2nd-n
 '(3 4) '((0 0) (1 2) (1 5) (2 9))
 '((0 0) (3 4) (4 9) (5 1)) 12)
--> ((0 0) (1 5) (2 9))
```

This function is very similar to the function check-potential-translators. The difference is that the translation of the 2nd element is being carried out modulo n.

### dataset-restricted-to-m-in-nth

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	
Called by	
Comments/see also	

Example:

```
(dataset-restricted-to-m-in-nth
'((12 41 49 1 1) (12 81 72 2 0) (13 53 56 1 1)
  (14 55 57 1 1) (14 74 68 2 0) (15 43 50 1 1)
  (16 36 46 2 1) (16 72 67 1/2 0)) 1 4)
--> ((12 41 49 1 1) (13 53 56 1 1) (14 55 57 1 1)
      (15 43 50 1 1) (16 36 46 2 1))
```

This function acts on a list of sublists. The  $n$ th item of each sublist is tested for equality (`equalp`) with the second argument. If it is equal it is retained, otherwise it is not included in the output.

### maximal-translatable-pattern-mod-2nd-n

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	add-two-lists-mod-2nd-n, test-equal<list-elements
Called by	
Comments/see also	As with maximal-translatable-pattern, the implementation could be improved.

Example:

```
(maximal-translatable-pattern-mod-2nd-n
' (2 0) '((0 0) (1 1) (1 2) (2 0) (2 5) (3 1)) 12)
--> ((0 0) (1 1))
```

This function computes the maximal translatable pattern of an arbitrary vector  $\mathbf{u}$ , searching in some dataset  $D$ , and treating the second element of each datapoint modulo  $n$ .

### mod-column

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	firstn, lastn
Called by	test-translation-mod-2nd-n-no-length-check
Comments/see also	

Example:



```
(mod-column
  '((1 2 12 4) (1 2 16 -1) (2 4 32 6) (5 2 50 6)) 7 2)
--> ((1 2 5 4) (1 2 2 -1) (2 4 4 6) (5 2 1 6))
```

The first argument to this function is a list, assumed to contain sublists of equal length. The second argument specifies what modulo will be calculated for the  $n$ th item of each sublist, where  $n$  is given by the third argument.

### restrict-dataset-in-nth-to-xs

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	
Called by	
Comments/see also	

Example:

```
(restrict-dataset-in-nth-to-xs
  '((2 4 -1 6 9) (0 0 4 2 -7) (-3 -2 -1 -1 1)
    (12 0 -7 5 3) (1 2 3 4 3) (1 2 5 4 5)
    (12 0 -6 5 4) (-3 -2 1 -1 0) (12 0 -7 5 4))
  3 '(4 5 6))
--> ((2 4 -1 6 9) (12 0 -7 5 3) (1 2 3 4 3)
    (1 2 5 4 5) (12 0 -6 5 4) (12 0 -7 5 4))
```

The first argument to this function is a dataset. We are interested in the  $n$ th dimension of each vector, where  $n$  is the second argument. A datapoint is retained in the output if its  $n$ th value is a member of the list specified by the third argument. Note it will not recognise 1.0 as 1.

### SIA-reflected

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	assoc-files, subtract-two-lists, update-written-file, write-to-file
Called by	
Comments/see also	SIA-reflected-merge-sort for a more efficient implementation.

Example:

```
(SIA-reflected
'((0 61) (0 65) (1 64) (4 62) (4 66) (5 65) (8 60)
  (8 64) (9 63) (12 56) (13 69) (15 65) (16 57)
  (16 59) (17 64) (19 63))
(concatenate
'string
'MCStylistic-Oct2010-example-files-path*
"/SIA output") 50)
--> 2
```

This function is a version of the SIA algorithm. It is called ‘SIA-reflected’ because the results (pairs of vectors and the corresponding MTPs) are the other way round to the algorithm specified by Meredith et al. (2002). The example causes two files to be created in the specified location.

### SIA-reflected-mod-2nd-n

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	assoc-files, subtract-two-lists-mod-2nd-n, update-written-file, write-to-file
Called by	
Comments/see also	SIA-reflected

Example:

```
(SIA-reflected-mod-2nd-n
'((0 61) (0 65) (1 64) (4 62) (4 66) (5 65) (8 60)
  (8 64) (9 63) (12 56) (13 69) (15 65) (16 57)
  (16 59) (17 64) (19 63))
12
(concatenate
'string
'MCStylistic-Oct2010-example-files-path*
"/SIA mod 2nd output") 50)
--> 2
```

This function is a version of the SIA algorithm that works with a pitch representation modulo  $n$ . The example causes two files to be created in the specified location.

**subtract-list-from-each-list-mod-2nd-n**

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	subtract-two-lists-mod-2nd-n
Called by	translators-of-pattern-in-dataset-mod-2nd-n
Comments/see also	subtract-list-from-each-list

Example:

```
(subtract-list-from-each-list-mod-2nd-n
 '( (8 -2 -3) (4 6 6) (0 0 0) (4 7 -3) ) '(4 7 -3) 12)
--> ((4 3 0) (0 11 9) (-4 5 3) (0 0 0))
```

The function subtract-two-lists-mod-2nd-n is applied recursively to each sub-list in the first list argument, and the second argument.

**subtract-two-lists-mod-2nd-n**

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	subtract-two-lists
Called by	subtract-list-from-each-list-mod-2nd-n
Comments/see also	subtract-two-lists

Example:

```
(subtract-two-lists-mod-2nd-n '(8 60 1) '(4 67 2) 12)
--> (4 5 -1)
```

Subtracts the second list from the first, element-by-element. The subtraction of the second elements is performed modulo  $n$ , where  $n$  is the third argument to the function. It is assumed that the list is at least of length 2.

**test-equal<potential-translator-mod-2nd-n**

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	add-two-lists-mod-2nd-n
Called by	check-potential-translators-mod-2nd-n
Comments/see also	test-equal<potential-translator

Example:

```
(test-equal<potential-translator-mod-2nd-n
  '((0 0) (3 4) (4 9) (5 1)) '(2 9) '(3 4) 12)
--> ((3 4))
```

This function is very similar to the function `test-equal<potential-translator`. The difference is the call to the function `add-two-lists-mod-2nd-n` (as opposed to calling `add-two-lists`), and this requires the inclusion of an extra argument.

### test-translation-mod-2nd-n

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	test-translation-mod-2nd-n-no-length-check
Called by	
Comments/see also	test-translation

Example:

```
(test-translation-mod-2nd-n
  '((2 2) (4 5)) '((11 9) (13 0)) 12)
--> T
```

This function is very similar to the function `test-translation`, except that here the translation in the second dimension is performed modulo the third argument.

### test-translation-mod-2nd-n-no-length-check

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	mod-column, sort-dataset-asc, subtract-two-lists-mod-2nd-n, translation-mod-2nd-n
Called by	test-translation-mod-2nd-n
Comments/see also	test-translation-no-length-check

Example:

```
(test-translation-mod-2nd-n-no-length-check
  '((40 0) (40 10) (43 7)) '((44 7) (44 9) (47 4)) 12)
--> T
```

This function ought to be very similar to the function `test-translation-no-length-check`. However simply altering the translation in the second dimension to modulo  $n$  (the third argument) can be problematic: In the above example, the pitch classes `Bb`, `C`, `G` are a translation of `G`, `A`, `E`, but when these are ordered modulo 12, the `C` and the `Bb` swap positions. The function below accounts for this but will generally take longer to return an answer than `test-translation-no-length-check`.

### **translation-mod-2nd-n**

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	<code>add-two-lists-mod-2nd-n</code>
Called by	<code>test-translation-mod-2nd-n-no-length-check</code> , <code>translations-mod-2nd-n</code>
Comments/see also	<code>translation</code>

Example:

```
(translation-mod-2nd-n
 '( (8 0 3) (9 11 1) (9 4 2)) '(3 3 0) 12)
--> ((11 3 3) (12 2 1) (12 7 2))
```

The first argument is a list of sublists, but we imagine it as a set of vectors (all members of the same  $n$ -dimensional vector space). The second argument—another list—is also an  $n$ -dimensional vector, and this is added to each of the members of the first argument. ‘Added’ means vector addition, that is element-wise, and addition in the second dimension is performed modulo the third argument. The resulting set is a translation of the first argument by the second.

### **translations-mod-2nd-n**

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	<code>translation-mod-2nd-n</code>
Called by	
Comments/see also	<code>translations</code>

Example:

```
(translations-mod-2nd-n
  '((8 0 3) (9 11 1) (9 4 2)) '((0 0 0) (3 3 0)) 12)
--> (((8 0 3) (9 4 1) (9 11 2))
      ((11 3 3) (12 2 1) (12 7 2)))
```

There are three arguments to this function, a pattern, some translators and a modulo argument. The pattern is translated by each translator, modulo  $n$  in the second dimension, and the results returned.

### translators-of-pattern-in-dataset-mod-2nd-n

Started, last checked	15/1/2010, 15/1/2010
Location	Structural induction mod
Calls	check-potential-translators-mod-2nd-n, subtract-list-from-each-list-mod-2nd-n
Called by	
Comments/see also	As with translators-of-pattern-in-dataset, the implementation could be improved.

Example:

```
(translators-of-pattern-in-dataset-mod-2nd-n
  '((8 3) (8 7))
  '((4 7) (8 3) (8 4) (8 7) (9 3) (10 7)
    (11 3) (13 0) (13 4)) 12)
--> ((0 0) (5 9))
```

A pattern and dataset are provided. The translators of the pattern in the dataset are returned.

## 4.4.2 Structural induction merge

These functions implement SIA (Structural Induction Algorithm, Meredith et al., 2002) using a merge sort.

### collect-by-car

Started, last checked	6/9/2010, 6/9/2010
Location	Structural induction merge
Calls	
Called by	collect-by-cars, collect-by-cars-partition
Comments/see also	

Example:

```
(collect-by-car
 '(((1 -14) 7/2 60) ((1 -14) 2 74) ((1 -2) 5/2 64)))
--> ((2 74))
```

A list is the only argument to this function. The car of the first element is compared with the cars of proceeding elements, and these proceeding elements are returned so long as there is equality.

### collect-by-cars

Started, last checked	6/9/2010, 6/9/2010
Location	Structural induction merge
Calls	collect-by-car, restn
Called by	collect-by-cars-partition, SIA-reflected-merge-sort
Comments/see also	

Example:

```
(collect-by-cars
 '(((1/2 -14) 7/2 60) ((1/2 -10) 2 74)
 ((1/2 -2) 5/2 64) ((1/2 -2) 3 62) ((1/2 2) 1/2 67)
 ((1/2 2) 1 69) ((1/2 3) 3/2 71) ((1/2 14) 0 53)
 ((1 21) 2 74) ((1 21) 3 62) ((1 21) 4 46)
 ((1 -7) 3/2 71) ((1 -4) 5/2 64) ((1 4) 1/2 67)))
--> (((1/2 -14) (7/2 60)) ((1/2 -10) (2 74))
 ((1/2 -2) (5/2 64) (3 62))
 ((1/2 2) (1/2 67) (1 69))
 ((1/2 3) (3/2 71)) ((1/2 14) (0 53))
 ((1 21) (2 74) (3 62) (4 46))
 ((1 -7) (3/2 71)) ((1 -4) (5/2 64))
 ((1 4) (1/2 67)))
```

A list is the only argument to this function. The function collect-by-car is applied to each new vector appearing as the car of each element of the list.

## collect-by-cars-partition

Started, last checked	6/9/2010, 6/9/2010
Location	Structural induction merge
Calls	collect-by-cars, write-to-file-append
Called by	SIA-reflected-merge-sort
Comments/see also	

Example:

```
(collect-by-cars-partition
'(((1/2 -14) 7/2 60) ((1/2 -10) 2 74)
  ((1/2 -2) 5/2 64) ((1/2 -2) 3 62) ((1/2 2) 1/2 67)
  ((1/2 2) 1 69) ((1/2 3) 3/2 71) ((1/2 14) 0 53)
  ((1 21) 2 74) ((1 21) 3 62) ((1 21) 4 46)
  ((1 -7) 3/2 71) ((1 -4) 5/2 64) ((1 4) 1/2 67))
(concatenate
'string
'MCStylistic-Oct2010-example-files-path*
"/collected-by-cars.txt") 5)
--> NIL
```

The function `collect-by-cars` can cause a stack overflow for moderately sized lists. This function writes the output of `collect-by-cars` to a text file (using `write-to-file-append`) every so often to prevent stack overflow. The example causes a file to be created in the specified location.

## SIA-reflected-merge-sort

Started, last checked	6/9/2010, 6/9/2010
Location	Structural induction merge
Calls	collect-by-cars-partition, subtract-two-lists, vector<vector-car
Called by	
Comments/see also	

Example: see *Discovering and rating musical patterns* (Sec. 3.1), especially lines 83-88).

This function is a faster version of the function `SIA-reflected`. The improved runtime is due to the use of merge-sort.



**vector<vector-car**

Started, last checked	6/9/2010, 6/9/2010
Location	Structural induction merge
Calls	vector<vector-t-or-nil
Called by	SIA-reflected-merge-sort
Comments/see also	vector<vector

Example:

```
(vector<vector-car '((1 1) . (1 3)) '((2 2) . (1 3)))
--> T
```

Applies the function vector<vector-t-or-nil to the car of each list (the two arguments).

**vector<vector-t-or-nil**

Started, last checked	6/9/2010, 6/9/2010
Location	Structural induction merge
Calls	
Called by	vector<vector-car
Comments/see also	vector<vector

Example:

```
(vector<vector-t-or-nil '(4 6 7) '(4 6 7.1))
--> T
```

The function vector<vector returns "equal" if the arguments were equal. This function returns nil in such a scenario.

**4.4.3 Further structural induction algorithms**

The functions below implement SIATEC (Structural Induction Algorithm for Transational Equivalence Classes) as described by Meredith et al. (2002), and COSIATEC (COVERing Strucutral Induction Algorithm for Translational Equivalence Classes) as described by Forth and Wiggins (2009); Meredith et al. (2003).

## COSIATEC

Started, last checked	25/1/2010, 25/1/2010
Location	Further structural induction algorithms
Calls	argmax-of-threeCs, read-from-file, remove-pattern-occurrences-from-dataset, SIA-reflected-for-COSIATEC, SIATEC, threeCs-pattern-translators-pairs, write-to-file
Called by	
Comments/see also	A more efficient implementation is required. See also COSIATEC-mod-2nd-n

Example:

```
(COSIATEC
'((0 61) (0 65) (1 64) (4 62) (4 66) (5 65) (8 60)
  (8 64) (9 63) (12 56) (13 69) (15 65) (16 57)
  (16 59) (17 64) (19 63))
(concatenate
'string
'MCStylistic-Oct2010-example-files-path*
"/COSIATEC output"))
--> 1 2 T
```

Implementation of the COSIATEC algorithm. It can be verified (by checking the files created in the specified location) that the output (pattern- translators pairs) constitutes a cover of the input dataset.

## COSIATEC-mod-2nd-n

Started, last checked	25/1/2010, 25/1/2010
Location	Further structural induction algorithms
Calls	argmax-of-threeCs, read-from-file, remove-pattern-occs-from-dataset-mod-2nd-n, SIA-reflected-for-COSIATEC-mod-2nd-n, SIATEC-mod-2nd-n, threeCs-pattern-trans-pairs-mod-2nd-n, write-to-file
Called by	
Comments/see also	A more efficient implementation is required. See also COSIATEC

Example:

```
(COSIATEC-mod-2nd-n
'((0 1) (0 5) (1 4) (4 2) (4 6) (5 5) (8 0)
  (8 4) (9 3) (12 8) (13 9) (15 5) (16 9)
  (16 11) (17 4) (19 3))
12
(concatenate
'string
'MCStylistic-Oct2010-example-files-path*
"/COSIATEC mod 2nd output"))
--> 1 2 T
```

Implementation of the COSIATEC algorithm, where translations in the second dimension are performed modulo the second argument. It can be verified (by checking the files created in the specified location) that the output above (pattern-translators pairs) constitutes a cover of the input dataset.

### remove-pattern-occurrences-from-dataset

Started, last checked	25/1/2010, 25/1/2010
Location	Further structural induction algorithms
Calls	set-difference-multidimensional-sorted-asc, translations, unions-multidimensional-sorted-asc
Called by	COSIATEC
Comments/see also	remove-pattern-occs-from-dataset-mod-2nd-n

Example:

```
(remove-pattern-occurrences-from-dataset
'(((0 60) (1 61)) (0 0) (1 1) (4 -1))
'((0 60) (1 61) (2 62) (3 60) (4 59) (5 60) (6 57)))
--> ((3 60) (6 57))
```

All of the datapoints that are members of occurrences of a given pattern are calculated. These datapoints are then removed from the dataset (calling the function set-difference-multidimensional-sorted- asc), and the new dataset returned.

**remove-pattern-occs-from-dataset-mod-2nd-n**

Started, last checked	25/1/2010, 25/1/2010
Location	Further structural induction algorithms
Calls	set-difference-multidimensional-sorted-asc, translations-mod-2nd-n, unions-multidimensional-sorted-asc
Called by	COSIATEC-mod-2nd-n
Comments/see also	remove-pattern-occurrences-from-dataset

Example:

```
(remove-pattern-occs-from-dataset-mod-2nd-n
'(((0 0) (1 1)) (0 0) (1 1) (4 11))
'((0 0) (1 1) (2 2) (3 0) (4 11) (5 0) (6 9))
12)
--> ((3 0) (6 9))
```

All of the datapoints that are members of occurrences of a given pattern are calculated, where translations in the second dimension are carried out modulo the third argument. These datapoints are then removed from the dataset (calling the function `set-difference-multidimensional-sorted-asc`), and the new dataset returned.

**SIA-reflected-for-COSIATEC**

Started, last checked	25/1/2010, 25/1/2010
Location	Further structural induction algorithms
Calls	subtract-two-lists, write-to-file
Called by	COSIATEC
Comments/see also	Deprecated, contingent on a rewrite of COSIATEC.

Example:

```
(SIA-reflected-for-COSIATEC
'((0 61) (0 65) (1 64) (4 62) (4 66) (5 65) (8 60)
(8 64) (9 63) (12 56) (13 69) (15 65) (16 57)
(16 59) (17 64) (19 63))
(concatenate
'string
*MCStylistic-Oct2010-example-files-path*)
```

```
"/SIA4COSIATEC output.txt"))
--> T
```

This function is a version of the SIA algorithm. It is called ‘SIA-reflected-for-COSIATEC’ because it is a slight variant on SIA-reflected. In particular it does not allow a partition size to be set.

### SIA-reflected-for-COSIATEC-mod-2nd-n

Started, last checked	25/1/2010, 25/1/2010
Location	Further structural induction algorithms
Calls	subtract-two-lists-mod-2nd-n, write-to-file
Called by	COSIATEC-mod-2nd-n
Comments/see also	Deprecated, contingent on a rewrite of COSIATEC-mod-2nd-n.

Example:

```
(SIA-reflected-for-COSIATEC-mod-2nd-n
'((0 1) (0 5) (1 4) (4 2) (4 6) (5 5) (8 0)
(8 4) (9 3) (12 8) (13 9) (15 5) (16 9)
(16 11) (17 4) (19 3))
12
(concatenate
'string
'MCStylistic-Oct2010-example-files-path*
"/SIA4COSIATEC mod 2nd output.txt"))
--> T
```

This function is a version of the SIA algorithm. It is called ‘SIA-reflected-for-COSIATEC’ because it is a slight variant on SIA-reflected. In particular it does not allow a partition size to be set. Also in the mod-2nd-n version, translations in the second dimension are made modulo the second argument.

### SIATEC

Started, last checked	25/1/2010, 25/1/2010
Location	Further structural induction algorithms
Calls	translators-of-pattern-in-dataset, write-to-file
Called by	COSIATEC
Comments/see also	SIATEC-mod-2nd-n

Example:

```
(progn
  (setq
    SIA-output
    '(((1/2 60) (1 62) (3/2 64) (2 67) (5/2 69) (3 71)
      (7/2 74) (4 71) (9/2 69) (5 67) (11/2 64)
      (6 60))
      ((49/4 71) (25/2 72) (51/4 73) (13 69) (13 74)
      (27/2 68) (27/2 73) (14 69) (14 74) (29/2 68)
      (29/2 73) (15 69) (15 74))))))
  (setq
    dataset
    (read-from-file
      (concatenate
        'string
        *MCStylistic-Oct2010-example-files-path*
        "/scarlatti-L10-bars1-19.txt"))))
  (setq
    projected-dataset
    (orthogonal-projection-unique-equalp
      dataset '(1 0 1 0 0)))
  (setq
    path&name
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/SIATEC output.txt"))
  (SIATEC SIA-output projected-dataset path&name))
--> T
```

This function applies the SIATEC algorithm to the output of the function SIA-reflected. The example causes a file to be created in the specified location.

**SIATEC-mod-2nd-n**

Started, last checked	25/1/2010, 25/1/2010
Location	Further structural induction algorithms
Calls	translators-of-pattern-in-dataset-mod-2nd-n, write-to-file
Called by	COSIATEC-mod-2nd-n
Comments/see also	SIATEC

Example:

```
(progn
  (setq
    SIA-mod-2nd-n-output
    '(((1/2 4) (1 6) (3/2 1) (2 4) (5/2 6) (3 1)
      (7/2 4) (4 1) (9/2 6) (5 4) (11/2 1) (6 4))
      ((49/4 1) (25/2 2) (51/4 3) (13 6) (13 4)
      (27/2 5) (27/2 3) (14 6) (14 4) (29/2 5)
      (29/2 3) (15 6) (15 4))))
  (setq
    dataset
    (read-from-file
      (concatenate
        'string
        *MCStylistic-Oct2010-example-files-path*
        "/scarlatti-L10-bars1-19.txt"))))
  (setq
    dataset-1-0-1-0-0
    (orthogonal-projection-unique-equalp
      dataset '(1 0 1 0 0)))
  (setq
    dataset-1-0-1*-1-0
    (sort-dataset-asc
      (mod-column
        dataset-1-0-1-0-0 7 1)))
  (setq
    path&name
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/SIATEC mod 2nd output.txt")))
```

```
(SIATEC-mod-2nd-n
  SIA-mod-2nd-n-output dataset-1-0-1*-1-0 7
  path&name))
--> T
```

This function applies the SIATEC algorithm to the output of the function SIA-reflected, where translations in the second dimension are carried out modulo the third argument. The example causes a file to be created in the specified location.

#### 4.4.4 Evaluation for SIA+

The aim of these functions is to provide support for the implementation of COSIATEC (Meredith et al., 2003; Forth and Wiggins, 2009).

#### argmax-of-threeCs

Started, last checked	10/8/2009, 10/8/2009
Location	Evaluation for SIA+
Calls	multiply-two-lists, max-argmax, normalise-0-1
Called by	
Comments/see also	

Example:

```
(argmax-of-threeCs
  '((1 5 5/4) (1/10 4 4/3) (1 6 1) (4/5 12 2)))
--> 3
```

The argument to this function is a list of sublists, each containing three elements. Lists are constructed from these elements along dimensions one to three, and normalised linearly to  $[0, 1]$ . Then the lists are multiplied element-wise, and the resulting list is searched for the argument of the maximum element.



**index-target-translation-in-list-assoc**

Started, last checked	10/8/2009, 10/8/2009
Location	Evaluation for SIA+
Calls	test-translation
Called by	number-of-targets-translation-in-list-assoc
Comments/see also	

Example:

```
(setq
 a-list
 '((((151/3 84 1/3) (152/3 83 1/3) (51 81 1/3))
   (-8 0 0) (-4 0 0) (0 0 0) (11/3 7 0) (19/3 0 0)
   (23/3 0 0) (26/3 -5 0))
  (((143/3 84 1/3) (48 83 1/3) (146/3 86 1/3))
   (0 0 0) (23/3 0 0))
  (((52 43 2) (54 31 2) (56 36 2))
   (0 0 0) (8 7 0))
  (((5 76 1/2) (11/2 79 1/2))
   (0 0 0) (225/4 0 -1/4))))
(index-target-translation-in-list-assoc
 '((62 44 2) (64 32 2) (66 37 2)) a-list)
--> 2
```

The sublists of the list each contain a pattern and its translators. We want to know if any of the patterns are translations of the first argument, the target. The index of the first extant translation is returned, and nil otherwise. This function is used for checking the output of COSIATEC, as it uses assoc.

**index-target-translation-in-list-rassoc**

Started, last checked	10/8/2009, 10/8/2009
Location	Evaluation for SIA+
Calls	test-translation
Called by	number-of-targets-translation-in-list-rassoc
Comments/see also	

Example:

```
(setq
```

```

a-list
'(((1 0 0)
  (66 55 1) (66 65 1) (67 55 1) (68 55 1) (68 64 1)
  (69 55 1))
 ((11/3 -42 5/3)
  (163/3 90 1/3))
 ((10/3 -11 0)
  (163/3 90 1/3))
 ((3 -9 0)
  (163/3 90 1/3) (164/3 88 1/3) (56 88 1/3))))
(index-target-translation-in-list-rassoc
 '((166/3 60 1/3) (167/3 58 1/3) (57 58 1/3)) a-list)
--> 3

```

The sublists of the list each contain a pattern and its translators. We want to know if any of the patterns are translations of the first argument, the target. The index of the first extant translation is returned, and nil otherwise. This function is used for checking the output of SIA, as it uses rassoc.

### index-target-translation-mod-in-list-assoc

Started, last checked	10/8/2009, 10/8/2009
Location	Evaluation for SIA+
Calls	test-translation-mod-2nd-n
Called by	number-of-targets-trans-mod-in-list-assoc
Comments/see also	

Example:

```

(setq
 a-list
 '((((151/3 0 1/3) (152/3 11 1/3) (51 10 1/3))
  (-8 0 0) (-4 0 0) (0 0 0) (11/3 7 0) (19/3 0 0)
  (23/3 0 0) (26/3 -5 0))
 ((143/3 0 1/3) (48 11 1/3) (146/3 10 1/3))
 (0 0 0) (23/3 0 0))
 ((52 7 2) (54 7 2) (56 0 2))
 (0 0 0) (8 7 0))
 (((5 4 1/2) (11/2 7 1/2))
 (0 0 0) (225/4 0 -1/4))))
(index-target-translation-mod-in-list-assoc

```

```
'((62 0 2) (64 0 2) (66 5 2)) a-list 12)
--> 2
```

This function is very similar to the function `index-target-translation-in-list-assoc`, except that in the second dimension translations are carried out modulo the third argument. The sublists of the list each contain a pattern and its translators. We want to know if any of the patterns are translations of the first argument, the target. The index of the first extant translation is returned, and nil otherwise. This function is used for checking the output of the function `COSIATEC-mod-2nd-n`, as it uses `assoc` (when the dataset has been projected modulo  $n$ ).

### index-target-translation-mod-in-list-rassoc

Started, last checked	10/8/2009, 10/8/2009
Location	Evaluation for SIA+
Calls	test-translation-mod-2nd-n
Called by	number-of-targets-trans-mod-in-list-rassoc
Comments/see also	

Example:

```
(setq
 a-list
 '(((1 0 0)
   (66 55 1) (66 65 1) (67 55 1) (68 55 1) (68 64 1)
   (69 55 1))
  ((11/3 -42 5/3)
   (163/3 90 1/3))
  ((10/3 -11 0)
   (163/3 90 1/3))
  ((3 -9 0)
   (163/3 90 1/3) (164/3 88 1/3) (56 88 1/3))))
(index-target-translation-mod-in-list-rassoc
 '((166/3 0 1/3) (167/3 10 1/3) (57 10 1/3))
 a-list 12)
--> 3
```

This function is very similar to the function `index-target-translation-in-list-rassoc`, except that in the second dimension translations are carried out modulo the third argument. The sublists of the list each contain a pattern and

its translators. We want to know if any of the patterns are translations of the first argument, the target. The index of the first extant translation is returned, and nil otherwise. This function is used for checking the output of the function SIA-mod-2nd-n, as it uses rassoc (when the dataset has been projected modulo  $n$ ).

### number-of-targets-translation-in-list-assoc

Started, last checked	10/8/2009, 10/8/2009
Location	Evaluation for SIA+
Calls	index-target-translation-in-list-assoc
Called by	
Comments/see also	

Example:

```
(setq
 a-list
 '((((151/3 84 1/3) (152/3 83 1/3) (51 81 1/3))
 (-8 0 0) (-4 0 0) (0 0 0) (11/3 7 0) (19/3 0 0)
 (23/3 0 0) (26/3 -5 0))
 (((143/3 84 1/3) (48 83 1/3) (146/3 86 1/3))
 (0 0 0) (23/3 0 0))
 (((52 43 2) (54 31 2) (56 36 2))
 (0 0 0) (8 7 0))
 (((5 76 1/2) (11/2 79 1/2))
 (0 0 0) (225/4 0 -1/4))))
(number-of-targets-translation-in-list-assoc
 '(((62 44 2) (64 32 2) (66 37 2))
 ((5 76 1/2) (11/2 79 1/2))
 ((5 76 1/2) (6 79 1/2)))
 a-list)
--> 2
```

The function index-target-translation-in-list-assoc is applied recursively to each member of the first argument of this function. This argument is a list of targets. Each time a translation of a target is detected, the output (initially set to zero) is incremented by one.

**number-of-targets-translation-in-list-rassoc**

Started, last checked	10/8/2009, 10/8/2009
Location	Evaluation for SIA+
Calls	index-target-translation-in-list-rassoc
Called by	
Comments/see also	

Example:

```
(setq
 a-list
 '(((1 0 0)
   ((66 55 1) (66 65 1) (67 55 1) (68 55 1) (68 64 1)
     (69 55 1))
   ((11/3 -42 5/3)
    (163/3 90 1/3))
   ((10/3 -11 0)
    (163/3 90 1/3))
   ((3 -9 0)
    (163/3 90 1/3) (164/3 88 1/3) (56 88 1/3))))
 (number-of-targets-translation-in-list-rassoc
  '(((166/3 60 1/3) (167/3 58 1/3) (57 58 1/3))
    ((66 55 1) (66 65 1) (67 55 1) (68 55 1) (68 64 1)
      (69 55 1))
    ((163/3 90 1/3)))
 a-list)
--> 3
```

The function `index-target-translation-in-list-rassoc` is applied recursively to each member of the first argument of this function. This argument is a list of targets. Each time a translation of a target is detected, the output (initially set to zero) is incremented by one.

**number-of-targets-trans-mod-in-list-assoc**

Started, last checked	10/8/2009, 10/8/2009
Location	Evaluation for SIA+
Calls	index-target-translation-mod-in-list-assoc
Called by	
Comments/see also	

Example:

```
(setq
  a-list
  '((((151/3 84 1/3) (152/3 83 1/3) (51 81 1/3))
      (-8 0 0) (-4 0 0) (0 0 0) (11/3 7 0) (19/3 0 0)
      (23/3 0 0) (26/3 -5 0))
    (((143/3 84 1/3) (48 83 1/3) (146/3 86 1/3))
      (0 0 0) (23/3 0 0))
    (((52 43 2) (54 31 2) (56 36 2))
      (0 0 0) (8 7 0))
    (((5 76 1/2) (11/2 79 1/2))
      (0 0 0) (225/4 0 -1/4))))
(number-of-targets-trans-mod-in-list-assoc
  '(((62 8 2) (64 8 2) (66 1 2))
    ((5 4 1/2) (11/2 7 1/2))
    ((5 4 1/2) (6 7 1/2))))
  a-list 12)
--> 2
```

The function `index-target-translation-mod-in-list-assoc` is applied recursively to each member of the first argument of this function. This argument is a list of targets. Each time a translation (modulo the third argument) of a target is detected, the output (initially set to zero) is incremented by one.

### **number-of-targets-trans-mod-in-list-rassoc**

Started, last checked	10/8/2009, 10/8/2009
Location	Evaluation for SIA+
Calls	<code>index-target-translation-mod-in-list-rassoc</code>
Called by	
Comments/see also	

Example:

```
(setq
  a-list
  '(((1 0 0)
      (66 55 1) (66 65 1) (67 55 1) (68 55 1) (68 64 1)
      (69 55 1))
    ((11/3 -42 5/3)
```

```

      (163/3 90 1/3))
    ((10/3 -11 0)
     (163/3 90 1/3))
    ((3 -9 0)
     (163/3 90 1/3) (164/3 88 1/3) (56 88 1/3))))
(number-of-targets-trans-mod-in-list-rassoc
 '(((166/3 1 1/3) (167/3 11 1/3) (57 11 1/3))
   ((66 8 1) (66 6 1) (67 8 1) (68 8 1) (68 11 1)
    (69 8 1))
   ((163/3 6 1/3)))
a-list 12)
--> 2

```

The function `index-target-translation-mod- in-list-rassoc` is applied recursively to each member of the first argument of this function. This argument is a list of targets. Each time a translation (modulo the third argument) of a target is detected, the output (initially set to zero) is incremented by one.

### threeCs-pattern-trans-pair-mod-2nd-n

Started, last checked	10/8/2009, 10/8/2009
Location	Evaluation for SIA+
Calls	coverage-mod-2nd-n, index-item-1st-occurs, my-last
Called by	threeCs-pattern-trans-pairs-mod-2nd-n
Comments/see also	

Example:

```

(threeCs-pattern-trans-pair-mod-2nd-n
 '((0 0) (1 1)) '((0 0) (1 1) (3 0))
 '((0 0) (1 1) (2 2) (3 0) (5/2 7) (4 1)) 12)
--> (1 5 5/4)

```

A pattern and its translators in a projected dataset are supplied as arguments to this function. The output is the compactness, coverage and compression ratio, with translations in the second dimension being carried out modulo the fourth argument.

**threeCs-pattern-trans-pairs-mod-2nd-n**

Started, last checked	10/8/2009, 10/8/2009
Location	Evaluation for SIA+
Calls	threeCs-pattern-trans-pair-mod-2nd-n
Called by	
Comments/see also	

Example:

```
(threeCs-pattern-trans-pairs-mod-2nd-n
'(((0 11) (1 0) (3 11)) (0 0) (1 1))
  (((0 11)) (0 0) (1 1) (2 2) (3 0) (5/2 8) (4 1)))
'((0 11) (1 0) (2 1) (3 11) (5/2 7) (4 0))
12)
--> ((3/4 5 5/4) (1 6 1))
```

Pairs (consisting of patterns and their translators and sometimes referred to as SIATEC- output) in a projected dataset are supplied as arguments to this function. The output is a list of lists, each of which contains the compactness, coverage and compression ratio of the corresponding pattern. Translations in the second dimension are carried out modulo the third argument.

**threeCs-pattern-translators-pair**

Started, last checked	10/8/2009, 10/8/2009
Location	Evaluation for SIA+
Calls	coverage, index-item-1st-occurs, my-last
Called by	threeCs-pattern-translators-pairs
Comments/see also	

Example:

```
(threeCs-pattern-translators-pair
'((0 60) (1 61)) '((0 0) (1 1) (3 0))
'((0 60) (1 61) (2 62) (3 60) (5/2 67) (4 61)))
--> (1 5 5/4)
```

A pattern and its translators in a projected dataset are supplied as arguments to this function. The output is the compactness, coverage and compression ratio.



**threeCs-pattern-translators-pairs**

Started, last checked	10/8/2009, 10/8/2009
Location	Evaluation for SIA+
Calls	threeCs-pattern-translators-pair
Called by	
Comments/see also	

Example:

```
(threeCs-pattern-translators-pairs
'(((0 60) (1 61)) (0 0) (1 1) (3 0))
  (((0 60)) (0 0) (1 1) (2 2) (3 0) (5/2 7) (4 1)))
'((0 60) (1 61) (2 62) (3 60) (5/2 67) (4 61)))
--> ((1 5 5/4) (1 6 1))
```

Pairs (consisting of patterns and their translators and sometimes referred to as SIATEC- output) in a projected dataset are supplied as arguments to this function. The output is a list of lists, each of which contains the compactness, coverage and compression ratio of the corresponding pattern.

**4.4.5 Compactness trawl**

These functions are designed to trawl through already- discovered patterns (usually MTPs) from beginning to end. They return subpatterns that have compactness (Meredith et al., 2003) and cardinality greater than thresholds that can be specified (Collins et al., 2010).

**compact-subpatterns**

Started, last checked	12/1/2010, 30/1/2010
Location	Compactness trawl
Calls	compactness, my-last
Called by	
Comments/see also	A more efficient implementation could be achieved by retaining the index of data-points. See also compact-subpatterns-more-output

Example:

```
(compact-subpatterns
'((1/2 72 67 1/2) (1 76 69 1/2) (3/2 79 71 1/2)
  (2 84 74 2) (7/2 60 60 1/2) (5 76 69 1/2)
  (11/2 79 71 1/2) (6 84 74 2) (13/2 67 64 1/2)
  (15/2 60 60 1/2))
'((0 48 53 2) (1/2 72 67 1/2) (1 76 69 1/2)
  (3/2 79 71 1/2) (2 84 74 2) (5/2 67 64 1/2)
  (3 64 62 1/2) (7/2 60 60 1/2) (4 36 46 2)
  (9/2 72 67 1/2) (5 76 69 1/2) (11/2 79 71 1/2)
  (6 84 74 2) (13/2 67 64 1/2) (7 64 62 1/2)
  (15/2 60 60 1/2) (8 36 46 2) (17/2 72 67 1/2))
2/3 3)
--> (((1/2 72 67 1/2) (1 76 69 1/2) (3/2 79 71 1/2)
      (2 84 74 2) (7/2 60 60 1/2))
      ((5 76 69 1/2) (11/2 79 71 1/2) (6 84 74 2)
      (13/2 67 64 1/2) (15/2 60 60 1/2)))
```

This function takes a pattern and looks within that pattern for subpatterns that have compactness and cardinality greater than certain thresholds, which are optional arguments. In this version, just the subpatterns are returned.

### compact-subpatterns-more-output

Started, last checked	12/1/2010, 30/1/2010
Location	Compactness trawl
Calls	compactness, my-last
Called by	compactness-trawler
Comments/see also	A more efficient implementation could be achieved by retaining the index of data-points. See also compact-subpatterns

Example:

```
(compact-subpatterns-more-output
'((1/2 72 67 1/2) (1 76 69 1/2) (3/2 79 71 1/2)
  (2 84 74 2) (7/2 60 60 1/2) (5 76 69 1/2)
  (11/2 79 71 1/2) (6 84 74 2) (13/2 67 64 1/2)
  (15/2 60 60 1/2))
'((0 48 53 2) (1/2 72 67 1/2) (1 76 69 1/2)
  (3/2 79 71 1/2) (2 84 74 2) (5/2 67 64 1/2)
  (3 64 62 1/2) (7/2 60 60 1/2) (4 36 46 2))
```

```

(9/2 72 67 1/2) (5 76 69 1/2) (11/2 79 71 1/2)
(6 84 74 2) (13/2 67 64 1/2) (7 64 62 1/2)
(15/2 60 60 1/2) (8 36 46 2) (17/2 72 67 1/2))
2/3 3)
--> (((((1/2 72 67 1/2) (1 76 69 1/2) (3/2 79 71 1/2)
(2 84 74 2) (7/2 60 60 1/2))
((5 76 69 1/2) (11/2 79 71 1/2) (6 84 74 2)
(13/2 67 64 1/2) (15/2 60 60 1/2)))
(5/7 5/6))

```

This function takes a pattern and looks within that pattern for subpatterns that have compactness and cardinality greater than certain thresholds, which are optional arguments. In this version, the subpatterns and corresponding compactness values are returned.

### compactness-trawler

Started, last checked	12/1/2010, 30/1/2010
Location	Compactness trawl
Calls	compact-subpatterns-more-output, test-translation, write-to-file
Called by	
Comments/see also	

Example: see Discovering and rating musical patterns (Sec. 3.1), especially lines 101-107).

The compactness trawler (Collins et al., 2010) applies the function compact-subpatterns-more-output recursively to the output of SIA (Structure Induction Algorithm, Meredith et al., 2002), or any output with an analogous list format.

#### 4.4.6 Evaluation for SIACT

The purpose of these functions is to rate the trawled patterns, according to the formula for perceived pattern importance (Collins et al., 2011).

**collect-indices&ratings**

Started, last checked	19/1/2010, 30/1/2010
Location	Evaluation for SIACT
Calls	
Called by	evaluate-variables-of-patterns2hash
Comments/see also	

Example:

```
(setq
 patterns-hash
 (list
  (make-hash-table :test #'equal)
  (make-hash-table :test #'equal)
  (make-hash-table :test #'equal)))
(setf (gethash "index" (first patterns-hash)) 0)
(setf (gethash "rating" (first patterns-hash)) 3.3)
(setf (gethash "index" (second patterns-hash)) 1)
(setf (gethash "rating" (second patterns-hash)) 8.0)
(setf (gethash "index" (third patterns-hash)) 2)
(setf (gethash "rating" (third patterns-hash)) 2.1)
(collect-indices&ratings patterns-hash)
--> ((0 3.3) (1 8.0) (2 2.1))
```

This function collects the index and rating from each sublist of a list, where the sublist is a hash table consisting of information about a pattern.

**evaluate-variables-of-pattern2hash**

Started, last checked	19/1/2010, 30/1/2010
Location	Evaluation for SIACT
Calls	add-to-list, choose, coverage, first-n-naturals, index-item-1st-occurs, likelihood-of-translations-reordered, multiply-list-by-constant, my-last, nth-list, translators-of-pattern-in-dataset
Called by	evaluate-variables-of-patterns2hash
Comments/see also	

Example:

```

(setq
  pattern&source
  '(((1/2 72 67 1/2) (1 76 69 1/2) (3/2 79 71 1/2)
    (2 84 74 2) (5/2 67 64 1/2) (3 64 62 1/2)
    (7/2 60 60 1/2))
    16/23 (140 5 0) 1 (104 -5 0) 4/5 (96 -5 0)))
(setq
  dataset
  '((0 48 53 2) (1/2 72 67 1/2) (1 76 69 1/2)
    (3/2 79 71 1/2) (2 84 74 2) (5/2 67 64 1/2)
    (3 64 62 1/2) (7/2 60 60 1/2) (4 36 46 2)
    (9/2 72 67 1/2) (5 76 69 1/2) (11/2 79 71 1/2)
    (6 84 74 2) (13/2 67 64 1/2) (7 64 62 1/2)
    (15/2 60 60 1/2) (8 36 46 2) (17/2 72 67 1/2)
    (9 76 69 1/2) (19/2 79 71 1/2)))
(setq
  dataset-palette
  (orthogonal-projection-not-unique-equalp
   dataset
   (append
    (list 0)
    (constant-vector
     1
     (- (length
        (first (first pattern&source))) 1))))))
(setq
  empirical-mass
  (empirical-mass dataset-palette))
(setq
  pattern-hash
  (evaluate-variables-of-pattern2hash
   pattern&source dataset 20 dataset-palette
   empirical-mass
   '(4.277867 3.422478734 -0.038536808 0.651073171)
   '(73.5383283152 0.02114878519) 1))
--> #<HASH-TABLE
      :TEST EQUAL size 12/60 #x3000418C079D>
(dispatch-el pattern-hash)
--> (("name" . "pattern 1") ("compactness" . 16/23)
      ("expected occurrences" . 62.352943)
      ("rating" . 5.3952165))

```

```

("pattern"
 (1/2 72 67 1/2) (1 76 69 1/2) (3/2 79 71 1/2)
 (2 84 74 2) (5/2 67 64 1/2) (3 64 62 1/2)
 (7/2 60 60 1/2))
("translators" (0 0 0 0) (4 0 0 0)) ("index" . 1)
("cardinality" . 7)
("MTP vectors" (96 -5 0) (104 -5 0) (140 5 0))
("compression ratio" . 7/4)
("region"
 (1/2 72 67 1/2) (1 76 69 1/2) (3/2 79 71 1/2)
 (2 84 74 2) (5/2 67 64 1/2) (3 64 62 1/2)
 (7/2 60 60 1/2)) ("occurrences" . 2))

```

This function evaluates variables of the supplied pattern, such as cardinality and expected occurrences.

### evaluate-variables-of-patterns2hash

Started, last checked	19/1/2010, 30/1/2010
Location	Evaluation for SIACT
Calls	collect-indices&ratings, constant-vector, empirical-mass, evaluate-variables-of-pattern2hash, nth-list, nth-list-of-lists, orthogonal-projection-not-unique-equalp, sort-by
Called by	
Comments/see also	

Example:

```

(setq
 pattern&sources
 '((((1/2 72 67 1/2) (1 76 69 1/2) (3/2 79 71 1/2)
 (2 84 74 2) (5/2 67 64 1/2) (3 64 62 1/2)
 (7/2 60 60 1/2))
 16/23 (140 5 0) 1 (104 -5 0) 4/5 (96 -5 0))
 (((1/2 72 67 1/2) (3/2 79 71 1/2))
 1 (130 0 0) 2/3 (100 0 1/2))))
(setq
 dataset

```

```
'((0 48 53 2) (1/2 72 67 1/2) (1 76 69 1/2)
  (3/2 79 71 1/2) (2 84 74 2) (5/2 67 64 1/2)
  (3 64 62 1/2) (7/2 60 60 1/2) (4 36 46 2)
  (9/2 72 67 1/2) (5 76 69 1/2) (11/2 79 71 1/2)
  (6 84 74 2) (13/2 67 64 1/2) (7 64 62 1/2)
  (15/2 60 60 1/2) (8 36 46 2) (17/2 72 67 1/2)
  (9 76 69 1/2) (19/2 79 71 1/2)))
(setq
 patterns-hash
 (evaluate-variables-of-patterns2hash
  pattern&sources dataset
  '(4.277867 3.422478734 -0.038536808 0.651073171)
  '(73.5383283152 0.02114878519)))
--> (#<HASH-TABLE
      :TEST EQUAL size 12/60 #x300041916ACD>
      #<HASH-TABLE
      :TEST EQUAL size 12/60 #x30004188107D>)
(dispatch-el (first patterns-hash))
--> (("name" . "pattern 1") ("compactness" . 1)
     ("expected occurrences" . 72.79239)
     ("rating" . 5.8717685)
     ("pattern" (1/2 72 67 1/2) (3/2 79 71 1/2))
     ("translators" (0 0 0 0) (4 0 0 0) (8 0 0 0))
     ("index" . 1) ("cardinality" . 2)
     ("MTP vectors" (100 0 1/2) (130 0 0))
     ("compression ratio" . 3/2)
     ("region"
      (1/2 72 67 1/2) (1 76 69 1/2) (3/2 79 71 1/2))
     ("occurrences" . 3))
```

This function applies the function `evaluate-variables-of-pattern2hash` recursively.

## 4.5 Markov models

### 4.5.1 Segmentation

The fundamental functions here are used to segment datapoints based on ontime and offtime. Subsequent functions do things like computing chord spacing and holding types.

**append-offtimes**

Started, last checked	16/1/2009, 24/1/2009
Location	Segmentation
Calls	
Called by	segments, segments-strict
Comments/see also	

Example:

```
(append-offtimes '((0 48 2) (1 60 1) (1 57 1/2)))
--> '((0 48 2 2) (1 60 1 2) (1 57 1/2 3/2))
```

This function takes a list, assumed to be datapoints, and appends the offset of each datapoint as the final item.

**chord-candidates-offtimes**

Started, last checked	16/1/2009, 24/1/2009
Location	Segmentation
Calls	my-last
Called by	segment
Comments/see also	chord-candidates-offtimes-strict, chord-candidates-ontimes

Example:

```
(chord-candidates-offtimes
'((1579 66 191 2 49 1770 5) (1974 64 191 3 49 2165 2)
(1974 67 191 2 49 2165 3) (2368 66 191 2 49 2559 0)
(2368 62 191 3 49 2559 4) (2763 64 191 2 49 2954 6)
(2763 57 191 3 49 2954 7) (2800 72 191 1 49 2991 8)
(3158 38 191 4 49 3349 9)
(1579 62 1920 3 49 3499 1)
(3158 54 385 3 49 3543 10)
(3158 62 385 2 49 3543 11)
(3553 42 191 4 49 3744 12)
(3947 45 191 4 49 4138 13)
(4342 50 191 4 49 4533 14))) 15 2368 0)
--> (5 2 3)
```



There are four arguments to this function: a list of datapoints (ordered by offtimes ascending and appended with an enumeration), the length  $l$  of the list, a point in time  $x$ , and an index  $s$  from which to begin searching. When the  $n$ th offtime equals or exceeds  $x$ , the search stops. As subsequent calls to this function use larger values of  $x$ , the search can begin at the  $sth$  offtime.

### chord-candidates-offtimes-strict

Started, last checked	16/1/2009, 24/1/2009
Location	Segmentation
Calls	my-last
Called by	segment-strict
Comments/see also	chord-candidates-offtimes, chord-candidates-ontimes

Example:

```
(chord-candidates-offtimes-strict
'((3 55 57 3/4 1 15/4 1) (3 60 60 3/4 1 15/4 2)
(3 67 64 3/4 0 15/4 3) (3 76 69 3/4 0 15/4 4)
(15/4 59 59 1/4 1 4 5) (15/4 65 63 1/4 0 4 6)
(15/4 74 68 1/4 0 4 7) (3 48 53 3 1 6 0)
(4 60 60 2 1 6 8) (4 64 62 2 0 6 9)
(4 72 67 2 0 6 10)) 11 15/4 0)
--> (1 2 3 4)
```

Contrast the output of this function with the function `chord-candidate-offtimes`. The difference is that the present function will not return indices of datapoints whose offtimes coincide with the provided time  $x$ . There are four arguments to this function: a list of datapoints (ordered by offtimes ascending and appended with an enumeration), the length  $l$  of the list, a point in time  $x$ , and an index  $s$  from which to begin searching. When the  $n$ th offtime equals or exceeds  $x$ , the search stops. As subsequent calls to this function use larger values of  $x$ , the search can begin at the  $sth$  offtime.

**chord-candidates-ontimes**

Started, last checked	16/1/2009, 24/1/2009
Location	Segmentation
Calls	my-last
Called by	segment, segment-strict
Comments/see also	chord-candidates-offtimes, chord-candidates-offtimes-strict

Example:

```
(chord-candidates-ontimes
'((1579 62 1920 3 49 3499 1)
  (1579 66 191 2 49 1770 5) (1974 64 191 3 49 2165 2)
  (1974 67 191 2 49 2165 3) (2368 66 191 2 49 2559 0)
  (2368 62 191 3 49 2559 4) (2763 64 191 2 49 2954 6)
  (2763 57 191 3 49 2820 7) (2800 72 191 1 49 2991 8)
  (3158 38 191 4 49 3349 9)
  (3158 54 385 3 49 3543 10)
  (3158 62 385 2 49 3543 11)
  (3553 42 191 4 49 3744 12)
  (3947 45 191 4 49 4138 13)
  (4342 50 191 4 49 4533 14))) 15 2368 0)
--> (1 5 2 3 0 4)
```

There are four arguments to this function: a list of datapoints (ordered by ontimes and appended with offtimes and an enumeration), the length  $l$  of the list, a point in time  $x$ , and an index  $s$  from which to begin searching. When the  $n$ th ontime exceeds  $x$ , the search stops. As subsequent calls to this function use larger values of  $x$ , the search can begin at the  $s$ th ontime.

**enumerate-append**

Started, last checked	16/1/2009, 24/1/2009
Location	Segmentation
Calls	
Called by	segments, segments-strict
Comments/see also	

Example:

```
(enumerate-append '((3 53) (6 0) (42 42)))
```

```
--> ((3 53 0) (6 0 1) (42 42 2))
```

This function enumerates a list by appending the next natural number, counting from 0, to the end of each list.

### prepare-for-segments

Started, last checked	16/1/2009, 24/1/2009
Location	Segmentation
Calls	sort-by
Called by	segments, segments-strict
Comments/see also	

Example:

```
(prepare-for-segments
'((2368 66 191 2 49 2559 0)
  (1579 62 1920 3 49 3499 1)
  (1974 64 191 3 49 2165 2) (1974 67 191 2 49 2165 3)
  (2368 62 191 3 49 2559 4) (1579 66 191 2 49 1770 5)
  (2763 64 191 2 49 2954 6) (2763 57 191 3 49 2954 7)
  (2800 72 191 1 49 2991 8) (3158 38 191 4 49 3349 9)
  (3158 54 385 3 49 3543 10)
  (3158 62 385 2 49 3543 11)
  (3553 42 191 4 49 3744 12)
  (3947 45 191 4 49 4138 13)
  (4342 50 191 4 49 4533 14)))
--> (((1579 62 1920 3 49 3499 1)
      (1579 66 191 2 49 1770 5)
      (1974 64 191 3 49 2165 2)
      (1974 67 191 2 49 2165 3)
      (2368 66 191 2 49 2559 0)
      (2368 62 191 3 49 2559 4)
      (2763 64 191 2 49 2954 6)
      (2763 57 191 3 49 2820 7)
      (2800 72 191 1 49 2991 8)
      (3158 38 191 4 49 3349 9)
      (3158 54 385 3 49 3543 10)
      (3158 62 385 2 49 3543 11)
      (3553 42 191 4 49 3744 12)
      (3947 45 191 4 49 4138 13))
```

```

(4342 50 191 4 49 4533 14))
((1579 66 191 2 49 1770 5)
 (1974 64 191 3 49 2165 2)
 (1974 67 191 2 49 2165 3)
 (2368 66 191 2 49 2559 0)
 (2368 62 191 3 49 2559 4)
 (2763 64 191 2 49 2954 6)
 (2763 57 191 3 49 2954 7)
 (2800 72 191 1 49 2991 8)
 (3158 38 191 4 49 3349 9)
 (1579 62 1920 3 49 3499 1)
 (3158 54 385 3 49 3543 10)
 (3158 62 385 2 49 3543 11)
 (3553 42 191 4 49 3744 12)
 (3947 45 191 4 49 4138 13)
 (4342 50 191 4 49 4533 14)))

```

The datapoints already have offtimes appended and are enumerated. They are sent to two lists; one ordered by ontime, the other by offtime.

## segment

Started, last checked	16/1/2009, 24/1/2009
Location	Segmentation
Calls	add-to-list, chord-candidates-offtimes, chord-candidates-ontimes, first-n-naturals, nth-list
Called by	segments
Comments/see also	segment-strict

Example:

```

(segment
 1579
 '( (2368 66 191 2 49) (1579 62 1920 3 49)
    (1974 64 191 3 49) (1974 67 191 2 49)
    (2368 62 191 3 49) (1579 66 191 2 49)
    (2763 64 191 2 49) (2763 57 191 3 49)
    (2800 72 191 1 49) (3158 38 191 4 49)
    (3158 54 385 3 49) (3158 62 385 2 49)
    (3553 42 191 4 49) (3947 45 191 4 49)

```

```

(4342 50 191 4 49))
15
'(((1579 62 1920 3 49 3499 1)
  (1579 66 191 2 49 1770 5)
  (1974 64 191 3 49 2165 2)
  (1974 67 191 2 49 2165 3)
  (2368 66 191 2 49 2559 0)
  (2368 62 191 3 49 2559 4)
  (2763 64 191 2 49 2954 6)
  (2763 57 191 3 49 2820 7)
  (2800 72 191 1 49 2991 8)
  (3158 38 191 4 49 3349 9)
  (3158 54 385 3 49 3543 10)
  (3158 62 385 2 49 3543 11)
  (3553 42 191 4 49 3744 12)
  (3947 45 191 4 49 4138 13)
  (4342 50 191 4 49 4533 14)))
((1579 66 191 2 49 1770 5)
 (1974 64 191 3 49 2165 2)
 (1974 67 191 2 49 2165 3)
 (2368 66 191 2 49 2559 0)
 (2368 62 191 3 49 2559 4)
 (2763 64 191 2 49 2954 6)
 (2763 57 191 3 49 2954 7)
 (2800 72 191 1 49 2991 8)
 (3158 38 191 4 49 3349 9)
 (1579 62 1920 3 49 3499 1)
 (3158 54 385 3 49 3543 10)
 (3158 62 385 2 49 3543 11)
 (3553 42 191 4 49 3744 12)
 (3947 45 191 4 49 4138 13)
 (4342 50 191 4 49 4533 14))))
--> (((1579 66 191 2 49) (1579 62 1920 3 49))
      (1 5) (14 13 12 11 10 9 8 7 6 5 4 3 2 1 0))

```

This function takes an ontime  $t$ , a list of datapoints of length  $N$ , with offsets and enumeration appended, but in original order, as well as the datapoints having had the function prepared-for-segments applied. It returns any datapoints which exist at the point  $t$ , as well as lists which help speed up any subsequent searches.

**segment-strict**

Started, last checked	16/1/2009, 24/1/2009
Location	Segmentation
Calls	add-to-list, chord-candidates-offtimes-strict, chord-candidates-ontimes, first-n-naturals, nth-list
Called by	segments-strict
Comments/see also	segment

Example:

```
(segment-strict
 15/4
'((3 48 53 3 1 6 0) (3 55 57 3/4 1 15/4 1)
  (3 60 60 3/4 1 15/4 2) (3 67 64 3/4 0 15/4 3)
  (3 76 69 3/4 0 15/4 4) (15/4 59 59 1/4 1 4 5)
  (15/4 65 63 1/4 0 4 6) (15/4 74 68 1/4 0 4 7)
  (4 60 60 2 1 6 8) (4 64 62 2 0 6 9)
  (4 72 67 2 0 6 10))
11
'(((3 48 53 3 1 6 0) (3 55 57 3/4 1 15/4 1)
  (3 60 60 3/4 1 15/4 2) (3 67 64 3/4 0 15/4 3)
  (3 76 69 3/4 0 15/4 4) (15/4 59 59 1/4 1 4 5)
  (15/4 65 63 1/4 0 4 6) (15/4 74 68 1/4 0 4 7)
  (4 60 60 2 1 6 8) (4 64 62 2 0 6 9)
  (4 72 67 2 0 6 10))
 ((3 55 57 3/4 1 15/4 1) (3 60 60 3/4 1 15/4 2)
  (3 67 64 3/4 0 15/4 3) (3 76 69 3/4 0 15/4 4)
  (15/4 59 59 1/4 1 4 5) (15/4 65 63 1/4 0 4 6)
  (15/4 74 68 1/4 0 4 7) (3 48 53 3 1 6 0)
  (4 60 60 2 1 6 8) (4 64 62 2 0 6 9)
  (4 72 67 2 0 6 10))))
--> (((15/4 74 68 1/4 0 4 7) (15/4 65 63 1/4 0 4 6)
  (15/4 59 59 1/4 1 4 5) (3 48 53 3 1 6 0))
  (0 1 2 3 4 5 6 7) (10 9 8 7 6 5 0))
```

This function uses the function `chord-candidate-offtimes-strict` instead of `chord-candidate-offtimes`, and performs a sort on the output, according to the optional argument `sort-index`. The function takes an ontime  $t$ , a list of datapoints of length  $N$ , with offsets and enumeration appended, but in

original order, as well as the datapoints having had the function prepared-for-segments applied. It returns any datapoints which exist at the point  $t$ , as well as lists which help speed up any subsequent searches.

## segments

Started, last checked	16/1/2009, 24/1/2009
Location	Segmentation
Calls	add-to-list, append-offtimes, enumerate-append, first-n-naturals, nth-list-of-lists, prepare-for-segments
Called by	
Comments/see also	A more efficient implementation is required.

Example:

```
(segments
'((2368 66 191 2 49) (1579 62 1920 3 49)
  (1974 64 191 3 49) (1974 67 191 2 49)
  (2368 62 191 3 49) (1579 66 191 2 49)
  (2763 64 191 2 49) (2763 57 191 3 49)
  (2800 72 191 1 49) (3158 38 191 4 49)
  (3158 54 385 3 49) (3158 62 385 2 49)
  (3553 42 191 4 49) (3947 45 191 4 49)
  (4342 50 191 4 49)))
--> ((1579 ((1579 66 191 2 49 1770 5)
  (1579 62 1920 3 49 3499 1)))
  (1770 ((1579 66 191 2 49 1770 5)
  (1579 62 1920 3 49 3499 1)))
  (1974 ((1974 67 191 2 49 2165 3)
  (1974 64 191 3 49 2165 2)
  (1579 62 1920 3 49 3499 1)))
  (2165 ((1974 67 191 2 49 2165 3)
  (1974 64 191 3 49 2165 2)
  (1579 62 1920 3 49 3499 1)))
  (2368 ((2368 62 191 3 49 2559 4)
  (2368 66 191 2 49 2559 0)
  (1579 62 1920 3 49 3499 1)))
  (2559 ((2368 62 191 3 49 2559 4)
  (2368 66 191 2 49 2559 0)
  (1579 62 1920 3 49 3499 1)))
```

```

(2763 ((2763 57 191 3 49 2954 7)
(2763 64 191 2 49 2954 6)
(1579 62 1920 3 49 3499 1)))
(2800 ((2800 72 191 1 49 2991 8)
(2763 57 191 3 49 2954 7)
(2763 64 191 2 49 2954 6)
(1579 62 1920 3 49 3499 1)))
(2954 ((2800 72 191 1 49 2991 8)
(2763 57 191 3 49 2954 7)
(2763 64 191 2 49 2954 6)
(1579 62 1920 3 49 3499 1)))
(2991 ((2800 72 191 1 49 2991 8)
(1579 62 1920 3 49 3499 1)))
(3158 ((3158 62 385 2 49 3543 11)
(3158 54 385 3 49 3543 10)
(3158 38 191 4 49 3349 9)
(1579 62 1920 3 49 3499 1)))
(3349 ((3158 62 385 2 49 3543 11)
(3158 54 385 3 49 3543 10)
(3158 38 191 4 49 3349 9)
(1579 62 1920 3 49 3499 1)))
(3499 ((3158 62 385 2 49 3543 11)
(3158 54 385 3 49 3543 10)
(1579 62 1920 3 49 3499 1)))
(3543 ((3158 62 385 2 49 3543 11)
(3158 54 385 3 49 3543 10)))
(3553 ((3553 42 191 4 49 3744 12)))
(3744 ((3553 42 191 4 49 3744 12)))
(3947 ((3947 45 191 4 49 4138 13)))
(4138 ((3947 45 191 4 49 4138 13)))
(4342 ((4342 50 191 4 49 4533 14)))
(4533 ((4342 50 191 4 49 4533 14)))

```

This function takes a list of datapoints as its argument. First it creates a variable containing the distinct times (on and off) of the datapoints. Then it returns the segment for each of these times.



**segments-strict**

Started, last checked	16/1/2009, 24/1/2009
Location	Segmentation
Calls	add-to-list, append-offtimes, enumerate-append, first-n-naturals, nth-list-of-lists, prepare-for-segments
Called by	
Comments/see also	A more efficient implementation is required.

Example:

```
(segments-strict
'((3 48 53 3 1) (3 67 64 3/4 0) (3 76 69 3/4 0)
  (15/4 65 63 1/4 0) (15/4 74 68 1/4 0) (4 64 62 2 0)
  (4 72 67 2 0) (13/2 61 60 1/2 0) (7 62 61 1/2 0)
  (15/2 64 62 1/2 0) (8 50 54 1 1) (8 65 63 1 0))
1 3)
--> ((3 ((3 48 53 3 1 6 0) (3 67 64 3/4 0 15/4 1)
  (3 76 69 3/4 0 15/4 2)))
  (15/4 ((3 48 53 3 1 6 0) (15/4 65 63 1/4 0 4 3)
  (15/4 74 68 1/4 0 4 4)))
  (4 ((3 48 53 3 1 6 0) (4 64 62 2 0 6 5)
  (4 72 67 2 0 6 6)))
  (6 NIL)
  (13/2 ((13/2 61 60 1/2 0 7 7)))
  (7 ((7 62 61 1/2 0 15/2 8)))
  (15/2 ((15/2 64 62 1/2 0 8 9)))
  (8 ((8 50 54 1 1 9 10) (8 65 63 1 0 9 11)))
  (9 NIL))
```

This function uses the function `segment-strict` instead of `segement`. The function takes a list of datapoints as its argument. First it creates a variable containing the distinct times (on and off) of the datapoints. Then it returns the segment for each of these times.

**4.5.2 Spacing states**

The functions here use segmentations to build different types of states. One, output by the function `spacing-holding-states`, consists of chord spacing and holding types. Another, output by the function `beat-spacing-states`, consists of beat-of-bar and chord spacing.

**bass-steps**

Started, last checked	24/8/2010, 24/8/2010
Location	Spacing states
Calls	
Called by	spacing-holding-states
Comments/see also	bass-steps-with-rests

Example:

```
(bass-steps
'(((56 0 0) (60 1 1) (72 1 2))
  ((58 1 3) (60 2 1) (72 3 2))
  ((58 2 3) (65 1 4) (72 3 2))
  ((56 0 5) (65 2 4) (72 2 2))
  ((55 0 6) (64 0 7) (73 1 8)) ((NIL NIL NIL))
  ((54 2 9) (70 2 10) (74 0 11))
  ((59 0 12) (63 1 13) (75 1 14))))
--> '(2 0 -2 -1 NIL NIL 5)
```

This function takes a list of sorted holding types and returns the intervals between the bass notes of adjacent segments. It handles null entries, but these will have been removed if it is being called by the function spacing-holding-states.

**bass-steps-with-rests**

Started, last checked	24/8/2010, 24/8/2010
Location	Spacing states
Calls	
Called by	beat-spacing-states, beat-spacing-states<-
Comments/see also	bass-steps

Example:

```
(bass-steps-with-rests
'((3 ((3 48 53 3 1 6 0) (3 67 64 3/4 0 15/4 1)
      (3 76 69 3/4 0 15/4 2)))
  (15/4 ((3 48 53 3 1 6 0) (15/4 65 63 1/4 0 4 3)
        (15/4 74 68 1/4 0 4 4)))
  (4 ((3 48 53 3 1 6 0) (4 64 62 2 0 6 5))
```

```

      (4 72 67 2 0 6 6)))
(6 NIL)
(13/2 ((13/2 61 60 1/2 0 7 7)))
(7 ((7 62 61 1/2 0 15/2 8)))
(15/2 ((15/2 64 62 1/2 0 8 9)))
(8 ((8 50 54 1 1 9 10) (8 65 63 1 0 9 11)))
(9 NIL)))
--> '(0 0 NIL 13 1 2 -14)

```

This function is similar to the function `bass-steps`. Rather than waiting for the next two consecutive non-nil states to calculate step sizes, it calculates step sizes across a rest state.

### beat-spacing-states

Started, last checked	24/8/2010, 24/8/2010
Location	Spacing states
Calls	append-offtimes, bass-steps-with-rests, enumerate-append, nth-list-of-lists, segments-strict, spacing
Called by	
Comments/see also	beat-spacing-states<-, spacing-holding-states

Example:

```

(beat-spacing-states
 '( (3 48 53 3 1) (3 67 64 3/4 0) (3 76 69 3/4 0)
    (15/4 65 63 1/4 0) (15/4 74 68 1/4 0) (4 64 62 2 0)
    (4 72 67 2 0) (13/2 61 60 1/2 0) (7 62 61 1/2 0)
    (15/2 64 62 1/2 0) (8 50 54 1 1) (8 65 63 1 0))
  "C-68-3-mini" 3 1 3)
--> (((1 (19 9))
      (NIL NIL "C-68-3-mini"
        ((3 48 53 3 1 6 0) (3 67 64 3/4 0 15/4 1)
          (3 76 69 3/4 0 15/4 2)))))
    ((7/4 (17 9))
      (0 0 "C-68-3-mini"
        ((3 48 53 3 1 6 0) (15/4 65 63 1/4 0 4 3)
          (15/4 74 68 1/4 0 4 4)))))
    ((2 (16 8))

```

```

(0 0 "C-68-3-mini"
  ((3 48 53 3 1 6 0) (4 64 62 2 0 6 5)
   (4 72 67 2 0 6 6))))
((1 "rest")
 (NIL NIL "C-68-3-mini" NIL))
((3/2 NIL)
 (13 7 "C-68-3-mini"
  ((13/2 61 60 1/2 0 7 7))))
((2 NIL)
 (1 1 "C-68-3-mini"
  ((7 62 61 1/2 0 15/2 8))))
((5/2 NIL)
 (2 1 "C-68-3-mini"
  ((15/2 64 62 1/2 0 8 9))))
((3 (15))
 (-14 -8 "C-68-3-mini"
  ((8 50 54 1 1 9 10) (8 65 63 1 0 9 11))))

```

Suppose you have three states  $X_{n-1}, X_n, X_{n+1}$ . The function `beat-spacing-states` looks at the beat and spacing of  $X_n$ , and also records the difference between the bass notes of  $X_n$  and  $X_{n-1}$ .

### **beat-spacing-states<-**

Started, last checked	24/8/2010, 24/8/2010
Location	Spacing states
Calls	append-offtimes, bass-steps-with-rests, enumerate-append, nth-list-of-lists, segments-strict, spacing
Called by	
Comments/see also	beat-spacing-states, spacing-holding-states

Example:

```

(beat-spacing-states<-
 '( ( (3 48 53 3 1) (3 67 64 3/4 0) (3 76 69 3/4 0)
      (15/4 65 63 1/4 0) (15/4 74 68 1/4 0) (4 64 62 2 0)
      (4 72 67 2 0) (13/2 61 60 1/2 0) (7 62 61 1/2 0)
      (15/2 64 62 1/2 0) (8 50 54 1 1) (8 65 63 1 0))
  "C-68-3-mini" 3 1 3)
--> (((1 (19 9))

```

```

(NIL NIL "C-68-3-mini"
  ((3 48 53 3 1 6 0) (3 67 64 3/4 0 15/4 1)
   (3 76 69 3/4 0 15/4 2))))
((7/4 (17 9))
 (0 0 "C-68-3-mini"
  ((3 48 53 3 1 6 0) (15/4 65 63 1/4 0 4 3)
   (15/4 74 68 1/4 0 4 4))))
((2 (16 8))
 (0 0 "C-68-3-mini"
  ((3 48 53 3 1 6 0) (4 64 62 2 0 6 5)
   (4 72 67 2 0 6 6))))
((1 "rest")
 (NIL NIL "C-68-3-mini" NIL))
((3/2 NIL)
 (13 7 "C-68-3-mini"
  ((13/2 61 60 1/2 0 7 7))))
((2 NIL)
 (1 1 "C-68-3-mini"
  ((7 62 61 1/2 0 15/2 8))))
((5/2 NIL)
 (2 1 "C-68-3-mini"
  ((15/2 64 62 1/2 0 8 9))))
((3 (15))
 (-14 -8 "C-68-3-mini"
  ((8 50 54 1 1 9 10) (8 65 63 1 0 9 11))))

```

This function is very similar to the function `beat-spacing-states`. Suppose you have three states  $X_{n-1}, X_n, X_{n+1}$ . The function `beat-spacing-states` looks at the beat and spacing of  $X_n$ , and also records the difference between the bass notes of  $X_n$  and  $X_{n-1}$ . The function `beat-spacing-states<-` looks at the beat and spacing of  $X_n$ , and also records the difference between the bass notes of  $X_{n+1}$  and  $X_n$ .

## holding-type

Started, last checked	24/8/2010, 24/8/2010
Location	Spacing states
Calls	holding-type-finish, holding-type-normal, holding-type-start
Called by	holding-types
Comments/see also	

Example:

```
(holding-type
 '(1/2
  ((1/2 65 1/2 1 58 1 4) (1/3 58 1/3 1 69 2/3 3)
   (0 72 1 1 71 1 2) (0 60 1/2 1 66 1/2 1)))
 '(2/3
  ((2/3 56 1/3 1 60 1 5) (1/2 65 1/2 1 58 1 4)
   (1/3 58 1/3 1 69 2/3 3) (0 72 1 1 71 1 2)))
 '(1
  ((1 73 3/2 1 69 5/2 8) (1 64 1 1 69 2 7)
   (1 55 1 1 66 2 6) (2/3 56 1/3 1 60 1 5)
   (1/2 65 1/2 1 58 1 4) (0 72 1 1 71 1 2))))
--> ((56 0 5) (65 2 4) (72 2 2))
```

The function `holding-type` calls to one of `holding-type-start`, `holding-type-normal` or `holding-type-finish`, according to the emptiness of its arguments.

## holding-type-finish

Started, last checked	24/8/2010, 24/8/2010
Location	Spacing states
Calls	<code>index-item-1st-occurs</code> , <code>nth-list-of-lists</code>
Called by	<code>holding-type</code>
Comments/see also	<code>holding-type-normal</code> , <code>holding-type-start</code>

Example:

```
(holding-type-finish
 '(11/2 ((4 67 2 1 55 6 20) (4 76 3/2 1 69 11/2 18)))
 '(6 ((4 67 2 1 55 6 20))))
--> (NIL NIL NIL)
```

The function `holding-type-finish` is called by the function `holding-type` in the event that the variable `next-segment` is empty. This only happens at the end of a list of segments. I am yet to think of an example where something other than an empty list should be returned.

**holding-type-normal**

Started, last checked	24/8/2010, 24/8/2010
Location	Spacing states
Calls	index-item-1st-occurs, my-last, nth-list-of-lists
Called by	holding-type
Comments/see also	holding-type-finish, holding-type-start

Example:

```
(holding-type-normal
 '(0 ((0 72 1 1 71 1 2) (0 60 1/2 1 66 1/2 1)
      (0 56 1/3 1 47 1/3 0)))
 '(1/3 ((1/3 58 1/3 1 69 2/3 3) (0 72 1 1 71 1 2)
        (0 60 1/2 1 66 1/2 1) (0 56 1/3 1 47 1/3 0)))
 '(1/2 ((1/2 65 1/2 1 58 1 4) (1/3 58 1/3 1 69 2/3 3)
        (0 72 1 1 71 1 2) (0 60 1/2 1 66 1/2 1))))
--> ((58 1 3) (72 3 2) (60 2 1))
```

The function `holding-type-normal` is called by the function `holding-type`, in ‘non-boundary circumstances’. Holding types are assigned appropriately, and returned as the second item in a sublist of lists, along with MIDI note numbers and identifiers.

**holding-type-start**

Started, last checked	24/8/2010, 24/8/2010
Location	Spacing states
Calls	index-item-1st-occurs, my-last, nth-list-of-lists
Called by	holding-type
Comments/see also	holding-type-finish, holding-type-normal

Example:

```
(holding-type-start
 '(0 ((0 72 1 1 71 1 2) (0 60 1/2 1 66 1/2 1)
      (0 56 1/3 1 47 1/3 0)))
 '(1/3 ((1/3 58 1/3 1 69 2/3 3) (0 72 1 1 71 1 2)
        (0 60 1/2 1 66 1/2 1) (0 56 1/3 1 47 1/3 0))))
--> ((72 1) (60 1) (56 0))
```

The function `holding-type-start` is called by the function `holding-type` in the datapoint that the variable `previous-segment` is empty. This only happens at the beginning of a list of segments. Holding types are assigned appropriately, and returned as the second item in a sublist of lists, along with MIDI note numbers and identifiers. It is possible to generate an error using this function, if there are ontimes less than the initial ontime present.

## holding-types

Started, last checked	24/8/2010, 24/8/2010
Location	Spacing states
Calls	<code>holding-type</code>
Called by	<code>spacing-holding-states</code>
Comments/see also	

Example:

```
(holding-types
'((0 ((0 72 1 1 71 1 2) (0 60 1/2 1 66 1/2 1)
      (0 56 1/3 1 47 1/3 0)))
  (1/3 ((1/3 58 1/3 1 69 2/3 3) (0 72 1 1 71 1 2)
        (0 60 1/2 1 66 1/2 1) (0 56 1/3 1 47 1/3 0)))
  (1/2 ((1/2 65 1/2 1 58 1 4) (1/3 58 1/3 1 69 2/3 3)
        (0 72 1 1 71 1 2) (0 60 1/2 1 66 1/2 1)))
  (2/3 ((2/3 56 1/3 1 60 1 5) (1/2 65 1/2 1 58 1 4)
        (1/3 58 1/3 1 69 2/3 3) (0 72 1 1 71 1 2)))
  (1 ((2/3 56 1/3 1 60 1 5) (1/2 65 1/2 1 58 1 4)
      (0 72 1 1 71 1 2)))))
--> (((72 1 2) (60 1 1) (56 0 0))
      ((58 1 3) (72 3 2) (60 2 1))
      ((65 1 4) (58 2 3) (72 3 2))
      ((56 0 5) (65 2 4) (72 2 2))
      ((NIL NIL NIL) (NIL NIL NIL) (NIL NIL NIL)))
```

This function assigns holding-types to the datapoints at each segment: 0 for unheld; 1 for held- forward; 2 for held-backward; 3 for held-both. This information is returned, along with the MIDI note numbers and identifiers.



**index-rests**

Started, last checked	24/8/2010, 24/8/2010
Location	Spacing states
Calls	
Called by	spacing-holding-states
Comments/see also	

Example:

```
(index-rests
 '(((59 0 12) (63 0 13) (75 0 14)) NIL
   ((60 1 15) (63 0 16)) ((60 2 15)) (NIL NIL NIL)))
--> (1)
```

A list of sorted holdings is the only argument to this function. The output is the indices of those sub-lists which are empty (excluding the last sub-list) and therefore harbour rests.

**intervals-above-bass**

Started, last checked	24/8/2010, 24/8/2010
Location	Spacing states
Calls	
Called by	
Comments/see also	Deprecated.

Example:

```
(intervals-above-bass
 0 '((59 0 12) (63 1 13) (75 1 14)))
--> (0 4 16)
```

An index  $n$  is provided as first argument; a list of lists is the second argument. The  $n$ th item of each sub-list is a MIDI note number, and these sub-lists are in order of ascending MIDI note number. The intervals above the bass are returned. It is possible to produce nonsense output if null values are interspersed with non-null values. I use the function chord-spacing in preference to the function intervals-above-bass.

**sort-holding-types**

Started, last checked	24/8/2010, 24/8/2010
Location	Spacing states
Calls	sort-by
Called by	spacing-holding-states
Comments/see also	

Example:

```
(sort-holding-types
 '(((72 1 2) (60 1 1) (56 0 0)) ((NIL NIL NIL))
   ((58 1 3) (72 3 2) (58 3 1))))
--> (((56 0 0) (60 1 1) (72 1 2)) ((NIL NIL NIL))
      ((58 1 3) (58 3 1) (72 3 2)))
```

The sub-lists are returned, ordered by MIDI note number and then holding-type (both ascending). The function checks for empty chords to avoid errors occurring in the sort function.

**spacing**

Started, last checked	24/8/2010, 24/8/2010
Location	Spacing states
Calls	
Called by	beat-spacing-states, beat-spacing-states<-, spacing-holding-states
Comments/see also	intervals-above-bass

Example:

```
(spacing 0 '((59 0 12) (63 1 13) (75 1 14)))
--> (4 12)
```

An index  $n$  is provided as first argument; a list of lists is the second argument. The  $n$ th item of each sub-list is a MIDI note number, and these sub-lists are in order of ascending MIDI note number. The intervals between adjacent notes (chord spacing) are returned. It is possible to produce nonsense output if null values are interspersed with non-null values.

**spacing-holding-states**

Started, last checked	24/8/2010, 24/8/2010
Location	Spacing states
Calls	append-offtimes, bass-steps, enumerate-append, index-rests, nth-list, nth-list-of-lists, remove-nth-list, sort-holding-types, spacing
Called by	
Comments/see also	beat-spacing-states, beat-spacing-states<-

Example:

```
(spacing-holding-states
'((0 74 1/2 1 84) (0 52 1 2 84) (1/2 76 1/4 1 84)
(3/4 78 1/4 1 84) (1 80 1/4 1 84) (5/4 81 1/4 1 84)
(3/2 83 1/2 1 84) (4 67 1 2 84) (4 64 1 2 84)
(4 79 1/2 1 84) (9/2 78 1/2 1 84) (5 67 1 2 84)
(5 64 1 2 84) (5 76 2 1 84)) "D Scarlatti L484" 2)
--> (((((22) (1 0))
(NIL 1/2 "D Scarlatti L484"
((0 52 1 2 84 1 1) (0 74 1/2 1 84 1/2 0))))
(((24) (3 0))
(0 1/4 "D Scarlatti L484"
((0 52 1 2 84 1 1) (1/2 76 1/4 1 84 3/4 2))))
(((26) (2 0))
(0 1/4 "D Scarlatti L484"
((0 52 1 2 84 1 1) (3/4 78 1/4 1 84 1 3))))
((NIL (0))
(28 1/4 "D Scarlatti L484"
((1 80 1/4 1 84 5/4 4))))
((NIL (0))
(1 1/4 "D Scarlatti L484"
((5/4 81 1/4 1 84 3/2 5))))
((NIL (0))
(2 5/2 "D Scarlatti L484"
((3/2 83 1/2 1 84 2 6))))
(((3 12) (1 1 0))
(-19 1/2 "D Scarlatti L484"
((4 64 1 2 84 5 8) (4 67 1 2 84 5 7)
(4 79 1/2 1 84 9/2 9)))))
```

```

(((3 11) (2 2 0))
 (0 1/2 "D Scarlatti L484"
  ((4 64 1 2 84 5 8) (4 67 1 2 84 5 7)
   (9/2 78 1/2 1 84 5 10))))
(((3 9) (0 0 1))
 (0 1 "D Scarlatti L484"
  ((5 64 1 2 84 6 12) (5 67 1 2 84 6 11)
   (5 76 2 1 84 7 13))))
((NIL (2))
 (12 1 "D Scarlatti L484"
  ((5 76 2 1 84 7 13)))))

```

This function takes datapoints as its argument, and some optional catalogue information about those datapoints. It converts the input into a list of sub-lists, with each sub-list consisting of a pair of lists. The first of the pair contains a chord spacing, followed by holding types relating to the notes of the chord. The second of the pair retains the following information: the step (in semitones) between the bass note of the previous chord and the current state; the duration of the state (which can exceed the minimum duration of the constituent datapoints if rests are present); the catalogue information; the relevant original datapoints, with offtimes and enumeration appended.

### 4.5.3 Markov analyse

The functions here are designed to analyse data according to a Markov-chain model. At present the code handles a first-order analysis. The aim is to build a state transition matrix for some variables (referenced by variable-names and catalogue). Hence, the variable variable-names points to some actual data (note the use of the function symbol-value) which is indexed by the variable catalogue. Using the function write-to-file, the information can be sent to a text file, to avoid having to display it.

#### accumulate-to-stm

Started, last checked	27/1/2009, 24/8/2010
Location	Markov analyse
Calls	
Called by	present-to-stm
Comments/see also	accumulate-to-stm<-, add-to-stm

Example:

```
(accumulate-to-stm
 '(((4) ("Piece A")) ((2) ("Piece A"))))
 '((4) (((1) ("Piece B")) ((2) ("Piece C"))))
 '(((1) (((5) ("Piece A")) ((4) ("Piece B"))))
   ((2) (((5) ("Piece A"))))
   ((4) (((1) ("Piece B"))
          ((2) ("Piece C"))))
   ((5) (((4) ("Piece B"))))))
--> '(((4) (((2) ("Piece A")) ((1) ("Piece B"))
   ((2) ("Piece C"))))
   ((1) (((5) ("Piece A")) ((4) ("Piece B"))))
   ((2) (((5) ("Piece A"))))
   ((5) (((4) ("Piece B")))))
```

The first argument is a listed state; the second is the relevant row of the state transition matrix; the third is the state transition matrix itself. This function is called when the state of the first item of the listed state has appeared in the state transition matrix before. The references of the event are included.

## add-to-stm

Started, last checked	27/1/2009, 24/8/2010
Location	Markov analyse
Calls	
Called by	present-to-stm
Comments/see also	accumulate-to-stm, add-to-stm<-

Example:

```
(add-to-stm
 '(((3) ("Piece A")) ((4) ("Piece A"))))
 '(((1) (((5) ("Piece A")) ((4) ("Piece B"))))
   ((2) (((5) ("Piece A"))))
   ((4) (((1) ("Piece B")) ((2) ("Piece C"))))
   ((5) (((4) ("Piece B"))))))
--> '(((3) (((4) ("Piece A"))))
   ((1) (((5) ("Piece A")) ((4) ("Piece B"))))
   ((2) (((5) ("Piece A"))))
   ((4) (((1) ("Piece B")) ((2) ("Piece C"))))
   ((5) (((4) ("Piece B")))))
```

The first argument is a listed state; the second is the state transition matrix. This function is called when the state of the first item of the listed state has not appeared in the state transition matrix before. It is added.

### construct-initial-states

Started, last checked	27/1/2009, 24/8/2010
Location	Markov analyse
Calls	beat-spacing-states, firstn, spacing-holding-states
Called by	
Comments/see also	construct-final-states, construct-stm, construct-stm<-

Example:

```
(progn
  (setq
    variable-1
    '((0 30 1 1 84) (0 33 1 1 84) (1 40 1 1 84)
      (1 41 1 1 84)))
  (setq
    variable-2
    '((0 60 1 1 84) (0 63 1 1 84) (1 62 1 1 84)
      (1 63 1 1 84)))
  (setq *variable-names* '(variable-1 variable-2))
  (setq *catalogue* '("variable-1" "variable-2"))
  (construct-initial-states
    *variable-names* *catalogue*))
--> '((((3) (0 0))
      (NIL 1 "variable-1"
        ((0 30 1 1 84 1 0) (0 33 1 1 84 1 1))))
      ((3) (0 0))
      (NIL 1 "variable-2"
        ((0 60 1 1 84 1 0) (0 63 1 1 84 1 1)))))
```

This recursion analyses one variable name at a time, taking a catalogue name from the variable catalogue, and outputs initial states accordingly.

**construct-stm**

Started, last checked	27/1/2009, 24/8/2010	
Location	Markov analyse	
Calls	beat-spacing-states, spacing-holding-states	markov-analyse,
Called by		
Comments/see also	construct-final-states, states, construct-stm<-	construct-initial-

Example:

```
(progn
  (setq
    variable-1
    '((0 30 1 1 84) (0 33 1 1 84) (1 40 1 1 84)
      (1 41 1 1 84)))
  (setq
    variable-2
    '((0 60 1 1 84) (0 63 1 1 84) (1 62 1 1 84)
      (1 63 1 1 84)))
  (setq *variable-names* '(variable-1 variable-2))
  (setq *catalogue* '("variable-1" "variable-2"))
  (construct-stm
    *variable-names* *catalogue* "beat-spacing-states"
    2 4 1)
--> "Finished"
*transition-matrix*
--> (((1 (3))
      ((2 (1))
        (2 0 "variable-2"
          ((1 62 1 1 84 2 2) (1 63 1 1 84 2 3))))
      ((2 (1))
        (10 0 "variable-1"
          ((1 40 1 1 84 2 2) (1 41 1 1 84 2 3)))))))
```

This recursion analyses one variable name at a time, taking a catalogue name from the variable catalogue, and updates the transition matrix accordingly. The output "Finished" is preferable to the transition matrix, which is large enough that it can cause the Listener to crash.

**firstn-list**

Started, last checked	27/1/2009, 24/8/2010
Location	Markov analyse
Calls	firstn
Called by	markov-analyse
Comments/see also	

Example:

```
(firstn-list 3 '(1 2 3 4 5)
--> '((1 2 3) (2 3 4) (3 4 5))
```

This function applies the function `firstn` recursively to a list. It is like producing an *n*-gram, and is useful for building a first-order Markov model. I call the output 'listed states'.

**markov-analyse**

Started, last checked	27/1/2009, 24/8/2010
Location	Markov analyse
Calls	update-stm
Called by	construct-stm
Comments/see also	markov-analyse<-

Example:

```
(markov-analyse
'(((3) ("Piece A")) ((6) ("Piece A"))
  ((4) ("Piece A")) ((4) ("Piece A"))
  ((3) ("Piece A")) ((2) ("Piece A")))))
--> "Finished"
*transition-matrix*
--> '(((3) ((2) ("Piece A")) ((6) ("Piece A"))))
      ((4) ((3) ("Piece A")) ((4) ("Piece A"))))
      ((6) ((4) ("Piece A")))))
```

This function has one argument - some states which are to be analysed according to a first-order Markov model. Note the need to define a variable here, `*transition-matrix*`. The output "Finished" is preferable to the transition matrix, which is large enough that it can cause the Listener to crash.



**present-to-stm**

Started, last checked	27/1/2009, 24/8/2010
Location	Markov analyse
Calls	add-to-stm, accumulate-to-stm
Called by	update-stm
Comments/see also	present-to-stm<-

Example:

```
(present-to-stm
'(((4) ("Piece A")) ((2) ("Piece A"))))
'(((1) (((5) ("Piece A")) ((4) ("Piece B"))))
((2) (((5) ("Piece A"))))
((4) (((1) ("Piece B")) ((2) ("Piece C"))))
((5) (((4) ("Piece B"))))))
--> '(((4) (((2) ("Piece A")) ((1) ("Piece B"))
((2) ("Piece C"))))
((1) (((5) ("Piece A")) ((4) ("Piece B"))))
((2) (((5) ("Piece A"))))
((5) (((4) ("Piece B"))))))).
```

This function calls either the function `accumulate-to-stm`, or `add-to-stm`, depending on whether the first argument, a listed-state, has appeared in the second argument, a state-transition matrix, before. The example above results in `accumulate-to-stm` being called, as the state of (4) has occurred before. However, changing this state to (3) in the argument would result in `add-to-stm` being called.

**update-stm**

Started, last checked	27/1/2009, 24/8/2010
Location	Markov analyse
Calls	present-to-stm
Called by	markov-analyse
Comments/see also	update-stm<-

Example:

```
(update-stm
'(((3) ("Piece A")) ((6) ("Piece A"))))
```

```

      (((6) ("Piece A")) ((4) ("Piece A")))
      (((4) ("Piece A")) ((4) ("Piece A")))
      (((4) ("Piece A")) ((3) ("Piece A")))
      (((3) ("Piece A")) ((2) ("Piece A"))))
--> '(((3) (((2) ("Piece A")) ((6) ("Piece A"))))
      ((4) (((3) ("Piece A")) ((4) ("Piece A"))))
      ((6) (((4) ("Piece A")))))

```

This function has as its argument listed states, and it applies the function `present-to-stm` recursively to these listed states. The variable `*transition-matrix*` is updated as it proceeds.

#### 4.5.4 Markov analyse backwards

The functions here are very similar to those contained in the file `markov-analyse.lisp`. Whereas those functions are designed to analyse data according to a Markov-chain model that runs forward in time, these functions do the same for going backwards in time.

##### **accumulate-to-stm<-**

Started, last checked	4/10/2010, 4/10/2010
Location	Markov analyse backwards
Calls	
Called by	<code>present-to-stm&lt;-</code>
Comments/see also	<code>accumulate-to-stm</code> , <code>add-to-stm&lt;-</code>

Example:

```

(accumulate-to-stm<-
 '(((4) ("Piece A")) ((2) ("Piece A"))))
 '((2) (((5) ("Piece A"))))
 '(((1) (((5) ("Piece A")) ((4) ("Piece B"))))
      ((2) (((5) ("Piece A"))))
      ((4) (((1) ("Piece B")) ((2) ("Piece C"))))
      ((5) (((4) ("Piece B")))))
--> '(((2) (((4) ("Piece A")) ((5) ("Piece A"))))
      ((1) (((5) ("Piece A")) ((4) ("Piece B"))))
      ((4) (((1) ("Piece B")) ((2) ("Piece C"))))
      ((5) (((4) ("Piece B")))))

```

This function is similar to the function `accumulate-to-stm`, the difference being  $X_n$  is looked up and  $X_{n-1}$  accumulated to the state- transition matrix. The first argument is a listed state; the second is the relevant row of the state transition matrix; the third is the state transition matrix itself. This function is called when the state of the second item of the listed state has appeared in the state transition matrix before. The references of the event are included.

### **add-to-stm<-**

Started, last checked	4/10/2010, 4/10/2010
Location	Markov analyse backwards
Calls	
Called by	<code>present-to-stm&lt;-</code>
Comments/see also	<code>accumulate-to-stm&lt;-</code> , <code>add-to-stm</code>

Example:

```
(add-to-stm<-
'(((4) ("Piece A")) ((3) ("Piece A"))))
'(((1) (((5) ("Piece A")) ((4) ("Piece B"))))
  ((2) (((5) ("Piece A"))))
  ((4) (((1) ("Piece B")) ((2) ("Piece C"))))
  ((5) (((4) ("Piece B"))))))
--> '(((3) (((4) ("Piece A"))))
      ((1) (((5) ("Piece A")) ((4) ("Piece B"))))
      ((2) (((5) ("Piece A"))))
      ((4) (((1) ("Piece B")) ((2) ("Piece C"))))
      ((5) (((4) ("Piece B"))))))
```

This function is similar to the function `add-to-stm`, the difference being  $X_n$  is looked up and  $X_{n-1}$  added to the state-transition matrix. The first argument is a listed state; the second is the state transition matrix. This function is called when the state of the first item of the listed state has not appeared in the state transition matrix before. It is added.

**construct-final-states**

Started, last checked	4/10/2010, 4/10/2010
Location	Markov analyse backwards
Calls	beat-spacing-states, lastn, spacing-holding-states
Called by	
Comments/see also	construct-initial-states, construct-stm, construct-stm<-

Example:

```
(progn
  (setq
    variable-1
    '((0 60 60 2 0) (0 63 62 1 0) (1 67 64 2 0)
      (2 59 59 1 0)))
  (setq
    variable-2
    '((0 64 62 1 0) (1 62 61 1 0) (1 69 65 2 0)
      (2 66 63 1 0)))
  (setq *variable-names* '(variable-1 variable-2))
  (setq *catalogue* '("variable-1" "variable-2"))
  (construct-final-states
    *variable-names* *catalogue* "beat-spacing-states"
    10 3 3 1))
--> '(((3 (8))
  (NIL NIL "variable-1"
    ((2 59 59 1 0 3 3) (1 67 64 2 0 3 2))))
  ((3 (3))
  (NIL NIL "variable-2"
    ((2 66 63 1 0 3 3) (1 69 65 2 0 3 2)))))
```

This function is similar to the function `construct-stm`, the difference being  $X_n$  is looked up and  $X_{n-1}$  is accumulated or added to a state- transition matrix. This recursion analyses one variable name at a time, taking a catalogue name from the variable catalogue, and outputs final states accordingly.

**construct-stm<-**

Started, last checked	4/10/2010, 4/10/2010
Location	Markov analyse backwards
Calls	beat-spacing-states, markov-analyse<-, spacing-holding-states
Called by	
Comments/see also	construct-final-states, construct-initial-states, construct-stm

Example:

```
(progn
  (setq
    variable-1
    '((0 60 60 2 0) (0 63 62 1 0) (1 67 64 2 0)
      (2 59 59 1 0)))
  (setq
    variable-2
    '((0 64 62 1 0) (1 62 61 1 0) (1 69 65 2 0)
      (2 66 63 1 0)))
  (setq *variable-names* '(variable-1 variable-2))
  (setq *catalogue* '("variable-1" "variable-2"))
  (construct-stm<-
    *variable-names* *catalogue* "beat-spacing-states"
    3 3 1))
--> "Finished"
*transition-matrix*
--> (((3 (3))
      ((2 (7))
        (4 2 "variable-2"
          ((1 62 61 1 0 2 1) (1 69 65 2 0 3 2))))))
      ((2 (7))
        ((1 NIL)
          (-2 -1 "variable-2"
            ((0 64 62 1 0 1 0))))
        ((1 (3))
          (0 0 "variable-1"
            ((0 60 60 2 0 2 0) (0 63 62 1 0 1 1))))))
      ((3 (8))
        ((2 (7))
```

```
(-1 -1 "variable-1"
  ((0 60 60 2 0 2 0) (1 67 64 2 0 3 2))))))
```

This function is similar to the function `construct-stm`, the difference being  $X_n$  is looked up and  $X_{n-1}$  is accumulated or added to a state- transition matrix. This recursion analyses one variable name at a time, taking a catalogue name from the variable catalogue, and updates the transition matrix accordingly. The output "Finished" is preferable to the transition matrix, which is large enough that it can cause the Listener to crash.

### **markov-analyse<-**

Started, last checked	4/10/2010, 4/10/2010
Location	Markov analyse backwards
Calls	update-stm<-
Called by	construct-stm<-
Comments/see also	markov-analyse

Example:

```
(markov-analyse<-
  '(((3) ("Piece A")) ((6) ("Piece A"))
    ((4) ("Piece A")) ((4) ("Piece A"))
    ((3) ("Piece A")) ((2) ("Piece A")))))
--> "Finished"
*transition-matrix*
--> '(((2) (((3) ("Piece A")))))
      ((3) (((4) ("Piece A")))))
      ((4) (((4) ("Piece A")) ((6) ("Piece A"))))
      ((6) (((3) ("Piece A")))))
```

This function is similar to the function `markov-analyse`, the difference being  $X_n$  is looked up and  $X_{n-1}$  is accumulated or added to a state- transition matrix. This function has one argument - some states which are to be analysed according to a backwards first-order Markov model. Note the need to define a variable here, `*transition-matrix*`. The output "Finished" is preferable to the transition matrix, which is large enough that it can cause the Listener to crash.

**present-to-stm<-**

Started, last checked	4/10/2010, 4/10/2010
Location	Markov analyse backwards
Calls	add-to-stm<-, accumulate-to-stm<-
Called by	update-stm<-
Comments/see also	present-to-stm

Example:

```
(present-to-stm<-
 '(((4) ("Piece A")) ((2) ("Piece A"))))
 '(((1) (((5) ("Piece A")) ((4) ("Piece B"))))
   ((2) (((5) ("Piece A"))))
   ((4) (((1) ("Piece B")) ((2) ("Piece C"))))
   ((5) (((4) ("Piece B"))))))
--> '(((2) (((4) ("Piece A")) ((5) ("Piece A"))))
    ((1) (((5) ("Piece A")) ((4) ("Piece B"))))
    ((4) (((1) ("Piece B")) ((2) ("Piece C"))))
    ((5) (((4) ("Piece B"))))))
```

This function is similar to the function `present-to-stm`, the difference being  $X_n$  is looked up and  $X_{n-1}$  is accumulated or added to a state- transition matrix. The function calls either the function `accumulate-to-stmj-`, or `add-to-stmj-`, depending on whether the first argument, a listed- state, has appeared in the second argument, a state- transition matrix, before. The example above results in `accumulate-to-stmj-` being called, as the state of (2) has occurred before. However, changing this state to (3) in the argument would result in `add-to-stmj-` being called.

**update-stm<-**

Started, last checked	4/10/2010, 4/10/2010
Location	Markov analyse backwards
Calls	present-to-stm<-
Called by	markov-analyse<-
Comments/see also	update-stm

Example:

```
(update-stm<-
```

```

'(((3) ("Piece A")) ((6) ("Piece A")))
  (((6) ("Piece A")) ((4) ("Piece A")))
  (((4) ("Piece A")) ((4) ("Piece A")))
  (((4) ("Piece A")) ((3) ("Piece A")))
  (((3) ("Piece A")) ((2) ("Piece A"))))
nil)
--> '(((2) (((3) ("Piece A"))))
      ((3) (((4) ("Piece A"))))
      ((4) (((4) ("Piece A")) ((6) ("Piece A"))))
      ((6) (((3) ("Piece A")))))

```

This function is similar to the function `update-stm`, the difference being  $X_n$  is looked up and  $X_{n-1}$  is accumulated or added to a state- transition matrix. This function has as its argument listed states, and it applies the function `present-to-stmj` recursively to these listed states. The variable `*transition-matrix*` is updated as it proceeds.

#### 4.5.5 Markov compose

These functions realise a sequence of states in some given transition matrix. The states are converted to datapoints so that they can be written to a MIDI file. A pivotal function is `states2datapoints`.

#### create-MIDI-note-numbers

Started, last checked	27/1/2009, 10/2/2009
Location	Markov compose
Calls	spacing2note-numbers
Called by	states2datapoints
Comments/see also	create-MIDI&morphetic-numbers, create-MIDI&morphetic-numbers<-

Example:

```

(create-MIDI-note-numbers
 '(((12 3 4) (1 0 1 1))
  (NIL 500 "b707b"
   ((3000 57 1000 4 96 4000 0)
    (3000 69 500 3 96 3500 1)
    (3000 72 1000 2 96 4000 2)
    (3000 76 1000 1 96 4000 3)))))

```



```

(((10 5 4) (2 0 3 2))
 (0 500 "b41500b"
  ((43000 52 1000 4 96 44000 54)
   (43500 62 500 3 96 44000 134)
   (43000 67 1500 2 96 44500 201)
   (43000 71 1000 1 96 44000 256))))))
--> (((((48 60 63 67) (1 0 1 1))
 (NIL 500 "b707b"
  ((3000 57 1000 4 96 4000 0)
   (3000 69 500 3 96 3500 1)
   (3000 72 1000 2 96 4000 2)
   (3000 76 1000 1 96 4000 3))))))
 (((48 58 63 67) (2 0 3 2))
  (0 500 "b41500b"
   ((43000 52 1000 4 96 44000 54)
    (43500 62 500 3 96 44000 134)
    (43000 67 1500 2 96 44500 201)
    (43000 71 1000 1 96 44000 256))))))

```

A list of realised states is provided, and this function returns so-called ‘half-states’: MIDI note numbers have been created from the chord spacings. To do this, we take the MIDI note number of the previous bass note, and the variable bass-step, which is the interval in semitones between the bass note of the current state and previous state as they appeared in the original data. If the current state is an initial state in some original data, then this will be empty, and so it is set to zero.

### half-state2datapoints

Started, last checked	27/1/2009, 10/2/2009
Location	Markov compose
Calls	state-note2datapoint
Called by	states2datapoints
Comments/see also	half-state2datapoints-by-lookup

Example:

```

(half-state2datapoints 0
 '(((48 60 63 67) (1 0 1 1))
  (NIL 500 "b707b"
   ((3000 57 1000 4 96 4000 0)

```

```

      (3000 69 500 3 96 3500 1)
      (3000 72 1000 2 96 4000 2)
      (3000 76 1000 1 96 4000 3))))
(((48 58 63 67) (2 0 3 2))
 (0 500 "b41500b"
  ((43000 52 1000 4 96 44000 54)
   (43500 62 500 3 96 44000 134)
   (43000 67 1500 2 96 44500 201)
   (43000 71 1000 1 96 44000 256))))
(((41 56 63 68) (1 1 2 1))
 (-7 500 "b37800n"
  ((62000 50 1000 4 96 63000 62)
   (62000 65 1000 3 96 63000 127)
   (61000 72 1500 2 96 62500 189)
   (62000 77 1000 1 96 63000 244))))
' (500 500 500 500 500) ' (0 500 1000 1500 2000 2500))
--> ((0 48 1000 4 96) (0 60 500 3 96)
      (0 63 1500 2 96) (0 67 1000 1 96))

```

This function increments over the  $i$ th note of a half-state,  $i = 0, 1, \dots, n - 1$ . If the  $i$ th note in this state is of tie-type 0 or 1 (corresponding to ‘untied’ or ‘tied-forward’) then the function `state-note2datapoint` is applied.

## index-of-offtime

Started, last checked	27/1/2009, 10/2/2009
Location	Markov compose
Calls	index-item-1st-occurs
Called by	state-note2datapoint
Comments/see also	index-of-offtime-by-lookup

Example:

```

(index-of-offtime 0 63
 '(((48 60 63 67) (1 0 1 1))
  (NIL 500 "b707b"
   ((3000 57 1000 4 96 4000 0)
    (3000 69 500 3 96 3500 1)
    (3000 72 1000 2 96 4000 2)
    (3000 76 1000 1 96 4000 3))))
 (((48 58 63 67) (2 0 3 2))

```

```

(0 500 "b41500b"
 ((43000 52 1000 4 96 44000 54)
  (43500 62 500 3 96 44000 134)
  (43000 67 1500 2 96 44500 201)
  (43000 71 1000 1 96 44000 256))))
(((41 56 63 68) (1 1 2 1))
 (-7 500 "b37800n"
  ((62000 50 1000 4 96 63000 62)
   (62000 65 1000 3 96 63000 127)
   (61000 72 1500 2 96 62500 189)
   (62000 77 1000 1 96 63000 244))))))
--> 2

```

Given a starting index, a note-number and some half-states to search through, this function returns the index of the half-state where the note-number in question comes to an end. This will be where its tie type is first equal to 0 or 2, indicating ‘untied’ and ‘tied-back’ respectively.

### realise-states

Started, last checked	27/1/2009, 10/2/2009
Location	Markov compose
Calls	choose-one
Called by	
Comments/see also	

Example:

```

(realise-states *initial-states* *stm* 2)
--> (((((4 3 5) (0 0 1 1))
  (NIL 500 "b43800b"
   ((3000 48 500 4 96 3500 0)
    (3000 52 500 3 96 3500 1)
    (3000 55 1000 2 96 4000 2)
    (3000 60 1000 1 96 4000 3))))))
(((4 5 5) (0 0 2 2))
 (-2 500 "b42600b"
  ((46500 60 500 4 96 47000 56)
   (46500 64 500 3 96 47000 126)
   (46000 69 1000 2 96 47000 191)
   (46000 74 1000 1 96 47000 253))))))

```

Given some initial states and a transition matrix, and an optional argument called count, this function realises a total of count states in the transition matrix. If a closed state is reached, then the process is terminated, and however many states have been generated by this stage are returned.

### scale-datapoints-by-factor

Started, last checked	27/1/2009, 10/2/2009
Location	Markov compose
Calls	choose-one
Called by	
Comments/see also	

Example:

```
(scale-datapoints-by-factor 2
 '( (0 48 1000 4 96) (0 60 500 3 96) (0 63 1500 2 96)
    (0 67 1000 1 96) (500 58 500 3 96)
    (1000 41 1000 4 96) (1000 56 1000 3 96)))
--> ((0 48 2000 4 96) (0 60 1000 3 96)
     (0 63 3000 2 96) (0 67 2000 1 96)
     (1000 58 1000 3 96) (2000 41 2000 4 96)
     (2000 56 2000 3 96))
```

The ontimes and durations of datapoints are scaled up or down by a constant factor.

### spacing2note-numbers

Started, last checked	27/1/2009, 10/2/2009
Location	Markov compose
Calls	add-to-list, fibonacci-list
Called by	create-MIDI-note-numbers
Comments/see also	

Example:

```
(spacing2note-numbers '(3 12) 64)
--> (64 67 79)
```

A chord spacing and note-number are inputs to this function. Returned are the MIDI note numbers of the chord whose lowest note is given by note-number, and whose spacing is as provided.

**state-durations**

Started, last checked	27/1/2009, 10/2/2009
Location	Markov compose
Calls	
Called by	states2datapoints
Comments/see also	state-durations-by-beat

Example:

```
(state-durations
'((((10 5 4) (2 0 3 2))
  (0 500 "b41500b"
    ((43000 52 1000 4 96 44000 54)
     (43500 62 500 3 96 44000 134)
     (43000 67 1500 2 96 44500 201)
     (43000 71 1000 1 96 44000 256))))
(((15 7 5) (1 1 2 1))
  (-7 500 "b37800n"
    ((62000 50 1000 4 96 63000 62)
     (62000 65 1000 3 96 63000 127)
     (61000 72 1500 2 96 62500 189)
     (62000 77 1000 1 96 63000 244))))
(((15 6 6) (2 2 0 2))
  (0 500 "b42600b"
    ((39000 45 1000 4 96 40000 47)
     (39000 60 1000 3 96 40000 119)
     (39500 66 500 2 96 40000 183)
     (39000 72 1000 1 96 40000 247))))
(((12 9 7) (1 0 0 1))
  (1 500 "b39100b"
    ((35000 53 2000 4 96 37000 31)
     (35000 65 500 3 96 35500 95)
     (35000 74 500 2 96 35500 162)
     (35000 81 1000 1 96 36000 225))))))
--> (500 500 500 500)
```

This function takes a list of states as its argument, and returns a list containing the duration of each state in a list. The set of so-called ‘partition points’ can be generated easily by applying the function `fibonacci-list`.

**state-note2datapoint**

Started, last checked	27/1/2009, 10/2/2009
Location	Markov compose
Calls	index-item-1st-occurs, index-of-offtime, min-item
Called by	half-state2datapoints
Comments/see also	state-note2datapoint-by-lookup

Example:

```
(state-note2datapoint 2 0
'((((48 60 63 67) (1 0 1 1))
  (NIL 500 "b707b"
    ((3000 57 1000 4 96 4000 0)
     (3000 69 500 3 96 3500 1)
     (3000 72 1000 2 96 4000 2)
     (3000 76 1000 1 96 4000 3))))
((48 58 63 67) (2 0 3 2))
(0 500 "b41500b"
  ((43000 52 1000 4 96 44000 54)
   (43500 62 500 3 96 44000 134)
   (43000 67 1500 2 96 44500 201)
   (43000 71 1000 1 96 44000 256))))
((41 56 63 68) (1 1 2 1))
(-7 500 "b37800n"
  ((62000 50 1000 4 96 63000 62)
   (62000 65 1000 3 96 63000 127)
   (61000 72 1500 2 96 62500 189)
   (62000 77 1000 1 96 63000 244))))
'(500 500 500) '(0 500 1000 1500))
--> (0 63 1500 2 96)
```

The  $i$ th note of the  $j$ th half-state is transformed into a so-called ‘datapoint’, meaning we find its ontime (the  $j$ th element of the partition points), its MIDI note number, its offtime, which is trickier. Other information, such as voicing and relative dynamics, are drawn from the initial occurrence of the half-state in question.

Returning to the calculation of offtime, we find the half-state  $k$  where the note ends and use this to calculate the duration of the note up until the  $k$ th state. Whichever is less—the  $k$ th state duration or the duration of this note

within the  $k$ th state—is added to give the total duration. This encapsulates the implicit encoding of rests.

## states2datapoints

Started, last checked	27/1/2009, 10/2/2009
Location	Markov compose
Calls	create-MIDI-note-numbers, fibonacci-list, half-state2datapoints, state-durations
Called by	
Comments/see also	states2datapoints-by-lookup, states2datapoints-by-lookup<-

Example:

```
(states2datapoints
'(((12 3 4) (1 0 1 1))
  (NIL 500 "b707b"
    ((3000 57 1000 4 96 4000 0)
     (3000 69 500 3 96 3500 1)
     (3000 72 1000 2 96 4000 2)
     (3000 76 1000 1 96 4000 3))))
(((10 5 4) (2 0 3 2))
 (0 500 "b41500b"
  ((43000 52 1000 4 96 44000 54)
   (43500 62 500 3 96 44000 134)
   (43000 67 1500 2 96 44500 201)
   (43000 71 1000 1 96 44000 256)))) 48)
--> ((0 48 1000 4 96) (0 60 500 3 96) (0 63 1000 2 96)
      (0 67 1000 1 96) (500 58 500 3 96))
```

This function applies the function `half-state2datapoint` recursively to a list of states. Some initial calculations are performed to obtain half-states, state durations and partition points.

### 4.5.6 Generating beat MNN spacing forwards

The main function here is called `generate-beat-MNN-spacing->`. Given initial states, a state-transition matrix, an upper limit for ontime, and a template dataset, it generates datapoints (among other output) that conform to various criteria, which can be specified using the optional arguments. The

criteria are things like: not too many consecutive states from the same source, the range is comparable with that of the template, and the likelihood of the states is comparable with those of the template.

## checklistp

Started, last checked	28/9/2010, 28/9/2010
Location	Generating beat MNN spacing forwards
Calls	comparable-likelihood-profilep, index-item-1st-doesnt-occur, lastn, mean&range, my-last, pitch&octave-spellingp, segments-strict
Called by	generate-beat-MNN-spacing->, generate-beat-spacing-forcing->
Comments/see also	checklist<-p

Example:

```
(setq
states
'(((1 (60 72 79 84 88) (60 67 71 74 76))
(NIL NIL "C-63-1"
((0 35 45 1/2 1 1/2 0)
(0 47 52 1/2 1 1/2 1)
(0 54 56 1/2 0 1/2 2)
(0 59 59 1/2 0 1/2 3)
(0 63 61 1/2 0 1/2 4)))))
((3/2 NIL NIL)
(NIL NIL "C-63-1" NIL))
((7/4 (54) (57))
(-6 -3 "C-63-1"
((831/4 56 57 1/4 0 208 701)))))
((2 (28 40 54 60 63) (42 49 57 60 62))
(-26 -15 "C-63-1"
((208 30 42 1 1 209 702)
(208 42 49 1 1 209 703)
(208 56 57 1 0 209 704)
(208 62 60 1 0 209 705)
(208 65 62 1 0 209 706))))))
(setq datapoints nil)
(setq checklist '("originalp"))
```



```

(setq c-sources 3)
(setq c-bar 12)
(setq c-min 7)
(setq c-max 7)
(setq c-beats 12)
(setq c-prob 0.1)
(checklistp
 states datapoints dataset-template
 template-segments checklist c-sources c-bar c-min
 c-max c-beats c-prob)
--> NIL

```

This function checks that the previous c-sources sources are not all the same, it checks whether the range is acceptable (using c-bar, c-min, and c-max), and whether the chord likelihoods are acceptable (using c-beats and c-prob). If all three of these aspects are acceptable, the function returns T, and NIL otherwise.

### choose-one-with-beat

Started, last checked	28/9/2010, 28/9/2010
Location	Generating beat MNN spacing forwards
Calls	
Called by	generate-beat-MNN-spacing->, generate-beat-spacing-forcing->
Comments/see also	

Example:

```

(setq
 mini-initial-states
 '(((3 NIL)
  (NIL NIL "C-6-1" ((-1 66 63 4/3 0 1/3 0))))
  ((1 (7 9 8))
  (NIL NIL "C-6-2"
   ((0 44 50 1 1 1 0) (0 51 54 1 1 1 1)
    (0 60 59 1 1 1 2) (0 68 64 1 0 1 3))))
  ((1 (7))
  (NIL NIL "C-6-3"
   ((0 52 55 1 1 1 0) (0 59 59 1 1 1 1))))
  ((3 NIL)

```

```

(NIL NIL "C-6-4" ((-1 70 66 3/2 0 1/2 0))))
((1 (24))
 (NIL NIL "C-7-1"
  ((0 41 49 1 1 1 0) (0 65 63 1/2 0 1/2 1)))))
(choose-one-with-beat 1 mini-initial-states)
--> ((1 (7))
      (NIL NIL "C-6-3"
       ((0 52 55 1 1 1 0) (0 59 59 1 1 1 1))))

```

This function takes a beat of a bar and a list of initial states as its arguments. These states may be genuinely initial, or constructed from appropriate beginnings. A search of the states is made beginning at a random index, and the first state whose beat matches that of the first argument is returned. In the event that all the states are searched, the output reverts to the original random index, so something is always output.

### comparable-likelihood-profilep

Started, last checked	28/9/2010, 28/9/2010
Location	Generating beat MNN spacing forwards
Calls	geom-mean-likelihood-of-subset, linearly-interpolate, max-item, min-item, nth-list-of-lists, orthogonal-projection-not-unique-equalp
Called by	checklistp
Comments/see also	comparable-likelihood-profile<-p

Example:

```

(setq
  ontime-state-points-pair
  '(7/2
    ((3 45 51 1 0) (7/2 71 66 1/2 0))))
(setq
  datapoints
  '((0 52 55 1 1) (0 59 59 1 1) (0 64 62 1 0)
    (0 68 64 1 0) (1 52 55 2 1) (1 59 59 1 1)
    (1 64 62 1 0) (1 68 64 1/2 0) (3/2 69 65 1/2 0)
    (2 62 61 1 0) (2 71 66 1/2 0) (5/2 66 63 1/2 0)
    (3 45 51 1 0) (3 64 62 1/2 0) (7/2 71 66 1/2 0)
    (4 52 55 2 1) (4 57 58 2 1) (4 61 60 2 1))

```

```

(4 69 65 1/2 0) (9/2 73 67 1/2 0) (5 76 69 1 0)
(6 38 47 1 1) (6 71 66 1/2 0) (13/2 69 65 1/2 0)
(7 50 54 1 1) (7 54 56 1 1) (7 57 58 2 1)
(7 66 63 1/2 0) (15/2 67 64 1/2 0) (8 49 53 1 1)
(8 52 55 1 1) (8 69 65 1 0) (9 33 44 1 1)
(9 64 62 1/2 0) (19/2 61 60 1/2 0) (10 45 51 1 1)
(10 52 55 1 1) (10 57 58 1 0) (11 45 51 1 1)
(11 52 55 1 1) (11 64 62 2 0) (12 45 51 1 1)
(12 57 58 1 1) (12 60 60 1 0)))
(setq c-beats 12)
(setq
  template-likelihood-profile
  '((0 0.19999999) (1 0.19999999) (2 0.16054831)
    (11/4 0.1875) (3 0.10939984) (4 0.07914095)
    (19/4 0.09988681) (5 0.08333333) (6 0.03448276)))
(setq c-prob 0.1)
(comparable-likelihood-profilep
  ontime-state-points-pair datapoints c-beats
  template-likelihood-profile c-prob)
--> T

```

This function takes a pair consisting of an ontime and points that sound at the ontime. Based on an empirical distribution over the argument named datapoints (with a context governed by c-beats), it calculates the geometric mean of the likelihood of these points. This likelihood is then compared with that at the same ontime in the template. If the absolute difference between the likelihoods is less than the threshold c-prob, T is returned, and NIL otherwise. T will also be returned if there are no points.

### full-segment-nearest;ontime

Started, last checked	28/9/2010, 28/9/2010
Location	Generating beat MNN spacing forwards
Calls	index-1st-sublist-item>, nth-list-of-lists
Called by	mean&range
Comments/see also	

Example:

```

(setq
  mini-template-segments

```

```

'((0
  ((0 52 55 1 1 1 0) (0 62 61 1 0 1 1)
   (0 64 62 1 0 1 2) (0 68 64 1 0 1 3)
   (0 71 66 1 0 1 4)))
 (1
  ((1 52 55 1 1 2 5) (1 62 61 1 0 2 6)
   (1 64 62 1 0 2 7) (1 68 64 1 0 2 8)
   (1 71 66 1 0 2 9)))
 (2
  ((2 52 55 1 1 3 10) (2 62 61 1 0 3 11)
   (2 64 62 1 0 3 12) (2 68 64 1 0 3 13)
   (2 72 67 3/4 0 11/4 14)))
 (11/4
  ((2 52 55 1 1 3 10) (2 62 61 1 0 3 11)
   (2 64 62 1 0 3 12) (2 68 64 1 0 3 13)
   (11/4 71 66 1/4 0 3 15)))
 (3
  ((3 45 51 3 1 6 16) (3 52 55 3 1 6 17)
   (3 60 60 3 0 6 18) (3 64 62 3 0 6 19)
   (3 71 66 1 0 4 20))))
(full-segment-nearest<ontime 1 mini-template-segments)
--> (1
  ((1 52 55 1 1 2 5) (1 62 61 1 0 2 6)
   (1 64 62 1 0 2 7) (1 68 64 1 0 2 8)
   (1 71 66 1 0 2 9)))

```

This function takes an ontime and a list of segments as its arguments. It returns the full (that is, non-null) segment whose ontime is closest to and less than the first argument. There should always be such a segment, but if there is not, NIL is returned.

**generate-beat-MNN-spacing->**

Started, last checked	28/9/2010, 28/9/2010
Location	Generating beat MNN spacing forwards
Calls	checklistp, choose-one, choose-one-with-beat, geom-mean-likelihood-of-states, index-1st-sublist-item>=, my-last, segments-strict, sort-dataset-asc, states2datapoints-by-lookup, translate-datapoints-to-first-ontime
Called by	
Comments/see also	Consider subdividing into several functions. See also generate-beat-MNN-spacing<-, generate-beat-spacing-forcing->.

Example:

```
(progn
  (setq
    initial-states
    (read-from-file
      (concatenate
        'string
        *MCStylistic-Oct2010-example-files-path*
        "/Racchman-Oct2010 example"
        "/initial-states.txt"))))
  (setq
    stm
    (read-from-file
      (concatenate
        'string
        *MCStylistic-Oct2010-example-files-path*
        "/Racchman-Oct2010 example"
        "/transition-matrix.txt"))))
  (setq no-ontimes> 6)
  (setq
    dataset-all
    (read-from-file
      (concatenate
        'string
```

```

*MCStylistic-Oct2010-data-path*
"/Dataset/C-41-2-ed.txt"))))
(setq
  dataset-template
  (subseq dataset-all 0 184))
(setq
  *rs* #.(CCL::INITIALIZE-RANDOM-STATE 477 10894))
"Data loaded and *rs* set.")
(generate-beat-MNN-spacing->
  initial-states stm no-ontimes> dataset-template)
--> (((1 NIL)
      (NIL NIL "C-59-1" ((0 76 69 1/2 0 1/2 0))))
      ((3/2 NIL)
      (2 1 "C-56-1" ((289/2 72 67 1/2 0 145 495))))
      ((7/4 (26 12))
      (0 0 "C-30-2"
      ((39 38 47 1 1 40 134)
      (159/4 64 62 1/4 0 40 136)
      (159/4 76 69 1/4 0 40 137)))))
      ((2 (7 5 12))
      (12 7 "C-30-2"
      ((40 50 54 1 1 41 138) (40 57 58 1 1 41 139)
      (40 62 61 2 0 42 140)
      (40 74 68 2 0 42 141)))))
      ((5/2 (7 9 8))
      (0 0 "C-63-1"
      ((46 54 56 1 1 47 209) (46 61 60 1 1 47 210)
      (93/2 70 65 1/2 0 47 213)
      (46 78 70 5/2 0 97/2 212)))))
      ((3 (7 5 7))
      (0 0 "C-63-2"
      ((92 43 50 1 1 93 302) (92 50 54 1 1 93 303)
      (92 55 57 1 0 93 304)
      (92 62 61 1 0 93 305)))))
      ((1 (5 2))
      (13 8 "C-63-2"
      ((72 56 58 1/2 1 145/2 232)
      (72 61 61 2 0 74 233)
      (72 63 62 2 0 74 234)))))
      ((3/2 (6 2))
      (-1 -1 "C-50-3"

```

```

((277/2 67 63 1/2 1 139 448)
 (138 73 67 1 0 139 447)
 (137 75 68 2 0 139 446))))
((2 NIL)
 (-16 -9 "C-50-3"
 ((415 51 54 1/2 1 831/2 1350))))
((3 (9))
 (7 4 "C-17-1"
 ((131 46 52 1 1 132 647)
 (131 55 57 1 1 132 648))))))
((0 52 55 1/2 0) (1/2 54 56 1/2 0)
 (3/4 80 71 1/4 0) (3/4 92 78 1/4 0)
 (1 66 63 3 1) (1 73 67 3 1) (1 78 70 1/2 0)
 (1 90 77 1 0) (3/2 82 72 1/2 0) (2 78 70 2 0)
 (2 85 74 2 0) (4 79 71 1/2 1) (4 84 74 1 0)
 (4 86 75 1 0) (9/2 78 70 1/2 1) (5 62 61 1 1)
 (6 69 65 1 1) (6 78 70 1 1))
376 (0 0 0 0 0 0 3 0 0 0))

```

Given initial states, a state-transition matrix, an upper limit for ontime, and a template dataset, this function generates datapoints (among other output) that conform to various criteria, which can be specified using the optional arguments. The criteria are things like: not too many consecutive states from the same source (c-sources), the range is comparable with that of the template (c-bar, c-min, and c-max), and the likelihood of the states is comparable with that of the template (c-beats and c-prob). A record, named index-failures, is kept of how many times a generated state fails to meet the criteria. When a threshold c-failures is exceeded at any state index, the penultimate state is removed and generation continues. If the value of c-failures is exceeded for the first state, a message is returned.

This function returns the states as well as the datapoints, and also index-failures and *i*, the total number of iterations.

**generate-beat-spacing-forcing->**

Started, last checked	28/9/2010, 28/9/2010
Location	Generating beat MNN spacing forwards
Calls	beat-spacing-states, checklistp, choose-one, choose-one-with-beat, geom-mean-likelihood-of-states, index-1st-sublist-item>=, my-last, segments-strict, sort-dataset-asc, states2datapoints-by-lookup, translate-datapoints-to-first-ontime
Called by	
Comments/see also	Consider subdividing into several functions. See also generate-beat-MNN-spacing->, generate-beat-spacing-forcing<-.

Example:

```
(progn
  (setq
    initial-states
    (read-from-file
      (concatenate
        'string
        *MCStylistic-Oct2010-example-files-path*
        "/Racchman-Oct2010 example"
        "/initial-states.txt"))))
  (setq
    stm
    (read-from-file
      (concatenate
        'string
        *MCStylistic-Oct2010-example-files-path*
        "/Racchman-Oct2010 example"
        "/transition-matrix.txt"))))
  (setq no-ontimes> 14)
  (setq
    dataset-all
    (read-from-file
      (concatenate
        'string
```



```

      *MCStylistic-Oct2010-data-path*
      "/Dataset/C-41-2-ed.txt"))))
(setq
 dataset-template
 (subseq dataset-all 0 184))
(setq
 *rs* #.(CCL::INITIALIZE-RANDOM-STATE 477 10894))
(setq
 datapoints-from-previous-interval
 '((17/2 63 62 1/2 0) (17/2 72 67 1/2 0)
  (9 34 45 1 1) (9 46 52 1 1) (9 65 63 1/2 0)
  (9 74 68 1/2 0) (39/4 65 63 1/4 0)))
(setq
 previous-state-context-pair
 (my-last
  (beat-spacing-states
   datapoints-from-previous-interval
   "No information" 3 1 3)))
(setq generation-interval '(13 15))
(setq
 pattern-region
 '((27/2 66 63) (27/2 69 65) (14 55 57) (14 62 61)
  (14 67 64) (14 71 66) (29/2 69 65) (29/2 72 67)))
"Data loaded and variables set.")
(generate-beat-spacing-forcing->
 initial-states stm no-ontimes> dataset-template
 generation-interval pattern-region
 previous-state-context-pair (list "originalp")
 3 10 4 19 12 12 12 .15)
--> (((((7/4 (12 19))
  (0 0 "No information"
   ((9 34 45 1 1 10 2) (9 46 52 1 1 10 3)
    (39/4 65 63 1/4 0 10 6)))))
 ((2 (7 5 4 3 5))
  (12 7 "C-17-1"
   ((202 46 52 1 1 203 908)
    (202 53 56 1 1 203 909)
    (202 58 59 1 1 203 910)
    (202 62 61 1 0 203 911)
    (202 65 63 1 0 203 912)
    (202 70 66 1 0 203 913)))))

```

```

((3 (7 5 4 3 9))
 (0 0 "C-17-1"
  ((203 46 52 1 1 204 914)
   (203 53 56 1 1 204 915)
   (203 58 59 1 1 204 916)
   (203 62 61 1 0 204 917)
   (203 65 63 1 0 204 918)
   (203 74 68 1 0 204 919))))
((15/4 (7 5 4 3 9))
 (0 0 "C-41-2"
  ((137 47 52 1 1 138 539)
   (137 54 56 1 1 138 540)
   (137 59 59 1 1 138 541)
   (137 63 61 1 0 138 542)
   (137 66 63 1 0 138 543)
   (551/4 75 68 1/4 0 138 544))))
((1 NIL)
 (28 16 "C-41-2" ((66 75 68 2 0 68 261))))
((3/2 NIL)
 (1 1 "C-30-1" ((61/2 75 69 1/2 0 31 110))))
((2 NIL)
 (-5 -3 "C-56-1"
  ((409 68 65 1/2 0 819/2 1334))))
((3 NIL)
 (0 0 "C-56-3" ((143 62 61 1 0 144 423))))
((9 34 45 1 1) (9 46 52 2 1) (39/4 65 63 1/4 0)
 (10 53 56 1 1) (10 58 59 1 1) (10 62 61 1 0)
 (10 65 63 1 0) (10 70 66 1 0) (11 46 52 1 1)
 (11 53 56 1 1) (11 58 59 1 1) (11 62 61 1 0)
 (11 65 63 1 0) (11 74 68 1 0) (12 74 68 1/2 0)
 (25/2 75 69 1/2 0) (13 70 66 1 0)
 (14 70 66 1 0))
20 (0 0 0 1 0 0 0 0))

```

This function appears to be very similar to the function `generate-beat-MNN-spacing->`. The difference is that there are some extra arguments here, which allow for using either external or internal initial/final states, and for using information from a discovered pattern or previous/next state to further guide the generation, hence ‘forcing’.

**geom-mean-likelihood-of-states**

Started, last checked	28/9/2010, 28/9/2010
Location	Generating beat MNN spacing forwards
Calls	geom-mean-likelihood-of-subset, max-item, min-item, nth-list-of-lists, orthogonal-projection-not-unique-equalp
Called by	generate-beat-MNN-spacing->, generate-beat-spacing-forcing->
Comments/see also	

Example:

```
(progn
  (setq
    ontime-state-points-pairs
    '((0 ((0 38 47 1/2 1 1/2 0) (0 62 61 1/2 0 1/2 1)))
      (1/2 NIL)
      (1
        ((1 50 54 2 1 3 2) (1 57 58 1/2 1 3/2 3)
          (1 60 60 3 0 4 4) (1 66 63 1/2 0 3/2 5)))
      (3/2
        ((1 50 54 2 1 3 2) (3/2 55 57 1/2 1 2 6)
          (1 60 60 3 0 4 4) (3/2 64 62 1/2 0 2 7)))
      (2
        ((1 50 54 2 1 3 2) (2 54 56 1/2 1 5/2 8)
          (1 60 60 3 0 4 4) (2 62 61 1/2 0 5/2 9)))
      (5/2
        ((1 50 54 2 1 3 2) (5/2 57 58 1/2 1 3 10)
          (1 60 60 3 0 4 4) (5/2 66 63 1/2 0 3 11)))
      (3
        ((3 50 54 15/4 1 27/4 12) (1 60 60 3 0 4 4)
          (3 69 65 1/2 0 7/2 13)))
      (7/2
        ((3 50 54 15/4 1 27/4 12) (1 60 60 3 0 4 4)))
      (15/4
        ((3 50 54 15/4 1 27/4 12) (1 60 60 3 0 4 4)
          (15/4 71 66 1/4 0 4 14)))
      (4
        ((3 50 54 15/4 1 27/4 12) (4 60 60 2 0 6 15)
          (4 62 61 2 1 6 16) (4 66 63 2 0 6 17))
```

```

      (4 72 67 2 0 6 18)))
(6
  ((6 43 50 2 1 8 19) (3 50 54 15/4 1 27/4 12)
   (6 62 61 1/2 0 13/2 20) (6 67 64 1/2 0 13/2 21)
   (6 71 66 1/2 0 13/2 22)))
(13/2
  ((6 43 50 2 1 8 19) (3 50 54 15/4 1 27/4 12)))
(27/4
  ((6 43 50 2 1 8 19) (27/4 50 54 1/4 1 7 23)
   (27/4 60 60 1/4 0 7 24)
   (27/4 69 65 1/4 0 7 25)))
(7
  ((6 43 50 2 1 8 19) (7 55 57 2 1 9 26)
   (7 59 59 1 0 8 27) (7 67 64 1 0 8 28)))
(8
  ((8 43 50 2 1 10 29) (7 55 57 2 1 9 26)
   (8 59 59 1 0 9 30) (8 62 61 1 0 9 31)
   (8 71 66 1 0 9 32)))
(9
  ((8 43 50 2 1 10 29) (9 49 53 1 1 10 33)
   (9 58 58 1 1 10 34) (9 64 62 1 0 10 35)
   (9 67 64 1 0 10 36) (9 76 69 1 0 10 37)))
(10 NIL)))
(setq
 dataset
 '( ( (0 38 47 1/2 1) (0 62 61 1/2 0) (1 50 54 2 1)
      (1 57 58 1/2 1) (1 60 60 3 0) (1 66 63 1/2 0)
      (3/2 55 57 1/2 1) (3/2 64 62 1/2 0)
      (2 54 56 1/2 1) (2 62 61 1/2 0) (5/2 57 58 1/2 1)
      (5/2 66 63 1/2 0) (3 50 54 15/4 1)
      (3 69 65 1/2 0) (15/4 71 66 1/4 0) (4 60 60 2 0)
      (4 62 61 2 1) (4 66 63 2 0) (4 72 67 2 0)
      (6 43 50 2 1) (6 62 61 1/2 0) (6 67 64 1/2 0)
      (6 71 66 1/2 0) (27/4 50 54 1/4 1)
      (27/4 60 60 1/4 0) (27/4 69 65 1/4 0)
      (7 55 57 2 1) (7 59 59 1 0) (7 67 64 1 0)
      (8 43 50 2 1) (8 59 59 1 0) (8 62 61 1 0)
      (8 71 66 1 0) (9 49 53 1 1) (9 58 58 1 1)
      (9 64 62 1 0) (9 67 64 1 0) (9 76 69 1 0)))
 (setq c-beats 4)
 "Variables set.")

```

```
(geom-mean-likelihood-of-states
 ontime-state-points-pairs dataset c-beats)
--> ((0 0.5) (1 0.16666667) (3/2 0.125) (2 0.11892071)
      (5/2 0.11785113) (3 0.089994356)
      (7/2 0.101015255) (15/4 0.08399473)
      (4 0.10777223) (6 0.075700045) (13/2 0.061487548)
      (27/4 0.09343293) (7 0.05662891) (8 0.09750821)
      (9 0.058608957))
```

This function applies the function `geom-mean-likelihood-of-subset` recursively, having extracted a subset from each ontime-state-points pair.

### geom-mean-likelihood-of-subset

Started, last checked	28/9/2010, 28/9/2010
Location	Generating beat MNN spacing forwards
Calls	empirical-mass, index-1st-sublist-item>=, index-1st-sublist-item>, likelihood-of-subset
Called by	comparable-likelihood-profilep, geom-mean-likelihood-of-states
Comments/see also	

Example:

```
(progn
 (setq
  subset
  '((8 43 50 2 1 10 29) (7 55 57 2 1 9 26)
    (8 59 59 1 0 9 30) (8 62 61 1 0 9 31)
    (8 71 66 1 0 9 32)))
 (setq
  subset-palette
  (orthogonal-projection-not-unique-equalp
   subset '(0 1)))
 (setq first-subset-ontime 7)
 (setq last-subset-ontime 8)
 (setq
  dataset
  '((0 38 47 1/2 1) (0 62 61 1/2 0) (1 50 54 2 1)
    (1 57 58 1/2 1) (1 60 60 3 0) (1 66 63 1/2 0)
    (3/2 55 57 1/2 1) (3/2 64 62 1/2 0))
```

```

(2 54 56 1/2 1) (2 62 61 1/2 0) (5/2 57 58 1/2 1)
(5/2 66 63 1/2 0) (3 50 54 15/4 1)
(3 69 65 1/2 0) (15/4 71 66 1/4 0) (4 60 60 2 0)
(4 62 61 2 1) (4 66 63 2 0) (4 72 67 2 0)
(6 43 50 2 1) (6 62 61 1/2 0) (6 67 64 1/2 0)
(6 71 66 1/2 0) (27/4 50 54 1/4 1)
(27/4 60 60 1/4 0) (27/4 69 65 1/4 0)
(7 55 57 2 1) (7 59 59 1 0) (7 67 64 1 0)
(8 43 50 2 1) (8 59 59 1 0) (8 62 61 1 0)
(8 71 66 1 0) (9 49 53 1 1) (9 58 58 1 1)
(9 64 62 1 0) (9 67 64 1 0) (9 76 69 1 0)))
(setq
  dataset-palette
  (orthogonal-projection-not-unique-equalp
   dataset '(0 1)))
(setq
  ontimes-list (nth-list-of-lists 0 dataset))
(setq c-beats 4)
"Variables set.")
(geom-mean-likelihood-of-subset
 subset subset-palette first-subset-ontime
 last-subset-ontime dataset-palette
 ontimes-list c-beats)
--> 0.09750821

```

The first argument to this function, called `subset`, is a point set. Both in the scenario of likelihood calculation for an original excerpt and for a generated passage, the point set is a segment of the music. The argument `subset-palette` consists of a (listed) list of MIDI note numbers from the subset. Note: `first-subset-ontime` is not necessarily the ontime of the first datapoint, as they will have been sorted by MIDI note number. The variables `dataset` and `dataset-palette` are analogous, `ontimes-list` is a list of ontimes from the dataset. The threshold `c-beats` determines how far back we look to form the empirical distribution. The output of this function is the geometric mean of the likelihood of the subset (that is, a product of the individual empirical probabilities of the constituent MIDI note numbers).

**mean&range**

Started, last checked	28/9/2010, 28/9/2010
Location	Generating beat MNN spacing forwards
Calls	full-segment-nearest;ontime, max-item, min-item, nth-list-of-lists
Called by	checklistp
Comments/see also	

Example:

```
(setq
 mini-template-segments
 '( (0
    ((0 52 55 1 1 1 0) (0 62 61 1 0 1 1)
     (0 64 62 1 0 1 2) (0 68 64 1 0 1 3)
     (0 71 66 1 0 1 4)))
    (1
     ((1 52 55 1 1 2 5) (1 62 61 1 0 2 6)
      (1 64 62 1 0 2 7) (1 68 64 1 0 2 8)
      (1 71 66 1 0 2 9)))
    (2
     ((2 52 55 1 1 3 10) (2 62 61 1 0 3 11)
      (2 64 62 1 0 3 12) (2 68 64 1 0 3 13)
      (2 72 67 3/4 0 11/4 14)))
    (11/4
     ((2 52 55 1 1 3 10) (2 62 61 1 0 3 11)
      (2 64 62 1 0 3 12) (2 68 64 1 0 3 13)
      (11/4 71 66 1/4 0 3 15)))
    (3
     ((3 45 51 3 1 6 16) (3 52 55 3 1 6 17)
      (3 60 60 3 0 6 18) (3 64 62 3 0 6 19)
      (3 71 66 1 0 4 20))))))
(setq
 datapoints-segment
 '(3/2 ((1 64 62 1 0 2 7) (1 68 64 1 0 2 8))))
(mean&range
 datapoints-segment mini-template-segments 4 3 3)
--> NIL
```

This function takes five arguments: a pair consisting of an ontime and a list of datapoints, a list of pairs as above, and three thresholds. It uses

the ontime in the first argument to determine which list is relevant in the second argument. Then the two sets of MIDI note numbers are compared, in terms of their mean, min, and max values. If, for each of these summary statistics, the absolute difference between each set of MNNs is smaller than the threshold, then T is returned, and NIL otherwise.

### **pitch&octave-spellingp**

Started, last checked	28/9/2010, 28/9/2010
Location	Generating beat MNN spacing forwards
Calls	MIDI-morphetic-pair2pitch&octave
Called by	checklistp
Comments/see also	

Example:

```
(pitch&octave-spellingp
'((12 50 54 1 1 13 42) (12 62 61 1 0 13 43)
(12 65 63 1 0 13 44) (12 69 65 1 0 13 45)))
--> T
```

This function converts each MIDI-morphetic pair (assumed to be second and third entries of each list) to pitch and octave number. If the spelling requires more than two flats or sharps, then NIL will be returned, and T otherwise.

### **translate-datapoints-to-first-ontime**

Started, last checked	28/9/2010, 28/9/2010
Location	Generating beat MNN spacing forwards
Calls	constant-vector, translation
Called by	generate-beat-MNN-spacing->, generate-beat-spacing-forcing->
Comments/see also	translate-datapoints-to-last-ontime

Example:

```
(translate-datapoints-to-first-ontime
4 0
'((28 44 51 1 1) (28 48 53 1 1) (28 56 58 1 0)
(30 44 51 1 1) (31 48 53 1 1) (34 56 58 1 0)))
--> ((4 44 51 1 1) (4 48 53 1 1) (4 56 58 1 0)
(6 44 51 1 1) (7 48 53 1 1) (10 56 58 1 0))
```



This function takes three arguments: an ontime, an ontime index and a list of datapoints (assumed to be sorted in lexicographical order). It translates these datapoints such that the ontime of the first datapoint equals the first argument.

### 4.5.7 Generating beat MNN spacing backwards

The main function here is called `generate-beat-MNN-spacing<-`. Given final states, a state-transition matrix, a lower limit for the ontime of the first state, and a template dataset, it generates datapoints (among other output) that conform to various criteria, which can be specified using the optional arguments. The criteria are things like: not too many consecutive states from the same source, the range is comparable with that of the template, and the likelihood of the states is comparable with that of the template.

#### `checklist<-p`

Started, last checked	12/10/2010, 12/10/2010
Location	Generating beat MNN spacing backwards
Calls	<code>comparable-likelihood-profile&lt;-p</code> , <code>index-item-1st-doesnt-occur</code> , <code>lastn</code> , <code>mean&amp;range</code> <code>p</code> , <code>pitch&amp;octave-spelling</code> <code>p</code> , <code>segments-strict</code>
Called by	<code>generate-beat-MNN-spacing&lt;-</code> , <code>generate-beat-spacing-forcing&lt;-</code>
Comments/see also	<code>checklistp</code>

Example:

```
(setq
 states<-
 '(((2 (7 5 4))
 (NIL NIL "C-24-2"
 ((358 48 53 2 1 360 6) (358 55 57 2 1 360 7)
 (358 60 60 2 0 360 8) (358 64 62 2 0 360 9))))
 ((3/2 (19 7))
 (12 7 "C-30-2"
 ((153 45 51 1 1 154 599) (153 64 62 1 0 154 600)
 (307/2 71 66 1/2 0 154 602))))))
(setq
 datapoints
```

```

'((67/2 32 44 1/2 1) (67/2 51 55 5/2 0)
  (67/2 58 59 1/2 0) (34 44 51 2 1) (34 56 58 2 0)
  (34 60 60 2 0)))
(setq
  template-segments
  '((27
    ((27 39 48 1 1 28 91) (27 63 62 1/2 0 55/2 92)))
    (55/2 ((27 39 48 1 1 28 91)))
    (111/4
      ((27 39 48 1 1 28 91) (111/4 72 67 1/4 0 28 93)))
    (28
      ((28 51 55 1 1 29 94) (28 60 60 1 1 29 95)
        (28 68 65 1 1 29 96) (28 84 74 1 0 29 97)))
    (29 ((29 82 73 1/3 0 88/3 98)))
    (88/3 ((88/3 80 72 1/3 0 89/3 99)))
    (89/3 ((89/3 77 70 1/3 0 30 100)))
    (30
      ((30 39 48 1 1 31 101) (30 79 71 1/2 0 61/2 102)))
    (61/2
      ((30 39 48 1 1 31 101) (61/2 77 70 1/2 0 31 103)))
    (31
      ((31 51 55 1 1 32 104) (31 55 57 1 1 32 105)
        (31 61 61 1 1 32 106) (31 75 69 1/2 0 63/2 107)))
    (63/2
      ((31 51 55 1 1 32 104) (31 55 57 1 1 32 105)
        (31 61 61 1 1 32 106) (63/2 73 68 1/2 0 32 108)))
    (32
      ((32 51 55 1 1 33 109) (32 55 57 1 1 33 110)
        (32 61 61 1 1 33 111) (32 70 66 1/2 0 65/2 112)))
    (65/2
      ((32 51 55 1 1 33 109) (32 55 57 1 1 33 110)
        (32 61 61 1 1 33 111) (65/2 65 63 1/2 0 33 113)))
    (33
      ((33 44 51 2 1 35 114) (33 63 62 1/2 0 67/2 115)))
    (67/2 ((33 44 51 2 1 35 114)))
    (135/4
      ((33 44 51 2 1 35 114)
        (135/4 72 67 1/4 0 34 116)))
    (34
      ((33 44 51 2 1 35 114) (34 51 55 1 1 35 117)
        (34 60 60 1 1 35 118) (34 68 65 1 0 35 119))))))

```

```

(setq
  template-likelihood-profile
  '((27 0.11785113) (55/2 1/6) (111/4 0.10878566)
    (28 0.08494337) (29 1/15) (88/3 1/14) (89/3 1/7)
    (30 0.06666667) (61/2 0.06666667) (31 0.11632561)
    (63/2 0.11632561) (32 0.108109735)
    (65/2 0.108109735) (33 0.16666667) (67/2 1/6)
    (135/4 0.16666667) (34 0.16666667)))
(setq
  checklist '("originalp" "range&meanp" "likelihoodp"))
(setq c-sources 3)
(setq c-bar 12)
(setq c-min 7)
(setq c-max 7)
(setq c-beats 3)
(setq c-prob 0.1)
(checklist<-p
  states<- datapoints template-segments
  template-likelihood-profile checklist c-sources c-bar
  c-min c-max c-beats c-prob)
--> T

```

Checks are made of sources, of the range and mean of the notes supplied in the last element of the backwards-generated states, and their likelihoods.

### comparable-likelihood-profile<-p

Started, last checked	12/10/2010, 12/10/2010
Location	Generating beat MNN spacing backwards
Calls	geom-mean-likelihood-of-subset<-, linearly-interpolate, max-item, min-item, nth-list-of-lists, orthogonal-projection-not-unique-equalp
Called by	checklist<-p
Comments/see also	comparable-likelihood-profilep

Example:

```

(setq
  ontime-state-points-pair
  '(111/4

```

```

      ((27 39 48 1 1) (111/4 72 67 1/4 0))))
(setq
 datapoints
 '((27 39 48 1 1) (27 63 62 1/2 0) (111/4 72 67 1/4 0)
   (28 51 55 1 1) (28 60 60 1 1) (28 68 65 1 1)
   (28 84 74 1 0) (29 82 73 1/3 0) (88/3 80 72 1/3 0)
   (89/3 77 70 1/3 0) (30 39 48 1 1) (30 79 71 1/2 0)
   (61/2 77 70 1/2 0) (31 51 55 1 1) (31 55 57 1 1)
   (31 61 61 1 1) (31 75 69 1/2 0) (63/2 73 68 1/2 0)
   (32 51 55 1 1) (32 55 57 1 1) (32 61 61 1 1)
   (32 70 66 1/2 0) (65/2 65 63 1/2 0) (33 44 51 2 1)
   (33 63 62 1/2 0) (135/4 72 67 1/4 0) (34 51 55 1 1)
   (34 60 60 1 1) (34 68 65 1 0)))
(setq c-beats 3)
(setq
 template-likelihood-profile
 '((27 0.07142857) (55/2 1/14) (111/4 0.062499996)
   (28 0.10958345) (29 0.09672784) (30 0.11785113)
   (91/3 0.083333336) (92/3 0.11785113) (31 0.1514267)
   (32 0.13999122) (33 0.16666667) (67/2 1/6)
   (135/4 0.16666667) (34 0.3333333)))
(setq c-prob 0.1)
(comparable-likelihood-profile<-p
 ontime-state-points-pair datapoints c-beats
 template-likelihood-profile c-prob)
--> T

```

This function is similar to the function `comparable-likelihood-profilep`, the difference being it calls the function `geom-mean-likelihood-of-subsetj-` (forwards looking for the empirical distribution) rather than `geom-mean-likelihood-of-subset`. It takes a pair consisting of an ontime and points that sound at the ontime. Based on an empirical distribution over the argument named `datapoints` (with a context governed by `c-beats`), it calculates the geometric mean of the likelihood of these points. This likelihood is then compared with that at the same ontime in the template. If the absolute difference between the likelihoods is less than the threshold `c-prob`, `T` is returned, and `NIL` otherwise. `T` will also be returned if there are no points.

**generate-beat-MNN-spacing<-**

Started, last checked	12/10/2010, 12/10/2010
Location	Generating beat MNN spacing backwards
Calls	checklist<-p, choose-one, choose-one-with-beat, geom-mean-likelihood-of-states<-, index-1st-sublist-item>=, my-last, segments-strict, sort-dataset-asc, states2datapoints-by-lookup<-, translate-datapoints-to-last-ontime
Called by	
Comments/see also	Consider subdividing into several functions. See also generate-beat-MNN-spacing->, generate-beat-spacing-forcing<-.

Example:

```
(progn
  (setq
    final-states
    (read-from-file
      (concatenate
        'string
        *MCStylistic-Oct2010-example-files-path*
        "/Racchman-Oct2010 example"
        "/final-states.txt"))))
  (setq
    stm<-
    (read-from-file
      (concatenate
        'string
        *MCStylistic-Oct2010-example-files-path*
        "/Racchman-Oct2010 example"
        "/transition-matrix<-.txt"))))
  (setq no-ontimes< 111/4)
  (setq
    dataset-all
    (read-from-file
      (concatenate
        'string
```

```

*MCStylistic-Oct2010-data-path*
"/Dataset/C-24-3-ed.txt"))))
(setq
  dataset-template
  (subseq dataset-all 0 120))
(setq
  *rs* #.(CCL::INITIALIZE-RANDOM-STATE 477 10894))
"Data loaded and *rs* set.")
(generate-beat-MNN-spacing<-
  final-states stm<- no-ontimes< dataset-template)
--> (((3 NIL)
      (NIL NIL "C-68-4" ((184 65 63 2 0 186 9))))
      ((2 (7 5 5))
       (16 9 "C-17-2"
        ((10 55 57 1 1 11 34) (10 62 61 1 1 11 35)
         (9 67 64 2 0 11 32) (9 72 67 2 0 11 33)))))
      ((1 (24 5))
       (12 7 "C-17-2"
        ((165 43 50 1 1 166 608)
         (165 67 64 2 0 167 609)
         (165 72 67 2 0 167 610)))))
      ((3 (7 3 6 6))
       (-7 -4 "C-33-2"
        ((212 52 55 1 1 213 956)
         (212 59 59 1 1 213 957)
         (212 62 61 1 0 213 958)
         (211 68 64 2 0 213 955)
         (212 74 68 1 0 213 959)))))
      ((2 (7 3 6 6))
       (0 0 "C-33-2"
        ((235 52 55 1 1 236 1057)
         (235 59 59 1 1 236 1058)
         (235 62 61 1 0 236 1059)
         (235 68 64 2 0 237 1060)
         (704/3 74 68 4/3 0 236 1056)))))
      ((1 (12 12))
       (24 14 "C-17-1"
        ((204 36 46 1 1 205 920)
         (204 48 53 1 1 205 921)
         (204 60 60 1 0 205 922)))))
      ((3 (5 4 3 5 4))

```

```

(-19 -11 "C-50-3"
 ((101 52 55 1 1 102 289)
  (101 57 58 1 1 102 290)
  (101 61 60 1 0 102 291)
  (101 64 62 1 1 102 292)
  (101 69 65 1 0 102 293)
  (101 73 67 1 0 102 294))))))
((26 18 36 2 1) (26 23 39 2 1) (26 27 41 2 0)
 (26 30 43 2 1) (26 35 46 2 0) (26 39 48 2 0)
 (28 -1 25 1 1) (28 11 32 1 1) (28 23 39 1 0)
 (29 23 39 1 1) (29 30 43 1 1) (29 33 45 1 0)
 (29 39 48 3 0) (29 45 52 3 0) (30 23 39 2 1)
 (30 30 43 2 1) (30 33 45 2 0) (32 16 35 1 1)
 (32 40 49 2 0) (32 45 52 2 0) (33 28 42 1 1)
 (33 35 46 1 1) (34 44 51 2 0))
8 (0 0 0 1 0 0 0))

```

This function is similar to the function `generate-beat-MNN-spacing-i`, the difference is that the former generates a passage backwards one state at a time. The checking process is analogous. Given final states, a state-transition matrix, a lower limit for ontime, and a template dataset, this function generates datapoints (among other output) that conform to various criteria, which can be specified using the optional arguments. The criteria are things like: not too many consecutive states from the same source (`c-sources`), the range is comparable with that of the template (`c-bar`, `c-min`, and `c-max`), and the likelihood of the states is comparable with that of the template (`c-beats` and `c-prob`). A record, named `index-failures`, is kept of how many times a generated state fails to meet the criteria. When a threshold `c-failures` is exceeded at any state index, the penultimate state is removed and generation continues. If the value of `c-failures` is exceeded for the first state, a message is returned.

This function returns the states as well as the datapoints, and also `index-failures` and `i`, the total number of iterations.

**generate-beat-spacing-forcing<-**

Started, last checked	12/10/2010, 12/10/2010
Location	Generating beat MNN spacing backwards
Calls	beat-spacing-states, checklist<-p, choose-one, choose-one-with-beat, geom-mean-likelihood-of-states<-, index-1st-sublist-item>=, my-last, nth-list-of-lists, segments-strict, sort-dataset-asc, states2datapoints-by-lookup<-, translate-datapoints-to-last-ontime
Called by	
Comments/see also	Consider subdividing into several functions. See also generate-beat-MNN-spacing<-, generate-beat-spacing-forcing->.

Example:

```
(progn
  (setq
    final-states
    (read-from-file
      (concatenate
        'string
        *MCStylistic-Oct2010-example-files-path*
        "/Racchman-Oct2010 example"
        "/internal-final-states.txt"))))
  (setq
    stm<-
    (read-from-file
      (concatenate
        'string
        *MCStylistic-Oct2010-example-files-path*
        "/Racchman-Oct2010 example"
        "/transition-matrix<-.txt"))))
  (setq no-ontimes< 2)
  (setq
    dataset-all
    (read-from-file
      "/Users/tec69/Open/Music/Datasets/C-24-3-ed.txt")))
```



```

(setq
  dataset-template
  (subseq dataset-all 0 120))
(setq
  *rs* #.(CCL::INITIALIZE-RANDOM-STATE 48164 60796))
(setq
  datapoints-from-next-interval
  '((5/2 63 62 1/2 0) (5/2 72 67 1/2 0)
    (3 34 45 1 1) (3 46 52 1 1) (3 65 63 1/2 0)
    (3 74 68 1/2 0) (15/4 65 63 1/4 0)))
(setq
  next-state-context-pair
  (first
   (beat-spacing-states
    datapoints-from-next-interval "No information"
    3 1 3)))
(setq generation-interval '(1 3))
(setq
  pattern-region
  '((1 51 55) (1 55 57) (1 61 61) (1 63 62) (2 51 55)
    (2 55 57) (2 61 61) (5/2 73 68)))
"Data loaded and variables set.")
(generate-beat-spacing-forcing<-
 final-states stm<- no-ontimes< dataset-template
 generation-interval pattern-region
 next-state-context-pair (list "originalp")
 3 10 4 19 12 12 12 .15)
--> (((((7/2 (9))
  (NIL NIL "No information"
    ((5/2 63 62 1/2 0 3 0)
     (5/2 72 67 1/2 0 3 1))))))
  ((3 (9))
   (-2 -1 "C-6-3"
    ((101 71 66 1/2 0 203/2 424)
     (101 80 71 1/2 0 203/2 425))))))
  ((2 65 63 1/2 0) (2 74 68 1/2 0)
   (5/2 63 62 1/2 0) (5/2 72 67 1/2 0))
  2 (0 0))

```

This function appears to be very similar to the function `generate-beat-MNN-spacing<-`. The difference is that there are some extra arguments here, which

allow for using either external or internal initial/final states, and for using information from a discovered pattern or previous/next state to further guide the generation, hence ‘forcing’.

### **geom-mean-likelihood-of-states<-**

Started, last checked	12/10/2010, 12/10/2010
Location	Generating beat MNN spacing backwards
Calls	geom-mean-likelihood-of-subset<-, max-item, min-item, nth-list-of-lists, orthogonal-projection-not-unique-equalp
Called by	generate-beat-MNN-spacing<-, generate-beat-spacing-forcing<-
Comments/see also	

Example:

```
(setq
 ontime-state-points-pairs
 '( (27
    ((27 42 49 1 1 28 0) (27 70 65 1/2 0 55/2 1)))
    (55/2 ((27 42 49 1 1 28 0)))
    (111/4
    ((27 42 49 1 1 28 0) (111/4 67 64 1/4 0 28 2)
    (111/4 79 71 1/4 0 28 3)))
    (28
    ((28 54 56 1 1 29 4) (28 58 58 1 1 29 5)
    (28 64 62 1 1 29 6) (28 66 63 2 0 30 7)
    (28 78 70 2 0 30 8)))
    (29
    ((29 54 56 1 1 30 9) (29 58 58 1 1 30 10)
    (29 64 62 1 1 30 11) (28 66 63 2 0 30 7)
    (28 78 70 2 0 30 8)))
    (30
    ((30 47 52 1 1 31 12) (30 74 68 1/3 0 91/3 13)))
    (91/3
    ((30 47 52 1 1 31 12) (91/3 76 69 1/3 0 92/3 14)))
    (92/3
    ((30 47 52 1 1 31 12) (92/3 74 68 1/3 0 31 15)))
    (31
    ((31 54 56 1 1 32 16) (31 62 61 1 1 32 17))
```

```

      (31 73 67 1 0 32 18)))
(32
  ((32 54 56 1 1 33 19) (32 62 61 1 1 33 20)
   (32 71 66 1 0 33 21)))
(33
  ((33 42 49 1 1 34 22) (33 69 65 1/2 0 67/2 23)))
(67/2 ((33 42 49 1 1 34 22)))
(135/4
  ((33 42 49 1 1 34 22) (135/4 67 64 1/4 0 34 24)))
(34
  ((34 54 56 1 1 35 25) (34 57 58 1 1 35 26)
   (34 61 60 1 1 35 27))) (35 NIL)))
(setq
 dataset
 '( (27 42 49 1 1) (27 70 65 1/2 0) (111/4 67 64 1/4 0)
   (111/4 79 71 1/4 0) (28 54 56 1 1) (28 58 58 1 1)
   (28 64 62 1 1) (28 66 63 2 0) (28 78 70 2 0)
   (29 54 56 1 1) (29 58 58 1 1) (29 64 62 1 1)
   (30 47 52 1 1) (30 74 68 1/3 0) (91/3 76 69 1/3 0)
   (92/3 74 68 1/3 0) (31 54 56 1 1) (31 62 61 1 1)
   (31 73 67 1 0) (32 54 56 1 1) (32 62 61 1 1)
   (32 71 66 1 0) (33 42 49 1 1) (33 69 65 1/2 0)
   (135/4 67 64 1/4 0) (34 54 56 1 1) (34 57 58 1 1)
   (34 61 60 1 1)))
(geom-mean-likelihood-of-states<-
 ontime-state-points-pairs dataset 3)
--> ((27 0.07142857) (55/2 1/14) (111/4 0.062499996)
      (28 0.10958345) (29 0.09672784) (30 0.11785113)
      (91/3 0.083333336) (92/3 0.11785113)
      (31 0.1514267) (32 0.13999122) (33 0.16666667)
      (67/2 1/6) (135/4 0.16666667) (34 0.3333333))

```

Applies the function `geom-mean-likelihood-of-subset<-` recursively to the first argument.

**geom-mean-likelihood-of-subset<-**

Started, last checked	12/10/2010, 12/10/2010
Location	Generating beat MNN spacing backwards
Calls	empirical-mass, index-1st-sublist-item>=, index-1st-sublist-item>, likelihood-of-subset
Called by	comparable-likelihood-profilep, geom-mean-likelihood-of-states
Comments/see also	

Example:

```
(setq
 subset
 '((27 42 49 1 1 28 0) (111/4 67 64 1/4 0 28 2)
 (111/4 79 71 1/4 0 28 3)))
(setq
 subset-palette
 (orthogonal-projection-not-unique-equalp
 subset '(0 1)))
(setq first-subset-ontime 27)
(setq last-subset-ontime 111/4)
(setq
 dataset
 '((27 42 49 1 1) (27 70 65 1/2 0) (111/4 67 64 1/4 0)
 (111/4 79 71 1/4 0) (28 54 56 1 1) (28 58 58 1 1)
 (28 64 62 1 1) (28 66 63 2 0) (28 78 70 2 0)
 (29 54 56 1 1) (29 58 58 1 1) (29 64 62 1 1)
 (30 47 52 1 1) (30 74 68 1/3 0) (91/3 76 69 1/3 0)
 (92/3 74 68 1/3 0) (31 54 56 1 1) (31 62 61 1 1)
 (31 73 67 1 0) (32 54 56 1 1) (32 62 61 1 1)
 (32 71 66 1 0) (33 42 49 1 1) (33 69 65 1/2 0)
 (135/4 67 64 1/4 0) (34 54 56 1 1) (34 57 58 1 1)
 (34 61 60 1 1)))
(setq
 dataset-palette
 (orthogonal-projection-not-unique-equalp
 dataset '(0 1)))
(setq
 ontimes-list (nth-list-of-lists 0 dataset))
(setq c-beats 4)
```

```
(geom-mean-likelihood-of-subset<-
 subset subset-palette first-subset-ontime
 last-subset-ontime dataset-palette ontimes-list
 c-beats)
--> 0.052631576
```

This function is similar to the function `geom-mean-likelihood-of-subset`, the difference being we look forward to form the empirical distribution, rather than backward. The first argument to this function, called `subset`, is a point set. Both in the scenario of likelihood calculation for an original excerpt and for a generated passage, the point set is a segment of the music. The argument `subset-palette` consists of a (listed) list of MIDI note numbers from the subset. Note: `first-subset-ontime` is not necessarily the ontime of the first datapoint, as they will have been sorted by MIDI note number. The variable `dataset-palette` is analogous, `ontimes-list` is a list of ontimes from the dataset. The threshold `c-beats` determines how far forward we look to form the empirical distribution. The output of this function is the geometric mean of the likelihood of the subset (that is, a product of the individual empirical probabilities of the constituent MIDI note numbers).

### **translate-datapoints-to-last-offtime**

Started, last checked	12/10/2010, 12/10/2010
Location	Generating beat MNN spacing backwards
Calls	constant-vector, translation
Called by	
Comments/see also	Deprecated.

Example:

```
(translate-datapoints-to-last-offtime
 30
 '( (0 44 51 1 1) (0 48 53 1 1) (0 56 58 1 0)
    (2 44 51 1 1) (3 48 53 5 1) (6 56 58 1 0)))
--> ((22 44 51 1 1) (22 48 53 1 1) (22 56 58 1 0)
     (24 44 51 1 1) (25 48 53 5 1) (28 56 58 1 0))
```

This function takes two arguments: a time  $t$  and a list of datapoints. It calculates the maximum offtime of the datapoints, and translates the datapoints, such that the maximum offtime is now  $t$ .

**translate-datapoints-to-last-ontime**

Started, last checked	12/10/2010, 12/10/2010
Location	Generating beat MNN spacing backwards
Calls	constant-vector, my-last, translation
Called by	generate-beat-MNN-spacing->, generate-beat-spacing-forcing->
Comments/see also	translate-datapoints-to-first-ontime

Example:

```
(translate-datapoints-to-last-ontime
 34 0
 '( (0 44 51 1 1) (0 48 53 1 1) (0 56 58 1 0)
    (2 44 51 1 1) (3 48 53 1 1) (6 56 58 1 0)))
--> ((28 44 51 1 1) (28 48 53 1 1) (28 56 58 1 0)
     (30 44 51 1 1) (31 48 53 1 1) (34 56 58 1 0)).
```

This function takes three arguments: an ontime, an ontime index and a list of datapoints (assumed to be sorted in lexicographical order). It translates these datapoints such that the ontime of the last datapoint equals the first argument.

**4.5.8 Generating beat MNN spacing for&back**

The main function here is called generate-beat-MNN-spacing<->. Given initial and final states, forwards- and backwards-running state-transition matrices, and a template dataset, it generates datapoints (among other output) that conform to various criteria, which can be specified using the optional arguments. The idea is to join forwards- and backwards-generated phrases, choosing whichever pair leads to a phrase whose mean deviation from the template likelihood profile is minimal.

The criteria are things like: not too many consecutive states from the same source, the range is comparable with that of the template, and the likelihood of the states is comparable with that of the template.

**generate-beat-MNN-spacing<->**

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	generate-forwards-or-backwards-no-failure, my-last, segments-strict, unite-datapoints
Called by	
Comments/see also	Consider simplifying/renaming generating functions.

Example: see Stylistic composition with Racchman-Oct2010 (Sec. 3.2, especially lines 498-502).

This function unites several forwards- and backwards running realisations of Markov models built on the arguments initial-states, stm->, final-states, and stm<-. It is constrained by a template (the argument dataset-template) and various parameters: like not too many consecutive states from the same source (c-sources), the range is comparable with that of the template (c-bar, c-min, and c-max), and the likelihood of the states is comparable with that of the template (c-beats and c-prob).

The numbers of forwards- and backwards- realisations generated are determined by the arguments c-forwards and c-backwards respectively. The output is a list of three hash tables (one containing the forwards candidates, one the backwards candidates, and one the united candidates). If c-forwards =  $m$  and c-backwards =  $n$ , then the number of united candidates is  $3mn$ .

**generate-beat-spacing-forced<->**

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	generate-forced<->no-failure, generate-forwards-or-backwards-no-failure, segments-strict, unite-datapoints
Called by	
Comments/see also	Consider simplifying/renaming generating functions.

Example:

```
(progn
  (setq generation-interval '(12 24))
```

```

(setq terminal->p nil)
(setq terminal<-p nil)
(setq
  external-initial-states
  (read-from-file
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/Racchmaninof-Oct2010 example"
      "/initial-states.txt"))))
(setq
  internal-initial-states
  (read-from-file
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/Racchmaninof-Oct2010 example"
      "/internal-initial-states.txt"))))
(setq
  stm->
  (read-from-file
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/Racchmaninof-Oct2010 example"
      "/transition-matrix.txt"))))
(setq
  external-final-states
  (read-from-file
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/Racchmaninof-Oct2010 example"
      "/final-states.txt"))))
(setq
  internal-final-states
  (read-from-file
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/Racchmaninof-Oct2010 example"

```



```

    "/internal-final-states.txt"))))
(setq
  stm<-
  (read-from-file
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/Racchmaninof-Oct2010 example"
      "/transition-matrix<-.txt"))))
(setq
  dataset-all
  (read-from-file
    "/Users/tec69/Open/Music/Datasets/C-56-1-ed.txt"))
(setq
  dataset-template
  (subseq dataset-all 0 132))
(setq
  pattern-region
  '((12 60 60) (12 64 62) (25/2 57 58) (51/4 64 62)
    (13 52 55) (13 64 62) (14 54 56) (29/2 62 61)
    (15 55 57) (15 59 59) (63/4 64 62) (16 43 50)
    (16 50 54) (16 66 63) (17 67 64) (18 57 58)
    (18 60 60) (18 64 62) (75/4 66 63) (19 43 50)
    (19 50 54) (19 67 64) (20 66 63) (20 69 65)
    (21 59 59) (21 67 64) (21 71 66) (87/4 74 68)
    (22 43 50) (22 50 54) (22 74 68) (23 62 61)
    (24 60 60) (24 64 62)))
(setq state-context-pair-> nil)
(setq state-context-pair<- nil)
(setq
  checklist
  (list "originalp" "mean&range" "likelihoodp"))
(setq
  *rs* #.(CCL::INITIALIZE-RANDOM-STATE 6086 61144))
(setq time-a (get-internal-real-time))
(setq
  output
  (generate-beat-spacing-forced<->
    generation-interval terminal->p terminal<-p
    external-initial-states internal-initial-states
    stm-> external-final-states internal-final-states

```

```

    stm<- dataset-template pattern-region
    state-context-pair-> state-context-pair<-
    checklist 3 10 4 19 12 12 12 0.2 3 3))
  (setq time-b (get-internal-real-time))
  (float
   (/
    (- time-b time-a)
    internal-time-units-per-second)))
--> 15.091431 seconds.
(setq
 output-datapoints
 (gethash
  "united,2,3,backwards-dominant" (third output)))
(saveit
 (concatenate
  'string
  *MCStylistic-Oct2010-example-files-path*
  "/united,2,3,backwards-dominant.mid")
 (modify-to-check-dataset
  (translation
   output-datapoints
   (list
    (- 0 (first (first output-datapoints)))
    0 0 0 0)) 900))

```

This function is similar to the function `generate-beat-MNN-spacing<->`. The difference is that there are some extra arguments here, which allow for using either external or internal initial/final states, and for using information from a discovered pattern or previous/next state to further guide the generation.

The function unites several forwards- and backwards running realisations of Markov models built on the arguments `initial-states`, `stm-i`, `final-states`, and `stm-j`. It is constrained by a template (the argument `dataset-template`) and various parameters: like not too many consecutive states from the same source (`c-sources`), the range is comparable with that of the template (`c-bar`, `c-min`, and `c-max`), and the likelihood of the states is comparable with that of the template (`c-beats` and `c-prob`).

The numbers of forwards- and backwards- realisations generated are determined by the arguments `c-forwards` and `c-backwards` respectively. The output is a list of three hash tables (one containing the forwards candidates, one the backwards candidates, and one the united candidates). If `c-forwards` =  $m$  and `c-backwards` =  $n$ , then the number of united candidates is  $3mn$ .

**generate-forced<->no-failure**

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	generate-beat-spacing-forcing->, generate-beat-spacing-forcing<-, segments-strict
Called by	generate-beat-spacing-forced<->
Comments/see also	Consider simplifying/renaming generating functions.

Example:

```
(progn
  (setq
    internal-states->
    (read-from-file
      (concatenate
        'string
        *MCStylistic-Oct2010-example-files-path*
        "/Racchmaninof-Oct2010 example"
        "/internal-initial-states.txt"))))
  (setq
    internal-states<-
    (read-from-file
      (concatenate
        'string
        *MCStylistic-Oct2010-example-files-path*
        "/Racchmaninof-Oct2010 example"
        "/internal-final-states.txt"))))
  (setq
    stm->
    (read-from-file
      (concatenate
        'string
        *MCStylistic-Oct2010-example-files-path*
        "/Racchmaninof-Oct2010 example"
        "/transition-matrix.txt"))))
  (setq
    stm<-
    (read-from-file
```

```

(concatenate
  'string
  *MCStylistic-Oct2010-example-files-path*
  "/Racchmaninof-Oct2010 example"
  "/transition-matrix<-.txt"))))
(setq no-ontimes> 29)
(setq
  dataset-all
  (read-from-file
    "/Users/tec69/Open/Music/Datasets/C-17-1-ed.txt"))
(setq
  dataset-template
  (subseq dataset-all 0 250))
(setq generation-interval '(25 29))
(setq
  pattern-region
  '((25 60 60) (25 67 64) (25 70 66) (25 76 69)
    (25 82 73) (53/2 60 60) (53/2 67 64) (53/2 70 66)
    (53/2 76 69) (53/2 81 72) (27 60 60) (27 67 64)
    (27 70 66) (27 76 69) (27 78 70) (111/4 60 60)
    (111/4 67 64) (111/4 70 66) (111/4 76 69)
    (111/4 79 71) (28 60 60) (28 67 64) (28 70 66)
    (28 76 69) (28 81 72) (29 60 60) (29 67 64)
    (29 70 66) (29 76 69) (29 79 71)))
(setq
  checklist
  (list "originalp" "mean&range" "likelihoodp"))
(setq
  *rs* #.(CCL::INITIALIZE-RANDOM-STATE 6086 61144))
(setq
  output
  (generate-forced<->no-failure
    "forwards" nil nil internal-states-> stm->
    no-ontimes> dataset-template generation-interval
    pattern-region nil checklist 3 10 4 19 12 12 12
    0.2))
  (first output))
--> 0.335408 seconds
(if (listp (fifth output))
  (saveit
    (concatenate

```

```

'string
*MCStylistic-Oct2010-example-files-path*
"/test.mid")
(modify-to-check-dataset
 (translation
  (fifth output)
  (list
   (- 0 (first (first (fifth output))))
   0 0 0 0)) 900)))

```

This function is similar to the function `generate-forwards-or-backwards-no-failure`. The difference is that this can take a pattern or a previous or next state as extra constraints. This is necessary when generating a passage according to a template. It generates states (and realisations of those states), taking initial (or final) states and a forwards- (or backwards-) running stm as arguments. The direction must be specified as the first argument, so that the appropriate generating function is called. Depending on the values of the parameters, a call to a generating function can fail to produce a generated passage, in which case this function runs again, until a passage has been generated, hence 'no failure'.

### **generate-forwards-or-backwards-no-failure**

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	generate-beat-MNN-spacing->, generate-beat-MNN-spacing<-, segments-strict
Called by	generate-beat-MNN-spacing<->, generate-beat-spacing-forced<->
Comments/see also	Consider simplifying/renaming generating functions.

Example:

```

(progn
 (setq
  initial-states
  (read-from-file
   (concatenate
    'string

```

```

    *MCStylistic-Oct2010-example-files-path*
    "/Racchmaninof-Oct2010 example"
    "/initial-states.txt"))))
(setq
  stm
  (read-from-file
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/Racchmaninof-Oct2010 example"
      "/transition-matrix.txt"))))
(setq no-ontimes> 24)
(setq
  dataset-all
  (read-from-file
    "/Users/tec69/Open/Music/Datasets/C-59-3-ed.txt"))
(setq
  dataset-template (subseq dataset-all 48 184))
(setq
  checklist
  (list "originalp" "mean&range" "likelihoodp"))
(setq
  *rs* (CCL::INITIALIZE-RANDOM-STATE 2249 23752))
(setq
  output
  (generate-forwards-or-backwards-no-failure
    "forwards" initial-states stm no-ontimes>
    dataset-template checklist 3 10 4 19 12 12 12
    0.2))
(first output))
--> 0.048711 seconds.
(if (listp (fifth output))
  (saveit
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/test.mid")
    (modify-to-check-dataset
      (translation
        (fifth output)
        (list

```

```
(- 0 (first (first (fifth output))))
0 0 0 0)) 900)))
```

This function generates states (and realisations of those states), taking initial (or final) states and a forwards- (or backwards-) running stm as arguments. The direction must be specified as the first argument, so that the appropriate generating function is called. Depending on the values of the parameters, a call to a generating function can fail to produce a generated passage, in which case this function runs again, until a passage has been generated, hence ‘no failure’.

### keys-of-states-in-transition-matrix

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	state-in-transition-matrixp
Called by	most-plausible-join
Comments/see also	

Example:

```
(setq A (make-hash-table :test #'equal))
(setf
 (gethash "cand,1,1,superimpose" A)
 '((3/4 60 60 1 0) (3/4 64 62 1 0) (3/4 67 64 1 0)))
(setf
 (gethash "cand,1,2,superimpose" A)
 '((0 60 60 1 0) (3/4 64 62 1 0) (2 67 64 1 0)))
(setf
 (gethash "cand,2,1,superimpose" A)
 '((3/4 60 60 1 0) (3/4 64 62 1 0) (3/4 69 65 1 0)))
(setf
 (gethash "cand,2,2,superimpose" A)
 '((3/4 60 60 1 0) (3/4 64 62 1 0) (3/4 72 67 1 0)))
(setq
 dataset-keys
 '("cand,1,1,superimpose" "cand,1,2,superimpose"
 "cand,2,1,superimpose" "cand,2,2,superimpose"))
(setq ontime 3/4)
(setq
 stm
```

```
'(((7/4 (4 5)) "etc") ((7/4 (4 3)) "etc")
  ((7/4 (4 3 17)) "etc"))))
(keys-of-states-in-transition-matrix
 A dataset-keys ontime stm "beat-spacing-states" 3 3
 1)
--> ("cand,1,1,superimpose" "cand,2,1,superimpose")
```

This function takes a hash table consisting of datasets and a list of keys for that hash table as its first two arguments. The function `state-in-transition-matrixp` is applied to the dataset associated with each key, and if it is in the state-transition matrix, this key is included in the returned list. This function can be used to check that the composer actually wrote the chords that are created at the bisection.

### min-max-abs-diffs-for-likelihood-profiles

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	abs-differences-for-curves-at-points, geom-mean-likelihood-of-states, max-item, min-argmin, nth-list-of-lists segments-strict
Called by	most-plausible-join
Comments/see also	

Example:

```
(setq A (make-hash-table :test #'equal))
(setf
 (gethash "cand,1,1,superimpose" A)
 '(((0 60 60 3/4 0) (0 64 62 3/4 0) (0 67 64 3/4 0)
   (3/4 60 60 1 0) (3/4 64 62 1 0) (3/4 67 64 1 0)
   (7/4 60 60 1 0) (7/4 64 62 1 0) (7/4 67 64 1 0))))
(setf
 (gethash "cand,1,2,superimpose" A)
 '(((0 60 60 1 0) (3/4 64 62 1 0) (2 67 64 1 0))))
(setf
 (gethash "cand,2,1,superimpose" A)
 '(((0 61 60 3/4 0) (0 65 62 3/4 0) (0 68 64 3/4 0)
   (3/4 60 60 1 0) (3/4 64 62 1 0) (3/4 67 64 1 0)
   (7/4 62 61 1 0) (7/4 66 63 1 0) (7/4 69 65 1 0))))
(setf
```



```

(gethash ' "cand,2,2,superimpose" A)
'((3/4 60 60 1 0) (3/4 64 62 1 0) (3/4 72 67 1 0)))
(setq
 dataset-keys
 '("cand,1,1,superimpose" "cand,1,2,superimpose"
  "cand,2,1,superimpose" "cand,2,2,superimpose"))
(setq
 template-dataset
 '((0 60 60 3/4 0) (0 64 62 3/4 0) (0 67 64 3/4 0)
  (3/4 59 59 1 0) (3/4 62 61 1 0) (3/4 67 64 1 0)
  (7/4 60 60 1 0) (7/4 64 62 1 0) (7/4 67 64 1 0)))
(setq c-beats 12)
(min-max-abs-diffs-for-likelihood-profiles
 A dataset-keys template-dataset c-beats)
--> "cand,1,1,superimpose"

```

This function takes a hash table consisting of datasets and a list of keys for that hash table as its first two arguments. Its third argument is the dataset for a template. The idea is to compare each of the likelihood profiles for the datasets associated with the keys with the likelihood profile of the template dataset, using the function `abs-differences-for-curves-at-points`. Each comparison will produce a maximal difference. The key of the dataset that produces the minimum of the maximal differences is returned, and the intuition is that this will be the most plausible dataset, compared with the template.

### most-plausible-join

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	disp-ht-key, keys-of-states-in-transition-matrix, min-max-abs-diffs-for-likelihood-profiles
Called by	
Comments/see also	

Example:

```

(setq A (make-hash-table :test #'equal))
(setf
 (gethash ' "cand,1,1,superimpose" A)

```

```

'((0 60 60 3/4 0) (0 64 62 3/4 0) (0 67 64 3/4 0)
  (3/4 60 60 1 0) (3/4 64 62 1 0) (3/4 67 64 1 0)
  (7/4 60 60 1 0) (7/4 64 62 1 0) (7/4 67 64 1 0)))
(setf
  (gethash "cand,1,2,superimpose" A)
  '((0 60 60 1 0) (3/4 64 62 1 0) (2 67 64 1 0)))
(setf
  (gethash "cand,2,1,superimpose" A)
  '((0 61 60 3/4 0) (0 65 62 3/4 0) (0 68 64 3/4 0)
    (3/4 60 60 1 0) (3/4 64 62 1 0) (3/4 67 64 1 0)
    (7/4 62 61 1 0) (7/4 66 63 1 0) (7/4 69 65 1 0)))
(setf
  (gethash "cand,2,2,superimpose" A)
  '((3/4 60 60 1 0) (3/4 64 62 1 0) (3/4 72 67 1 0)))
(setq
  template-dataset
  '((0 60 60 3/4 0) (0 64 62 3/4 0) (0 67 64 3/4 0)
    (3/4 59 59 1 0) (3/4 62 61 1 0) (3/4 67 64 1 0)
    (7/4 60 60 1 0) (7/4 64 62 1 0) (7/4 67 64 1 0)))
(setq
  stm
  '(((7/4 (4 5)) "etc") ((1 (4 3)) "etc")
    ((11/4 (4 3 17)) "etc"))))
(setq c-beats 12)
(most-plausible-join A 3/4 template-dataset stm 3 3 1)
--> "cand,1,1,superimpose"

```

This function applies the function `keys-of-states-in-transition-matrix`, followed by the function `min-max-abs-diffs-for-likelihood-profiles`, to determine which dataset, out of several candidates, is the most plausible fit with the template dataset.

## remove-coincident-datapoints

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	remove-datapoints-coincident-with-datapoint
Called by	unite-datapoints
Comments/see also	

Example:

```
(remove-coincident-datapoints
'((12 64 61 1) (14 63 62 1) (31/2 65 63 1/2))
'((9 60 60 1) (10 64 62 3) (13 63 62 1)
  (13 72 67 5) (15 65 63 1) (16 65 63 2)) 1 3)
--> ((9 60 60 1) (13 63 62 1) (13 72 67 5)
      (16 65 63 2))
```

This function removes any datapoints (second argument) that sound at the same time as datapoints provided as the first argument.

### remove-datapoints-coincident-with-datapoint

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	append-offtimes, my-last
Called by	remove-coincident-datapoints
Comments/see also	

Example:

```
(remove-datapoints-coincident-with-datapoint
'(12 64 61 1)
'((9 60 60 1) (10 64 62 3) (13 63 62 1)
  (13 72 67 5) (15 65 63 1) (16 65 63 2)) 1 3)
--> ((9 60 60 1) (13 63 62 1) (13 72 67 5)
      (15 65 63 1) (16 65 63 2))
```

This function removes any datapoints (second argument) that sound at the same time as a datapoint provided as the first argument.

### remove-datapoints-with-nth-item<

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	index-1st-sublist-item>=, nth-list-of-lists
Called by	unite-datapoints
Comments/see also	

Example:

```
(remove-datapoints-with-nth-item<
  '((9 60) (10 64) (13 63) (13 72) (15 65) (16 65)) 10
  0)
--> ((10 64) (13 63) (13 72) (15 65) (16 65))
```

This function removes any datapoints whose nth-items are less than the second argument. Datapoints are assumed to be in lexicographic order.

### **remove-datapoints-with-nth-item<=**

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	index-1st-sublist-item>, nth-list-of-lists
Called by	unite-datapoints
Comments/see also	

Example:

```
(remove-datapoints-with-nth-item<=
  '((9 60) (10 64) (13 63) (13 72) (15 65) (16 65)) 10
  0)
--> ((13 63) (13 72) (15 65) (16 65))
```

This function removes any datapoints whose nth-items are less than or equal to the second argument. Datapoints are assumed to be in lexicographic order.

### **remove-datapoints-with-nth-item>**

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	index-1st-sublist-item>, nth-list-of-lists
Called by	unite-datapoints
Comments/see also	

Example:

```
(remove-datapoints-with-nth-item>
  '((9 60) (10 64) (13 63) (13 72) (15 65) (16 65)) 15
  0)
--> ((9 60) (10 64) (13 63) (13 72) (15 65))
```

This function removes any datapoints whose `nth`-items are greater than the second argument. Datapoints are assumed to be in lexicographic order.

### **remove-datapoints-with-nth-item>=**

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	index-1st-sublist-item>=, nth-list-of-lists
Called by	unite-datapoints
Comments/see also	

Example:

```
(remove-datapoints-with-nth-item>=
'((9 60) (10 64) (13 63) (13 72) (15 65) (16 65)) 15
0)
--> ((9 60) (10 64) (13 63) (13 72))
```

This function removes any datapoints whose `nth`-items are greater than or equal to the second argument. Datapoints are assumed to be in lexicographic order.

### **state-in-transition-matrixp**

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	beat-spacing-states, nth-list-of-lists, segments-strict, spacing-holding-states
Called by	keys-of-states-in-transition-matrix
Comments/see also	

Example:

```
(state-in-transition-matrixp
'((0 60 60 1 0) (0 64 62 1 0) (0 67 64 1 0))
0
'(((7/4 (4 5)) "etc") ((1 (4 3)) "etc")
((11/4 (4 3 17)) "etc"))
"beat-spacing-states" 3 3 1)
--> T
```

This function checks a state, which exists at a specified ontime in a given dataset, for membership in a state-transition matrix. If it is a member, T is returned, and NIL otherwise.

## unite-datapoints

Started, last checked	13/10/2010, 13/10/2010
Location	Generating beat MNN spacing for&back
Calls	remove-coincident-datapoints, remove-datapoints-with-nth-item<, remove-datapoints-with-nth-item<=, remove-datapoints-with-nth-item>=, remove-datapoints-with-nth-item>, sort-dataset-asc
Called by	generate-beat-MNN-spacing<->, generate-beat-spacing-forced<->
Comments/see also	

Example:

```
(unite-datapoints
 '( (9 60 60 1) (10 64 62 2) (13 63 62 1) (14 60 60 2)
   (15 65 63 2))
 '( (27/2 60 60 1/2) (14 60 60 1) (14 63 62 1)
   (31/2 65 63 1/2) (16 64 62 1) (17 59 59 1))
 14 "superimpose")
--> ((9 60 60 1) (10 64 62 2) (13 63 62 1)
     (14 60 60 2) (14 63 62 1) (31/2 65 63 1/2)
     (16 64 62 1) (17 59 59 1))
```

This function unites two sets of datapoints. The third argument, join-at, is the ontime at which they are united (specified to avoid overhanging notes from each set sounding during the other), and the fourth argument, join-by, gives the option of superimposing the sets, or letting the first or second set take precedence.

### 4.5.9 Pattern inheritance preliminaries

These functions filter the results of applying a pattern discovery algorithm. The result is a list consisting of hash tables, where each hash table consists of the keys: index, name, cardinality, occurrences, MTP vectors, rating,

compactness, expected occurrences, compression ratio, pattern, region, and translators. The most important function in this file is called `prepare-for-pattern-inheritance`.

## indices-of-patterns-equalp-trans&intersect

Started, last checked	20/10/2010, 20/10/2010
Location	Pattern inheritance preliminaries
Calls	intersection-multidimensional
Called by	remove-patterns-equalp-trans&intersect
Comments/see also	

Example:

```
(setq
 patterns-hash
 (read-from-file-balanced-hash-table
 (concatenate
 'string
 *MCStylistic-Oct2010-example-files-path*
 "/patterns-hash.txt")))
(indices-of-patterns-equalp-trans&intersect
 (gethash "pattern" (first patterns-hash))
 (gethash "translators" (first patterns-hash))
 (rest patterns-hash))
--> nil
```

This function takes information about a pattern from the first hash table in a list of hash tables. It then compares this with each pattern in the rest of the list. If a pair of patterns have the same translation vectors and their first occurrences have intersecting datapoints, then the second pattern in the pair will have to be removed. To this end, the index of the second pattern is returned.

**prepare-for-pattern-inheritance**

Started, last checked	20/10/2010, 20/10/2010
Location	Pattern inheritance preliminaries
Calls	evaluate-variables-of-patterns2hash, remove-overlapping-translators-of-patterns, remove-patterns-equalp-trans&intersect, remove-patterns-shorter-than, subset-scores-of-patterns+, translate-patterns-to-1st-occurrences
Called by	
Comments/see also	

Example:

```
(progn
  (setq
    SIACT-output
    '((((0 36 46) (0 48 53) (0 55 57) (0 60 60)
      (0 64 62) (1/2 36 46) (1/2 48 53) (1/2 55 57)
      (1/2 62 61) (1/2 65 63) (1 36 46) (1 48 53)
      (1 55 57) (1 64 62) (1 67 64) (2 48 53)
      (2 65 63) (2 69 65) (3 36 46) (3 48 53)
      (3 55 57) (3 64 62) (3 67 64) (7/2 36 46)
      (7/2 48 53) (7/2 55 57) (7/2 60 60) (7/2 64 62)
      (4 36 46) (4 48 53) (4 55 57)) 31/33 (6 0 0))
      (((1 36 46) (1 48 53) (1 55 57) (1 64 62)
        (1 67 64) (2 48 53) (2 65 63) (2 69 65)
        (3 36 46) (3 48 53)) 5/6 (6 0 0))
        (((6 60 60) (7 55 57) (9 55 57) (9 60 60)
          (10 48 53) (10 55 57) (10 64 62) (13 55 57)
          (13 59 59) (14 55 57) (14 59 59) (19 55 57)
          (19 59 59) (20 55 57) (20 59 59) (25 55 57)
          (25 62 61) (26 55 57) (26 62 61) (27 72 67)
          (28 48 53) (28 55 57) (28 64 62) (31 55 57)
          (31 62 61) (32 55 57) (32 62 61) (33 72 67)
          (34 48 53) (34 55 57) (34 64 62) (37 55 57)
          (37 59 59)) 11/50 (6 0 0))
          (((3 48 53) (7/2 48 53) (4 48 53))
            3/11 (45 26 15) 3/11 (3 7 4))
            (((11 71 66) (23/2 72 67) (12 54 56) (12 57 58)
```



(12 60 60) (12 62 61) (12 74 68) (25/2 74 68)  
 (13 53 56) (13 55 57) (13 59 59) (13 62 61)  
 (13 74 68) (14 53 56) (14 55 57) (14 59 59)  
 (14 62 61) (14 67 64) (29/2 71 66) (15 52 55)  
 (15 55 57) (15 60 60) (15 72 67) (31/2 74 68)  
 (16 48 53) (16 55 57) (16 64 62) (16 76 69)  
 (33/2 77 70) (17 79 71) (35/2 80 71) (18 43 50)  
 (18 81 72) (37/2 81 72) (19 55 57) (19 59 59)  
 (19 65 63) (20 55 57) (20 59 59) (20 65 63)  
 (20 79 71) (41/2 74 68) (21 48 53) (21 77 70)  
 (43/2 77 70) (22 57 58) (22 65 63) (22 77 70)  
 (23 55 57) (23 64 62) (23 76 69) (24 54 56)  
 (24 57 58) (24 60 60) (24 62 61) (24 74 68)  
 (49/2 74 68) (25 53 56) (25 55 57) (25 59 59)  
 (25 62 61) (25 74 68) (26 53 56) (26 55 57)  
 (26 59 59) (26 62 61) (26 67 64) (53/2 71 66)  
 (27 52 55) (27 55 57) (27 60 60) (27 72 67)  
 (55/2 74 68) (28 48 53) (28 55 57) (28 64 62)  
 (28 76 69) (57/2 77 70) (29 79 71) (59/2 84 74)  
 (30 43 50) (30 83 73) (123/4 81 72) (31 55 57)  
 (31 62 61) (31 65 63) (31 77 70) (63/2 74 68)  
 (32 55 57) (32 62 61) (32 65 63) (32 71 66)  
 (65/2 67 64) (33 48 53) (33 64 62) (33 72 67)  
 (100/3 74 68) (67/2 67 64) (101/3 76 69)  
 (34 48 53) (34 55 57) (34 60 60) (34 64 62)  
 (34 72 67)) 104/105 (24 0 0))  
 (((12 54 56) (12 57 58) (12 60 60) (12 62 61)  
 (12 74 68) (25/2 74 68) (13 53 56) (13 55 57)  
 (13 59 59) (13 62 61) (13 74 68) (14 53 56)  
 (14 55 57) (14 59 59) (14 62 61) (14 67 64)  
 (29/2 71 66) (15 52 55) (15 55 57) (15 60 60)  
 (15 72 67) (31/2 74 68) (16 48 53) (16 55 57)  
 (16 64 62) (16 76 69) (33/2 77 70) (17 79 71)  
 (18 43 50) (19 55 57) (19 65 63) (20 55 57)  
 (20 65 63) (21 48 53)) 17/21 (12 0 0))  
 (((36 54 56) (36 57 58) (36 60 60) (36 62 61)  
 (36 74 68) (73/2 74 68) (37 53 56) (37 55 57)  
 (37 59 59) (37 62 61) (37 74 68) (38 53 56)  
 (38 55 57) (38 59 59) (38 62 61) (38 67 64)  
 (77/2 71 66) (39 52 55) (39 55 57) (39 60 60)  
 (39 72 67) (79/2 74 68) (40 48 53) (40 55 57)

```

      (40 64 62) (40 76 69) (81/2 77 70) (41 79 71)
      (42 43 50) (43 55 57) (43 65 63) (44 55 57)
      (44 65 63) (45 48 53)) 34/41 (12 0 0)))
(setq
 dataset-all
 (read-from-file
  (concatenate
   'string
   *MCStylistic-Oct2010-data-path*
   "/Dataset/C-68-1-ed.txt")))
(setq dataset-mini (subseq dataset-all 0 350))
(setq
 projected-dataset
 (orthogonal-projection-unique-equalp
  dataset-mini '(1 1 1 0 0)))
"Data imported.")
(setq
 patterns-hash
 (prepare-for-pattern-inheritance
  SIACT-output projected-dataset 1))
--> (#<HASH-TABLE :TEST EQUAL
      size 15/60 #x300041ABBC9D>
      #<HASH-TABLE :TEST EQUAL
      size 15/60 #x3000419F57AD>
      #<HASH-TABLE :TEST EQUAL
      size 15/60 #x30004199959D>
      #<HASH-TABLE :TEST EQUAL
      size 15/60 #x3000419CE8AD>)
```

This function applies functions that prepare the output of SIACT run on a dataset for random generation Markov chain (RGMC) with pattern inheritance.

## remove-overlapping-translators

Started, last checked	20/10/2010, 20/10/2010
Location	Pattern inheritance preliminaries
Calls	
Called by	remove-overlapping-translators-of-patterns
Comments/see also	

Example:

```
(remove-overlapping-translators
 3 '((0 0 0) (1 2 3) (4 0 0) (5 0 0) (7 0 0) (8 2 1)))
--> ((0 0 0) (4 0 0) (7 0 0))
```

This function takes the duration of a pattern and its translators as arguments, and returns a list of those translators that do not produce overlapping patterns (in the sense of the argument pattern-duration).

### remove-overlapping-translators-of-patterns

Started, last checked	20/10/2010, 20/10/2010
Location	Pattern inheritance preliminaries
Calls	remove-overlapping-translators
Called by	prepare-for-pattern-inheritance
Comments/see also	

Example:

```
(setq
 patterns-hash
 (read-from-file-balanced-hash-table
  (concatenate
   'string
   *MCStylistic-Oct2010-example-files-path*
   "/patterns-hash.txt")))
(setq
 patterns-hash2
 (remove-overlapping-translators-of-patterns
  patterns-hash))
--> (#<HASH-TABLE :TEST EQUAL
      size 15/60 #x300041A38CFD>
      #<HASH-TABLE :TEST EQUAL
      size 15/60 #x300041A386ED>
      #<HASH-TABLE :TEST EQUAL
      size 15/60 #x300041A380DD>
      #<HASH-TABLE :TEST EQUAL
      size 15/60 #x300041A37ACD>)
```

This function applies the function remove-overlapping-translators recursively to a list consisting of hash tables. Each hash table contains information

about a discovered pattern, as returned by the function `evaluate-variables-of-patterns2hash`. The output is an updated hash table.

## **remove-patterns-equalp-trans&intersect**

Started, last checked	20/10/2010, 20/10/2010
Location	Pattern inheritance preliminaries
Calls	<code>indices-of-patterns-equalp-trans&amp;intersect</code> , <code>remove-nth-list</code>
Called by	<code>prepare-for-pattern-inheritance</code>
Comments/see also	

Example:

```
(setq
 patterns-hash
 (read-from-file-balanced-hash-table
  (concatenate
   'string
   *MCStylistic-Oct2010-example-files-path*
   "/patterns-hash.txt")))
(setq
 patterns-hash3
 (remove-patterns-equalp-trans&intersect
  patterns-hash))
--> (#<HASH-TABLE :TEST EQUAL
      size 15/60 #x300041A38CFD>
      #<HASH-TABLE :TEST EQUAL
      size 15/60 #x300041A386ED>
      #<HASH-TABLE :TEST EQUAL
      size 15/60 #x300041A380DD>
      #<HASH-TABLE :TEST EQUAL
      size 15/60 #x300041A37ACD>)
```

This function applies the function `indices-of-patterns-equalp-trans&intersect` recursively. The result is that the lower-rating of any pair of patterns is removed if the two patterns have the same translation vectors and their first occurrences have intersecting datapoints. It is assumed that each pattern has already been arranged so that its first translation vector is the zero vector.

**remove-patterns-shorter-than**

Started, last checked	20/10/2010, 20/10/2010
Location	Pattern inheritance preliminaries
Calls	my-last
Called by	prepare-for-pattern-inheritance
Comments/see also	

Example:

```
(setq
 pattern&sources
 '((((1/2 72 67 1/2) (1 76 69 1/2) (3/2 79 71 1/2)
      (2 84 74 2) (5/2 67 64 1/2) (3 64 62 1/2)
      (7/2 60 60 1/2))
 16/23 (140 5 0) 1 (104 -5 0) 4/5 (96 -5 0))
 (((1/2 72 67 1/2) (3/2 79 71 1/2))
 1 (130 0 0) 2/3 (100 0 1/2))))
(remove-patterns-shorter-than pattern&sources 3)
--> (((1/2 72 67 1/2) (1 76 69 1/2)
      (3/2 79 71 1/2) (2 84 74 2) (5/2 67 64 1/2)
      (3 64 62 1/2) (7/2 60 60 1/2))
 16/23 (140 5 0) 1 (104 -5 0) 4/5 (96 -5 0)))
```

Let  $a$  be the floor of the first ontime and  $b$  be the ceiling of the last offtime of a pattern. If this is less than the optional variable `duration-threshold`, then this pattern will not appear in the output of this function.

**subset-score-of-pattern**

Started, last checked	20/10/2010, 20/10/2010
Location	Pattern inheritance preliminaries
Calls	fibonacci-list, subset-multidimensional, translations
Called by	subset-scores-of-patterns+
Comments/see also	

Example:

```
(setq
 patterns-hash
```

```
(read-from-file-balanced-hash-table
 (concatenate
  'string
  *MCStylistic-Oct2010-example-files-path*
  "/patterns-hash.txt"))))
(subset-score-of-pattern
 (gethash "pattern" (nth 3 patterns-hash))
 3 patterns-hash)
--> 1
```

This function takes a pattern as its first argument, called the probe pattern, and a hash table of patterns as its second argument. It counts and returns the number of patterns in the hash table (including translations) of which the probe pattern is a subset.

### subset-scores-of-patterns+

Started, last checked	20/10/2010, 20/10/2010
Location	Pattern inheritance preliminaries
Calls	first-n-naturals, subset-score-of-pattern, translations
Called by	prepare-for-pattern-inheritance
Comments/see also	

Example:

```
(setq
 patterns-hash
 (read-from-file-balanced-hash-table
 (concatenate
  'string
  *MCStylistic-Oct2010-example-files-path*
  "/patterns-hash.txt"))))
(setq
 patterns-hash4
 (subset-scores-of-patterns+ patterns-hash))
--> (#<HASH-TABLE :TEST EQUAL
 size 15/60 #x30004188F86D>
 #<HASH-TABLE :TEST EQUAL
 size 15/60 #x30004188F25D>
 #<HASH-TABLE :TEST EQUAL
```

```
size 15/60 #x30004188EC4D>
#<HASH-TABLE :TEST EQUAL
size 15/60 #x30004188E63D>)
```

This function applies the function `subset-score-of-pattern` to each pattern (including translations) listed in a hash table of patterns. It also creates inheritance indices (for example the first occurrence of the highest-rating pattern is labelled  $P_{0,0}$ ) and a variable called inheritance addressed, set to "No" by default, but will revert to "Yes" when patterns are incorporated into the generated passage. This function is the last step in preparing a hash table of patterns for generation with pattern inheritance.

### translate-pattern-to-1st-occurrence

Started, last checked	20/10/2010, 20/10/2010
Location	Pattern inheritance preliminaries
Calls	constant-vector, multiply-list-by-constant, translation, vector<vector-t-or-nil
Called by	translate-patterns-to-1st-occurrences
Comments/see also	

Example:

```
(setq
 pattern
 '((1/2 72 67 1/2) (1 76 69 1/2) (3/2 79 71 1/2)
 (2 84 74 2) (5/2 67 64 1/2) (3 64 62 1/2)
 (7/2 60 60 1/2)))
(setq translators '((-1/2 0 0 0) (0 0 0 0) (3 2 1 0)))
(translate-pattern-to-1st-occurrence
 pattern translators)
--> (((0 72 67 1/2) (1/2 76 69 1/2) (1 79 71 1/2)
 (3/2 84 74 2) (2 67 64 1/2) (5/2 64 62 1/2)
 (3 60 60 1/2))
 ((0 0 0 0) (1/2 0 0 0) (7/2 2 1 0)))
```

Sometimes an occurrence of a pattern is found, other than the first occurrence in a piece. This function takes such instances and rearranges the pattern and the translators, so it is the first occurrence which is displayed.

**translate-patterns-to-1st-occurrences**

Started, last checked	20/10/2010, 20/10/2010
Location	Pattern inheritance preliminaries
Calls	constant-vector, translate-pattern-to-1st-occurrence
Called by	prepare-for-pattern-inheritance
Comments/see also	

Example:

```
(setq
 patterns-hash
 (read-from-file-balanced-hash-table
 (concatenate
 'string
 *MCStylistic-Oct2010-example-files-path*
 "/patterns-hash.txt")))
(setq
 patterns-hash5
 (translate-patterns-to-1st-occurrences
 patterns-hash))
--> (#<HASH-TABLE :TEST EQUAL
      size 15/60 #x30004188F86D>
      #<HASH-TABLE :TEST EQUAL
      size 15/60 #x30004188F25D>
      #<HASH-TABLE :TEST EQUAL
      size 15/60 #x30004188EC4D>
      #<HASH-TABLE :TEST EQUAL
      size 15/60 #x30004188E63D>)
```

This function applies the function `translate-pattern-to-1st-occurrence` recursively to a list consisting of hash tables. Each hash table contains information about a discovered pattern, as returned by the function `evaluate-variables-of-patterns2hash`. The output is an updated hash table.

**4.5.10 Generating with patterns preliminaries**

Most of these functions process lists that represent interval endpoints (interval in the mathematical sense). Others scan hash tables (typically a `patterns hash`) for instance in order to find the indices of elements with certain properties. There are also some custom merge-sort functions.



**car<**

Started, last checked	22/10/2010, 22/10/2010
Location	Generating with patterns preliminaries
Calls	
Called by	merge-sort-by-car<
Comments/see also	Consider changing location.

Example:

```
(car< '(1 "sprout") '(1.1 "purple"))
--> T
```

This function returns T if the first element of the first argument is less than the first element of the second argument, and NIL otherwise.

**car>**

Started, last checked	22/10/2010, 22/10/2010
Location	Generating with patterns preliminaries
Calls	
Called by	merge-sort-by-car>
Comments/see also	Consider changing location.

Example:

```
(car> '(1 "sprout") '(1.1 "purple"))
--> NIL
```

This function returns T if the first element of the first argument is greater than the first element of the second argument, and NIL otherwise.

**generate-intervals**

Started, last checked	22/10/2010, 22/10/2010
Location	Generating with patterns preliminaries
Calls	interval-intersectionsp, interval-subsetsp
Called by	
Comments/see also	

Example:

```
(setq existing-intervals '((11 17) (20 26) (26 30)))
(setq floor-ontime 1)
(setq ceiling-ontime 40)
(generate-intervals
 floor-ontime ceiling-ontime existing-intervals)
--> ((1 11) (17 20) (30 40))
```

If  $L = \{[a_1, b_1), [a_2, b_2), \dots, [a_l, b_l)\}$  is a list of non-overlapping intervals, with each interval a subset of  $[a, b)$ , then this function returns endpoints of the non-overlapping intervals  $M = \{[c_1, d_1), [c_2, d_2), \dots, [c_m, d_m)\}$  such that  $L \cup M = [a, b)$ .

### indices-of-max-subset-score

Started, last checked	22/10/2010, 22/10/2010
Location	Generating with patterns preliminaries
Calls	merge-sort-by-car>, merge-sort-by-vector<vector-car, my-last, unaddressed-patterns-subset-scores
Called by	
Comments/see also	

Example:

```
(setq
 patterns-hash
 (read-from-file-balanced-hash-table
 (concatenate
 'string
 *MCStylistic-Oct2010-example-files-path*
 "/patterns-hash.txt")))
(indices-of-max-subset-score patterns-hash)
--> (3 4)
```

This function takes a patterns-hash (a list of discovered translational equivalence classes, each with corresponding attributes) and returns the indices of the pattern that has the highest subset score. The first index is for the TEC, the second is for the occurrence.

**interval-intersectionp**

Started, last checked	22/10/2010, 22/10/2010
Location	Generating with patterns preliminaries
Calls	
Called by	interval-intersectionsp
Comments/see also	

Example:

```
(interval-intersectionp '(7 9) '(3 7.1))
--> T.
```

This function returns T if its two arguments, endpoints of the intervals  $X = [a, b]$  and  $Y = [c, d]$ , are such that  $X \cap Y \neq \emptyset$ , and NIL otherwise.

**interval-intersectionsp**

Started, last checked	22/10/2010, 22/10/2010
Location	Generating with patterns preliminaries
Calls	interval-intersectionp
Called by	generate-intervals
Comments/see also	

Example:

```
(interval-intersectionsp
 '(7 9) '((1 2) (2.2 2.4) (2 2.5) (3 7.1) (1 1)))
--> 3
```

This function has two arguments: the endpoints of a single interval  $X = [a, b]$ , and the endpoints of a list of intervals  $L = \{[a_1, b_1], [a_2, b_2], \dots, [a_l, b_l]\}$ . The function returns the minimum value of  $i$  such that  $[a, b] \cap [a_i, b_i] \neq \emptyset$ , or NIL if no such  $i$  exists.

**interval-subsetp**

Started, last checked	22/10/2010, 22/10/2010
Location	Generating with patterns preliminaries
Calls	
Called by	interval-subsetsp
Comments/see also	

Example:

```
(interval-subsetp '(7 9) '(7 10))
--> T
```

This function returns T if its two arguments, endpoints of the intervals  $X = [a, b]$  and  $Y = [c, d]$ , are such that  $X \subseteq Y$ , and NIL otherwise.

## interval-subsetsp

Started, last checked	22/10/2010, 22/10/2010
Location	Generating with patterns preliminaries
Calls	interval-subsetp
Called by	generate-intervals
Comments/see also	

Example:

```
(interval-subsetsp
 '(7 9) '((1 2) (2.2 2.4) (2 8.5) (4 9.1) (1 1)))
--> T
```

This function has two arguments: the endpoints of a single interval  $X = [a, b]$ , and the endpoints of a list of intervals  $L = \{[a_1, b_1], [a_2, b_2], \dots, [a_l, b_l]\}$ . The function returns T if there exists  $1 \leq i \leq l$  such that  $[a, b] \subseteq [a_i, b_i]$ , or NIL if no such  $i$  exists.

## merge-sort-by-car<

Started, last checked	22/10/2010, 22/10/2010
Location	Generating with patterns preliminaries
Calls	car<
Called by	
Comments/see also	Consider changing location.

Example:

```
(merge-sort-by-car<
 '((2 "b") (6 "j") (0 "a") (3 "i") (6 "h")))
--> ((0 "a") (2 "b") (3 "i") (6 "j") (6 "h"))
```

This function performs an ascending merge sort on a list of lists, using the first element of each list to determine position.

**merge-sort-by-car>**

Started, last checked	22/10/2010, 22/10/2010
Location	Generating with patterns preliminaries
Calls	car>
Called by	indices-of-max-subset-score
Comments/see also	Consider changing location.

Example:

```
(merge-sort-by-car>
'((2 "b") (6 "j") (0 "a") (3 "i") (6 "h")))
--> ((6 "j") (6 "h") (3 "i") (2 "b") (0 "a"))
```

This function performs a descending merge sort on a list of lists, using the first element of each list to determine position.

**merge-sort-by-vector<vector-car**

Started, last checked	22/10/2010, 22/10/2010
Location	Generating with patterns preliminaries
Calls	vector<vector-car
Called by	indices-of-max-subset-score
Comments/see also	Consider changing location. See also vector<vector.

Example:

```
(merge-sort-by-vector<vector-car
'(((1 8.968646) (0 0)) ((0 8.957496) (1 0))
((0 8.167285) (2 0)) ((2 3.8855853 (3 4)))))
--> (((0 8.167285) (2 0)) ((0 8.957496) (1 0))
((1 8.968646) (0 0)) ((2 3.8855853 (3 4)))))
```

This function performs an ascending merge sort on a list of lists, using the lexicographic order of first elements to determine position.

## unaddressed-patterns-subset-scores

Started, last checked	22/10/2010, 22/10/2010
Location	Generating with patterns preliminaries
Calls	pair-off-lists
Called by	indices-of-max-subset-score
Comments/see also	

Example:

```
(setq
 patterns-hash
 (read-from-file-balanced-hash-table
 (concatenate
 'string
 *MCStylistic-Oct2010-example-files-path*
 "/patterns-hash.txt")))
(unaddressed-patterns-subset-scores patterns-hash)
--> (((((1 (0 0)) (1 (0 1)) (1 (0 2)) (1 (0 3)))
      8.968646)
      (((0 (1 0)) (0 (1 1))) 8.957496)
      (((0 (2 0)) (0 (2 1))) 8.167285)
      (((1 (3 0)) (1 (3 1)) (1 (3 2)) (1 (3 3))
        (2 (3 4)) (0 (3 5)) (1 (3 6)) (2 (3 7))
        (2 (3 8)) (1 (3 9)) (2 (3 10))) 3.8855853)).
```

This function scans a patterns-hash for unaddressed patterns. If a pattern is unaddressed, its subset score and indices will appear in the output, as well as its pattern importance rating.

### 4.5.11 Generating with patterns

The main function here is generate-beat-spacing<->pattern-inheritance, at the heart of the model named Racchmaninof-Oct2010 (standing for RAndom Constrained CHain of Markovian Nodes with INheritance Of Form).

**generate-beat-spacing<->pattern-inheritance**

Started, last checked	25/10/2010, 25/10/2010
Location	Generating with patterns preliminaries
Calls	generate-beat-spacing-for-intervals, generate-intervals, indices-of-max-subset-score, merge-sort-by-vector<vector-car, my-last, nth-list-of-lists, translate-to-other-occurrences, translation
Called by	
Comments/see also	

Example: see Stylistic composition with Racchmaninof-Oct2010 (Sec. 3.3, especially lines 575-582).

This function is at the heart of the model named Racchmaninof-Oct2010 (standing for RAndom Constrained CHain of Markovian Nodes with INheritance Of Form). It takes nine mandatory arguments and twenty-two optional arguments. The mandatory arguments are initial-state and state-transition lists, and also information pertaining to a so-called *template with patterns*. The optional arguments are mainly for controlling various criteria like: not too many consecutive states from the same source, the range must be comparable with that of the template, and the likelihood of the states must be comparable with that of the template.

**generate-beat-spacing-for-interval**

Started, last checked	25/10/2010, 25/10/2010
Location	Generating with patterns preliminaries
Calls	beat-spacing-states, beat-spacing-states<-, generate-beat-spacing-forced<->, most-plausible-join, my-last, nth-list-of-lists, remove-datapoints-with-nth-item<, remove-datapoints-with-nth-item>
Called by	generate-beat-spacing-for-intervals
Comments/see also	

Example:

(progn

```
(setq
  external-initial-states
  (read-from-file
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/Racchmaninof-Oct2010 example"
      "/initial-states.txt"))))
(setq
  internal-initial-states
  (read-from-file
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/Racchmaninof-Oct2010 example"
      "/internal-initial-states.txt"))))
(setq
  stm->
  (read-from-file
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/Racchmaninof-Oct2010 example"
      "/transition-matrix.txt"))))
(setq
  external-final-states
  (read-from-file
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/Racchmaninof-Oct2010 example"
      "/final-states.txt"))))
(setq
  internal-final-states
  (read-from-file
    (concatenate
      'string
      *MCStylistic-Oct2010-example-files-path*
      "/Racchmaninof-Oct2010 example"
      "/internal-final-states.txt"))))
(setq
```



```

stm<-
(read-from-file
  (concatenate
    'string
    *MCStylistic-Oct2010-example-files-path*
    "/Racchmaninof-Oct2010 example"
    "/transition-matrix<-.txt")))
(setq
  dataset-all
  (read-from-file
    (concatenate
      'string
      *MCStylistic-Oct2010-data-path*
      "/Dataset/C-56-1-ed.txt")))
(setq
  dataset-template
  (subseq dataset-all 0 132))
"Data imported.")
(progn
  (setq generation-interval '(12 24))
  (setq
    whole-piece-interval
    (list
      (floor (first (first dataset-all)))
      (ceiling (first (my-last dataset-all)))))
  (setq A (make-hash-table :test #'equal))
  (setf
    (gethash
      "united-candidates,1,1,superimpose" A)
    '((9 70 66 3 0) (9 79 71 1/2 0) (19/2 74 68 3/2 0)
      (10 55 57 1 1) (10 62 61 1 1) (11 55 57 1 1)
      (11 62 61 1 1) (12 38 47 1 1) (12 69 65 1/2 0)))
  (setq B (make-hash-table :test #'equal))
  (setf
    (gethash
      "united-candidates,2,3,forwards-dominant" B)
    '((24 38 47 1 1) (49/2 66 63 1/2 0) (25 50 54 1 1)
      (25 57 58 1 1) (25 60 60 1 1) (25 62 61 1 0)
      (26 50 54 1 1) (26 57 58 1 1) (26 60 60 1 1)
      (26 62 61 1 1) (26 66 63 1 0) (26 70 66 3/4 0)
      (107/4 69 65 1/4 0) (27 43 50 1 1)

```

```

    (27 67 64 2 0)))
(setq
 interval-output-pairs
 (list
  (list
   (list 9 12)
   (list
    "united-candidates,1,1,superimpose"
    (list nil nil A)))
  (list
   (list 24 27)
   (list
    "united-candidates,2,3,forwards-dominant"
    (list nil nil B)))))
(setq
 pattern-region
 '((12 60 60) (12 64 62) (25/2 57 58) (51/4 64 62)
   (13 52 55) (13 64 62) (14 54 56) (29/2 62 61)
   (15 55 57) (15 59 59) (63/4 64 62) (16 43 50)
   (16 50 54) (16 66 63) (17 67 64) (18 57 58)
   (18 60 60) (18 64 62) (75/4 66 63) (19 43 50)
   (19 50 54) (19 67 64) (20 66 63) (20 69 65)
   (21 59 59) (21 67 64) (21 71 66) (87/4 74 68)
   (22 43 50) (22 50 54) (22 74 68) (23 62 61)
   (24 60 60) (24 64 62)))
"Argument instances defined.")
(progn
 (setq
  checklist
  (list "originalp" "mean&range" "likelihoodp"))
 (setq beats-in-bar 3) (setq c-failures 10)
 (setq c-sources 4) (setq c-bar 48) (setq c-min 38)
 (setq c-max 38) (setq c-beats 38) (setq c-prob 1)
 (setq c-forwards 3) (setq c-backwards 3)
 (setq
  *rs* #.(CCL::INITIALIZE-RANDOM-STATE 56302 14832))
 "Parameters set.")
(progn
 (setq
  interval-output-pair
  (generate-beat-spacing-for-interval

```

```

generation-interval whole-piece-interval
interval-output-pairs external-initial-states
internal-initial-states stm->
external-final-states internal-final-states stm<-
dataset-template pattern-region checklist
beats-in-bar c-failures c-sources c-bar c-min
c-max c-beats c-prob c-forwards c-backwards))
--> ((12 24)
      ("united,2,1,backwards-dominant"
       (#<HASH-TABLE
        :TEST EQUAL size 3/60 #x30004340CE3D>
        #<HASH-TABLE
        :TEST EQUAL size 3/60 #x30004340C82D>
        #<HASH-TABLE
        :TEST EQUAL size 27/60 #x30004340C21D>))))

```

This function generates material for a specified time interval, by calling the function `generate-beat-spacing-forcedj-i`.

### **generate-beat-spacing-for-intervals**

Started, last checked	25/10/2010, 25/10/2010
Location	Generating with patterns preliminaries
Calls	generate-beat-spacing-for-interval
Called by	generate-beat-spacing<->pattern-inheritance
Comments/see also	

Example: see example for `generate-beat-spacing-for-interval`.

This function applies the function `generate-beat-spacing-for-interval` to each member of a list called `interval-output-pairs`.

### **interval-output-pairs2dataset**

Started, last checked	25/10/2010, 25/10/2010
Location	Generating with patterns preliminaries
Calls	unite-datapoints
Called by	generate-beat-spacing<->pattern-inheritance
Comments/see also	

Example: see example for unite-datapoints.

This function applies the function unite-datapoints, to convert the output for various intervals into a dataset.

### translate-to-other-occurrence

Started, last checked	25/10/2010, 25/10/2010
Location	Generating with patterns preliminaries
Calls	translation
Called by	translate-to-other-occurrences
Comments/see also	

Example:

```
(translate-to-other-occurrence
 nil '(36 12 7) '((12 24))
 (make-hash-table :test #'equal)
 (translation
  '((12 38 47 1/2 1) (49/4 64 62 1/4 0)
    (25/2 50 54 1 1) (25/2 55 57 1 1) (25/2 58 59 1 1)
    (25/2 62 61 1 0)) '(36 12 7 0 0)))
--> (((48 60)
      ("translated material"
       (NIL NIL
        #<HASH-TABLE :TEST EQUAL
         size 1/60 #x3000436FF23D>))))))
```

This function takes a list of interval- output pairs as its argument (from one iteration of generate-beat-spacing-;pattern-inheritance) Its second argument is a translation vector, by which each of the output datasets must be translated.

**translate-to-other-occurrences**

Started, last checked	25/10/2010, 25/10/2010
Location	Generating with patterns preliminaries
Calls	my-last, nth-list-of-lists, remove-nth, subtract-list-from-each-list, translate-to-other-occurrence
Called by	generate-beat-spacing<->pattern- inheritance
Comments/see also	

Example: see example for translate-to-other-occurrence.

This function applies the function translate-to-other-occurrence to each member of a list called **translators**. It first determines whether the location to which material will be translated has been addressed.

**4.5.12 Realising states**

These functions are used to convert states generated using random generation Markov chains (RGMC) into datapoints. A lot of the functions have similar versions in the file markov-compose.lisp.

**create-MIDI&morphetic-numbers**

Started, last checked	1/9/2010, 1/9/2010
Location	Realising states
Calls	add-to-list, nth-list-of-lists
Called by	states2datapoints-by-lookup
Comments/see also	create-MIDI-note-numbers, create-MIDI&morphetic-numbers<-

Example:

```
(setq
 states
 '(((1 (12 7 5 4))
 (NIL NIL "C-63-1"
 ((0 35 45 1/2 1 1/2 0) (0 47 52 1/2 1 1/2 1)
 (0 54 56 1/2 0 1/2 2) (0 59 59 1/2 0 1/2 3)
 (0 63 61 1/2 0 1/2 4))))))
```

```

((3/2 "rest")
 (NIL NIL "C-63-1" NIL))
((7/4 NIL)
 (-6 -3 "C-63-1"
  ((831/4 56 57 1/4 0 208 701))))
((2 (12 14 6 3))
 (-26 -15 "C-63-1"
  ((208 30 42 1 1 209 702)
   (208 42 49 1 1 209 703)
   (208 56 57 1 0 209 704)
   (208 62 60 1 0 209 705)
   (208 65 62 1 0 209 706))))
((3 (12 12 9 3))
 (0 0 "C-63-1"
  ((209 30 42 1 1 210 707)
   (209 42 49 1 1 210 708)
   (209 54 56 1 0 210 709)
   (209 63 61 1 0 210 710)
   (209 66 63 1 0 210 711))))
((1 (12 16 6 4))
 (0 0 "C-63-1"
  ((216 30 42 1 1 217 740)
   (216 42 49 1 1 217 741)
   (216 58 58 1 0 217 742)
   (216 64 62 1 0 217 743)
   (216 68 64 1 0 217 744))))
((2 (5 4 3))
 (19 11 "C-63-1"
  ((43 56 57 1 1 44 195) (43 61 60 1 1 44 196)
   (43 65 62 1/2 0 87/2 197)
   (43 68 64 1 1 44 198))))
((5/2 (5 4 8 4))
 (0 0 "C-63-1"
  ((25 54 56 1 1 26 101) (25 59 59 1 1 26 102)
   (25 63 61 1 1 26 103)
   (51/2 71 66 1/2 0 26 105)
   (51/2 75 68 1/2 0 26 106))))
((3 (3))
 (19 11 "C-63-1"
  ((230 73 67 3/4 0 923/4 809)
   (230 76 69 3/4 0 923/4 810))))

```

```

((7/2 (4))
  (3 2 "C-67-1"
    ((41/2 72 67 1/2 0 21 94)
      (41/2 76 69 1/2 0 21 95))))))
(create-MIDI&morphic-numbers states)
--> (((1 (60 72 79 84 88) (60 67 71 74 76))
      (NIL NIL "C-63-1"
        ((0 35 45 1/2 1 1/2 0)
          (0 47 52 1/2 1 1/2 1)
          (0 54 56 1/2 0 1/2 2)
          (0 59 59 1/2 0 1/2 3)
          (0 63 61 1/2 0 1/2 4))))))
      ((3/2 NIL NIL)
        (NIL NIL "C-63-1" NIL))
      ((7/4 (54) (57))
        (-6 -3 "C-63-1"
          ((831/4 56 57 1/4 0 208 701))))
      ((2 (28 40 54 60 63) (42 49 57 60 62))
        (-26 -15 "C-63-1"
          ((208 30 42 1 1 209 702)
            (208 42 49 1 1 209 703)
            (208 56 57 1 0 209 704)
            (208 62 60 1 0 209 705)
            (208 65 62 1 0 209 706))))
      ((3 (28 40 52 61 64) (42 49 56 61 63))
        (0 0 "C-63-1"
          ((209 30 42 1 1 210 707)
            (209 42 49 1 1 210 708)
            (209 54 56 1 0 210 709)
            (209 63 61 1 0 210 710)
            (209 66 63 1 0 210 711))))
      ((1 (28 40 56 62 66) (42 49 58 62 64))
        (0 0 "C-63-1"
          ((216 30 42 1 1 217 740)
            (216 42 49 1 1 217 741)
            (216 58 58 1 0 217 742)
            (216 64 62 1 0 217 743)
            (216 68 64 1 0 217 744))))
      ((2 (47 52 56 59) (53 56 58 60))
        (19 11 "C-63-1"
          ((43 56 57 1 1 44 195) (43 61 60 1 1 44 196))

```

```

      (43 65 62 1/2 0 87/2 197)
      (43 68 64 1 1 44 198))))
((5/2 (47 52 56 64 68) (53 56 58 63 65))
 (0 0 "C-63-1"
  ((25 54 56 1 1 26 101) (25 59 59 1 1 26 102)
   (25 63 61 1 1 26 103)
   (51/2 71 66 1/2 0 26 105)
   (51/2 75 68 1/2 0 26 106))))
((3 (66 69) (64 66))
 (19 11 "C-63-1"
  ((230 73 67 3/4 0 923/4 809)
   (230 76 69 3/4 0 923/4 810))))
((7/2 (69 73) (66 68))
 (3 2 "C-67-1"
  ((41/2 72 67 1/2 0 21 94)
   (41/2 76 69 1/2 0 21 95)))))

```

This function is meant to take generated states and realise MIDI note numbers and morphetic pitch numbers for each state.

## half-state2datapoints-by-lookup

Started, last checked	1/9/2010, 1/9/2010
Location	Realising states
Calls	state-note2datapoint-by-lookup
Called by	states2datapoints-by-lookup
Comments/see also	half-state2datapoints

Example:

```

(setq
 half-states
 '(((1 (60 72 79 84 88) (60 67 71 74 76))
  (NIL NIL "C-63-1"
   ((0 35 45 1/2 1 1/2 0) (0 47 52 1/2 1 1/2 1)
    (0 54 56 1/2 0 1/2 2) (0 59 59 1/2 0 1/2 3)
    (0 63 61 1/2 0 1/2 4)))))
 ((3/2 NIL NIL)
  (NIL NIL "C-63-1" NIL))
 ((7/4 (54) (57))
  (-6 -3 "C-63-1"

```



```

      ((831/4 56 57 1/4 0 208 701))))
((2 (28 40 54 60 63) (42 49 57 60 62))
(-26 -15 "C-63-1"
  ((208 30 42 1 1 209 702)
   (208 42 49 1 1 209 703)
   (208 56 57 1 0 209 704)
   (208 62 60 1 0 209 705)
   (208 65 62 1 0 209 706))))
((3 (28 40 52 61 64) (42 49 56 61 63))
(0 0 "C-63-1"
  ((209 30 42 1 1 210 707)
   (209 42 49 1 1 210 708)
   (209 54 56 1 0 210 709)
   (209 63 61 1 0 210 710)
   (209 66 63 1 0 210 711))))
((1 (28 40 56 62 66) (42 49 58 62 64))
(0 0 "C-63-1"
  ((216 30 42 1 1 217 740)
   (216 42 49 1 1 217 741)
   (216 58 58 1 0 217 742)
   (216 64 62 1 0 217 743)
   (216 68 64 1 0 217 744))))
((2 (47 52 56 59) (53 56 58 60))
(19 11 "C-63-1"
  ((43 56 57 1 1 44 195) (43 61 60 1 1 44 196)
   (43 65 62 1/2 0 87/2 197)
   (43 68 64 1 1 44 198))))
((5/2 (47 52 56 64 68) (53 56 58 63 65))
(0 0 "C-63-1"
  ((25 54 56 1 1 26 101) (25 59 59 1 1 26 102)
   (25 63 61 1 1 26 103)
   (51/2 71 66 1/2 0 26 105)
   (51/2 75 68 1/2 0 26 106))))
((3 (66 69) (64 66))
(19 11 "C-63-1"
  ((230 73 67 3/4 0 923/4 809)
   (230 76 69 3/4 0 923/4 810))))
((7/2 (69 73) (66 68))
(3 2 "C-67-1"
  ((41/2 72 67 1/2 0 21 94)
   (41/2 76 69 1/2 0 21 95))))

```

```
(half-state2datapoints-by-lookup
  0 half-states
  '(500 500 500 500 500) '(0 500 1000 1500 2000 2500))
--> ((0 60 60 500 1) (0 72 67 500 1) (0 79 71 500 0)
      (0 84 74 500 0) (0 88 76 500 0))
```

This function increments over the  $i$ th note of a half-state,  $i = 0, 1, \dots, n - 1$ . The function `state-note2datapoint-by-lookup` is applied.

### index-of-offtime-by-lookup

Started, last checked	1/9/2010, 1/9/2010
Location	Realising states
Calls	nth-list-of-lists
Called by	state-note2datapoint-by-lookup
Comments/see also	index-of-offtime

Example:

```
(index-of-offtime-by-lookup
  3 28
  '(((1 (60 72 79 84 88) (60 67 71 74 76))
      (NIL NIL "C-63-1"
        ((0 35 45 1/2 1 1/2 0)
         (0 47 52 1/2 1 1/2 1)
         (0 54 56 1/2 0 1/2 2)
         (0 59 59 1/2 0 1/2 3)
         (0 63 61 1/2 0 1/2 4))))))
  ((3/2 NIL NIL)
   (NIL NIL "C-63-1" NIL))
  ((7/4 (54) (57))
   (-6 -3 "C-63-1"
    ((831/4 56 57 1/4 0 208 701))))
  ((2 (28 40 54 60 63) (42 49 57 60 62))
   (-26 -15 "C-63-1"
    ((208 30 42 2 1 209 702)
     (208 42 49 1 1 209 703)
     (208 56 57 1 0 209 704)
     (208 62 60 1 0 209 705)
     (208 65 62 1 0 209 706))))
  ((3 (28 40 52 61 64) (42 49 56 61 63))
```

```

      (0 0 "C-63-1"
        ((209 30 42 1 1 210 707)
         (209 42 49 1 1 210 708)
         (209 54 56 1 0 210 709)
         (209 63 61 1 0 210 710)
         (209 66 63 1 0 210 711))))))
' (1/2 1/4 1/4 1) 3)
--> 4

```

Given a starting index, a note-index and some half-states to search through, this function returns the index of the half-state where the note-number in question comes to an end.

### state-durations-by-beat

Started, last checked	1/9/2010, 1/9/2010
Location	Realising states
Calls	min-item, nth-list-of-lists
Called by	states2datapoints-by-lookup
Comments/see also	state-durations

Example:

```

(setq
 states
 '((((1 (12 7 5 4))
      (NIL NIL "C-63-1"
        ((0 35 45 1/2 1 1/2 0) (0 47 52 1/2 1 1/2 1)
         (0 54 56 1/2 0 1/2 2) (0 59 59 1/2 0 1/2 3)
         (0 63 61 1/2 0 1/2 4))))))
 ((3/2 "rest")
  (NIL NIL "C-63-1" NIL))
 ((7/4 NIL)
  (-6 -3 "C-63-1"
    ((831/4 56 57 1/4 0 208 701))))
 ((2 (12 14 6 3))
  (-26 -15 "C-63-1"
    ((208 30 42 1 1 209 702)
     (208 42 49 1 1 209 703)
     (208 56 57 1 0 209 704)
     (208 62 60 1 0 209 705)

```

```

        (208 65 62 1 0 209 706))))
((3 (12 12 9 3))
 (0 0 "C-63-1"
  ((209 30 42 1 1 210 707)
   (209 42 49 1 1 210 708)
   (209 54 56 1 0 210 709)
   (209 63 61 1 0 210 710)
   (209 66 63 1 0 210 711))))
((1 (12 16 6 4))
 (0 0 "C-63-1"
  ((216 30 42 1 1 217 740)
   (216 42 49 1 1 217 741)
   (216 58 58 1 0 217 742)
   (216 64 62 1 0 217 743)
   (216 68 64 1 0 217 744))))
((2 (5 4 3))
 (19 11 "C-63-1"
  ((43 56 57 1 1 44 195) (43 61 60 1 1 44 196)
   (43 65 62 1/2 0 87/2 197)
   (43 68 64 1 1 44 198))))
((5/2 (5 4 8 4))
 (0 0 "C-63-1"
  ((25 54 56 1 1 26 101) (25 59 59 1 1 26 102)
   (25 63 61 1 1 26 103)
   (51/2 71 66 1/2 0 26 105)
   (51/2 75 68 1/2 0 26 106))))
((3 (3))
 (19 11 "C-63-1"
  ((230 73 67 3/4 0 923/4 809)
   (230 76 69 3/4 0 923/4 810))))
((7/2 (4))
 (3 2 "C-67-1"
  ((41/2 72 67 1/2 0 21 94)
   (41/2 76 69 1/2 0 21 95))))))
(state-durations-by-beat states 3)
--> (1/2 1/4 1/4 1 1 1 1/2 1/2 1/2)

```

This function takes a list of states as its argument, and returns a list containing the duration of each state. It is a little more involved than the function `state-durations`, because of the nature of the beat-spacing states.

**state-note2datapoint-by-lookup**

Started, last checked	1/9/2010, 1/9/2010
Location	Realising states
Calls	index-of-offtime-by-lookup
Called by	half-state2datapoints-by-lookup
Comments/see also	state-note2datapoint

Example:

```
(setq
 half-states
 '(((1 (60 72 79 84 88) (60 67 71 74 76))
      (NIL NIL "C-63-1"
        ((0 35 45 1/2 1 1/2 0)
         (0 47 52 1/2 1 1/2 1)
         (0 54 56 1/2 0 1/2 2)
         (0 59 59 1/2 0 1/2 3)
         (0 63 61 1/2 0 1/2 4))))
      ((3/2 NIL NIL)
       (NIL NIL "C-63-1" NIL))
      ((7/4 (54) (57))
       (-6 -3 "C-63-1"
        ((831/4 56 57 1/4 0 208 701))))
      ((2 (28 40 54 60 63) (42 49 57 60 62))
       (-26 -15 "C-63-1"
        ((208 30 42 1 1 209 702)
         (208 42 49 1 1 209 703)
         (208 56 57 1 0 209 704)
         (208 62 60 1 0 209 705)
         (208 65 62 1 0 209 706))))
      ((3 (28 40 52 61 64) (42 49 56 61 63))
       (0 0 "C-63-1"
        ((209 30 42 1 1 210 707)
         (209 42 49 1 1 210 708)
         (209 54 56 1 0 210 709)
         (209 63 61 1 0 210 710)
         (209 66 63 1 0 210 711))))
      ((1 (28 40 56 62 66) (42 49 58 62 64))
       (0 0 "C-63-1"
        ((216 30 42 1 1 217 740))
```

```

      (216 42 49 1 1 217 741)
      (216 58 58 1 0 217 742)
      (216 64 62 1 0 217 743)
      (216 68 64 1 0 217 744))))
((2 (47 52 56 59) (53 56 58 60))
 (19 11 "C-63-1"
  ((43 56 57 1 1 44 195) (43 61 60 1 1 44 196)
   (43 65 62 1/2 0 87/2 197)
   (43 68 64 1 1 44 198))))
((5/2 (47 52 56 64 68) (53 56 58 63 65))
 (0 0 "C-63-1"
  ((25 54 56 1 1 26 101) (25 59 59 1 1 26 102)
   (25 63 61 1 1 26 103)
   (51/2 71 66 1/2 0 26 105)
   (51/2 75 68 1/2 0 26 106))))
((3 (66 69) (64 66))
 (19 11 "C-63-1"
  ((230 73 67 3/4 0 923/4 809)
   (230 76 69 3/4 0 923/4 810))))
((7/2 (69 73) (66 68))
 (3 2 "C-67-1"
  ((41/2 72 67 1/2 0 21 94)
   (41/2 76 69 1/2 0 21 95))))))
(state-note2datapoint-by-lookup
 4 0 half-states '(1/2 1/4 1/4 1 1 1 1/2 1/2 1/2 1/2)
 '(0 1/2 3/4 1 2 3 4 9/2 5 11/2 6))
--> (0 88 76 1/2 0)

```

The  $i$ th note of the  $j$ th half-state is transformed into a so-called ‘datapoint’, meaning we find its ontime (the  $j$ th element of the partition points), its MIDI note number, morphetic pitch number, duration, and voice.

**states2datapoints-by-lookup**

Started, last checked	1/9/2010, 1/9/2010
Location	Realising states
Calls	create-MIDI&morphic-numbers, fibonacci-list, half-state2datapoints-by-lookup, state-durations-by-beat
Called by	
Comments/see also	states2datapoints, states2datapoints-by-lookup<-

Example:

```
(setq
 states
 '(((1 (12 7 5 4))
  (NIL NIL "C-63-1"
   ((0 35 45 1/2 1 1/2 0) (0 47 52 1/2 1 1/2 1)
    (0 54 56 1/2 0 1/2 2) (0 59 59 1/2 0 1/2 3)
    (0 63 61 1/2 0 1/2 4))))))
 ((3/2 "rest")
  (NIL NIL "C-63-1" NIL))
 ((7/4 NIL)
  (-6 -3 "C-63-1"
   ((831/4 56 57 1/4 0 208 701))))
 ((2 (12 14 6 3))
  (-26 -15 "C-63-1"
   ((208 30 42 1 1 209 702)
    (208 42 49 1 1 209 703)
    (208 56 57 1 0 209 704)
    (208 62 60 1 0 209 705)
    (208 65 62 1 0 209 706))))
 ((3 (12 12 9 3))
  (0 0 "C-63-1"
   ((209 30 42 1 1 210 707)
    (209 42 49 1 1 210 708)
    (209 54 56 1 0 210 709)
    (209 63 61 1 0 210 710)
    (209 66 63 1 0 210 711))))
 ((1 (12 16 6 4))
```

```

(0 0 "C-63-1"
  ((216 30 42 1 1 217 740)
   (216 42 49 1 1 217 741)
   (216 58 58 1 0 217 742)
   (216 64 62 1 0 217 743)
   (216 68 64 1 0 217 744))))
((2 (5 4 3))
 (19 11 "C-63-1"
  ((43 56 57 1 1 44 195) (43 61 60 1 1 44 196)
   (43 65 62 1/2 0 87/2 197)
   (43 68 64 1 1 44 198))))
((5/2 (5 4 8 4))
 (0 0 "C-63-1"
  ((25 54 56 1 1 26 101) (25 59 59 1 1 26 102)
   (25 63 61 1 1 26 103)
   (51/2 71 66 1/2 0 26 105)
   (51/2 75 68 1/2 0 26 106))))
((3 (3))
 (19 11 "C-63-1"
  ((230 73 67 3/4 0 923/4 809)
   (230 76 69 3/4 0 923/4 810))))
((7/2 (4))
 (3 2 "C-67-1"
  ((41/2 72 67 1/2 0 21 94)
   (41/2 76 69 1/2 0 21 95))))))
(states2datapoints-by-lookup states 3 60 60)
--> ((0 60 60 1/2 1) (0 72 67 1/2 1) (0 79 71 1/2 0)
      (0 84 74 1/2 0) (0 88 76 1/2 0) (3/4 54 57 1/4 0)
      (1 28 42 1 1) (1 40 49 1 1) (1 54 57 1 0)
      (1 60 60 1 0) (1 63 62 1 0) (2 28 42 1 1)
      (2 40 49 1 1) (2 52 56 1 0) (2 61 61 1 0)
      (2 64 63 1 0) (3 28 42 1 1) (3 40 49 1 1)
      (3 56 58 1 0) (3 62 62 1 0) (3 66 64 1 0)
      (4 47 53 1 1) (4 52 56 1 1) (4 56 58 1/2 0)
      (4 59 60 1/2 1) (9/2 56 58 1/2 1)
      (9/2 64 63 1/2 0) (9/2 68 65 1/2 0)
      (5 66 64 1/2 0) (5 69 66 1 0)
      (11/2 73 68 1/2 0))

```

This function applies the function half-state2datapoint-by-lookup recursively to a list of states.



### 4.5.13 Realising states backwards

These functions are used to convert states generated using a backwards running random generation Markov chain (RGMC) into datapoints. The functions have similar versions in the files `realising-states.lisp` and `markov-compose.lisp`.

#### **create-MIDI&morphetic-numbers<-**

Started, last checked	1/9/2010, 1/9/2010
Location	Realising states backwards
Calls	add-to-list, nth-list-of-lists
Called by	states2datapoints-by-lookup<-
Comments/see also	create-MIDI&morphetic-numbers, create-MIDI-note-numbers

Example:

```
(setq
states<-
'(((3 NIL) (NIL NIL "C-6-2" ((285 61 60 3 0 288 6))))
((2 (5 3 9))
(17 10 "C-6-2"
((58 56 57 1 1 59 219) (58 61 60 1 1 59 220)
(58 64 62 1 1 59 221)
(58 73 67 3/2 0 119/2 222))))
((3/2 (3 9 14))
(7 4 "C-7-2"
((120 50 54 1 1 121 351) (120 53 56 1 1 121 352)
(120 62 61 1 1 121 353)
(241/2 76 69 1/2 0 121 355))))
((1 (3 9 15))
(0 0 "C-7-2"
((120 50 54 1 1 121 351) (120 53 56 1 1 121 352)
(120 62 61 1 1 121 353)
(120 77 70 1/2 0 241/2 354))))
((7/2 (3 6 15))
(-2 -1 "C-7-2"
((119 52 55 1 1 120 346) (119 55 57 1 1 120 347)
(119 61 60 1 1 120 348)
(239/2 76 69 1/2 0 120 350))))))
```

```

(create-MIDI&morphic-numbers<- states<- 57 58)
--> (((7/2 (35 38 44 59) (45 47 50 59))
      (-2 -1 "C-7-2"
        ((119 52 55 1 1 120 346)
         (119 55 57 1 1 120 347)
         (119 61 60 1 1 120 348)
         (239/2 76 69 1/2 0 120 350))))
      ((1 (33 36 45 60) (44 46 51 60))
       (0 0 "C-7-2"
        ((120 50 54 1 1 121 351)
         (120 53 56 1 1 121 352)
         (120 62 61 1 1 121 353)
         (120 77 70 1/2 0 241/2 354))))
      ((3/2 (33 36 45 59) (44 46 51 59))
       (7 4 "C-7-2"
        ((120 50 54 1 1 121 351)
         (120 53 56 1 1 121 352)
         (120 62 61 1 1 121 353)
         (241/2 76 69 1/2 0 121 355))))
      ((2 (40 45 48 57) (48 51 53 58))
       (17 10 "C-6-2"
        ((58 56 57 1 1 59 219) (58 61 60 1 1 59 220)
         (58 64 62 1 1 59 221)
         (58 73 67 3/2 0 119/2 222))))
      ((3 (57) (58))
       (NIL NIL "C-6-2" ((285 61 60 3 0 288 6)))))

```

This function is similar to the function `create-MIDI&morphic-numbers`. The difference is that states generated by a backwards-running Markov model are supplied as the argument, and the intervals between bass notes refer to states  $X_n$  and  $X_{n+1}$ , rather than  $X_n$  and  $X_{n-1}$ , so the unpacking proceeds differently. The states are reversed into temporal order at the end.

**states2datapoints-by-lookup<-**

Started, last checked	1/9/2010, 1/9/2010
Location	Realising states backwards
Calls	create-MIDI&morphetic-numbers<-, fibonacci-list, half-state2datapoints-by-lookup, state-durations-by-beat
Called by	
Comments/see also	states2datapoints, states2datapoints-by-lookup

Example:

```
(setq
states<-
'(((3 NIL) (NIL NIL "C-6-2" ((285 61 60 3 0 288 6))))
((2 (5 3 9))
(17 10 "C-6-2"
((58 56 57 1 1 59 219) (58 61 60 1 1 59 220)
(58 64 62 1 1 59 221)
(58 73 67 3/2 0 119/2 222))))
((3/2 (3 9 14))
(7 4 "C-7-2"
((120 50 54 1 1 121 351) (120 53 56 1 1 121 352)
(120 62 61 1 1 121 353)
(241/2 76 69 1/2 0 121 355))))
((1 (3 9 15))
(0 0 "C-7-2"
((120 50 54 1 1 121 351) (120 53 56 1 1 121 352)
(120 62 61 1 1 121 353)
(120 77 70 1/2 0 241/2 354))))
((7/2 (3 6 15))
(-2 -1 "C-7-2"
((119 52 55 1 1 120 346) (119 55 57 1 1 120 347)
(119 61 60 1 1 120 348)
(239/2 76 69 1/2 0 120 350))))))
(states2datapoints-by-lookup<- states<- 3 57 58)
--> ((0 35 45 1/2 1) (0 38 47 1/2 1) (0 44 50 1/2 1)
(0 59 59 1/2 0) (1/2 33 44 1 1) (1/2 36 46 1 1)
(1/2 45 51 2 1) (1/2 60 60 1/2 0) (1 59 59 1/2 0))
```

(3/2 40 48 1 1) (3/2 48 53 1 1) (3/2 57 58 4 0))

This function is very similar to the function `states2datapoints-by-lookup`. It applies the function `half-state2datapoint-by-lookup` recursively to a list of states generated by a backward-running Markov model.

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