

# Math Notes

chtunsw@gmail.com

# Contents

<b>1</b>	<b>Statistics</b>	<b>3</b>
1.1	Discrete Probability Distribution . . . . .	3
1.2	Continuous Probability Distribution . . . . .	3
1.2.1	Uniform Distribution . . . . .	3
1.2.2	Normal Distribution . . . . .	4

# 1 Statistics

## 1.1 Discrete Probability Distribution

Let  $X$  be a random variable with a finite number of finite outcomes  $x_1, x_2, \dots, x_n$  occurring with probabilities  $p_1, p_2, \dots, p_n$  respectively. The expectation of  $X$  is defined as

$$\mu = E[X] = \sum_{i=1}^n x_i p_i = x_1 p_1 + x_2 p_2 + \dots + x_n p_n$$

The variance of  $X$  is

$$\sigma^2 = Var(X) = \sum_{i=1}^n p_i \cdot (x_i - \mu)^2$$

For a collection of  $n$  equally likely values:

$$\mu = \frac{1}{n} \sum_{i=1}^n x_i$$

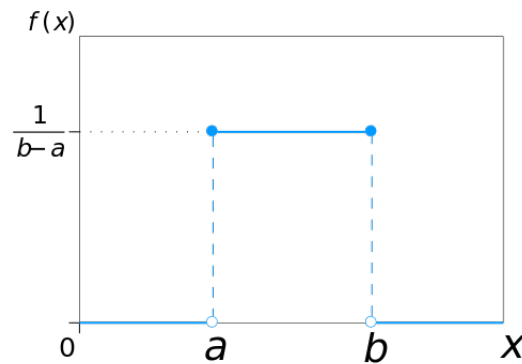
$$\sigma^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \mu)^2$$

## 1.2 Continuous Probability Distribution

If the random variable  $X$  has a probability density function  $f(x)$ , and  $F(x)$  is the corresponding cumulative distribution function, then

$$\mu = \int_{\mathbb{R}} x f(x) dx = \int_{\mathbb{R}} x dF(x)$$
$$\sigma^2 = \int_{\mathbb{R}} (x - \mu)^2 f(x) dx$$

### 1.2.1 Uniform Distribution

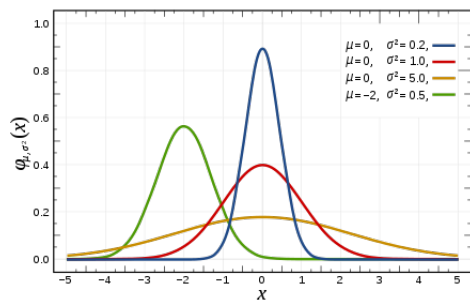


$$f(x) = \begin{cases} \frac{1}{b-a} & \text{for } a \leq x \leq b, \\ 0 & \text{for } x < a \text{ or } x > b \end{cases}$$

$$\mu = \frac{1}{2}(a + b)$$

$$\sigma^2 = \frac{1}{12}(b - a)^2$$

### 1.2.2 Normal Distribution



$$f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}$$