March 6, 2022

1 Question 3: Outlier Detection (10 points)

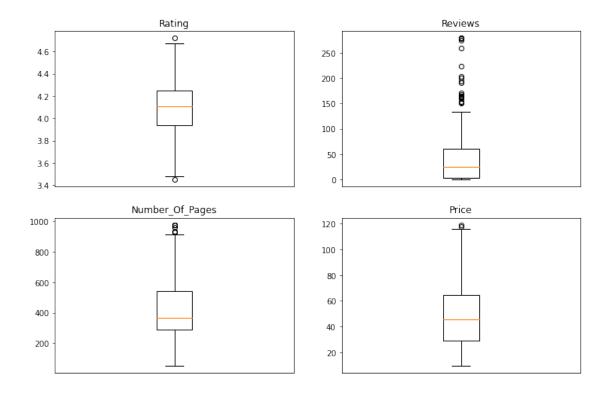
Chenran Ning (cn257)

```
[1]: import numpy as np
      import pandas as pd
      import matplotlib.pyplot as plt
      import seaborn as sns
[21]: # read data
      df = pd.read_csv("prog_book.csv", thousands=',')
      display(df)
          Rating
                   Reviews
                                                                     Book_title \
     0
             4.17
                      3829
                                                          The Elements of Style
             4.01
                      1406
                                 The Information: A History, a Theory, a Flood
     1
     2
             3.33
                                  Responsive Web Design Overview For Beginners
                         0
     3
             3.97
                            Ghost in the Wires: My Adventures as the World...
                      1658
     4
             4.06
                      1325
                                                               How Google Works
             •••
     266
             3.76
                             3D Game Engine Architecture: Engineering Real-...
             3.94
                        22
                                           An Introduction to Database Systems
     267
     268
             4.49
                        36
                            The Art of Computer Programming, Volumes 1-3 B...
     269
             4.77
                         4
                            The Art of Computer Programming, Volumes 1-4a ...
     270
             3.84
                         5
                                         A Discipline for Software Engineering
                                                   Description Number_Of_Pages \
     0
          This style manual offers practical advice on i...
                                                                           105
     1
          James Gleick, the author of the best sellers C...
                                                                           527
          In Responsive Web Design Overview For Beginner...
     2
                                                                            50
     3
          If they were a hall of fame or shame for compu...
                                                                           393
     4
          Both Eric Schmidt and Jonathan Rosenberg came ...
                                                                           305
     266
          Dave Eberly's 3D Game Engine Design was the fi...
                                                                           752
          Continuing in the eighth edition, An Introduct...
     267
                                                                          1040
     268
          Knuth's classic work has been widely acclaimed...
                                                                           896
     269
           "The bible of all fundamental algorithms and t...
                                                                          3168
     270
          Designed to help individual programmers develo...
                                                                           789
```

```
Price
                      Туре
0
                 Hardcover
                              9.323529
                             11.000000
1
                 Hardcover
2
           Kindle Edition 11.267647
3
                 Hardcover 12.873529
           Kindle Edition 13.164706
4
. .
                 Hardcover 203.108823
266
267
                 Paperback 212.097059
268
    Boxed Set - Hardcover 220.385294
269
                 Hardcover 220.385294
270
                 Hardcover 235.650000
[271 rows x 7 columns]
```

1.1 Task 1: Univariate Outlier detection (4 points)

```
[22]: detection_rows = ["Rating", "Reviews", "Number_Of_Pages", "Price"]
      def outlier detection(df, name):
          data = df[[name]].to_numpy()
          # finding the 1st quartile
          q1 = np.quantile(data, 0.25)
          # finding the 3rd quartile
          q3 = np.quantile(data, 0.75)
          med = np.median(data)
          # finding the iqr region
          iqr = q3 - q1
          # finding upper and lower whiskers
          upper_bound = q3 + (1.5 * iqr)
          lower_bound = q1 - (1.5 * iqr)
            print(iqr, upper bound, lower bound)
          # boxplot of data within the whisker
          data = data[(data >= lower_bound) & (data <= upper_bound)]</pre>
          plt.boxplot(data)
          plt.xticks([])
          plt.title(name)
      plt.figure(figsize = (12,8))
      i = 1
      for name in detection_rows:
          plt.subplot(2,2,i)
          i += 1
          outlier_detection(df, name)
      # plt.show()
```



1.2 Task 2: Multivariate Outlier detection (6 points)

1.2.1 bivariate analysis on all possible pairs of the above features and identify any outliers

features = ["Rating", "Reviews", "Number_Of_Pages", "Price", "Type_category"]

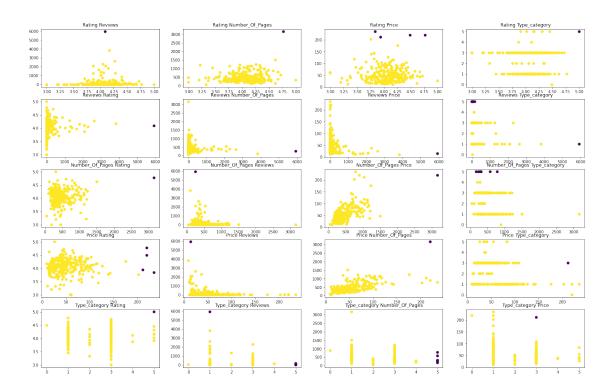
```
[118]: from sklearn.cluster import DBSCAN
    from sklearn.preprocessing import MinMaxScaler, RobustScaler

df["Type_category"] = df["Type"].astype('category').cat.codes
    features = ["Rating", "Reviews", "Number_Of_Pages", "Price", "Type_category"]
    i = 1
    j = 0
    plt.figure(figsize=(25,16))

outliers = {}

for feature1 in features:
    if feature2 in features:
        if feature1 == feature2:
            continue
        plt.subplot(5,4,i)
        i += 1
```

```
combined_feature = df[[feature1, feature2]].to_numpy()
        scaled_features = combined_feature.copy()
        # scale to 0.1
        scaler1 = MinMaxScaler()
        scaler1.fit(scaled_features[:,0].reshape(-1, 1))
        scaled_features[:,0] = scaler1.transform(scaled_features[:,0].
\rightarrowreshape(-1, 1)).reshape(-1)
        scaler2 = MinMaxScaler()
        scaler2.fit(scaled_features[:,1].reshape(-1, 1))
        scaled_features[:,1] = scaler2.transform(scaled_features[:,1].
 \rightarrowreshape(-1, 1)).reshape(-1)
        clustering = DBSCAN(eps=0.3, min_samples=10).fit(scaled_features)
        labels = clustering.labels_
        title = feature1 + " " + feature2
        indexs = np.array(np.where(labels < 0)).reshape(-1)</pre>
        out = np.array(combined_feature[indexs])
        out = pd.DataFrame(data = out, index = indexs, columns = [feature1,__
→feature2])
        outliers[title] = out
        plt.title(title)
        plt.scatter(combined_feature[:,0], combined_feature[:,1], c = labels)
plt.show()
```



```
[119]: # print the index and value of outliers

print("Outlier indexs and values")
for title, outlier in outliers.items():
    print(title + " : ")
    display(outlier)
```

Outlier indexs and values Rating Reviews :

Rating Reviews 6 4.09 5938.0

Rating Number_Of_Pages :

Rating Number_Of_Pages 269 4.77 3168.0

Rating Price :

Rating Price 267 3.94 212.097059 268 4.49 220.385294 269 4.77 220.385294 270 3.84 235.650000

Rating Type_category :

Rating Type_category 54 5.0 5.0

Reviews Rating:

Reviews Rating 6 5938.0 4.09

Reviews Number_Of_Pages :

Reviews Number_Of_Pages 6 5938 256

Reviews Price :

Reviews Price 6 5938.0 14.232353

Reviews Type_category :

	Reviews	Type_category
6	5938	1
54	0	5
78	33	5
88	161	5
107	18	5
166	57	5
228	88	5
229	3	5

Number_Of_Pages Rating :

Number_Of_Pages Rating 269 3168.0 4.77

Number_Of_Pages Reviews :

Number_Of_Pages Reviews 6 256 5938

Number_Of_Pages Price :

Number_Of_Pages Price 269 3168.0 220.385294

Number_Of_Pages Type_category :

	Number_Of_Pages	Type_category
54	317	5
78	237	5
88	176	5
107	320	5
166	283	5
228	787	5
229	582	5

Price Rating:

Price Rating 267 212.097059 3.94 268 220.385294 4.49 269 220.385294 4.77 270 235.650000 3.84

Price Reviews :

Price Reviews 6 14.232353 5938.0

Price Number_Of_Pages :

Price Number_Of_Pages 269 220.385294 3168.0

Price Type_category :

Price Type_category 267 212.097059 3.0

Type_category Rating :

Type_category Rating 54 5.0 5.0

Type_category Reviews :

	_	
	Type_category	Reviews
6	1	5938
54	5	0
78	5	33
88	5	161
107	5	18
166	5	57
228	5	88
229	5	3

Type_category Number_Of_Pages :

	Type_category	Number_Of_Pages
54	5	317
78	5	237
88	5	176
107	5	320
166	5	283
228	5	787
229	5	582

Type_category Price :

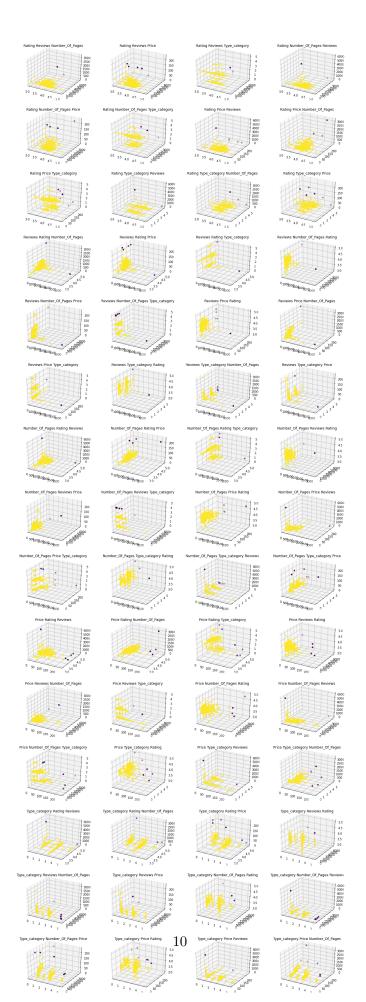
Type_category Price 267 3.0 212.097059

1.2.2 all combinations of three variables

```
[128]: df["Type_category"] = df["Type"].astype('category').cat.codes
       features = ["Rating", "Reviews", "Number_Of_Pages", "Price", "Type_category"]
       i = 1
       j = 0
       fig = plt.figure(figsize=(20,60))
       outliers = {}
       for feature1 in features:
           for feature2 in features:
               if feature1 == feature2:
                   continue
               for feature3 in features:
                   if feature2 == feature3 or feature3 == feature1:
                   ax = fig.add_subplot(15, 4, i, projection='3d')
                   combined_feature = df[[feature1, feature2, feature3]].to_numpy()
                   scaled_features = combined_feature.copy()
                   # scale to 0,1
                   scaler1 = MinMaxScaler()
                   scaler1.fit(scaled_features[:,0].reshape(-1, 1))
                   scaled_features[:,0] = scaler1.transform(scaled_features[:,0].
        \rightarrowreshape(-1, 1)).reshape(-1)
                   scaler2 = MinMaxScaler()
                   scaler2.fit(scaled_features[:,1].reshape(-1, 1))
                   scaled_features[:,1] = scaler2.transform(scaled_features[:,1].
        \rightarrowreshape(-1, 1)).reshape(-1)
                   scaler3 = MinMaxScaler()
                   scaler3.fit(scaled_features[:,2].reshape(-1, 1))
                   scaled_features[:,2] = scaler3.transform(scaled_features[:,2].
        \rightarrowreshape(-1, 1)).reshape(-1)
                   clustering = DBSCAN(eps=0.3, min_samples=10).fit(scaled_features)
                   labels = clustering.labels_
                   title = feature1 + " " + feature2 + " " + feature3
                   indexs = np.array(np.where(labels < 0)).reshape(-1)</pre>
                   out = np.array(combined_feature[indexs])
                   out = pd.DataFrame(data = out, index = indexs, columns = [feature1,_
        →feature2, feature3])
                   outliers[title] = out
```

```
ax.set_title(title)
    ax.scatter3D(combined_feature[:,0], combined_feature[:,1],
    combined_feature[:,2], c = labels)

plt.show()
```



```
[129]: print("Outlier indexs and values")
       for title, outlier in outliers.items():
           print(title + " : ")
           display(outlier)
      Outlier indexs and values
      Rating Reviews Number_Of_Pages :
           Rating Reviews Number_Of_Pages
      6
             4.09
                    5938.0
                                       256.0
      269
             4.77
                       4.0
                                      3168.0
      Rating Reviews Price :
           Rating Reviews
                                  Price
      6
             4.09
                    5938.0
                             14.232353
             3.94
      267
                      22.0 212.097059
             4.49
                      36.0 220.385294
      268
                       4.0 220.385294
             4.77
      269
      270
             3.84
                       5.0 235.650000
      Rating Reviews Type_category :
          Rating Reviews Type_category
            4.09
      6
                   5938.0
                                      1.0
      54
            5.00
                      0.0
                                      5.0
      Rating Number_Of_Pages Reviews :
           Rating Number_Of_Pages Reviews
             4.09
                             256.0
      6
                                      5938.0
             4.77
                            3168.0
      269
                                         4.0
      Rating Number_Of_Pages Price :
           Rating
                   Number_Of_Pages
                                          Price
                            1040.0
                                    212.097059
      267
             3.94
      268
             4.49
                             896.0
                                    220.385294
      269
             4.77
                            3168.0
                                    220.385294
      270
             3.84
                             789.0
                                    235.650000
      Rating Number_Of_Pages Type_category :
                   Number_Of_Pages Type_category
           Rating
      54
             5.00
                             317.0
                                               5.0
                             787.0
      228
             4.45
                                               5.0
             4.77
                            3168.0
      269
                                               1.0
      Rating Price Reviews :
           Rating
                        Price Reviews
```

4.09

6

14.232353

5938.0

```
      267
      3.94
      212.097059
      22.0

      268
      4.49
      220.385294
      36.0

      269
      4.77
      220.385294
      4.0

      270
      3.84
      235.650000
      5.0
```

Rating Price Number_Of_Pages :

	Rating	Price	Number_Of_Pages
267	3.94	212.097059	1040.0
268	4.49	220.385294	896.0
269	4.77	220.385294	3168.0
270	3.84	235.650000	789.0

Rating Price Type_category :

	Rating	Price	Type_category
54	5.00	25.855882	5.0
228	4.45	83.202941	5.0
267	3.94	212.097059	3.0
268	4.49	220.385294	0.0
269	4.77	220.385294	1.0
270	3.84	235.650000	1.0

Rating Type_category Reviews :

	Rating	Type_category	Reviews
6	4.09	1.0	5938.0
54	5.00	5.0	0.0

Rating Type_category Number_Of_Pages :

	Rating	Type_category	Number_Of_Pages
54	5.00	5.0	317.0
228	4.45	5.0	787.0
269	4.77	1.0	3168.0

Rating Type_category Price :

	Rating	Type_category	Price
54	5.00	5.0	25.855882
228	4.45	5.0	83.202941
267	3.94	3.0	212.097059
268	4.49	0.0	220.385294
269	4.77	1.0	220.385294
270	3.84	1.0	235.650000

Reviews Rating Number_Of_Pages :

	Reviews	Rating	Number_Of_Pages
6	5938.0	4.09	256.0
269	4.0	4.77	3168.0

Reviews Rating Price :

	Reviews	Rating	Price
6	5938.0	4.09	14.232353
267	22.0	3.94	212.097059
268	36.0	4.49	220.385294
269	4.0	4.77	220.385294
270	5.0	3.84	235.650000

Reviews Rating Type_category :

	Reviews	Rating	Type_category
6	5938.0	4.09	1.0
54	0.0	5.00	5.0

Reviews Number_Of_Pages Rating :

	Reviews	Number_Of_Pages	Rating
6	5938.0	256.0	4.09
269	4.0	3168.0	4.77

Reviews Number_Of_Pages Price :

	Reviews	Number_Of_Pages	Price
6	5938.0	256.0	14.232353
269	4.0	3168.0	220.385294

Reviews Number_Of_Pages Type_category :

	Reviews	Number_Of_Pages	Type_category
6	5938	256	1
54	0	317	5
78	33	237	5
88	161	176	5
107	18	320	5
166	57	283	5
228	88	787	5
229	3	582	5

Reviews Price Rating :

	Reviews	Price	Rating
6	5938.0	14.232353	4.09
267	22.0	212.097059	3.94
268	36.0	220.385294	4.49
269	4.0	220.385294	4.77
270	5.0	235.650000	3.84

Reviews Price Number_Of_Pages :

	Reviews	Price	Number_Of_Pages
6	5938.0	14.232353	256.0
269	4.0	220.385294	3168.0

Reviews Price Type_category :

Reviews Price Type_category 6 5938.0 14.232353 1.0 267 22.0 212.097059 3.0 Reviews Type_category Rating : Reviews Type_category Rating 5938.0 4.09 6 1.0 5.0 54 0.0 5.00 Reviews Type_category Number_Of_Pages : Type_category Number_Of_Pages Reviews 6 5938 256 1 54 0 5 317 78 33 5 237 88 161 5 176 18 5 107 320 166 57 5 283 228 88 5 787 229 3 5 582 Reviews Type_category Price : Reviews Type category Price 6 5938.0 1.0 14.232353 267 3.0 212.097059 22.0 Number_Of_Pages Rating Reviews : Number_Of_Pages Rating Reviews 256.0 4.09 6 5938.0 3168.0 4.77 269 4.0 Number_Of_Pages Rating Price : Number_Of_Pages Rating Price 267 1040.0 3.94 212.097059 268 896.0 4.49 220.385294 269 3168.0 4.77 220.385294 270 789.0 3.84 235.650000 Number_Of_Pages Rating Type_category : Number_Of_Pages Rating Type_category 54 317.0 5.00 5.0 228 787.0 4.45 5.0 269 3168.0 4.77 1.0 Number_Of_Pages Reviews Rating :

Number_Of_Pages

6

269

256.0

3168.0

Reviews Rating

4.09

4.77

5938.0

4.0

Number_Of_Pages Reviews Price :

	Number_Of_Pages	Reviews	Price
6	256.0	5938.0	14.232353
269	3168.0	4.0	220.385294

Number_Of_Pages Reviews Type_category :

	Number_Of_Pages	Reviews	Type_category
6	256	5938	1
54	317	0	5
78	237	33	5
88	176	161	5
107	320	18	5
166	283	57	5
228	787	88	5
229	582	3	5

Number_Of_Pages Price Rating :

	Number_Of_Pages	Price	Rating
267	1040.0	212.097059	3.94
268	896.0	220.385294	4.49
269	3168.0	220.385294	4.77
270	789.0	235.650000	3.84

Number_Of_Pages Price Reviews :

	Number_Uf_Pages	Price	Reviews
6	256.0	14.232353	5938.0
269	3168.0	220.385294	4.0

Number_Of_Pages Price Type_category :

	Number_Of_Pages	Price	Type_category
228	787.0	83.202941	5.0
229	582.0	83.211765	5.0
267	1040.0	212.097059	3.0
268	896.0	220.385294	0.0
269	3168.0	220.385294	1.0
270	789.0	235.650000	1.0

Number_Of_Pages Type_category Rating :

	Number_Of_Pages	Type_category	Rating
54	317.0	5.0	5.00
228	787.0	5.0	4.45
269	3168.0	1.0	4.77

Number_Of_Pages Type_category Reviews :

	Number_Of_Pages	Type_category	Reviews
6	256	1	5938
54	317	5	0

78	237	5	33
88	176	5	161
107	320	5	18
166	283	5	57
228	787	5	88
229	582	5	3

Number_Of_Pages Type_category Price :

	Number_Of_Pages	Type_category	Price
228	787.0	5.0	83.202941
229	582.0	5.0	83.211765
267	1040.0	3.0	212.097059
268	896.0	0.0	220.385294
269	3168.0	1.0	220.385294
270	789.0	1.0	235.650000

Price Rating Reviews :

	Price	Rating	Reviews
6	14.232353	4.09	5938.0
267	212.097059	3.94	22.0
268	220.385294	4.49	36.0
269	220.385294	4.77	4.0
270	235.650000	3.84	5.0

Price Rating Number_Of_Pages :

	Price	Rating	Number_Of_Pages
267	212.097059	3.94	1040.0
268	220.385294	4.49	896.0
269	220.385294	4.77	3168.0
270	235.650000	3.84	789.0

Price Rating Type_category :

	Price	Rating	Type_category
54	25.855882	5.00	5.0
228	83.202941	4.45	5.0
267	212.097059	3.94	3.0
268	220.385294	4.49	0.0
269	220.385294	4.77	1.0
270	235.650000	3.84	1.0

Price Reviews Rating :

	Price	Reviews	Rating
6	14.232353	5938.0	4.09
267	212.097059	22.0	3.94
268	220.385294	36.0	4.49
269	220.385294	4.0	4.77
270	235.650000	5.0	3.84

Price Reviews Number_Of_Pages :

	Price	Reviews	Number_Of_Pages
6	14.232353	5938.0	256.0
269	220.385294	4.0	3168.0

Price Reviews Type_category :

	Price	Reviews	Type_category
6	14.232353	5938.0	1.0
267	212.097059	22.0	3.0

Price Number_Of_Pages Rating :

	Price	Number_Of_Pages	Rating
267	212.097059	1040.0	3.94
268	220.385294	896.0	4.49
269	220.385294	3168.0	4.77
270	235.650000	789.0	3.84

Price Number_Of_Pages Reviews :

	Price	Number_Of_Pages	Reviews
6	14.232353	256.0	5938.0
269	220.385294	3168.0	4.0

Price Number_Of_Pages Type_category :

	Price	Number_Of_Pages	Type_category
228	83.202941	787.0	5.0
229	83.211765	582.0	5.0
267	212.097059	1040.0	3.0
268	220.385294	896.0	0.0
269	220.385294	3168.0	1.0
270	235.650000	789.0	1.0

Price Type_category Rating :

	Price	Type_category	Rating
54	25.855882	5.0	5.00
228	83.202941	5.0	4.45
267	212.097059	3.0	3.94
268	220.385294	0.0	4.49
269	220.385294	1.0	4.77
270	235.650000	1.0	3.84

Price Type_category Reviews :

	Price	Type_category	Reviews
6	14.232353	1.0	5938.0
267	212.097059	3.0	22.0

Price Type_category Number_Of_Pages :

	Price	Type_category	Number_Of_Pages
228	83.202941	5.0	787.0
229	83.211765	5.0	582.0
267	212.097059	3.0	1040.0
268	220.385294	0.0	896.0
269	220.385294	1.0	3168.0
270	235.650000	1.0	789.0

Type_category Rating Reviews :

	Type_category	Rating	Reviews
6	1.0	4.09	5938.0
54	5.0	5.00	0.0

Type_category Rating Number_Of_Pages :

	Type_category	Rating	Number_Of_Pages
54	5.0	5.00	317.0
228	5.0	4.45	787.0
269	1.0	4.77	3168.0

Type_category Rating Price :

	Type_category	Rating	Price
54	5.0	5.00	25.855882
228	5.0	4.45	83.202941
267	3.0	3.94	212.097059
268	0.0	4.49	220.385294
269	1.0	4.77	220.385294
270	1.0	3.84	235.650000

Type_category Reviews Rating :

	Type_category	Reviews	Rating
6	1.0	5938.0	4.09
54	5.0	0.0	5.00

Type_category Reviews Number_Of_Pages :

	Type_category	Reviews	Number_Of_Pages
6	1	5938	256
54	5	0	317
78	5	33	237
88	5	161	176
107	5	18	320
166	5	57	283
228	5	88	787
229	5	3	582

Type_category Reviews Price :

	Type_category	Reviews	Price
6	1.0	5938.0	14.232353
267	3.0	22.0	212.097059

Type_category Number_Of_Pages Rating :

	Type_category	Number_Of_Pages	Rating
54	5.0	317.0	5.00
228	5.0	787.0	4.45
269	1.0	3168.0	4.77

Type_category Number_Of_Pages Reviews :

	Type_category	Number_Of_Pages	Reviews
6	1	256	5938
54	5	317	0
78	5	237	33
88	5	176	161
107	5	320	18
166	5	283	57
228	5	787	88
229	5	582	3

Type_category Number_Of_Pages Price :

	Type_category	Number_Of_Pages	Price
228	5.0	787.0	83.202941
229	5.0	582.0	83.211765
267	3.0	1040.0	212.097059
268	0.0	896.0	220.385294
269	1.0	3168.0	220.385294
270	1.0	789.0	235.650000

Type_category Price Rating :

	Type_category	Price	Rating
54	5.0	25.855882	5.00
228	5.0	83.202941	4.45
267	3.0	212.097059	3.94
268	0.0	220.385294	4.49
269	1.0	220.385294	4.77
270	1.0	235.650000	3.84

Type_category Price Reviews :

	Type_category	Price	Reviews	
6	1.0	14.232353	5938.0	
267	3.0	212.097059	22.0	

Type_category Price Number_Of_Pages :

	Type_category	Price	Number_Of_Pages
228	5.0	83.202941	787.0
229	5.0	83.211765	582.0
267	3.0	212.097059	1040.0
268	0.0	220.385294	896.0

269	1.0	220.385294	3168.0
270	1.0	235.650000	789.0