

3.

$Ay=b$

若A可逆，等號兩邊同乘 $A^{-1}$ ：

$$\Rightarrow A^{-1} A y = A^{-1} b$$

$$\Rightarrow y = A^{-1} b$$

題目中  $M = \text{inv}(A) = A^{-1}$ ，則：

$$\Rightarrow y = M b$$

MATLAB演示：

```
>> A=round(10*rand(7));  
>> b=round(10*rand(7,1));
```

(1) 先算  $\det(A)$  看 A 是否可逆：A 可逆

```
>> det(A)  
  
ans =  
  
-4.9313e+04
```

(2) 算M

```
>> M=inv(A)  
  
M =  
  
-0.3150    1.3165   -0.9743   -0.8537   -0.0580    0.0415    0.8488  
 0.2707    0.1163   -0.0445   -0.1595    0.0017    0.0498   -0.1348  
-0.1230   -0.5834    0.3681    0.5101    0.0057   -0.1090   -0.0691  
-0.1018    0.9356   -0.7561   -0.8595   -0.0612    0.2466    0.6025  
 0.0634    1.0116   -0.6778   -0.9761    0.0343    0.1733    0.4678  
 0.0276   -1.6388    1.1147    1.4363    0.1042   -0.2144   -0.8401  
-0.0573   -0.4879    0.4592    0.4812   -0.0105   -0.0834   -0.3002
```

(3) 算出  $y = M * b$

```
>> y=M*b  
  
y =  
  
12.3576  
 1.2634  
-5.4126  
10.3076  
10.8908  
-16.1461  
-5.6623
```