



$$\begin{cases}
f = (m_0 + m_{\chi})\dot{\chi} + m_0 l_g \ddot{\theta} \cos \theta - m_0 l_g \dot{\theta}^* \sin \theta \\
0 = I \dot{\theta} + m_0 l_g \dot{\chi} \cos \theta + m_0 l_g \dot{\theta} - m_0 g l_g \sin \theta \\
\theta \sim 0, \dot{\theta} \sim 0
\end{cases}$$

I. Linearizing
$$\int_{0}^{\infty} f = (m_0 + m_x) \dot{x} + m_0 l_0 \dot{0}$$

$$0 = I \dot{0} + m_0 l_0 \dot{x} + m_0 l_0^2 \dot{0} - m_0 g l_0 \dot{0}$$

2.
$$\frac{\int aplace}{\int F(s)} = \frac{\int (m_0 + m_x) s^2}{\int (s)} \times \frac{\int (s) + m_0 l_g s^2}{\int (s)} \times \frac{\int (s) + m_0 l_g s^2}{\int (s)} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) - m_0 l_g s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) - m_0 l_g s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (m_0 + m_x) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (m_0 + m_x) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (m_0 + m_x) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{\int (s) + (I + m_0 l_g^2) s^2} \times \frac{\int (s) + (I + m_0 l_g^2) s^2}{$$

$$G(s) = \frac{\Theta(s)}{F(s)} = \frac{1}{\left[\frac{I(m_0 + m_x)}{m_0 l_g} + m_x l_g\right] s^2 + (m_0 + m_x) g}$$

4. Stability Analysis

Characteristic equation,
$$-\left[\frac{I(m_{\theta} + m_{\chi})}{m_{\theta} l_{g}} + m_{\chi} l_{g}\right] s^{2} + (m_{\theta} + m_{\chi}) g = 0$$

$$A = \left[\frac{I(m_{\theta} + m_{\chi})}{m_{\theta} l_{g}} + m_{\chi} l_{g}\right] > 0$$

$$B = (m_{\theta} + m_{\chi}) g > 0$$

Hurwitz stability criterion

$$[H] = \begin{bmatrix} 0 & 0 & 0 \\ -A & B & 0 \\ 0 & 0 & 0 \end{bmatrix} \qquad \begin{array}{c} \Delta_{i} = 0 \\ \Delta_{z} = 0 \\ \end{array} = \begin{array}{c} \Rightarrow \text{ Uns Jable system.} \end{array}$$