EE4C10 Analog Circuit Design Fundamentals

Homework Assignment II

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Simulation Files

Each question with simulation files will have their respective subfolder. Except for q6, the other questions will have separate subfolders for each sub questions.

Running the simulation files should be able to directly plot the graphs used (configured in the *.plt file). The folders for each question are arranged as follows after extracting:

spice			
-	q4		
		\mathbf{a}	
			step3
			step 4
		b	_
		e	
	q5		
		a	
		b	
	q6		

Problem 1

- (a) Overdrive voltage, $V_{\rm gt}$, for:
 - 1. M1

$$I_{D1} = \frac{\mu_n C_{OX}}{2} (\frac{W}{L})_1 (V_{GS_1} - V_{TH_1})^2 (1 + \lambda_1 V_{DS_1})$$

$$I_{D1} \approx \frac{\mu_n C_{OX}}{2} (\frac{W}{L})_1 (V_{gt_1})^2$$

$$V_{gt_1} \approx \sqrt{\frac{2I_{D_1}}{\mu_n C_{OX}} (\frac{L}{W})_1}$$

$$V_{gt_1} \approx 109.11 mV$$

2. M2

$$V_{gt_2} \approx \sqrt{\frac{2I_{D_2}}{\mu_p C_{OX}} (\frac{L}{W})_2}$$

$$V_{gt_2} \approx 377.96 mV$$

(b) Small-signal gain

$$g_{m1}V_{in} = \frac{-V_{out}}{r_{o1}//r_{o2}}$$

$$\frac{V_{out}}{V_{in}} = -g_{m1}(r_{o1}//r_{o2})$$

$$g_{m1} = \mu_n C_{OX}(\frac{W}{L})_1 V_{gt_1}$$
$$= 4.582mS$$

$$r_{o1} = \frac{1}{I_{D1}\lambda_n}$$
$$= 20k\Omega$$

$$r_{o2} = \frac{1}{I_{D2}\lambda_p}$$
$$= 40k\Omega$$

$$\frac{V_{out}}{V_{in}} \approx -61.09$$

(c) V_{out} output swing

For M_1 to be in saturation,

$$V_{DS1} \ge V_{gt1}$$
$$V_{out} \ge 0.109V$$

For M_2 to be in saturation,

$$V_{DS2} \ge V_{gt2}$$

$$V_{DD} - V_{out} \ge 0.377V$$

$$V_{out} \le 3.3V - 0.377V$$

$$V_{out} \le 2.923V$$

Swing of Vout,

$$0.109V < V_{out} < 2.923V$$

$$V_{out,pp} = 2.923V - 0.109V$$
$$= 2.814V$$

(d) The up-swing is limited by the PMOS leaving saturation, while the down swing is limited by the NMOS leaving saturation. The up-swing can be increased by connecting the base of the PMOS to the drain to form a diode connected structure, therefore $V_{\rm SD2}$ will always be larger than $V_{\rm gt2}$ by $V_{\rm TH2}$. As a result, $V_{\rm out}$ can be increased to $V_{\rm DD}$ - $V_{\rm TH2}$ without PMOS leaving saturation.

Problem 2

(a) For M1 to be 100mV from triode,

$$V_{DS1} = V_{GS1} - V_{TH,N} + 100mV$$
$$X = V_{in} - V_{TH,N} + 100mV$$

 $V_{\rm in}$ for M1 to be in saturation with $I_{\rm D1}$ of 0.35 mA,

$$I_{D1} = \frac{\mu_n C_{OX}}{2} (\frac{W}{L})_1 (V_{GS1} - V_{TH,N})^2$$

$$I_{D1} = \frac{\mu_n C_{OX}}{2} (\frac{W}{L})_1 (V_{in} - V_{TH,N})^2$$

$$V_{in} = \sqrt{\frac{2I_{D1}}{\mu_n C_{OX}}} (\frac{L}{W})_1 + V_{TH,N}$$

$$= 0.653V$$

$$X = \sqrt{\frac{2I_{D1}}{\mu_n C_{OX}} (\frac{L}{W})_1} + 100mV$$

$$\approx 0.253V$$

 $V_{\rm b}$ for M2 to be in saturation with $I_{\rm D2}$ of 0.35 mA,

$$\begin{split} I_{D2} &= \frac{\mu_n C_{OX}}{2} (\frac{W}{L})_2 (V_{GS2} - V_{TH,N})^2 \\ I_{D2} &= \frac{\mu_n C_{OX}}{2} (\frac{W}{L})_2 (V_b - X - V_{TH,N})^2 \\ V_b &= \sqrt{\frac{2I_{D2}}{\mu_n C_{OX}} (\frac{L}{W})_2} + X + V_{TH,N} \\ &\approx 0.906 V \end{split}$$

(b) Small-signal gain

$$G_m = \frac{g_{m1}(g_{m2}r_{o1}r_{o2} + r_{o1})}{g_{m2}r_{o1}r_{o2} + r_{o1} + r_{o2}}$$

$$\approx g_{m1}$$

$$R_{out} = (g_{m2}r_{o1}r_{o2} + r_{o1} + r_{o2})//R_d$$

Small-signal gain,

$$\frac{V_{out}}{V_{in}} = -G_m R_{out}$$

$$= -g_{m1}[(g_{m2}r_{o1}r_{o2} + r_{o1} + r_{o2})//R_d]$$

$$g_{m1} = \mu_n C_{OX}(\frac{W}{L})_1 (V_{GS1} - V_{TH,N})$$
$$= \mu_n C_{OX}(\frac{W}{L})_1 (V_{in} - V_{TH,N})$$
$$= 4.583mS$$

$$g_{m2} = \mu_n C_{OX}(\frac{W}{L})_2 (V_{GS2} - V_{TH,N})$$

$$\approx \mu_n C_{OX}(\frac{W}{L})_2 (V_b - X - V_{TH,N})$$

$$= 4.583mS$$

$$r_{o1} = \frac{1}{I_{D1}\lambda_n}$$

$$= 28.571k\Omega$$

$$r_{o2} = \frac{1}{I_{D2}\lambda_p}$$
$$= 28.571k\Omega$$

$$\frac{V_{out}}{V_{in}} \approx -22.88$$

(c) Assume V_b to be 1.65V, For M2 to be in saturation,

$$V_{out} - X \ge V_b - X - V_{TH,N}$$
$$V_{out} \ge 1.15V$$

When $I_D \geq 0$,

$$V_{out} \le V_{DD}$$
$$1.15V \le V_{out} \le 3.3V$$

$$V_{out,pp} = 2.15 V\,$$

(d) X_{pp} Gain of X,

$$\frac{X}{V_{in}} = \frac{-g_{m1}}{g_{m2} + \frac{1}{r_{o1}} + \frac{1}{r_{o2}}}$$

$$\approx \frac{-g_{m1}}{g_{m2}}$$

 X_{pp}

$$\frac{X}{V_{out}} = \frac{X}{V_{in}} \frac{V_{in}}{V_{out}}$$
$$= \frac{1}{22.88}$$

$$X_{pp} = 54.63 mV$$

Problem 3

- (a) Sketch of:
 - 1. Output voltage [[

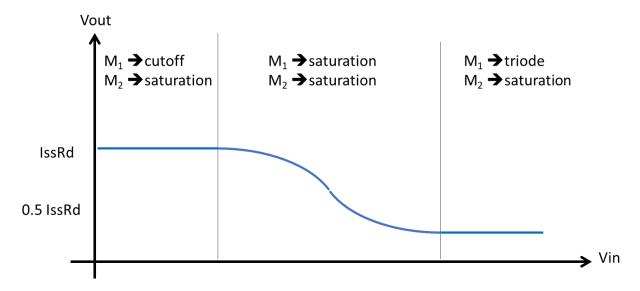
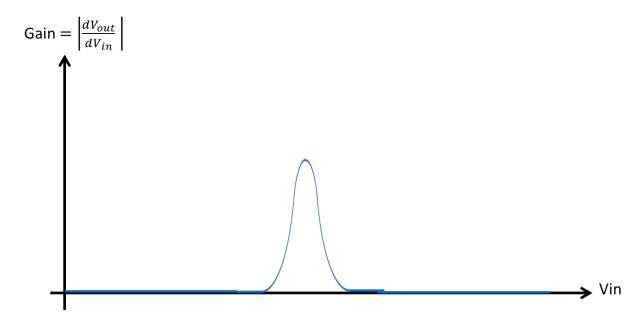


Figure 1: Output voltage sketch

2. Small-signal gain



 ${\bf Figure~2:~Small\text{-}signal~gain}$

(b) Small-signal model

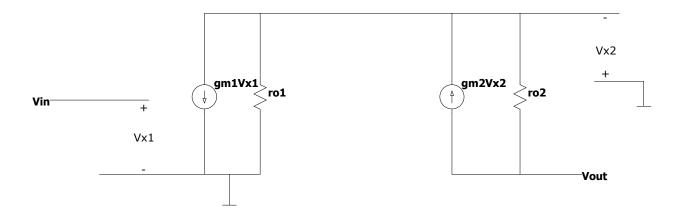


Figure 3: Small-signal model of folded-cascode stage

$$R_{out} = g_{m2}r_{o1}r_{o2} + r_{o1} + r_{o2}$$

$$\approx g_{m2}r_{o1}r_{o2}$$

$$G_m = \frac{-g_{m1}(g_{m2} + \frac{1}{r_{o1}})}{g_{m2} + \frac{1}{r_{o1}} + \frac{1}{r_{o2}}}$$

$$\approx -g_{m1}$$

$$\frac{V_{out}}{V_{in}} = g_{m1}g_{m2}r_{o1}r_{o2}$$

Problem 4

(a) Testbench

.lib 'C:\Program Files\LTC\LTspiceXVII\lib\cmp\log018.l' TT ;ac dec 10 1Meg 1G ;op ;step param Vb 0.5 2.5 0.25 .dc VIN 0 3.3 10m

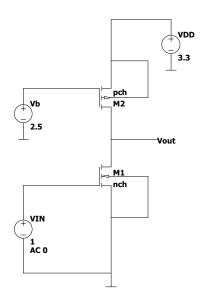


Figure 4: Testbench

$\rm V_{out}$ - $\rm V_{in}$ characteristics

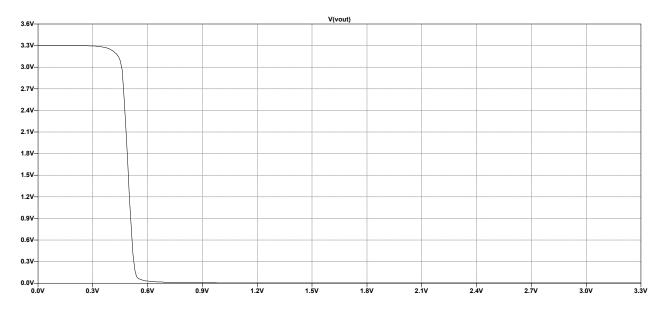


Figure 5: V_{out} - V_{in} characteristics

(b) Small-signal gain, $\frac{dV_{out}}{dV_{in}}$

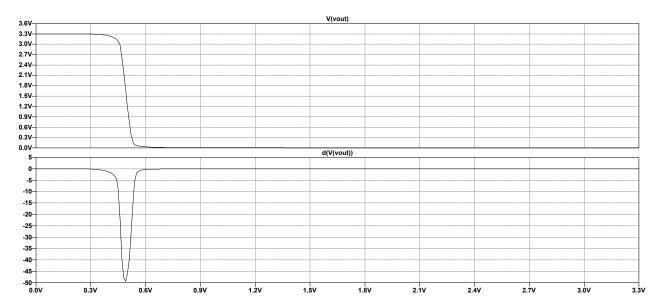


Figure 6: Small-signal gain, $\frac{dV_{out}}{dV_{in}}$

From figure 6 the gain when:

1.
$$V_{out} = 0.6 \text{ V}$$

 $\frac{dV_{out}}{dV_{in}} = -35.59$

$$\frac{dV_{out}}{dV_{in}} = -35.59$$

2.
$$V_{out} = 2.8 V$$

$$\begin{array}{r}
 dV_{in} & = 0.335 \\
 2. V_{out} & = 2.8 V \\
 \frac{dV_{out}}{dV_{in}} & = -32.77
 \end{array}$$

(c) From figure 6, the input voltage, V_{in} , for maximum gain, $max(|\frac{dV_{out}}{dV_{in}}|)$ is given to be:

$$max(|\frac{dV_{out}}{dV_{in}}|) = 50.07$$

$$V_{in} = 489mV$$

(d) Output voltage swing for gain of 1,

$$V_{out,max} = 3.24V$$

$$V_{out,min} = 56 mV \,$$

$$V_{out,pp} = 3.184V$$

Output peak to peak voltage

$$V_{out,pp} = 3.184V$$

(e) Small-signal voltage gain when:

1.
$$V_{out} = 0.6 V$$
, $V_{in} = 0.514 V$

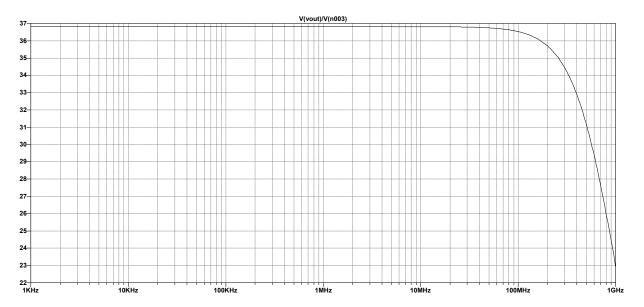


Figure 7: Small-signal gain, $|\frac{V_{out}}{V_{in}}|,\, \rm V_{out}=0.6~V,\, \rm V_{in}=0.514~V$

Gain = 36.82

$$2.\ V_{out}\,=\,2.8\ V,\ V_{in}\,=\,0.464\ V$$

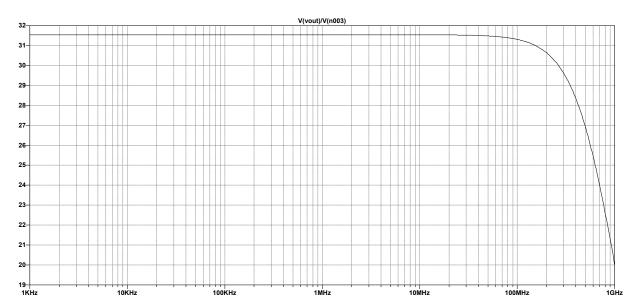


Figure 8: Small-signal gain, $|\frac{V_{out}}{V_{in}}|,\, \rm V_{out}\,=\,2.8~V,\, V_{in}\,=\,0.464~V$

Gain = 31.54

Problem 5

- (a) Procedure for designing V_b for M1 to be 100mV away from triode, $V_b = 0.825 \, V$, is determined by the following:
 - 1. Select an initial value V_b for M1 and M2 to be in saturation when $V_{in} > V_{TH1}$. In figure 9, $V_b = 1.5$ V. From the error logfile 10, $V_{DS1} > V_{GS1}$ V_{TH1} and $V_{DS2} > V_{GS2}$ V_{TH2} .



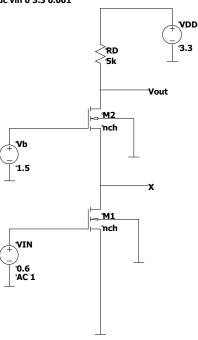


Figure 9: Testbench for Q5

```
Semiconductor Device Operating Points:
--- BSIM3 MOSFETS ---
                                     m1
Model:
Id:
                  nch.3
                                  nch.3
3.74e-04
                3.74e-04
Vgs:
Vds:
Vbs:
                                  6.00e-01
7.27e-01
                7.73e-01
7.05e-01
                7.27e-01
                                  0.00e+00
Vth:
Vdsat:
                                  4.97e-01
1.35e-01
                6.78e-01
                1.18e-01
Gm:
                4.21e-03
                                  4.42e-03
                1.29e-04
7.98e-04
                                  4.49e-05
1.27e-03
Gds:
Gmb
Cbd:
Cbs:
Cgsov:
                0.00e+00
                                  0.00e+00
                0.00e+00
6.59e-15
                                  0.00e+00
1.32e-14
Cgdov:
                6.59e-15
Cgbov:
dQgdVgb:
                3.18e-17
3.21e-14
                                  6.47e-17
1.00e-13
dQgdVdb:
dQgdVsb:
dQddVgb:
               -2.27e-14
-6.61e-15
                                 -7.78e-14
                                 -1.33e-14
dQddVdb:
                6.60e-15
                                  1.32e-14
dQddVsb:
dQbdVgb:
                2.09e-17
                                 9.01e-17
-1.24e-14
               -3.63e-15
dQbdVdb:
dQbdVsb:
               -2.22e-15
                                -1.44e-14
```

Figure 10: Semiconductor Device Operating Points

2. Doing a DC-sweep for I_{D1} - V_{in} , $V_{in} \approx 0.6V$ when $I_{D1} = 0.35$ mA.

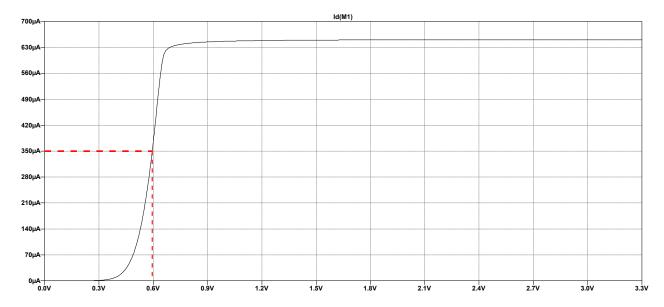


Figure 11: I_{D1} - V_{in}

3. From the operation point simulation int figure 10, V_{TH1} is determined to be 0.497V. For M1 to be 100mV from triode region,

$$V_x = V_{in} - V_{TH1} + 100mV$$

$$\approx 0.2V$$

4. DC-sweeping V_x - V_b and determining V_b for V_x = 0.2V. From the figure 12 , V_b = 0.825V.

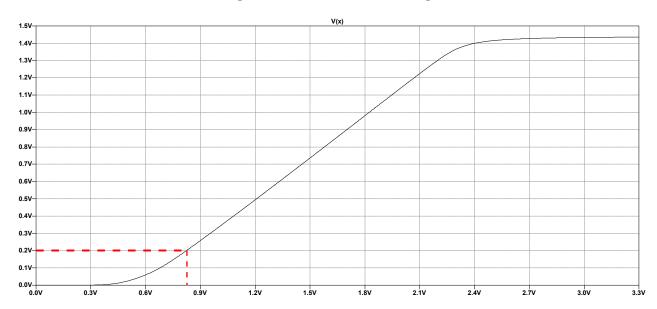


Figure 12: V_x - V_b

(b) $I_{\rm OUT}\text{-}V_{\rm OUT}$ when $V_{\rm IN}$ is fixed for $I_{\rm D1}=0.35~mA$

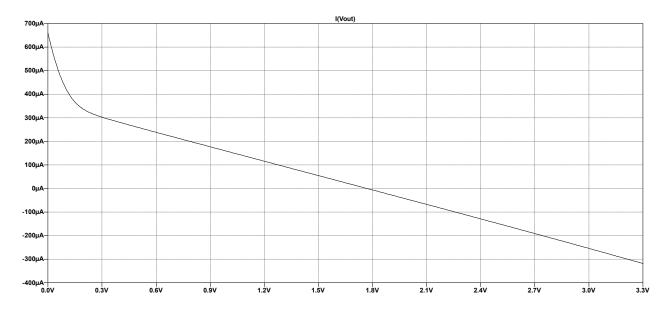


Figure 13: I_{OUT} - V_{OUT}

Problem 6

The output resistance, $R_{\rm out}$ is the reciprocal of the slope of $I_{\rm OUT}\mbox{-}V_{\rm OUT},$

$$R_{out} = (\frac{I_{OUT}}{V_{OUT}})^{-1}$$

The results are shown in figure 14,

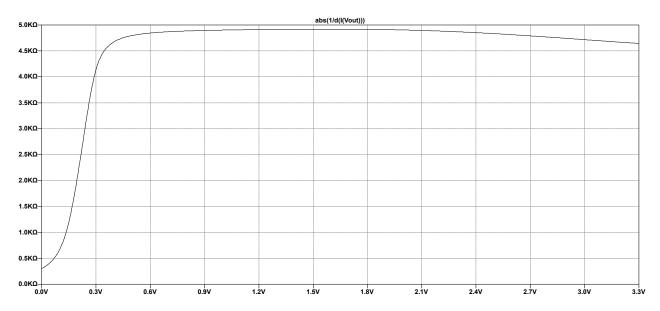


Figure 14: R_{OUT} - V_{OUT}

 $\begin{aligned} & From \ figure \ 15, \\ & max(R_{out}) = 4920 \ \Omega \\ & when, \\ & V_{out} = 1.53 \ V \end{aligned}$

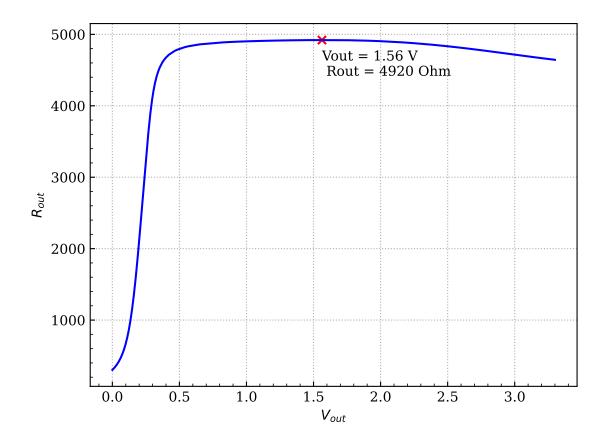


Figure 15: Maximum R_{out}