

6. We want to prove that the only prime triple is $3, 5, 7$.

Suppose there is another prime triple, say $m, m+2, m+4$ for some $m \in \mathbb{Z}$ and $m > 3$.

However, ~~so~~ from question 5, we proved that for any integer n , at least one of $n, n+2, n+4$ is divisible by 3.

Hence, $m, m+2, m+4$ must have at least one member divisible by 3, ~~this contradicts~~ i.e. one of them can be expressed in the form of $3k$ when $k > 1$ (since $m > 3$). This contradicts the fact that $m, m+2, m+4$ are primes.

So the only prime triple is $3, 5, 7$.