1. Using the number of vowels to detect ciphertext rectangles

I use the counting function to determine the matrix's rows and cols. (Same as quiz 2) As a result, this is a 11*7 matrix.

2. Using plaintext bigrams and trigrams to calculate conditional probabilities for Markov decision processing.

```
d3={}
d2={}
    markov():
def
    plain = plaintextref.translate({ord(c): None for c in string.whitespace})
#print(plain)
     for i in range(len(plain)-2):
         j=i+1
k=i+2
         temp=""
         temp+=plain[i]
         temp+=plain[j]
temp+=plain[k]
         if temp in d3:
             d3[temp]+=1
              d3[temp]=1
    for i in range(len(plain)-1):
j=i+1
         temp=""
         temp+=plain[i]
         temp+=plain[j]
         if temp in d2:
              d2[temp]+=1
              d2[temp]=1
```

I use the markov function to count the probabilities of 2 characters and 3 characters, then, I save them in dictionary d2 and d3.

```
strcol=[""]*m
ind=0
c=0
for t in text:
    if c==n:
        c=0
        ind+=1
    if t != " ":
        strcol[ind]+=t
        c+=1
for i in range(m):
    print(strcol[i])
firstcol = 2
seccol = 5
ndone = [0,1,2,3,4,5,6]
resultcol=[firstcol,seccol]
ndone.remove(firstcol)
ndone.remove(seccol)
```

In this section, I slice the ciphertext into strings of columns. The result is:

'EOEYEGTRNPS'

'ECEHHETYHSN'

'GNDDDDETOCR'

'AERAEMHTECS'

'EUSIARWKDRI'

'RNYARANUEYI'

'NTTCEIETUS'

Followed the hint, the first column should be 'GNDDDDETOCR' and the second column should be 'RNYARANUEYI'

3. Using MDP to recover columnar transposition ciphers

```
for i in range(2,m):
    maxprob=0
    choosecol=-1
    for j in ndone:
        probs=0
        for w in range(m):
char2=""
            char2 += strcol[firstcol][w]
            char2 += strcol[seccol][w]
            char3 = char2+strcol[j][w]
            if char2 not in d2 or char3 not in d3:
                probs+=math.log(26*(d3[char3]/d2[char2]))
        if probs>maxprob:
            maxprob=probs
            choosecol=j
    ndone.remove(choosecol)
    resultcol.append(choosecol)
    firstcol=seccol
    seccol=choosecol
plaintext=""
for i in range(n):
    for col in resultcol:
        plaintext+=strcol[col][i]
print(plaintext)
```

Every time I want to decide the next column, I run through the undone columns and count the total conditional probabilities of the column.

probs += math.log(26*(d3[char3]/d2[char2]))

Find the most appropriate column with the highest probability, remove it from the undone columns and redo this to find the next column.

Luckily, I find out the origin plaintext:

GREECEANNOUNCEDYESTERDAYITHADREACHEDAGREEMENTWITHTURKEYTOENDTHE CYPRUSCRISISNS