

AM207 Final Project

A dive into Bayesian Weather Modelling

Victor Lei

Institute for Applied Computational Science
52 Oxford Street
Cambridge, MA
vlei@g.harvard.edu

Leonhard Spiegelberg

Institute for Applied Computational Science
52 Oxford Street
Cambridge, MA
spiegelberg@g.harvard.edu

Charles Liu

Institute for Applied Computational Science
52 Oxford Street
Cambridge, MA
cliu02@g.harvard.edu

Vinay Subbiah

Institute for Applied Computational Science
52 Oxford Street
Cambridge, MA
vinaysubbiah@g.harvard.edu

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Abstract

Statistical weather modelling has a long tradition. In this project we apply different methods in a Bayesian context on historical weather data. Using a simplistic approach we implement and test Bayesian models based on a network topology (Bayesian Networks) and time series based models on weather measures like temperature, pressure or precipitation. In another modelling approach we investigate a hidden markov model on weather events like rain, snow or fog. Statistical Inference based on this models has a wide range of possible applications. In this project we try to infer values for either missing data points (i.e. when measurements are not sufficient) or for missing stations / points.

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1 Introduction

Traditional local and global weather modelling hugely relies on numerical simulations as well as statistical techniques. With the development and increasing popularity of Machine Learning algorithms in a Bayesian context, this project aims at serving as a study of techniques demonstrated along examples on how Bayesian techniques could be used for a data based approach in weather modelling.

Usually, weather data is collected at fixed weather stations that do not follow any particular pattern in terms of position or location. Hence, data is inherently spatially aware but not for every location data is available. Traditional approaches to infer missing data for specific locations rely either on numerical simulation results (and interpolating them) or on a local numerical simulation on a locally fine-grained grid. However, for many applications it is sufficient to use a statistical weather generator[1] which then can be used to infer a local distribution for weather parameters. One application of this could be for example to compute the risk of heavy rain for a location where no historical weather data is available. Another would be to actually use a statistical weather generator to construct initial boundary conditions of missing points that are then fed into a numerical model.

For this project we collected historical data of 18 stations from 1960-2015 around Boston from wunderground.com.



Figure 1: Illustration of the 18 stations which data has been used for this project with weather stations being located next to airports.

Since historical weather data is usually hard to get or hidden behind paywalls, though we secured a decent amount of variables we do not claim that our data base should be used for a real-world application. Instead, it serves more as a base for applying several techniques and investigating their feasibility. The first part of our study investigates the modelling of single weather measures demonstrated along precipitation whereas the second part focuses on a state-based approach for weather events.

2 Bayesian Networks

Due to its spatial awareness, a hierarchical structure based on independence is a natural candidate to model a single weather measure. Bayesian Networks have been successfully applied to model precipitation by using a combination of historical weather data and numerical simulation data [2].

2.1 Network construction

However, the question on how to construct the dependency graph which needs to be acyclic is non-trivial as it is a proven NP-hard problem. Thus, possible solutions often rely on greedy algorithms. In the context of weather modelling, dependency are usually inferred by a combination of manual dependencies obtained via domain knowledge and automated processing. As we do not possess any in-depth domain knowledge about weather dependencies we opted to push automatic network structure learning further by automating the whole process.

One of the most popular algorithms for structural learning of a Bayesian Network is the K2 algorithm. But to make it work, an initial ordering of the nodes (i.e. stations) is needed.

2.1.1 Initial Ordering

We assume that stations with a fewer distance are more likely to be dependent than stations that are farer away.



a. Minimum Spanning tree with euclidean Distance

b. Topological Ordering

Figure 2: Construction of an initial node order. Arrows denote a child-parent relation.

In a first step we construct a Minimum Spanning Tree (MST) with the euclidean distance used as edge weight (i.e. via Kruskal’s algorithm[3]). Using this MST we select a node (typically one that has many neighbors in the MST) and perform a Breadth First Search (BFS) to obtain a topological ordering which is then used as input for the K2 algorithm. It should be noted that neither the MST nor the topological ordering are unique. Running the algorithm several times to obtain a plausible ordering is therefore strongly encouraged. Furthermore, we see this ansatz as a practical approach to get an initial dependency layout which can then be manually refined if needed (cf. Figure 2).

2.1.2 K2 algorithm

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2.2 Inference

2.2.1 Direct Sampling

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2.2.2 Monte Carlo / Gibbs Sampling

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2.3 Application

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References

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