CHAPTER 4: LIST (2 HOURS)

CHAPTER 5: LINKED LIST (5 HOURS)

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LECTURER

LIST

- Introduction
- Static and dynamic List Structure
- Array Implementation of Lists
- Queue as a List

LINKED LIST

- Introduction
- Linked list as an ADT
- Dynamic implementation
- Insertion and deletion of node to and from a list
- Insertion and deletion and before nodes
- Linked stack and queues
- Doubly linked list and its advantages

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- A list is a collection of homogeneous set of elements or objects.
- If the size of list is fixed at compile time and do not grow or shrink at runtime then it is called static list however if the size of the list is not fixed at compile time and grow and shrink at runtime then it is called dynamic list.
- A list is said to be empty when it contains no elements
- The number of elements currently stored is called the length of the list.
- The beginning of the list is called head and the end of the list is called the tail.

STATIC IMPLEMENTATION OF LIST

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- Static implementation can be implemented using arrays.
- It is very simple method but it has static implementation.
- Once a size is declared, it cannot be change during the program execution.
- It is also not efficient for memory utilization.
- ► When array is declared, memory allocated is equal to the size of the array.
- The vacant space of array also occupies the memory space.
- In this cases, if we store fewer arguments than declared, the memory is wasted and if more elements are stored than declared, array cannot be expanded.
- It is suitable only when exact numbers of elements are to be stored.

SOME COMMON OPERATIONS PERFORMED ON STATIC LIST

5 Creating of an array

- Inserting new element at required position
- Deletion of any element
- Modification of any element
- Traversing of an array
- Merging of arrays

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Let A be an LIST of array implementation and it has n elements then it satisfied the following operations:

- CREATE (A) : Create an array A
- ► INSERT (A,X): Insert an element X into an array A in any location
- DELETE (A,X): Delete an element X from an array A
- MODIFY (A,X,Y): Modify element X by Y of an array A
- TRAVERSE (A): Access all elements of an array A
- ► MERGE (A,B): Merging elements of A and B into a third array C.

Thus by using a one dimensional array we can perform above operations thus an array acts as an ADT.

INSERTION OF AN ELEMENT IN ONE-DIMENSIONAL ARRAY

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Insertion at the end of an array:

Providing the memory space allocated for the array enough to accommodate the additional; element can easily do insertion at the end of an array.

Insertion at the required position

- For inserting the element at required position, element must be moved downwards to new locations to accommodate the new element and keep the order of the elements.
- For inserting an element into a linear array **insert**(a, len, pos, num) where a is a linear array, len be total number of elements with an array, pos is the position at which number num will be inserted.

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Algorithm to insert new element in a list:

6. end

- 1. [initialize the value of i] set **i=len-1**
- 2. Repeat for **i**= **len-1** down to **pos**

[shift the elements right by 1 position]

$$Set a[i+1] = a [i]$$

[end of loop]

3. [insert the element at required position]

$$Set a[pos] = num$$

- 4. [reset len] set len=len+1
- 5. Display the new list of arrays

DELETION OF AN ELEMENT FROM ONE-DIMENSIONAL ARRAY

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- Deleting an element at the end of an array presents no difficulties, but deleting element somewhere in the middle of the array would require to shift all the elements to fill the space emptied by the deletion of the element, then the element following it were moved left by one location.
- **num** is the item deleted and **len** is the no of element in the array. **pos** is the position from where the data item is deleted.

a. Shift elements 1 position left

b. Set a[j] = a[j+1]

Algorithm:

- $1. \quad \text{Set num} = \mathbf{a}[\mathbf{pos}]$
- 2. Repeat for j = pos to len-1

- 3. Reset len=len-1
- 4. Display the new list of element of array
- 5. end

- In static implementation of memory allocation, we cannot alter (increase or decrease) the size of an array and the memory allocation is fixed.
- So we have to adopt an alternative strategy to allocate memory only when it is required.
- There is a special data structure called linked list that provides a more flexible storage system and it does not required the use of array.
- The advantage of a list over an array occurs when it is necessary to insert or delete an element in the middle of a group of other elements.

- A linked list is a linear collection of specially designed data structure, called **nodes**, linked to one another by means of **pointer**.
- Each node is divided into 2 parts: the first part contains information of the element and the second part contains address of next node in the link list.



- The left part of each node contains the data items and the right part represents the address of the next node.
- The next pointer of the last node contains a special value, called the NULL pointer, which does not point to any address of the node.

LINKED LIST

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- That is NULL pointer indicates the end of linked list.
- START pointer will hold the address of the 1st node in the list START = NULL if there is no list (i.e. NULL list or empty list)

REPRESENTATION OF LINKED LIST:

Suppose we want to store a list of integer numbers using linked list. Then it can be schematically represented as

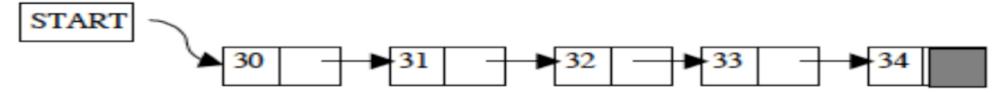


Figure 5: Representation of Linked List

We can declare linear linked list as follows

```
struct Node{
   int data; //instead of data we also use info
   struct Node *Next; //instead of Next we also use link
};
typedef struct Node *NODE;
```

ADVANTAGES AND DISADVANTAGES OF LINKED LIST

13 ADVANTAGES:

- Link list are dynamic data structure. That is they can grow or shrink during the execution of a program.
- Efficient memory utilization: in linked list memory is not pre-allocated. Memory is allocated whenever it is required. And it is deallocated when it is not needed.
- Insertion and deletion are easier and efficient. Linked list provides flexibility in inserting a data item at a specified position and deletion of a data item from the given position.
- Many complex applications can be easily carried out with linked list.

DISADVANTAGES:

- More memory: to store an integer number, a node with integer data and address field is allocated. That is more memory space is needed.
- Access to any arbitrary data item is little bit cumbersome and also time consuming.

OPERATIONS ON LINKED LIST

- The primitive operations performed on linked list is as follows:
 - Creation :
 - It is used to create a linked list.
 - Once a linked list is created with one node, insertion operation can be used to add more elements in a node.

Insertion:

- It is used to insert a new node at any specified location in the linked list.
- A new node may be inserted
 - ► At the beginning of the linked list
 - At the end of the linked list
 - At any specified position in between in a linked list

Deletion:

it is used to delete an item (or node) from the linked list.

- A node may ne deleted from the
 - Beginning of a linked list
 - End of a linked list
 - Specified location of the linked list
- **Traversing:**
 - It is the process of going through all the nodes from one end to another end of a linked list.
- Concatenation:
 - It is the process appending the second list to the end of the first list.
- Searching:
 - It is the process of finding the location of searched item.

TYPES OF LINKED LIST

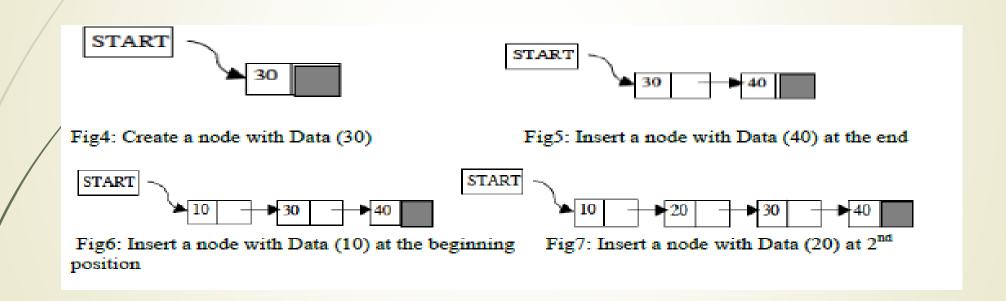
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Following are the types of Linked list depending upon the arrangements of the nodes.

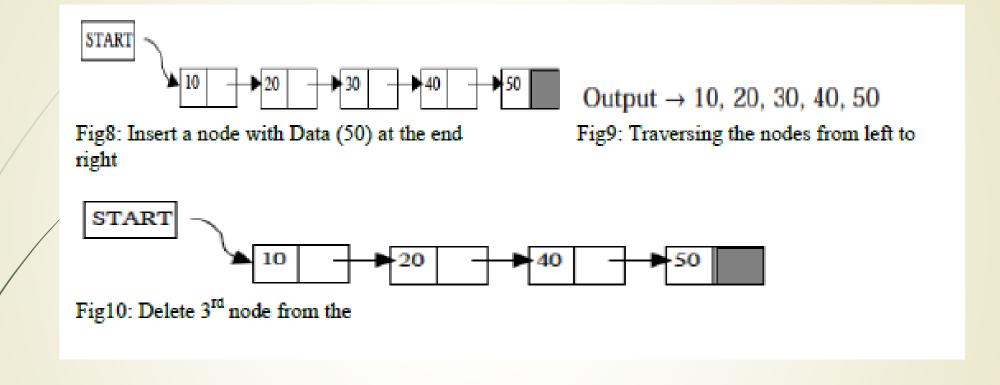
- Singly Linked List
- Doubly Linked List
- Circular Linked List
 - Circular singly linked list
 - Circular doubly linked list.

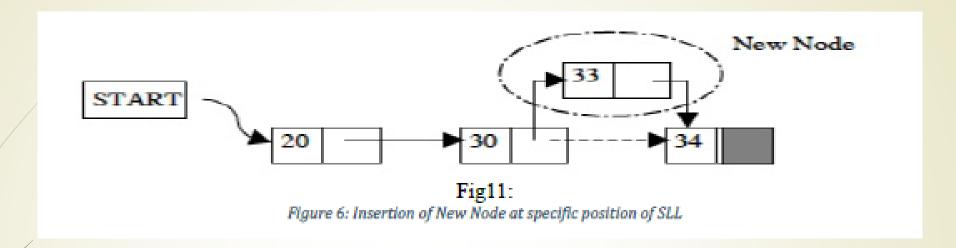
SINGLY LINKED LIST

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 - All the nodes in a singly linked list are arranged sequentially by linking with pointer.
 - A singly linked list can grow or shrink, because it is a dynamic data structure.
 - The following figure explains the different operations on singly linked list.



SINGLY LINKED LIST





Suppose START is the first position in linked list. Let DATA be the element to be inserted in the new node.

POS is the position where the new node is to be inserted. TEMP is a temporary pointer to hold the node address.

20 Insert a Node at the beginning of Linked List:

- 1. Input DATA to be inserted
- 2. Create a NewNode
- 3. NewNode → DATA = DATA
- 4. If(START == NULL)
 - $a. NewNode \rightarrow next = NULL$
- **5**. Else
 - a. NewNode \rightarrow next = START
- 6. START = NewNode
- 7. Exit

21 Insert a Node at the end of Linked List:

c. $TEMP \rightarrow next = NewNode$

- 1. Input DATA to be inserted
- 2. Create a NewNode
- 3. NewNode \rightarrow DATA = DATA
- 4. NewNode → next = NULL
- 5. If (START == NULL)
 - a. START = NewNode
- 6. Else
 - a. TEMP = START
 - b. While (TEMP→ next!=NULL)
 - i. TEMP=TEMP→next.

7. Exit

22 Insert a Node at any specified position of Linked

List:

- 1. Input DATA and POS to be inserted
- 2. Initialize TEMP=START and i=0
- 3. Repeat the step 3 while (i<POS-1)
 - \angle TEMP = TEMP \rightarrow next
 - b. If(TEMP == NULL)
 - a. Display "Node in the list less than the position"
 - b. Exit
 - c. i=i+1
- 4. Create a NewNode

- 5. NewNode → DATA = DATA
- 6. NewNode \rightarrow next=TEMP \rightarrow next
- 7. TEMP \rightarrow next =NewNode
- 8. Exit

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Suppose START is the address of the first node in the linked list.

- 1. If (START ==NULL)
 - a. Display "The list is Empty"
 - b. Exit
- 2. Initialize TEMP = START
- 3. Repeat the step 4 and 5 until (TEMP==NULL)
- ✓ Display "TEMP→DATA"
- 5. TEMP=TEMP \rightarrow next
- 6. Exit

ALGORITHM FOR DELETING A NODE

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Suppose START is the first position in linked list.

Let DATA be the element to be deleted. TEMP,

HOLD is a temporary pointer to hold the node address.

Deletion from the beginning:

- 1. If (START==NULL)
 - a. Display "List is empty"
 - b. exit
- 2. Else
 - a. HOLD=START
 - b. START=START→next

- c. Display the deleted node as HOLD→DATA
- d. Set free the node HOLD, which is deleted
- e. Exit

ALGORITHM FOR DELETING A NODE

Deletion from the end:

- 1. If (START==NULL)
 - a. Display "List is empty"
 - b. exit
- 2. Else IF (START→NEXT ==NULL)
 - a/ HOLD=START
 - b. START = NULL
 - c. Display the deleted node as HOLD→DATA
 - d. Set free the node HOLD, which is deleted
 - e. Exit
- a. ELSE

- a. HOLD = START
- b. WHILE(HOLD→next!=NULL)
 - a. TEMP=HOLD
 - b. HOLD=HOLD→next
- c. TEMP→NEXT=NULL
- d. Display the deleted node as HOLD→DATA
- e. Set free the node HOLD, which is deleted
- f. Exit

ALGORITHM FOR DELETING A NODE

Deletion from the given position:

- 1. Input the position POS from where data is to be deleted
- 2. Set i=0
- 3. If (START==NULL)
 - a. Display "The list is empty"
 - b. Exit
- 4. Else
 - a. If (POS==0)
 - i. HOLD = START

- ii. START=START→next
- iii. Display deleted data as HOLD→DATA
- iv. Set free the node HOLD, which is deleted
- v. Exit

- b. Else
 - i. HOLD=START
 - ii. WHILE(i<POS)
 - i. TEMP = HOLD
 - ii. $HOLD = HOLD \rightarrow next$
 - iii. IF(HOLD==NULL)
 - i. Display Position not found
 - ii. Exit
 - iv. i=i+1
 - v. TEMP→next=HOLD→next

- iii. Display deleted data asHOLD→DATA
- iv. Set free the node HOLD, which is deleted
- v. Exit

Suppose START is the address of the first node in the linked list and DATA is the information to be searched. After searching, if the DATA is found, POS will contain the corresponding position in the list.

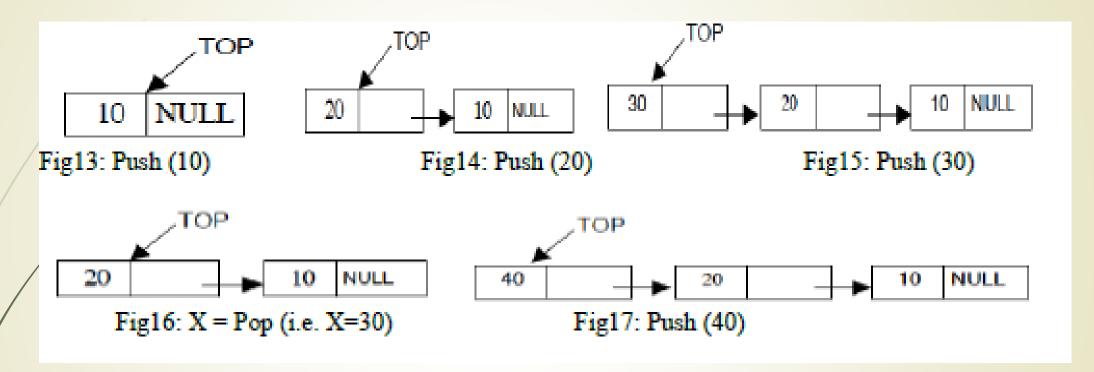
- 1. Input the DATA to be searched
- 2. Initialize TEMP = START; POS =0
- β . Repeat the step 4, 5 and 6 until (TEMP == NULL) 7.
- 4. If (TEMP \rightarrow DATA ==DATA)
 - a. Display "The data is found at POS"
 - b. Exit

- 5. $TEMP = TEMP \rightarrow next$
- 6. POS = POS+1
- 7. If (TEMP == NULL)
 - a. Display "The data is not found in the list"
 - 8. Exit

STACK USING LINKED LIST

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The following figures shows that the implementation of stack using linked list.



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Algorithm for PUSH operation:

- Suppose TOP is a pointer, which is pointing towards the topmost element of the stack. TOP is NULL when the stack is empty. DATA is the data item to be pushed.
- 1. Input the DATA to be pushed
- 2. Create a new Node
- 3. NewNode→DATA=DATA
- 4. NewNode → next = TOP
- 5. TOP=NewNOde
- 6. exit

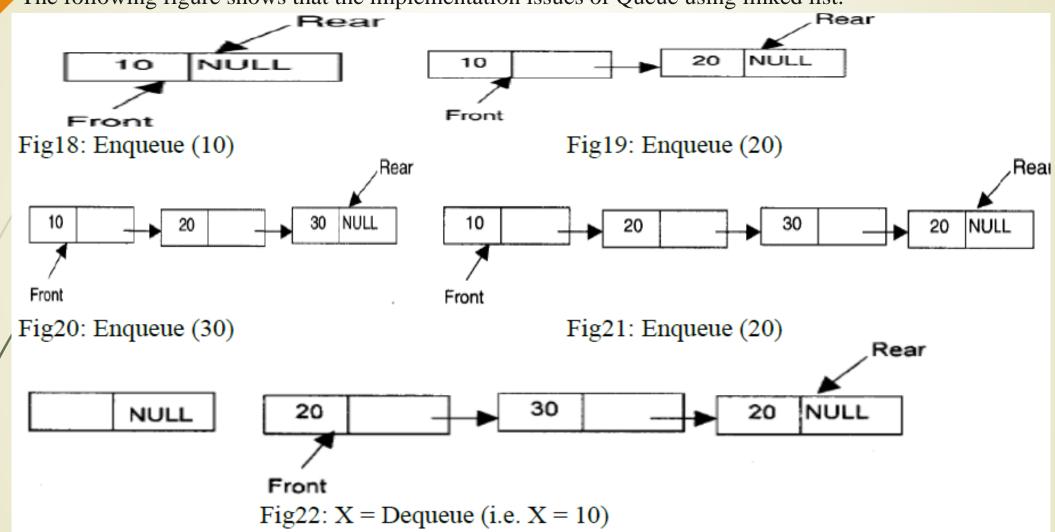
STACK USING LINKED LIST

Algorithm for POP operation:

- Suppose TOP is a pointer, which is pointing towards the topmost element of the stack. TOP is NULL when the stack is empty. TEMP is pointer variable to hold any nodes address. DATA is the information on the node which is just deleted.
- 1. If (TOP == NULL)
 - a. Display "The stack is empty"
- 2. /Else
 - a. TEMP = TOP
 - b. Disply "The popped elemet TOP→DATA"
 - c. $TOP = TEMP \rightarrow Next$
 - d. $TEMP \rightarrow next = NULL$
 - e. Free the TEMP node
- 3. Exit

QUEUE USING LINKED LIST

The following figure shows that the implementation issues of Queue using linked list.



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- REAR is a pointer in queue where the new elements are added. FRONT is a pointer, which is pointing to the queue where the elements are popped. DATA is an element to be pushed.
- 1. Input the DATA element to be pushed
- 2. Create a New Node
- 3. NewNode \rightarrow DATA = DATA
- 4. NewNode \rightarrow next = NULL
- 5. If (REAR != NULL)
 - a. $REAR \rightarrow next = NewNOde$
- 6. REAR = NewNode
- 7. Exit

ALGORITH FOR DEQUEUE AN ELEMENT FROM A QUEUE

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- REAR is a pointer in queue where the new elements are added. FRONT is a pointer, which is pointing to the queue where the elements are popped. DATA is an element popped from the queue.
- 1. If (FRONT == NULL)
 - a. Display "The queue is empty"
- 2. Else
 - a. Display "the popped element is FRONT → DATA"
 - b. If (FRONT != REAR)
 - i. $FRONT = FRONT \rightarrow Next$
 - c. Else,
 - i. Front = NULL
 - 3. exit

ADVANTAGE AND DISADVANTAGE OF SINGLY LINKED LIST

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Advantages:

- Accessibility of a node in the forward direction is easier
- Insertion and deletion of node are easier

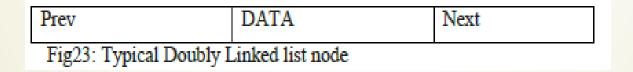
Disadvantages:

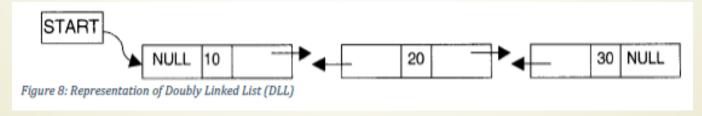
- Can insert only after a referenced node
- Removing node requires pointer to previous node
- **Can traverse list only in the forward direction.**

DOUBLY LINKED LIST

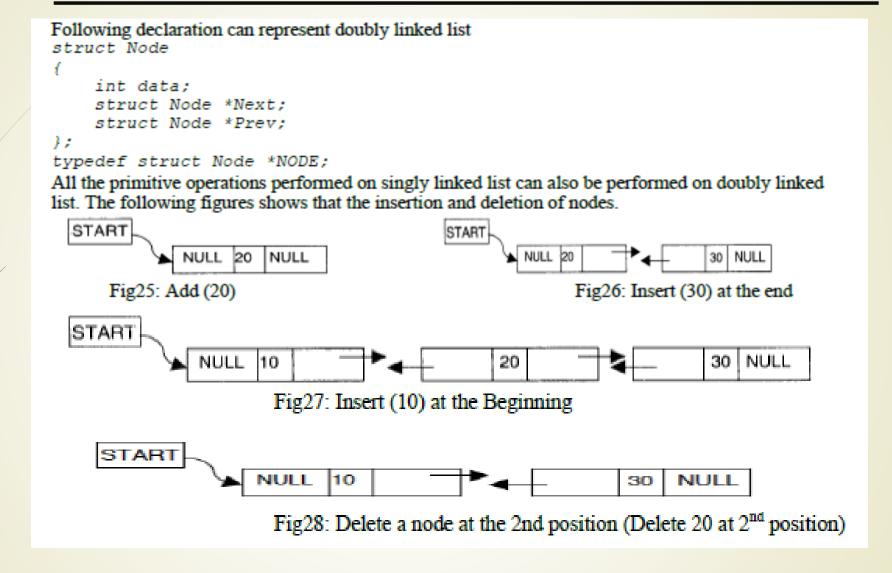
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- A doubly linked list is one in which all nodes are linked together by multiple links which help in accessing both the successor (next) and predecessor (previous) node for any arbitrary node within the list.
- Every nodes in the doubly linked list has three fields: LeftPointer (Prev), RightPointer (Next) and DATA
- **Prev** will point to the node in the left side i.e. **Prev** will hold the address of the previous node.
- Next will point to the node in the right side i.e. Next will hold the address of next node.
- **DATA** will store the information of the node.





REPRESENTATION OF DOUBLY LINKED LIST



ALGORITHM FOR INSERTING A NODE INTO DLL

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Suppose START is the first position in linked 5. Else list. Let DATA be the element to be inserted in the new node. TEMP is a temporary pointer to hold the node address and POS is the position where the NewNode is to be inserted.

At the beginning:

- Input DATA element to be inserted
- Create NewNode
- 3. NewNode → DATA =DATA
- 4. If (SART == NULL)
 - NewNode \rightarrow next = NULL
 - b. NewNode→prev = NULL

- \mathbf{a} . TEMP = START
- b. NewNode \rightarrow prev = NULL
- c. NewNode \rightarrow next = TEMP
- d. $TEMP \rightarrow prev = NewNode$
- Start=NewNode
- 7. exit

At the end:

- 1. Input DATA element to be inserted
- 2. Create NewNode
- 3. NewNode → DATA =DATA
- 4. If (SART == NULL)
 - a. NewNode \rightarrow next = NULL
 - b. NewNode \rightarrow prev = NULL
 - c. START=NewNode
- 5. Else
 - a. TEMP = START
 - b. While (TEMP→next != NULL)

- a. $TEMP = TEMP \rightarrow next$
- c. NewNode \rightarrow prev = TEMP
- d. NewNOde \rightarrow next = NULL
- e. TEMP→ next= NewNode
- 6. exit

ALGORITHM FOR INSERTING A NODE INTO DLL

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At the specified location:

- 1. Input DATA and POS
- 2. Create NewNode
- 3. NewNode → DATA =DATA
- 4. TEMP = START; i=0
- 5/ while((i<POS-1) && (TEMP!=NULL))
 - a. $TEMP = TEMP \rightarrow next$; i=i+1
- 6. If ((TEMP !=NULL) && (i==POS-1))
 - a. NewNode \rightarrow prev = TEMP
 - b. NewNOde \rightarrow next = TEMP \rightarrow next
 - c. $(TEMP \rightarrow next) \rightarrow prev = NewNode$

- d. $TEMP \rightarrow next = NewNode$
- 7. Else
 - a. Display "Position not found"
- 8. exit

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Suppose START is the address of the first node in the linked list. Let DATA is the number to be deleted. TEMP and PTR is the temporary pointer to hold the address of the node.

Deletion From the Beginning:

- 1. /IF (START==NULL)
 - 1. Display "List is empty"
 - 2. Exit
- 2. Else,
 - a. TEMP = START
 - b. $START = START \rightarrow Next$

- c. START \rightarrow Prev = NULL
- d. Display the deleted data as TEMP→DATA
- e. Free the TEMP
- f. Exit

ALGORITHM FOR DELETING A NODE

42 Deletion from the end:

- 1. If (START==NULL)
 - a. Display "List is empty"
 - b. exit
- 2. Else IF (START→NEXT ==NULL)
 - a/ HOLD=START
 - b. START = NULL
 - c. Display the deleted node as HOLD→DATA
 - d. Set free the node HOLD, which is deleted
 - e. Exit
- a. ELSE

- a. HOLD = START
- b. WHILE(HOLD→next!=NULL)
 - a. TEMP=HOLD
 - b. HOLD=HOLD→next
- c. TEMP→next=NULL
- d. HOLD→prev=NULL
- e. Display the deleted node as HOLD→DATA
- f. Set free the node HOLD, which is deleted
- g. Exit

ALGORITHM FOR DELETING A NODE

Deletion from the given position:

- 1. Input the position POS from where data is to be deleted
- 2. Set i=0
- 3. If (START==NULL)
 - a. Display "The list is empty"
 - b. Exit
- 4. Else
 - a. If (POS==0)
 - i. HOLD = START

- ii. START=START→next
- iii. START→prev =NULL
- iv. HOLD→next =NULL
- v. Display deleted data as HOLD→DATA
- vi. Set free the node HOLD, which is deleted
- vii. Exit

b. Else

- i. HOLD=START
- ii. WHILE(i<POS)
 - i. TEMP=HOLD
 - ii. $HOLD = HOLD \rightarrow next$
 - iii. IF(HOLD==NULL)
 - i. Display Position not found
 - ii. Exit
 - iv. i=i+1
- iii. TEMP→next=HOLD→next

- iv. (HOLD→next)→prev=TEMP
- v. Display deleted data as HOLD→DATA
- vi. HOLD→next =NULL
- vii. HOLD→prev=NULL
- viii.Set free the node HOLD, which is deleted
- ix. Exit

- Suppose START is the address of the first node in the linked list. Let DATA is the number to be deleted.
 TEMP and PTR is the temporary pointer to hold the address of the node.
- 1. If (STAR → DATA == DATA) (delete from beginning)
 - a. TEMP = START
 - b. $START = START \rightarrow next$
 - c. START \rightarrow Prev = NULL
 - d. Free the TEMP
- 2. PTR = START
- 3. Repeat until((PTR \rightarrow next) \rightarrow next !=NULL) (Delete from the position)
 - a. If $((PTR \rightarrow next) \rightarrow DATA == DATA)$
 - i. $TEMP = PTR \rightarrow next$

ALGORITHM FOR DELETING A NODE FROM DLL

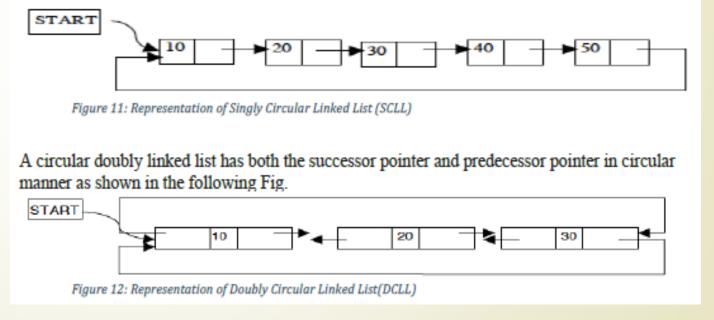
ii.
$$PTR \rightarrow next = TEMP \rightarrow next$$

iii.
$$(TEMP \rightarrow next) \rightarrow prev = PTR$$

- iv. Free the TEMP
- b. $PTR = PTR \rightarrow next$
- 4. If $((PTR \rightarrow next) \rightarrow DATA == DATA)$ (Delete from the last)
 - a. $TEMP = PTR \rightarrow next$
 - b. Free the TEMP
 - c. $PTR \rightarrow next == NULL$
- 5. Else
 - a. Display "Data not Found"
- 6. Exit

- A circular linked list is one, which has no beginning and no end.
- A singly linked list can be made a circular linked list by simply storing the address of the very first node in the linked field of the last node.
- Circular linked lists also make our implementation easier, because they eliminate the boundary conditions associated with the beginning and end of the list, thus eliminating the special case code required to handle

these boundary conditions.



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INSERTION ALGORITHM INTO CIRCULAR LINKED LIST

Suppose START is the first position in linked list.
Let DATA be the element to be inserted in the new node. LAST indicated the last node.

At the beginning:

- 1. Create a New Node
- 2. NewNOde \rightarrow DATA = DATA
- 3. If (START == NULL)
 - a. NewNode \rightarrow next = NewNode
 - b. START = NewNode

- c. LAST = NewNode
- 4. Else
 - a. NewNode \rightarrow next = START
 - b. START = NewNode
 - c. LAST \rightarrow next = NewNode
- 5. Exit

At the end:

- 1. Create a New Node
- 2. NewNOde→DATA = DATA
- 3. If (START == NULL)
 - \land NewNode \rightarrow next = NewNode
 - b. START = NewNode
 - c. LAST = NewNode
- 4. Else
 - a. LAST \rightarrow next = NewNode
 - b. LAST = NewNode
 - c. LAST \rightarrow next = START

5. Exit

At the beginning:

- 1. Declare a temporary node, PTR
- 2. If (START == NULL)
 - a. Display "Empty Circular queue"
 - b. Exit
- $\frac{3}{PTR} = START$
- 4. $START = START \rightarrow next$
- 5. Print, element deleted is PTR→ DATA
- 6. LAST \rightarrow next = START
- 7. Free PTR
- 8. Exit

At the end:

- 1. Declare a temporary node, PTR
- 2. If (START == NULL)
 - a. Display "Empty Circular queue"
 - b. Exit
- \mathcal{J} . PTR = START
- 4. While (PTR! = LAST)
 - a. PTR1 = PTR
 - b. $PTR = PTR \rightarrow next$
- 5. Print, element deleted is PTR→ DATA

- 6. LAST = PTR1
- 7. LAST \rightarrow next = START
- 8. Free PTR

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APPLICATION OF LINKED LIST IN COMPUTER SCIENCE

- Implementation of stacks and queues
- Implementation of graphs : Adjacency list representation of graphs is most popular which is uses linked list to store adjacent vertices.
- Dynamic memory allocation : We use linked list of free blocks.
- Maintaining directory of names
- Performing arithmetic operations on long integers
- Manipulation of polynomials by storing constants in the node of linked list
- representing sparse matrices

- Image viewer Previous and next images are linked, hence can be accessed by next and previous button.
- ▶ Previous and next page in web browser We can access previous and next url searched in web browser by pressing back and next button since, they are linked as linked list.
- Music Player Songs in music player are linked to previous and next song. you can play songs either from starting or ending of the list.





Suppose START is the first position in linked list. 4. While ((HOLD \rightarrow next \rightarrow next)!=NULL) Let DATA be the element to be deleted. TEMP, HOLD is a temporary pointer to hold the node address.

- Input the DATA to be deleted
- If (START→ DATA ==DATA) // Data at first nøde
 - TEMP=START
 - START=STAR→next
 - Set free the node TEMP, which is deleted
 - d. Exit
- 3. HOLD = START

- - a. $If((HOLD \rightarrow NEXT \rightarrow DATA) == DATA)$
 - $TEMP = HOLD \rightarrow next$
 - $HOLD \rightarrow next = TEMP \rightarrow next$
 - Set free the node TEMP, which is deleted
 - iv. Exit
 - $HOLD = HOLD \rightarrow next$
- If $((HOLD \rightarrow next \rightarrow DATA) == DATA)$
 - $TEMP = HOLD \rightarrow next$
 - Set free the node TEMP, which is deleted

- a. $HOLD \rightarrow next = NULL$
- b. Exit
- 6. Display "DATA not found"
- 7. Exit