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The best sentences

More seriously with math and graphs



# Star wars or not ?

- ▶ Dark vador is not my father.
- ▶ Are you sure Anakin ?
- ▶ Yes, my father said :
  - ▶ The yes needs the no to win against the no.<sup>1</sup>



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1. Jean-Pierre Raffarin, Archive INA, <https://www.youtube.com/watch?v=O27mdRvR1GY>

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# The conditions for augmenting Radomized CLinical Trials (RCT) with an external control group<sup>2</sup>

- C1. The respect for positivity between the external and RCT controls.
- C2. The absence of unmeasured confounders, i.e. determinants of both the outcome and the probability of inclusion in the RCT compared to the external group.
- C3. The absence of a direct effect on the outcome of being included in the RCT.

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2. Dang et al. A Cross-Validated Targeted Maximum Likelihood Estimator for Data-Adaptive Experiment Selection Applied to the Augmentation of RCT Control Arms with External Data.  
arXiv :2210.05802v1

## How to respect the condition C1 (positivity) ?

1. Use external data but from a recent period.
2. Use external data from the same centers, at least for a large part.
3. Check the inclusion criteria in both the RCT and external study : the targeted population of the RCT must be embedded.
4. Compare the characteristics of two samples of controls to validate the positivity,<sup>3</sup> and restrict the inclusion criteria until no issue is identified.

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3. Danelian G, Foucher Y, Léger M, Le Borgne F. and Chatton A. Identification of in-sample positivity violations using regression trees : The PoRT algorithm. Journal of Causal Inference (2023).

## How to respect the condition C2 (absence of unmeasured confounders) ?

1. Draw a causal diagram with the inclusion in the RCT versus external study as an element.
2. Propose a complete list of the prognostic factors of the studied outcomes.
3. Propose a complete list of the determinants of the inclusions in the RCT versus external study.
4. Make sure that the variables in the two lists #2 and #3 will be available in both the RCT and the external study with the same methods of collection.

## How to respect the condition C3 (no direct effect of being in the RCT) ?

- ▶ One can limit/prevent such a direct effect by :
  1. Check the studied treatments are identical in the two studies (doses, administration, etc.).
  2. Use the same definition of the collected outcomes.
  3. Ensure comparable monitoring in the two studies.
- ▶ Control patients in the RCT are required for a data-driven check of C3.
- ▶ An RCT based on a control arm completely-based with external data or digital twins does not allow for validating C3.

Problem #2 : these checks do not convince on the respect of C3

- ▶ **How to validate C3 by using the RCT data ?**



## Consider the following usual RCT for superiority with $k$ controls for 1 patient in the experimental arm

- ▶ A binary principal outcome  $Y$  with  $\pi_0$  and  $\pi_1$  the two expected proportions in the control and experimental arms.
- ▶  $N_{1s}$  and  $N_{0s}$  the required sample sizes for a bilateral test with targeted type-I and type-II errors,  $\alpha$  and  $\beta$  respectively.
- ▶  $N_{0s} = kN_{1s}$  and  $N_{1s} = (\pi_1 - \pi_0)^2(\pi_0(1 - \pi_0)/k + \pi_1(1 - \pi_1))/(z_{\alpha/2} + z_{\beta})^2$

### Example

- ▶ For  $k = 1$ ,  $\alpha = 0.05$ ,  $\beta = 0.20$ ,  $\pi_0 = 0.50$  and  $\pi_1 = 0.40$ ,
- ▶ the sample sizes are  $N_{0s} = N_{1s} = 385$ .

## Consider the following method to augment the RCT with external data (one method among others)

- ▶ A model  $M$  (for instance a logistic regression) is estimated from the external data to predict the outcome  $\hat{\pi}_{0i}$  given the characteristics  $X_i$  of a patient  $i$  with the control treatment.
- ▶ There is no direct effect of being in the RCT (condition C3) if  $M$  is well-calibrated for the outcome prediction at the inclusion in the control group of the RCT.
- ▶ A calibration measure can be  $O/E$  :
  - ▶  $O$  is the number of observed events :  $\sum_i Y_i$  among the control patients.
  - ▶  $E$  is the number of expected events :  $\sum_i \hat{\pi}_{0i}$  among the control patients.
- ▶ The value  $O/E = 1$  indicates a perfect calibration.

## Minimal sample size $N_{0c}$ to evaluate the calibration of the model $M$

- ▶ By using the delta method :<sup>4</sup>  $SE(\log(O/E)) \approx \sqrt{(1 - \pi_0)/(\pi_0 N_{0c})}$ .
- ▶ Depending on  $w$ , the targeted width of confidence interval of the O/E, one can compute  $SE_w(\log(O/E))$ .
- ▶ One can deduce that  $N_{0c} = (1 - \pi_0)/(\pi_0 SE_w(\log(O/E))^2)$

Example (continued, with  $k = 1$ ,  $\alpha = 0.05$ ,  $\beta = 0.20$ ,  $\pi_0 = 0.50$  and  $\pi_1 = 0.40$ )

- ▶ For  $\alpha = 0.05$  and  $w = 0.10$  (i.e.,  $SE_w(\log(O/E)) \approx 0.25$ ) then  $N_{0c} = 1541$ .
  - ▶  $N_{0c} > 385$  : we cannot check the respect of C3.
- ▶ For  $\alpha = 0.05$  and  $w = 0.20$  (i.e.,  $SE_w(\log(O/E)) \approx 0.51$ ,) then  $N_{0c} = 386$ .
  - ▶  $N_{0c} \approx 385$  : we can check the respect of C3.

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4. Debray et al. A framework for meta-analysis of prediction model studies with binary and time-to-event outcomes. Stat Methods Med Res. 2019 ;28 :2768-2786.





