Semantic Approximation for Reducing Code Bloat in Genetic Programming

Thi Huong Chu^a, Quang Uy Nguyen^a

^aFaculty of IT, Le Quy Don Technical University, Hanoi, Vietnam

Suppelment 2: Experimental results with the maximum depth of sTree = 1, 3 and 4.

Table 1: List of table results in supplement 2

No	Content	Table
1	Mean of the best fitness with the maximum depth	Table 2
	of $sTree = 1$	
2	Median of testing error with the maximum depth of	Table 3
	sTree = 1	
3	Average size of solutions with the maximum depth	Table 4
	of $sTree = 1$	
4	Average running time in seconds with the maximum	Table 5
	depth of $sTree = 1$	
5	Mean of the best fitness with the maximum depth	Table 6
	of $sTree = 1$	
6	Median of testing error with the maximum depth of	Table 7
	sTree = 1	
7	Average size of solutions with the maximum depth	Table 8
	of $sTree = 1$	

 $Email\ addresses: \verb+huongktqs@gmail.com+ (Thi\ Huong\ Chu\),\ \verb+quanguyhn@gmail.com+ (Quang\ Uy\ Nguyen)$

8	Average running time in seconds with the maximum	Table 9
	depth of $sTree = 1$	
9	Mean of the best fitness with the maximum depth	Table 10
	of $sTree = 1$	
10	Median of testing error with the maximum depth of	Table 11
	sTree = 1	
11	Average size of solutions with the maximum depth	Table 12
	of $sTree = 1$	
12	Average running time in seconds with the maximum	Table 13
	depth of $sTree = 1$	

Table 2: Mean of the best fitness with the maximum depth of sTree=1: bold face is better than GP, underline is the best result.

Pro	GP	SA10	SA20	SAD	DA10	DA20	DAD				
А. В	A. Benchmarking Problems										
F1	0.47	0.52	0.85	1.34	$\underline{0.41}$	0.95	1.16				
F2	1.91	1.11	2.27	4.25	$\underline{1.03}$	2.33	3.54				
F3	0.10	0.11	0.13	0.12	$\underline{0.10}$	0.12	0.11				
F4	0.51	0.19	0.43	1.98	$\underline{0.17}$	0.35	1.28				
F5	1.13	0.95	1.62	2.68	$\underline{0.88}$	1.54	2.40				
F6	0.26	0.25	0.25	0.25	$\underline{0.25}$	0.25	0.25				
F7	0.03	0.03	0.03	0.03	$\underline{0.03}$	0.03	0.03				
F8	9.90	11.58	24.61	41.36	10.56	23.17	30.25				
F9	0.38	0.37	0.49	0.49	$\underline{0.32}$	0.47	0.48				
F10	0.41	0.17	0.23	0.23	$\underline{0.14}$	0.17	0.18				
B. U	CI Pro	blems									
F11	0.47	0.48	0.52	0.53	$\underline{0.46}$	0.50	0.51				
F12	0.40	0.19	0.26	0.31	$\underline{0.15}$	0.16	0.17				
F13	3.28	3.33	3.41	3.44	$\underline{3.08}$	3.28	3.29				
F14	0.17	0.17	0.18	0.18	$\underline{0.17}$	0.17	0.17				
F15	0.82	0.54	0.80	0.87	$\underline{0.45}$	0.54	0.58				
F16	1.68	1.70	2.01	2.05	$\underline{1.61}$	1.84	1.93				
F17	0.91	0.94	1.11	1.11	$\underline{0.83}$	1.00	1.03				
F18	0.53	0.49	0.64	0.66	$\underline{0.42}$	0.55	0.60				

Table 3: Median of testing error with the maximum depth of sTree=1: bold face is better than GP, underline is the best result.

Pro	GP	SA10	SA20	SAD	DA10	DA20	DAD
A. E	Benchm	arking P	$_{ m roblems}$				
F1	1.69	1.17	$\underline{0.93}$	1.38	0.98	1.83	2.01
F2	10.17	4.77	5.10	5.61	$\underline{4.41}$	4.63	5.66
F3	0.06	0.05	0.06	0.06	0.05	0.05	$\underline{0.05}$
F4	0.31	0.16	0.25	3.52	$\underline{0.01}$	$\underline{0.01}$	2.94
F5	33.01	12.72	6.55	19.39	14.87	$\underline{3.56}$	8.87
F6	0.26	0.25	0.25	$\underline{0.25}$	0.25	0.25	0.25
F7	0.03	0.03	0.03	0.03	0.03	0.03	$\underline{0.03}$
F8	45.88	44.21	44.63	44.23	44.94	44.25	$\underline{43.90}$
F9	2.19	2.18	2.18	$\underline{2.18}$	2.19	2.18	2.18
В. Т	JCI Pro	blems					
F10	0.75	0.27	0.27	0.27	$\underline{0.24}$	0.25	0.25
F11	0.61	0.59	0.58	0.58	0.59	0.58	$\underline{0.58}$
F12	0.36	0.20	0.29	0.32	$\underline{0.16}$	0.17	0.18
F13	5.18	3.87	3.84	3.90	4.00	3.77	$\underline{3.74}$
F14	0.18	0.17	0.18	0.18	$\underline{0.17}$	0.17	0.17
F15	1.44	0.55	0.65	0.86	$\underline{0.52}$	0.53	0.53
F16	2.69	2.40	2.09	2.04	2.23	$\underline{2.04}$	2.07
F17	1.77	1.31	1.14	$\underline{1.12}$	1.54	1.30	1.32
F18	0.73	0.60	0.68	0.67	0.55	0.62	0.62

Table 4: Average size of solutions with the maximum depth of sTree = 1: bold face is better than GP, underline is the best result.

Pro	GP	SA10	SA20	SAD	DA10	DA20	DAD				
A. I	A. Benchmarking Problems										
F1	295.5	93.2	26.8	23.4	78.2	19.6	<u>17.1</u>				
F2	228.3	81.5	22.8	13.5	77.2	27.1	12.7				
F3	180.9	64.6	43.5	31.6	63.5	43.8	36.0				
F4	187.3	75.5	24.2	14.9	44.2	$\underline{11.3}$	11.9				
F5	162.5	59.1	12.8	$\underline{11.2}$	57.6	12.3	12.5				
F6	216.9	84.0	24.3	$\underline{10.6}$	68.2	21.6	16.7				
F7	153.6	68.8	22.5	23.4	72.3	$\underline{17.5}$	20.9				
F8	161.0	60.1	$\underline{14.1}$	20.2	62.3	17.7	17.6				
F9	237.8	79.2	12.1	10.5	73.6	11.8	11.9				
В. Т	JCI Pro	blems									
F10	196.4	55.7	10.9	$\underline{9.6}$	58.5	15.7	11.4				
F11	192.0	62.8	10.6	$\underline{6.7}$	82.0	19.2	16.5				
F12	151.7	65.5	21.2	$\underline{12.4}$	72.7	21.1	15.3				
F13	200.8	24.8	7.9	$\underline{6.7}$	70.6	11.9	7.2				
F14	170.5	58.0	10.1	7.3	62.3	11.7	10.8				
F15	187.4	58.3	9.9	7.7	68.9	13.8	8.8				
F16	192.6	60.1	9.7	9.1	72.4	19.2	14.9				
F17	177.5	63.5	10.7	8.5	84.3	17.6	12.5				
F18	181.8	50.6	8.7	7.2	61.3	16.5	11.4				

 $\begin{tabular}{ll} \textbf{Table 5:} Average running time in seconds with the maximum depth of $sTree=1$: bold face is better than GP, underline is the best result. \\ \end{tabular}$

Pro	GP	SA10	SA20	SAD	DA10	DA20	DAD
А. Е	Benchma	arking P	roblems				
F1	3.6	2.3	$\underline{0.8}$	1.8	2.1	1.5	1.9
F2	2.7	2.2	$\underline{1.3}$	1.4	2.6	2.0	1.6
F3	4.3	3.5	3.2	7.0	5.9	5.3	6.7
F4	63.2	34.7	14.2	15.3	48.3	31.4	57.6
F5	64.9	33.8	$\underline{11.9}$	15.9	43.8	39.0	88.0
F6	96.0	66.3	28.3	$\underline{17.7}$	66.7	47.4	81.2
F7	77.7	60.0	25.1	26.8	79.3	50.2	214.5
F8	79.7	44.0	13.9	18.0	62.6	$\boldsymbol{45.9}$	136.9
F9	82.7	46.6	16.0	<u>14.4</u>	66.6	44.7	62.4
В. С	JCI Pro	blems					
F10	46.0	16.8	8.1	14.8	31.2	25.4	47.6
F11	8.4	6.0	2.3	4.7	9.0	3.8	36.8
F12	43.8	31.2	$\underline{11.9}$	14.6	49.4	31.3	36.9
F13	7.2	2.6	$\underline{2.6}$	5.6	7.3	5.6	37.1
F14	63.1	40.4	$\underline{11.9}$	36.8	48.3	30.1	251.8
F15	4.1	1.9	$\underline{1.3}$	3.1	3.7	1.6	14.4
F16	4.0	2.1	$\underline{0.9}$	3.4	4.3	1.8	17.8
F17	4.0	2.1	<u>1.1</u>	3.4	5.0	1.8	17.8
F18	27.4	11.2	$\underline{5.9}$	18.6	23.3	15.6	145.7

Table 6: Mean of the best fitness with the maximum depth of sTree= 3: bold face is better than GP, underline is the best result.

Pro	GP	SA10	SA20	SAD	DA10	DA20	DAD			
A. Benchmarking Problems										
F1	0.47	0.51	1.00	1.36	0.49	0.95	1.16			
F2	1.91	1.18	2.54	4.20	$\underline{0.95}$	2.20	3.39			
F3	0.10	0.10	0.12	0.12	$\underline{0.09}$	0.12	0.11			
F4	0.51	0.23	0.72	1.91	$\underline{0.08}$	0.31	0.53			
F5	1.13	0.99	1.56	2.75	$\underline{0.83}$	1.49	2.66			
F6	0.26	0.25	0.25	0.26	$\underline{0.25}$	0.25	0.25			
F7	0.03	0.03	0.03	0.03	$\underline{0.03}$	0.03	0.03			
F8	9.90	11.28	20.92	37.54	7.56	15.66	21.01			
F9	0.38	0.38	0.48	0.49	$\underline{0.36}$	0.46	0.48			
В. С	CI Pro	blems								
F10	0.41	0.16	0.22	0.22	$\underline{0.14}$	0.17	0.18			
F11	0.47	0.48	0.52	0.53	$\underline{0.47}$	0.50	0.51			
F12	0.40	0.20	0.26	0.32	$\underline{0.16}$	0.16	0.17			
F13	3.28	3.31	3.43	3.44	3.07	3.26	3.28			
F14	0.17	0.17	0.18	0.18	$\underline{0.17}$	0.17	0.17			
F15	0.82	0.54	0.89	0.93	$\underline{0.49}$	0.52	0.56			
F16	1.68	1.72	2.01	2.06	$\underline{1.56}$	1.80	1.94			
F17	0.91	0.91	1.10	1.12	$\underline{0.87}$	1.01	1.04			
F18	0.53	0.50	0.65	0.66	0.42	0.55	0.60			

Table 7: Median of testing error with the maximum depth of sTree= 3: bold face is better than GP, underline is the best result

Pro	GP	SA10	SA20	SAD	DA10	DA20	DAD
A. E	Benchm	arking P	$_{ m roblems}$				
F1	1.69	1.19	1.11	1.52	1.54	1.33	2.08
F2	10.17	5.37	4.83	5.19	$\underline{4.26}$	4.27	5.68
F3	0.06	$\underline{0.05}$	0.05	0.05	0.05	0.05	0.05
F4	0.31	0.08	0.57	3.31	$\underline{0.00}$	0.01	0.02
F5	33.01	24.12	6.56	23.32	10.36	$\underline{5.08}$	19.74
F6	0.26	0.25	0.25	$\underline{0.25}$	0.25	0.25	0.25
F7	0.03	0.03	0.03	$\underline{0.03}$	0.03	0.03	0.03
F8	45.88	45.05	45.05	$\underline{44.29}$	45.97	45.58	44.60
F9	2.19	2.18	2.18	2.18	2.20	2.18	2.18
В. Т	JCI Pro	blems					
F10	0.75	0.27	0.28	0.26	$\underline{0.24}$	0.25	0.25
F11	0.61	0.58	0.57	0.58	0.58	$\underline{0.57}$	0.57
F12	0.36	0.20	0.27	0.33	$\underline{0.16}$	0.17	0.18
F13	5.18	3.86	3.90	3.97	3.99	$\underline{3.73}$	3.75
F14	0.18	0.17	0.18	0.18	0.17	$\underline{0.17}$	0.17
F15	1.44	0.56	0.89	0.94	0.56	$\underline{0.51}$	0.54
F16	2.69	2.31	2.10	2.06	2.17	2.10	1.97
F17	1.77	1.28	1.16	$\underline{1.13}$	1.29	1.29	1.31
F18	0.73	0.59	0.69	0.69	0.53	0.57	0.64

 $\begin{tabular}{ll} \textbf{Table 8:} & Average size of solutions with the maximum depth of $sTree=$ 3: bold face is better than GP, underline is the best result \\ \end{tabular}$

Pro	GP	SA10	SA20	SAD	DA10	DA20	DAD			
A. Benchmarking Problems										
F1	295.5	97.2	18.7	$\underline{15.2}$	75.9	21.8	15.8			
F2	228.3	81.5	20.4	20.9	76.1	25.4	15.4			
F3	180.9	67.3	42.4	30.9	76.6	43.7	$\underline{28.4}$			
F4	187.3	$\boldsymbol{66.4}$	20.5	11.9	54.3	13.3	$\underline{9.5}$			
F5	162.5	59.1	16.1	$\underline{11.4}$	54.6	13.4	12.3			
F6	216.9	79.1	21.9	$\underline{11.0}$	65.6	21.7	16.8			
F7	153.6	69.6	21.8	21.5	63.9	20.5	24.8			
F8	161.0	61.3	15.6	24.6	63.3	16.7	$\underline{11.6}$			
F9	237.8	85.0	16.3	<u>7.8</u>	60.3	15.9	11.3			
В. Т	JCI Pro	blems								
F10	196.4	58.5	8.6	12.0	70.7	16.5	15.5			
F11	192.0	66.1	10.8	8.1	75.0	17.3	12.8			
F12	151.7	57.5	16.9	$\underline{12.4}$	74.0	21.1	13.6			
F13	200.8	26.9	7.9	7.7	55.7	13.1	8.1			
F14	170.5	52.9	8.5	$\underline{6.7}$	65.4	12.8	9.9			
F15	187.4	51.6	10.8	8.7	68.9	15.9	9.2			
F16	192.6	61.1	10.0	8.4	74.3	20.3	13.7			
F17	177.5	68.0	8.8	7.6	76.0	16.3	13.5			
F18	181.8	46.0	9.2	8.1	61.3	17.1	15.5			

 $\begin{tabular}{ll} \textbf{Table 9:} Average running time in seconds with the maximum depth of $sTree=$ 3: bold face is better than GP, underline is the best result \\ \end{tabular}$

Pro	GP	SA10	SA20	SAD	DA10	DA20	DAD				
A. I	A. Benchmarking Problems										
F1	3.6	2.7	$\underline{0.8}$	1.7	2.9	1.1	2.6				
F2	2.7	2.3	$\underline{0.6}$	1.7	2.6	1.2	2.5				
F3	4.3	3.7	$\underline{2.9}$	6.3	6.7	5.8	6.0				
F4	63.2	39.4	$\underline{13.6}$	13.7	45.0	25.9	83.1				
F5	64.9	34.7	$\underline{12.2}$	20.6	49.4	29.3	115.6				
F6	96.0	67.9	$\underline{19.9}$	23.8	70.3	33.2	116.3				
F7	77.7	60.9	$\underline{20.9}$	34.3	82.8	36.0	224.2				
F8	79.7	51.6	$\underline{13.0}$	24.0	67.8	31.7	124.5				
F9	82.7	52.7	$\underline{15.4}$	22.9	61.4	36.4	74.6				
В. Т	JCI Pı	oblems									
F10	46.0	19.7	$\underline{14.0}$	15.6	36.1	23.5	54.3				
F11	8.4	4.9	$\underline{2.2}$	5.8	9.9	4.3	47.2				
F12	43.8	26.0	17.0	$\underline{13.7}$	46.6	30.6	43.8				
F13	7.2	2.5	$\underline{2.3}$	5.7	7.7	5.1	26.1				
F14	63.1	36.6	$\underline{20.1}$	43.3	50.2	28.7	333.8				
F15	4.1	1.5	$\underline{1.4}$	3.2	3.3	2.0	10.2				
F16	4.0	1.7	$\underline{1.3}$	3.5	3.7	1.9	13.0				
F17	4.0	1.8	$\underline{0.7}$	3.5	4.0	1.9	10.7				
F18	27.4	11.2	7.2	17.9	21.5	9.9	164.5				

Table 10: Mean of the best fitness with the maximum depth of sTree = 4: bold face is better than GP, underline is the best result

Pro	GP	SA10	SA20	SAD	DA10	DA20	DAD				
A. E	A. Benchmarking Problems										
F1	0.47	0.48	0.89	1.34	$\underline{0.43}$	0.90	1.17				
F2	1.91	1.17	2.35	4.18	$\underline{0.99}$	2.24	3.51				
F3	0.10	0.10	0.13	0.14	$\underline{0.10}$	0.12	0.12				
F4	0.51	0.16	0.52	1.94	$\underline{0.07}$	0.10	1.41				
F5	1.13	1.07	1.61	2.85	$\underline{1.01}$	1.42	2.79				
F6	0.26	0.25	0.25	0.26	$\underline{0.25}$	0.25	0.25				
F7	0.03	$\underline{0.03}$	0.03	0.03	0.03	0.03	0.03				
F8	9.90	$\boldsymbol{9.72}$	22.97	36.76	8.84	15.01	22.07				
F9	0.38	0.38	0.48	0.50	$\underline{0.32}$	0.45	0.48				
В. С	JCI Pro	blems									
F10	0.41	0.16	0.23	0.23	$\underline{0.14}$	0.16	0.18				
F11	0.47	0.48	0.52	0.53	$\underline{0.46}$	0.50	0.51				
F12	0.40	0.18	0.27	0.30	$\underline{0.16}$	0.16	0.17				
F13	3.28	3.31	3.42	3.44	$\underline{3.10}$	3.27	3.27				
F14	0.17	0.17	0.18	0.18	$\underline{0.17}$	0.17	0.17				
F15	0.82	0.58	0.81	0.89	$\underline{0.50}$	0.53	0.58				
F16	1.68	1.64	2.01	2.06	$\underline{1.55}$	1.80	1.92				
F17	0.91	0.94	1.10	1.11	$\underline{0.85}$	1.01	1.04				
F18	0.53	0.48	0.65	0.66	0.41	0.54	0.60				

Table 11: Median of testing error with the maximum depth of sTree = 4: bold face is better than GP, underline is the best result

Pro	GP	SA10	SA20	SAD	DA10	DA20	DAD					
A. I	A. Benchmarking Problems											
F1	1.69	1.14	$\underline{0.99}$	1.51	1.34	1.34	1.99					
F2	10.17	4.72	3.86	5.74	4.44	4.34	5.70					
F3	0.06	0.05	0.05	0.06	$\underline{0.05}$	0.05	0.05					
F4	0.31	0.14	0.21	3.99	0.01	$\underline{0.01}$	3.02					
F5	33.01	25.47	7.35	25.48	10.87	$\underline{6.77}$	24.63					
F6	0.26	0.26	0.25	$\underline{0.25}$	0.25	0.25	0.25					
F7	0.03	0.03	0.03	0.03	0.03	0.03	$\underline{0.03}$					
F8	45.88	45.59	45.51	$\underline{44.30}$	46.74	45.37	45.11					
F9	2.19	2.19	2.18	2.18	2.19	2.18	2.18					
В. Т	JCI Pro	blems										
F10	0.75	0.26	0.28	0.28	0.24	$\underline{0.23}$	0.25					
F11	0.61	0.59	0.57	0.58	0.59	$\underline{0.57}$	0.57					
F12	0.36	0.19	0.26	0.32	$\underline{0.17}$	0.17	0.18					
F13	5.18	3.85	3.82	3.82	3.92	3.72	3.77					
F14	0.18	0.17	0.18	0.18	$\underline{0.17}$	0.17	0.17					
F15	1.44	0.61	0.88	0.94	0.59	$\underline{0.51}$	0.53					
F16	2.69	2.17	2.05	2.04	2.43	2.04	$\underline{1.99}$					
F17	1.77	1.31	1.15	$\underline{1.13}$	1.32	1.29	1.33					
F18	0.73	0.60	0.65	0.69	0.55	0.59	0.60					

Table 12: Average size of solutions with the maximum depth of sTree = 4: bold face is better than GP, underline is the best result

Pro	GP	SA10	SA20	SAD	DA10	DA20	DAD
A. 1	Benchm	arking P	roblems				
F1	295.5	93.8	23.1	14.8	75.8	21.7	$\underline{14.4}$
F2	228.3	77.4	21.6	18.7	79.5	27.6	18.9
F3	180.9	67.3	29.5	28.5	65.1	39.6	$\underline{28.4}$
F4	187.3	65.4	19.0	$\underline{10.5}$	51.3	12.2	12.1
F5	162.5	61.6	13.5	$\underline{10.4}$	58.2	13.2	13.0
F6	216.9	77.1	17.7	8.9	$\boldsymbol{66.5}$	18.4	20.7
F7	153.6	75.1	20.9	19.9	69.6	18.5	18.8
F8	161.0	67.4	15.7	21.9	57.6	15.8	$\underline{13.8}$
F9	237.8	74.1	13.8	10.6	63.4	17.0	10.7
В. Т	UCI Pro	oblems					
F10	196.4	60.1	<u>7.8</u>	9.6	65.7	15.9	15.8
F11	192.0	55.8	10.3	7.2	77.1	18.3	11.3
F12	151.7	55.7	14.0	$\underline{11.3}$	71.4	21.0	12.4
F13	200.8	22.6	7.2	8.4	64.0	13.8	7.9
F14	170.5	48.3	8.9	$\underline{6.9}$	65.7	15.5	9.9
F15	187.4	$\boldsymbol{67.2}$	9.9	7.7	73.5	17.2	9.5
F16	192.6	63.2	9.2	7.6	75.7	19.5	15.3
F17	177.5	60.1	9.9	8.3	75.8	16.7	14.5
F18	181.8	58.7	8.4	7.0	66.6	18.6	14.8

 $\begin{tabular}{ll} \textbf{Table 13:} Average running time in seconds with the maximum depth of $sTree=$ 4: bold face is better than GP, underline is the best result \\ \end{tabular}$

Pro	GP	SA10	SA20	SAD	DA10	DA20	DAD
A. I	Benchn	narking	Probler	$\mathbf{n}\mathbf{s}$			
F1	3.6	2.6	$\underline{0.8}$	2.0	3.0	1.2	2.8
F2	2.7	2.1	$\underline{0.6}$	2.0	2.7	1.3	2.7
F3	4.3	4.9	$\underline{2.6}$	5.2	6.2	5.1	6.0
F4	63.2	39.3	$\underline{13.0}$	17.7	38.3	44.3	67.7
F5	64.9	38.6	$\underline{13.1}$	21.7	46.5	42.0	92.1
F6	96.0	68.8	24.1	$\underline{22.0}$	66.5	41.9	83.6
F7	77.7	67.2	$\underline{22.0}$	41.8	72.8	46.3	156.5
F8	79.7	51.9	$\overline{13.9}$	21.4	56.6	33.0	107.5
F9	82.7	51.0	$\underline{17.0}$	21.3	57.0	33.5	77.4
В. Т	JCI Pı	oblems					
F10	46.0	18.2	$\underline{15.9}$	20.2	37.0	23.4	43.5
F11	8.4	5.9	$\underline{2.6}$	6.9	10.4	4.7	37.0
F12	43.8	30.5	15.4	15.7	41.6	37.9	46.6
F13	7.2	2.7	2.7	6.2	7.8	6.6	35.5
F14	63.1	36.3	<u>18.8</u>	42.0	42.8	38.0	369.8
F15	4.1	3.1	$\underline{1.2}$	3.0	5.0	3.3	12.2
F16	4.0	2.7	<u>1.1</u>	3.0	5.4	2.8	18.1
F17	4.0	2.8	<u>1.1</u>	3.0	5.1	2.7	18.2
F18	27.4	12.6	7.5	17.4	18.5	12.1	136.2