



# Classification (Short Version)

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# Classification

- To learn more .....



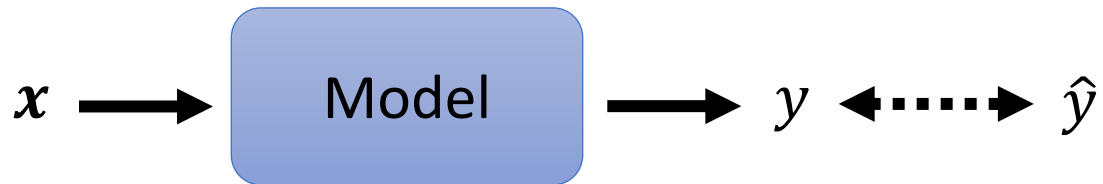
<https://youtu.be/fZAZUYEeIMg>  
(in Mandarin)



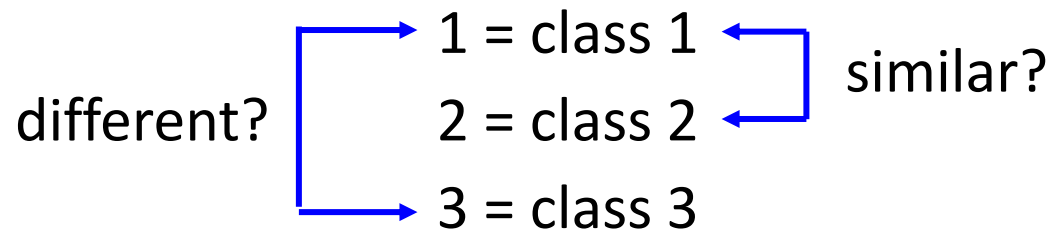
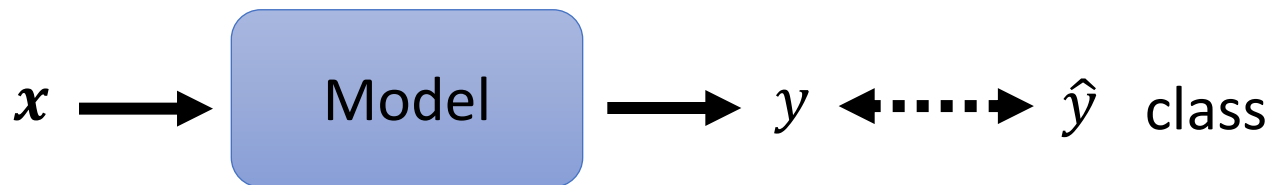
<https://youtu.be/hSXFuypLukA>  
(in Mandarin)

# Classification as Regression?

- Regression



- Classification as regression?



# Class as one-hot vector

Class 1

Class 2

Class 3

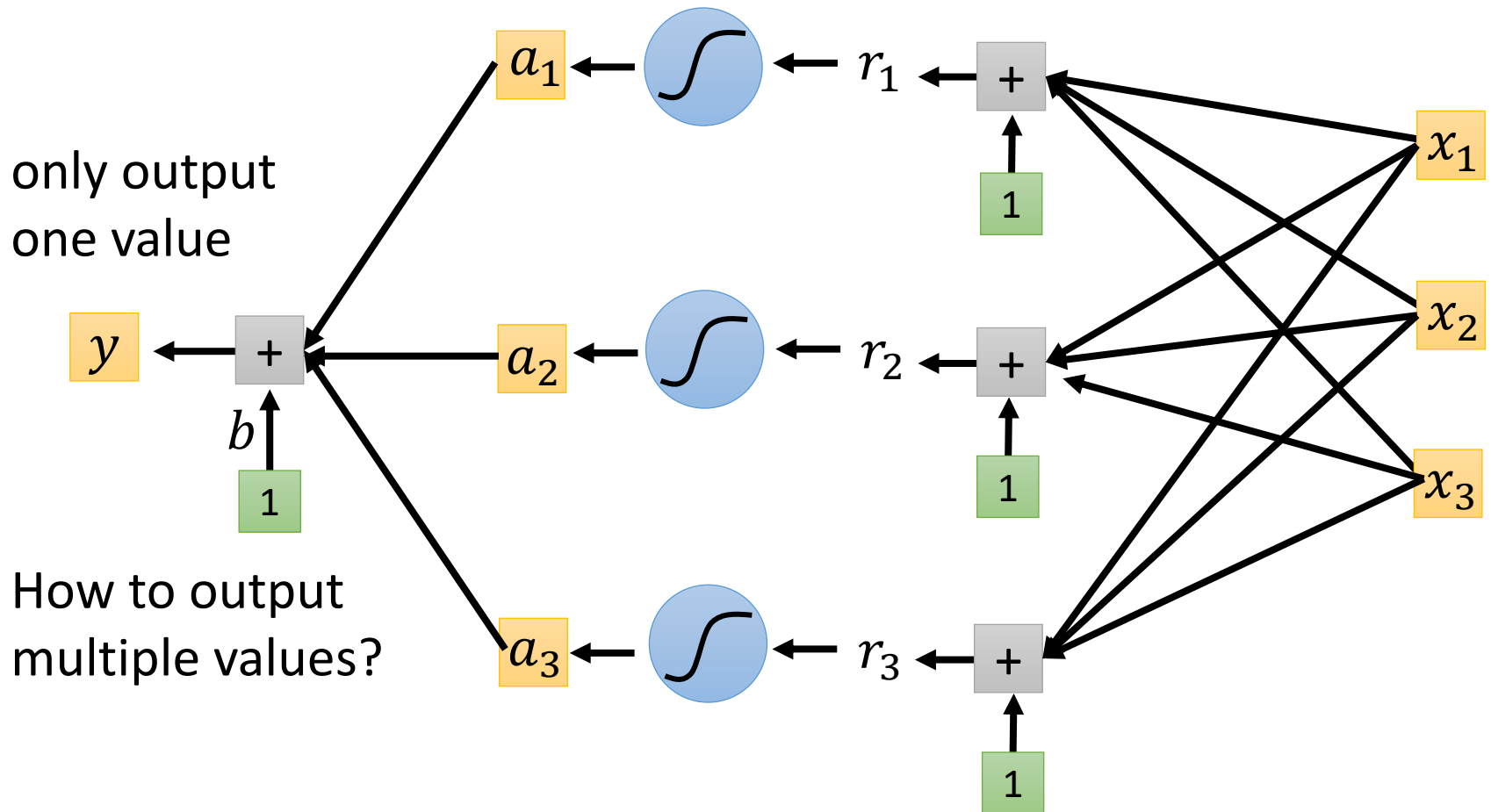
$$\hat{y} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

or

$$\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$$

or

$$\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$



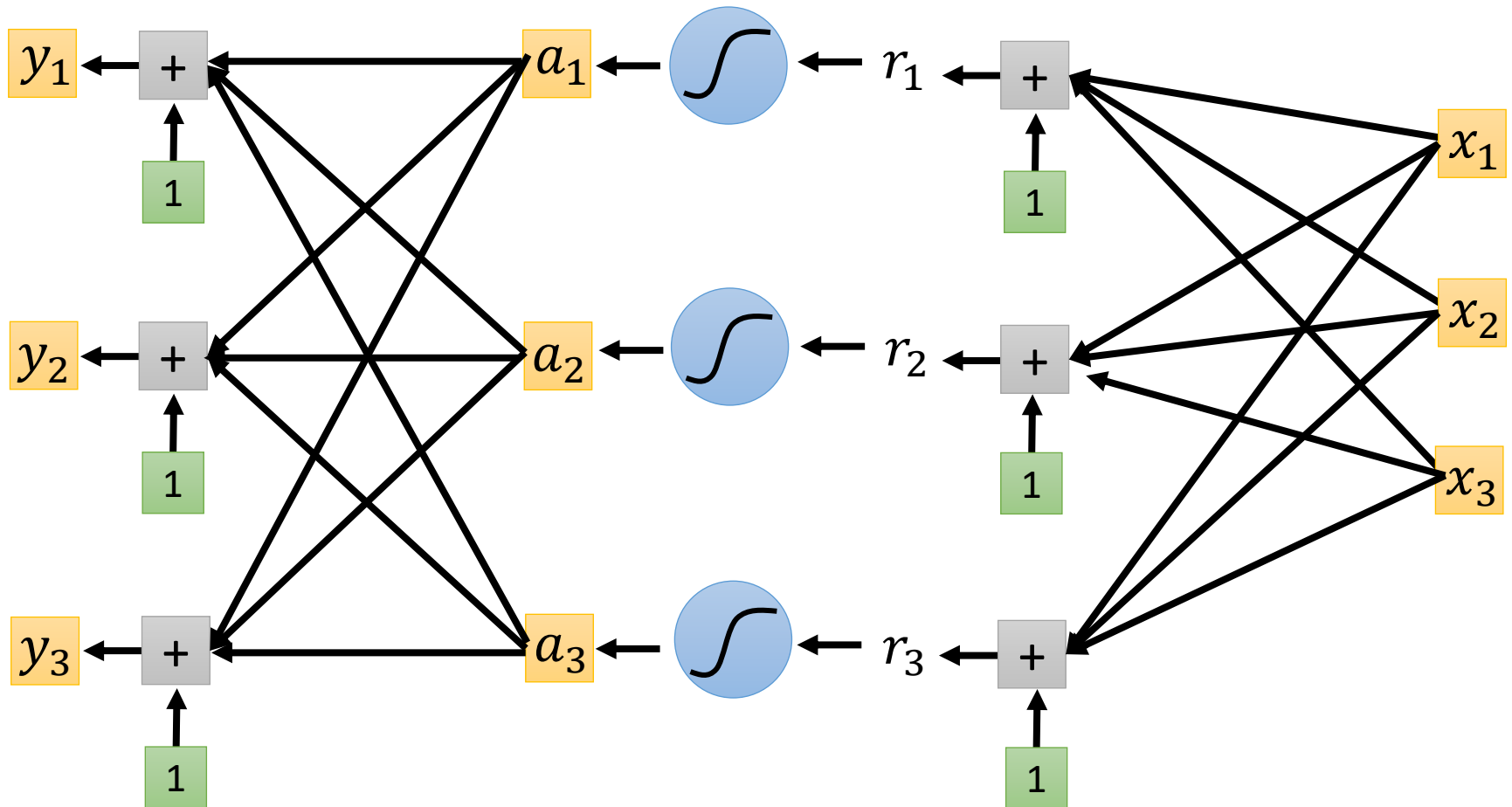
# Class as one-hot vector

Class 1

Class 2

Class 3

$$\hat{y} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \quad \text{or} \quad \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \quad \text{or} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$



## Regression

label

$$\hat{y} \longleftrightarrow y = b + c^T \sigma( b + W x )$$

feature

## Classification

feature

$$y = b' + W' \sigma( b + W x )$$

label

$$\hat{y} \longleftrightarrow y' = \text{softmax}( y )$$

0 or 1      Make all values between 0 and 1      Can have any value

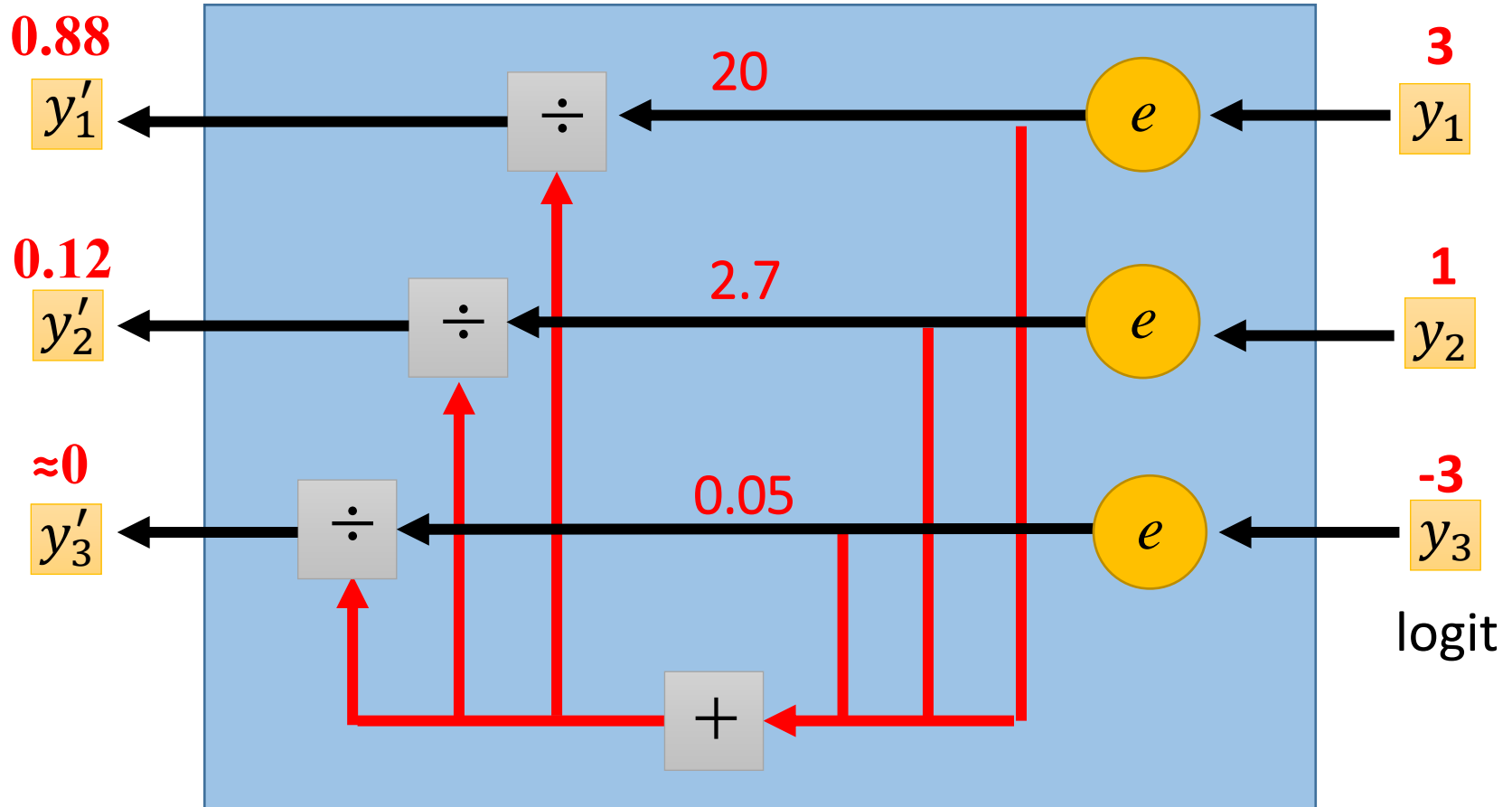
# Soft-max

$$y'_i = \frac{\exp(y_i)}{\sum_j \exp(y_j)}$$

- $1 > y'_i > 0$
- $\sum_i y'_i = 1$

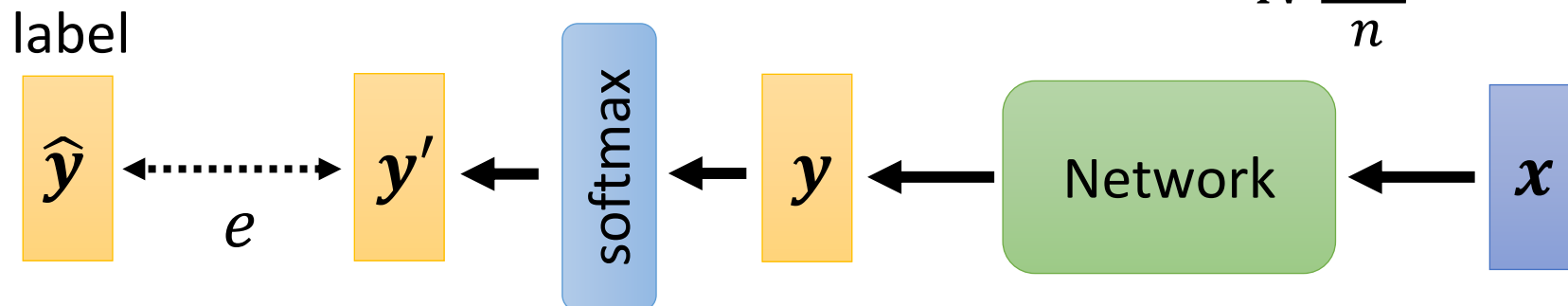
Softmax

How about **binary classification**? ☺



# Loss of Classification

$$L = \frac{1}{N} \sum_n e_n$$



Mean Square Error (MSE)

$$e = \sum_i (\hat{y}_i - y'_i)^2$$

在pytorch中，call cross entropy就會自動幫你加上softmax

Cross-entropy

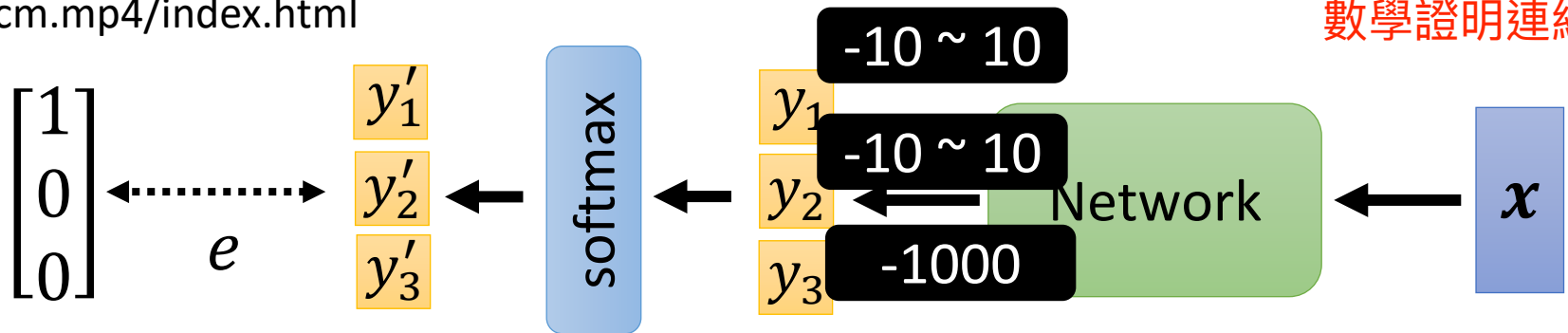


$$e = - \sum_i \hat{y}_i \ln y'_i$$

**Minimizing cross-entropy** is equivalent to **maximizing likelihood**.

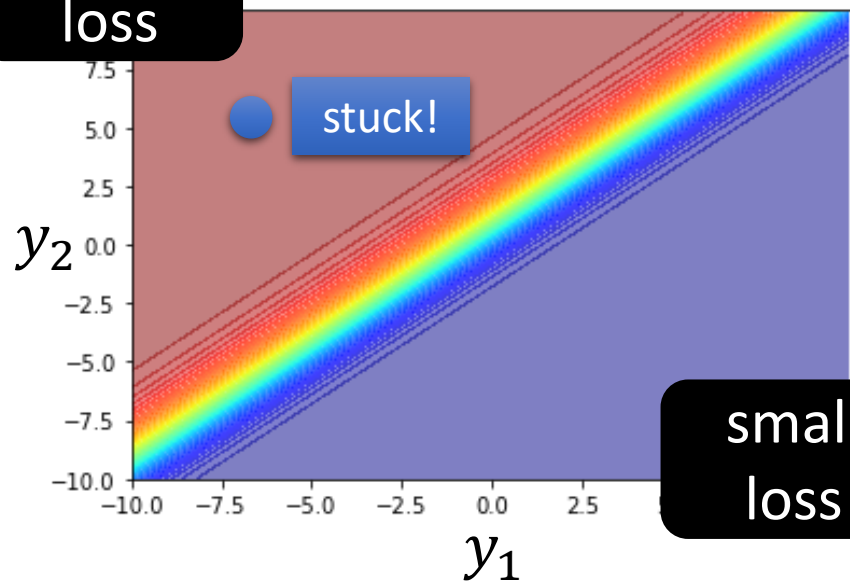


數學證明連結

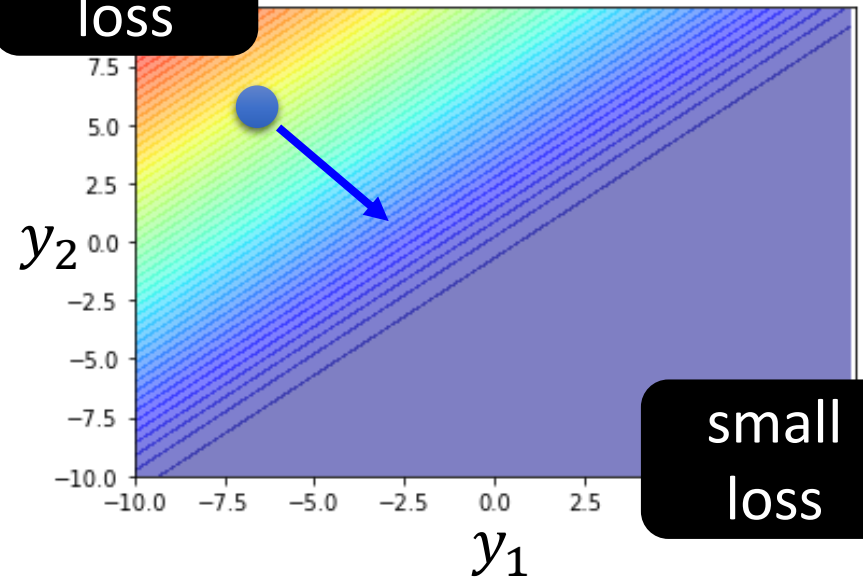


MSE很大時，他的斜率會很小？

large loss Mean Square Error (MSE)



large loss Cross-entropy



Changing the loss function can change the difficulty of optimization.