

CS573 Data Privacy and Security

Location Privacy

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Outline

- What is Location Privacy
- Basic Techniques
 - Private Information Retrieval
 - Probabilistic Approach
 - Stationary
 - Temporal



What is Location Privacy

- Location Based Services (LBS)
 - Yelp, Google+, facebook, Instagram, Twitter...
 - Restaurant check-in, finding the nearest gas station, navigation, tourist city guide, ...
- Location Sharing
 - Find Friends, Find my iphone, ...
- Location Based Social Networks
 - Foursquare, Swarm
- Risks?
 - Give your location data for the service



Location Privacy

- Risks
 - Give your location traces to Google, Apple or other service providers
 - Enable malicious apps to know your locations
 - <http://www.cnbc.com/2016/08/01/pokemon-go-and-other-apps-are-putting-your-privacy-at-risk.html>
 - Sharing in Facebook, but available throughout internet
 - Locations may be leaked to other attackers through network
 - Physical danger, e.g. <http://pleaserobme.com/>
- User's choices
 - Use LBS, give up privacy
 - Or preserve privacy, give up the LBS
 - Can we achieve the two goals: utility and privacy?

Features of Location Privacy

- Vs. Standard Differential Privacy
 - Differential Privacy: the outputs are similar whether a user opts in or out
 - For LBS, only one user
- Data Type
 - Standard Differential Privacy: tuples in Database
 - Location Privacy: where a user is
- Location data is only two-dimensional
 - Or at most three-dimensional

Techniques

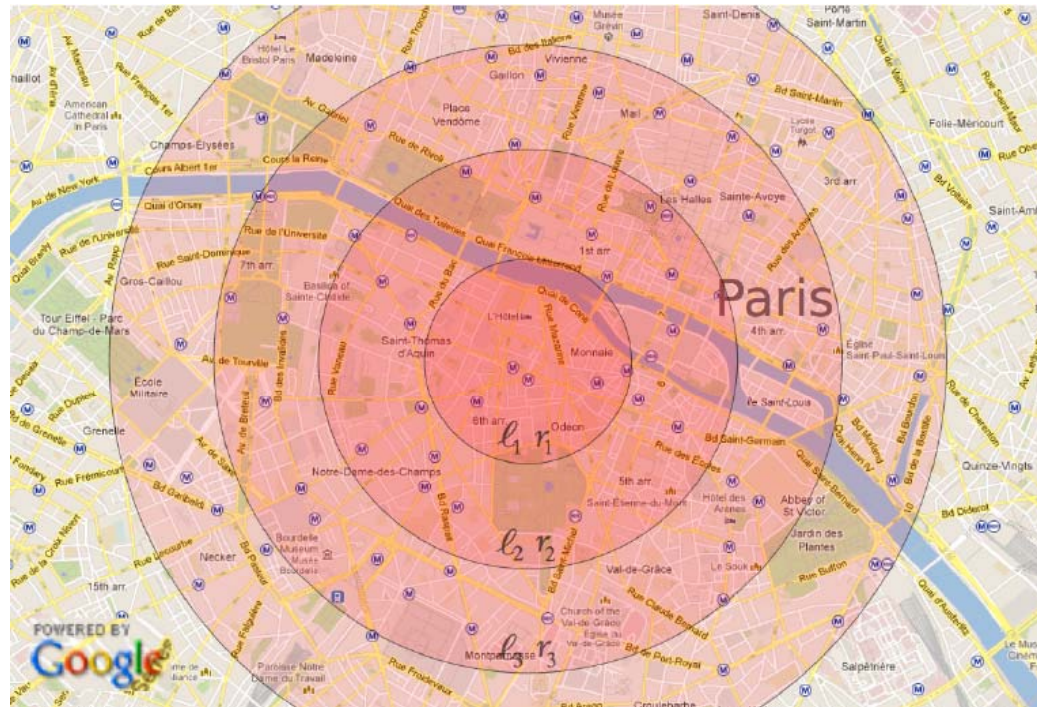
- Encryption-based Techniques
 - Private Information Retrieval
- Probabilistic Techniques
 - Location obfuscation, location cloaking
 - Location generalization
- Continuous Protection
 - Temporal correlations

Private Information Retrieval (PIR)

- Allow user to query database while hiding the identity of the data-items she is querying.
 - What is the nearest restaurant to me?
 - Send a query to the server
 - Get a restaurant from the server
- Computational PIR
 - Homomorphic encryption
- Intensive Computational Cost

Probabilistic Techniques

- Spatial Cloaking/Location Generalization
 - Instead of sending the exact location to the service providers, a user can send a “general area”.



Location Obfuscation

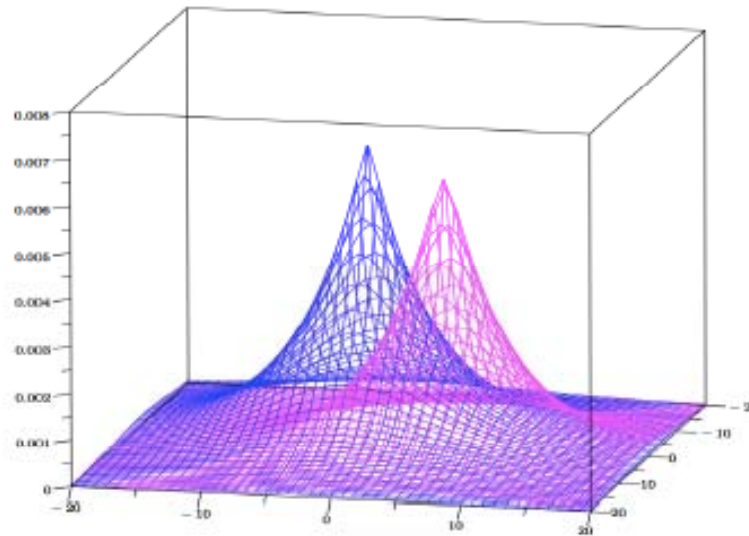
- Location Obfuscation
 - Instead of sending the exact location to the service providers, a user can send a “noisy” location.
 - Essentially, similar to spatial cloaking.
 - With the “general area”, a point can be randomly chosen to represent the “noisy” location.
 - The posterior probability of the “noisy” location will be the same as the “general area”. Can you prove it?

Probabilistic Techniques

- Privacy Guarantee
 - Uniform distribution in a circle
 - Uniform distribution in a polygon
 - Laplace distribution
 - Other distributions: 2D Gaussian distribution
- The trade-off between utility and privacy
 - What is the expected distance between the noisy location and the real location?
 - How much extra information does the noisy location give to attackers?
 - Can you derive the above distance function and the privacy function?

Geo-indistinguishability

- Geo-indistinguishability
 - A “differentially private” cloaking method
 - Based on the 2D Laplace distribution
 - Randomly draw a point from the distribution



Geo-indistinguishability

- Definition
 - $\Pr(z | x) \leq e^{\epsilon} \Pr(z | x')$
 - Where x and x' are any two locations in a circle with a radius r , z is the noisy location
- Features
 - Location data: x and x' are two points on a map
 - Neighboring databases: any points in the circle
 - Protection: indistinguishability in the circle

Geo-indistinguishability

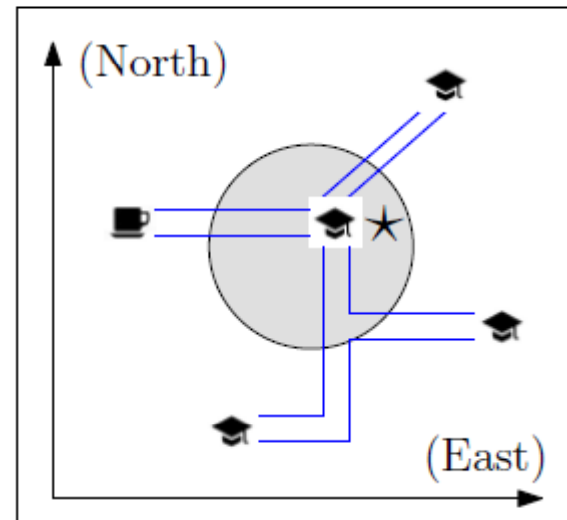
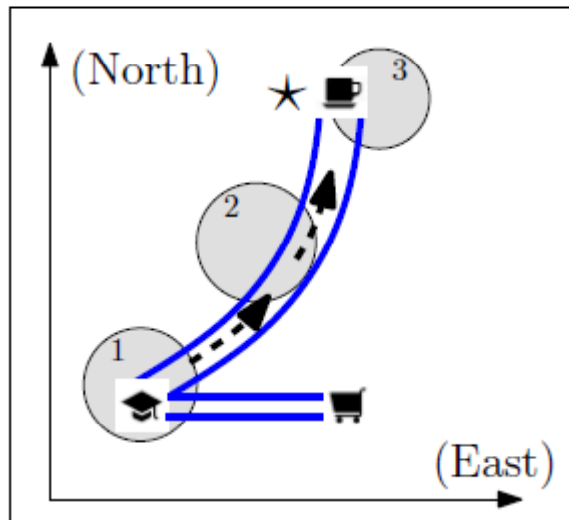
- Geo-indistinguishability
 - How to prove the privacy?

$$D_\epsilon(x_0)(x) = \frac{\epsilon^2}{2\pi} e^{-\epsilon d(x_0, x)}$$

- How much differential privacy can it provide?
- Open question:
 - Can you come up with a better sampling algorithm than the paper (Geo-indistinguishability ,CCS13)

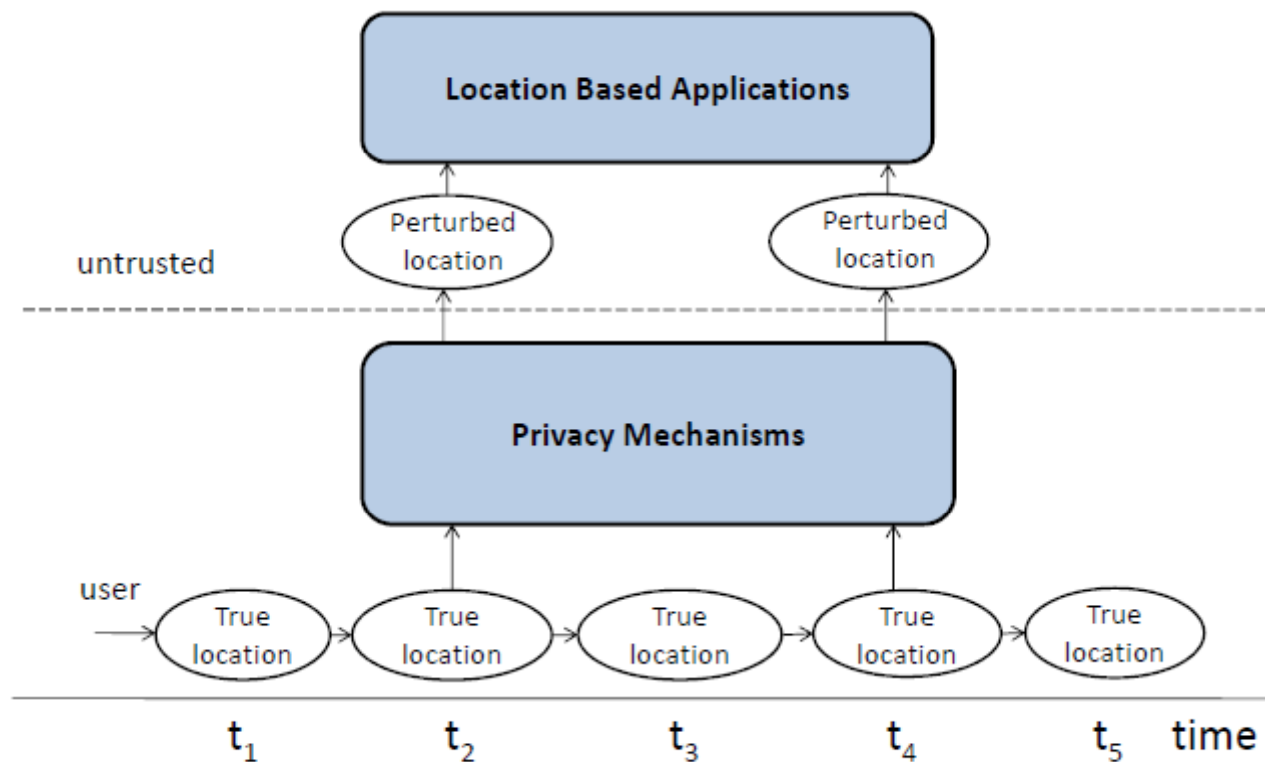
Continuous Approach

- Potential problems of the cloaking algorithms at stationary timestamps.
 - Not private in a period of time.
 - Examples:



Continuous Approach

- Location Release over time

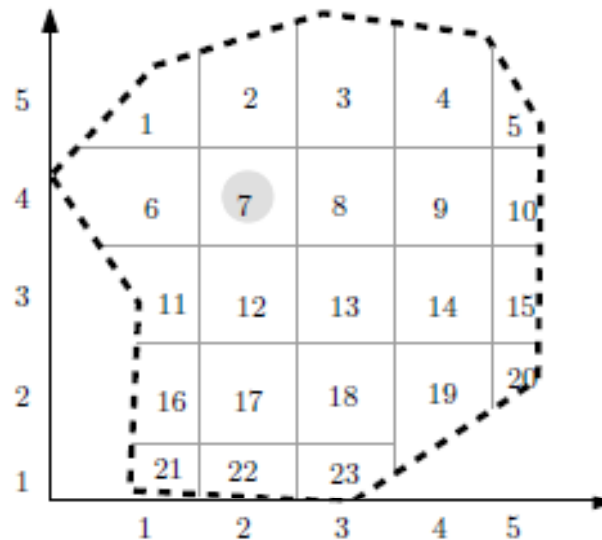


Continuous Approach

- Temporal Correlations
 - Road network
 - Moving patterns of a user
 - Example:
 - Given that Alice is at MSC building now, she may go to Starbucks with probability 0.3, DUC with probability 0.3, and library with probability 0.4.
- How to describe such correlations?
 - A common method is to use Markov model

Markov Model

- Markov Model
 - Coordinate System



$$\mathbf{u} = \mathbf{s}_7 = [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ \dots \ 0]$$
$$\mathbf{x} = [2, 4]^T \text{ with } x[1] = 2 \text{ and } x[2] = 4$$

Markov Model

- Markov Model
 - Transition Matrix
 - A matrix M denotes the probabilities that a user moves from one location to another
 - $M_{\{i,j\}}$ is the probability of moving from location i to location j .
 - $M_{\{i,j\}}$ is the element of i th row and j th column.

Markov Model

- Markov Model
 - Emission Probability
 - Given the real location i , what is the probability distribution of the noisy locations?

$$Pr(\mathbf{z}_t | \mathbf{u}_t^* = \mathbf{s}_i)$$

- Inference and Evolution

$$\mathbf{p}_t^+[i] = Pr(\mathbf{x}_t = \mathbf{s}_i | \mathbf{z}_t) = \frac{Pr(\mathbf{z}_t | \mathbf{x}_t = \mathbf{s}_i) \mathbf{p}_t^- [i]}{\sum_j Pr(\mathbf{z}_t | \mathbf{x}_t = \mathbf{s}_j) \mathbf{p}_t^- [j]}$$

Markov Model

- Derive the possible locations at current timestamp
 - Bayesian inference using the previously released locations.
 - A set of possible locations can be generated.
- Only protect the true location within this set of possible locations.
 - Recall the definition of “neighboring databases”
 - What is the new neighboring databases here?

Extended Differential Privacy

Definition (Differential Privacy)

At any timestamp t , a randomized mechanism \mathcal{A} satisfies ϵ -differential privacy on δ -location set if, for any output \mathbf{z}_t and any two locations \mathbf{x}_1 and \mathbf{x}_2 in δ -location set, the following holds:

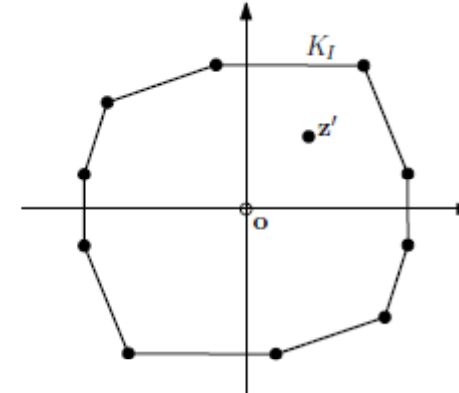
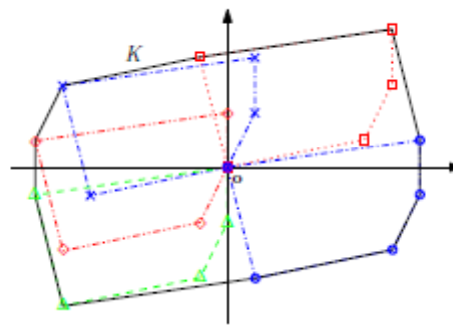
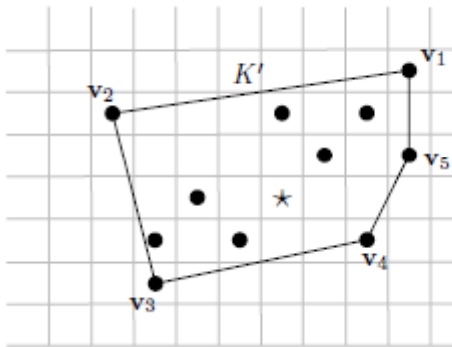
$$\frac{Pr(\mathcal{A}(\mathbf{x}_1) = \mathbf{z}_t)}{Pr(\mathcal{A}(\mathbf{x}_2) = \mathbf{z}_t)} \leq e^\epsilon$$

Intuition

the released location \mathbf{z}_t (observed by the adversary) will not help an adversary to differentiate any instances in δ -location set.

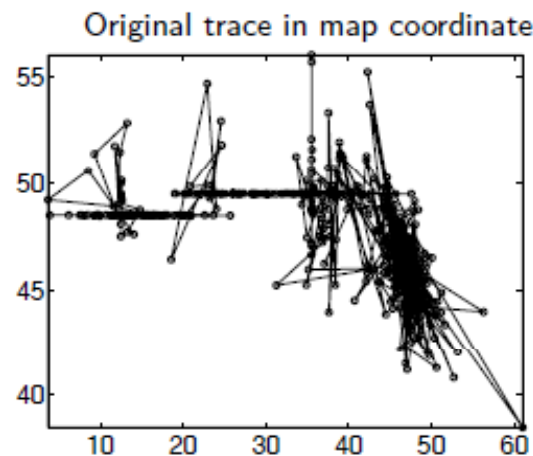
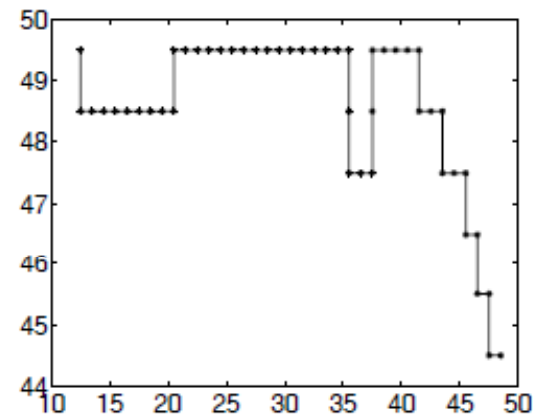
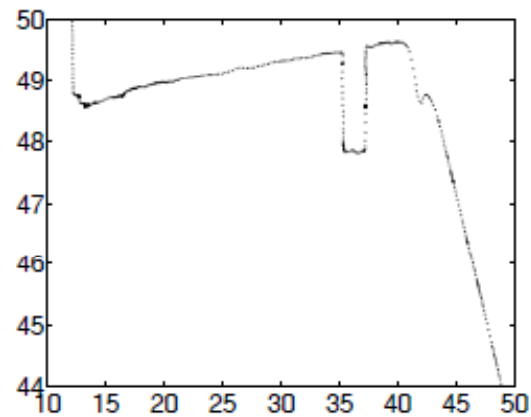
Probability Design

- Design a distribution on the set of possible locations.

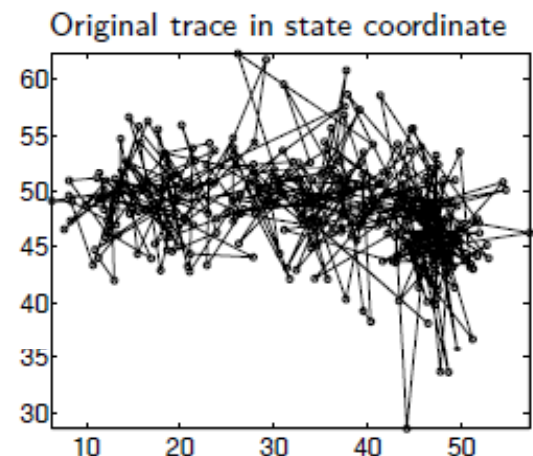


Continuous Released Locations

- Example: Released “Noisy” Locations



PIM released trace



LM released trace

References

- Geo-indistinguishability: differential privacy for location-based systems, CCS, 2013
- Protecting Locations with Differential Privacy under Temporal Correlations, CCS, 2015
- Quantifying Location Privacy, IEEE SP 2011
- In-Network Trajectory Privacy Preservation, ACM Computing Surveys (CSUR) 2015