



# ***Master Course***

## ***Algorithms in Sequence Alignment***

### ***Lecture 7***

### ***Homology searching (1)***



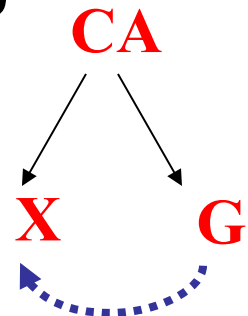
# Searching for similarities

- The main question: what is the function of the new gene?
- The “lazy” investigation without doing experiments:
  - Find a set of similar proteins
  - Identify similarities and differences
  - For long proteins it is often good to identify **domains** first and then compare the corresponding **(sub)sequences** separately
    - A domain is a unit of function
    - Multi-domain proteins have a compound function

# Inferring homology from similarity

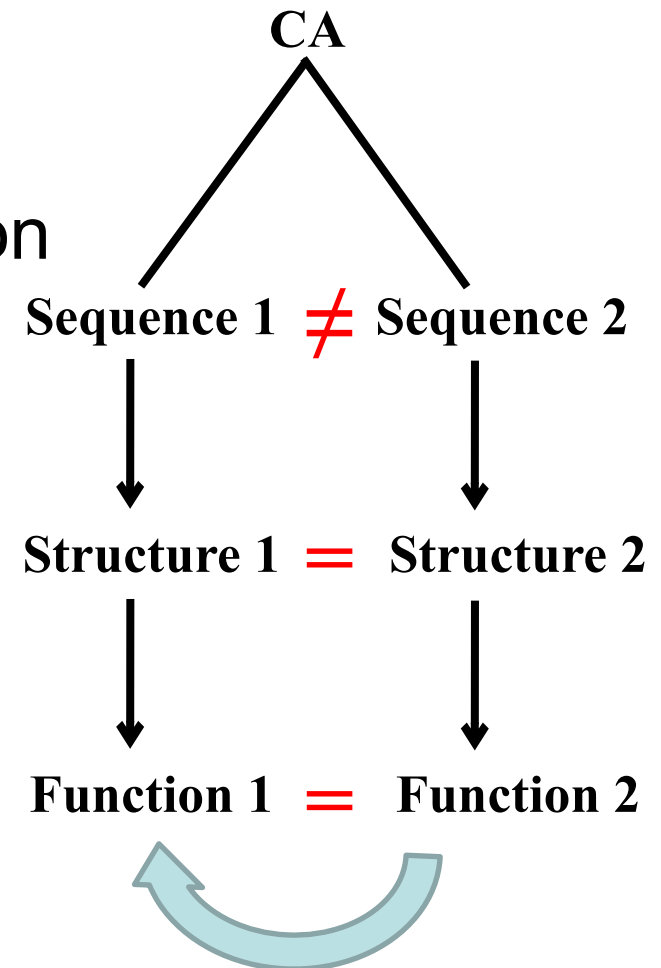
- Homology: sharing a common ancestor
  - a binary property (yes/no)
- Common ancestry makes it more likely that genes share the same function
  - It's a nice tool:

When (a known gene) *G* is *homologous* to (an unknown gene) *X*, we gain a lot of information on *X* by transferring what we know about *G*



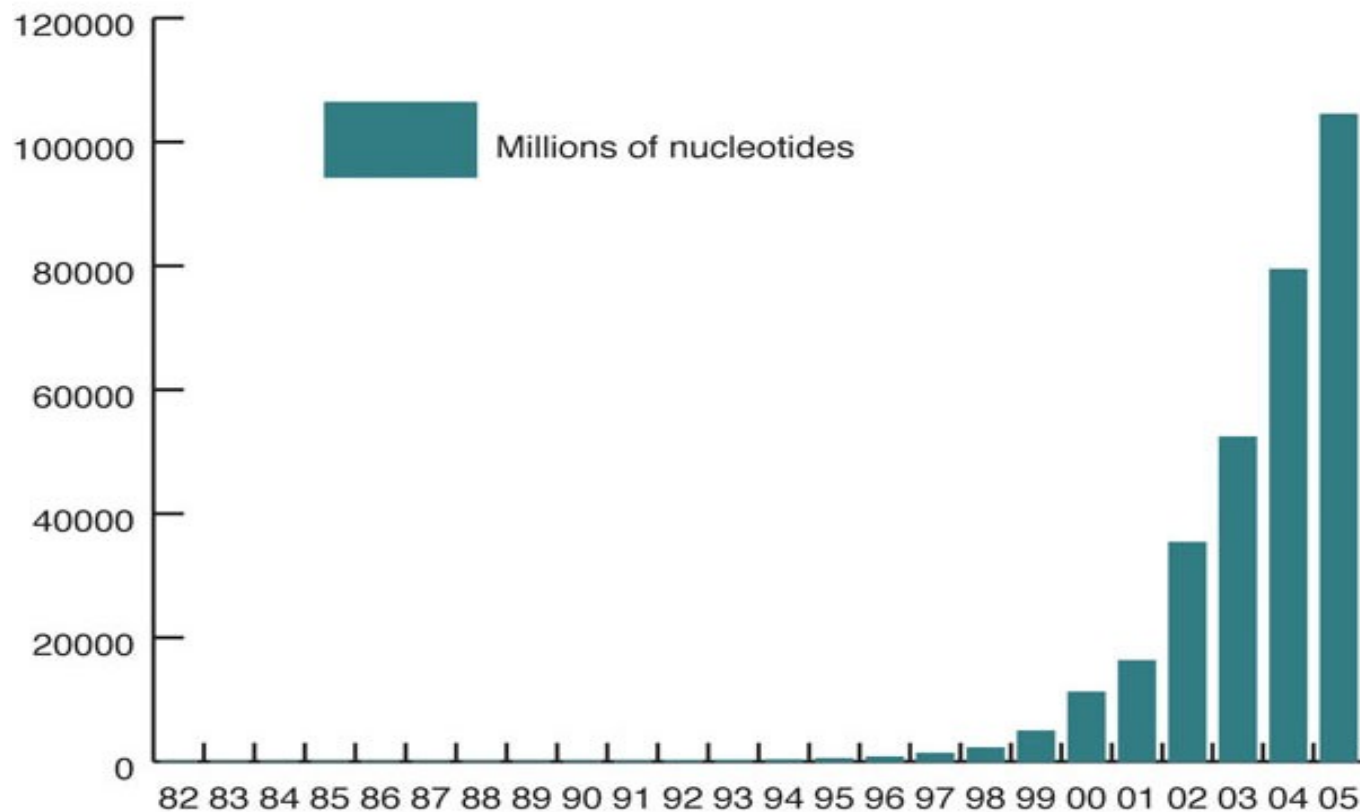
# Can we just transfer information about structure and/or function?

- Structure (and function) more conserved than sequence
- Sequence  $\rightarrow$  structure  $\rightarrow$  function
- So, if the sequences already tell us it's the same thing (homolog), then certainly the structures and functions are supposed to be the same.
- This works most of the time, but there are some cases where likely homology does not bear out.



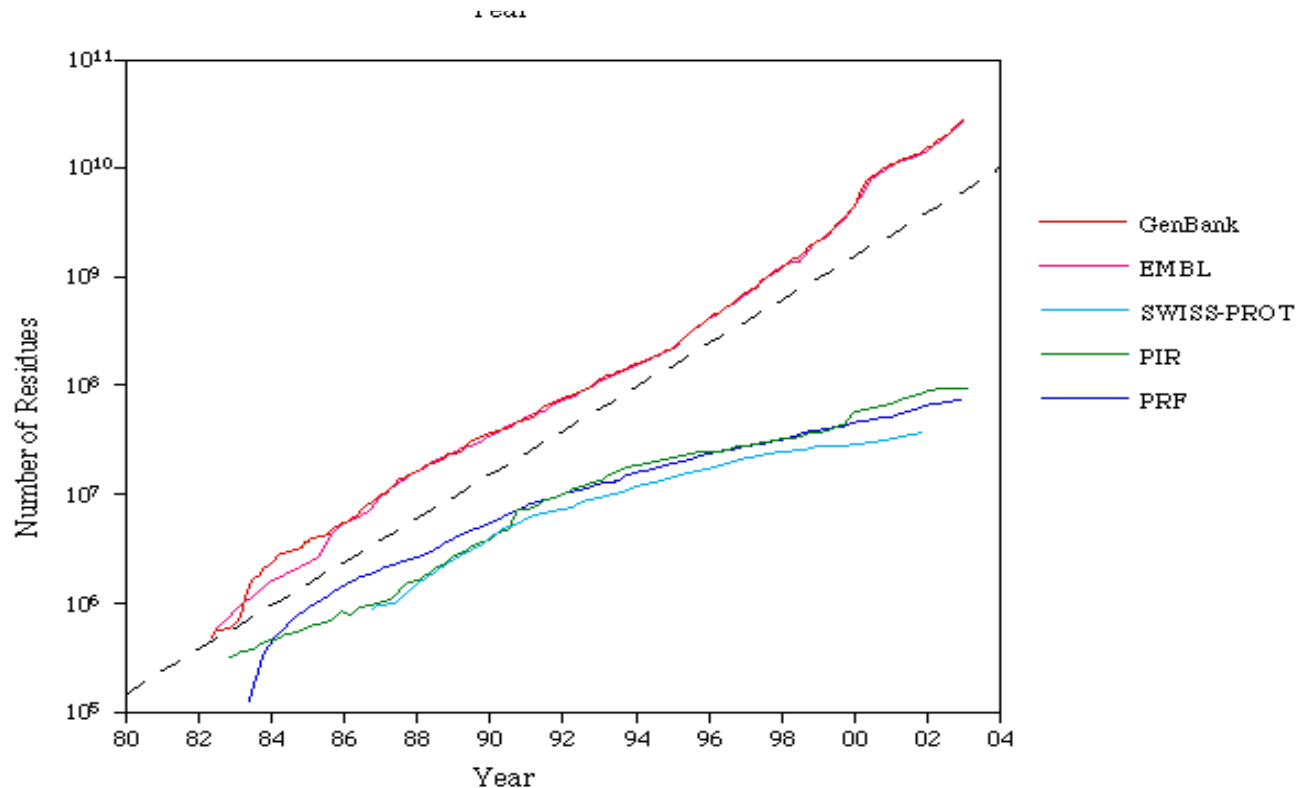
# Sequence searching - challenges

- Exponential growth of databases



# Sequence searching - challenges

- **Exponential growth of databases**



# Bioinformatics justification



- ***“Mind the Gap”***
- There are far more sequence data than structural/functional data
- We need to fill this gap by analysis and prediction pipelines

# Sequence searching - definition

- Task:
  - Query: **short**, new sequence (~1000 residues)
  - Database (searching space): **very many** sequences
  - Goal: find seqs **related** to query
- We want:
  - **fast tool**
  - **primarily a filter**: most sequences will be unrelated to the query
  - **fine-tune** the alignment later



# Heuristic Alignment

## Motivation

- heuristic methods perform **fast approximation** of dynamic programming
  - FASTA [Pearson & Lipman, 1988]
  - BLAST [Altschul *et al.*, 1990]
- the dynamic programming algorithm has complexity  $O(mn)$ , which is too slow for large databases with high query traffic

# Heuristic Alignment Motivation

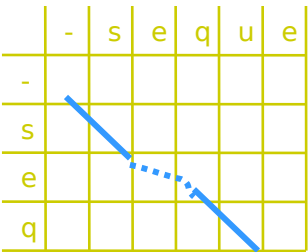
- consider the task of searching SWISS-PROT against a query sequence:
  - say our query sequence is 362 amino-acids long
  - SWISS-PROT release 38 contains 29,085,265 amino acids
- finding local alignments via dynamic programming would entail  $O(10^{10})$  matrix operations
- many servers handle thousands of such queries a day (NCBI  $> 10^6$ /day)
- Using the DP algorithm for this is clearly prohibitive
- Note: each database search can be sped up by 'trivial **parallelisation**' (each query-db comparison is independent)

# Heuristic Alignment

- Today: the methods **BLAST**, **PSI-BLAST** are discussed to show you a few of the tricks people have come up with to make alignment and database searching fast, while not losing too much quality.
- The earlier method **FASTA** is also discussed as a reference

# What is BLAST

- **B**asic **L**ocal **A**lignment **S**earch **T**ool
- Bad news: it is only **a heuristic**
  - Heuristics: A rule of thumb that often helps in solving a certain class of problems, but makes no guarantees.  
*Perkins, DN (1981) The Mind's Best Work*
  - Also see <http://en.wikipedia.org/wiki/Heuristic>
- Basic idea:
  - Discard putatively unrelated sequences fast
  - High scoring segments have **well conserved** (almost identical) part
  - As well-conserved segments are identified, **extend these** to the *real* alignment



# What does *well conserved* mean in BLAST?

- BLAST works with *k-words* (words of length  $k$ )
  - $k$  is a parameter
  - different for DNA ( $>10$ ) and proteins (2..4), default  $k$  values are 11 and 3, resp.
- word  $w_1$  is *T-similar* to  $w_2$  if the **sum of pair scores** is at least  $T$  (e.g.  $T=8$ )

| <i>Similar 3-words</i> |   |   |   |               |
|------------------------|---|---|---|---------------|
| $W_1 :$                | R | K | P |               |
| $W_2 :$                | R | R | P |               |
| Score :                | 5 | 2 | 7 | $\Sigma = 14$ |

# BLAST algorithm

## 3 basic steps

- 1) Preprocess
- 2) Scan
- 3) Extend

- 1) **Preprocess** the query sequence: extract all the *k*-words
- 2) **Scan** for *T*-similar matches in database (fast step)
- 3) **Extend** these to alignments (slow step)

# BLAST, Step 1: Preprocess the query

- 1) Preprocess
- 2) Scan
- 3) Extend

- Take the query (e.g. LVNRKPVVP)
- **Chop** it into overlapping k-words (k=3 in this case)

|        |           |
|--------|-----------|
| Query: | LVNRKPVVP |
| Word1: | LVN       |
| Word2: | VNR       |
| Word3: | NRK       |
| ...    |           |

- For each word **find all similar words** (scoring at least  $T$ )
  - Build a table of similar words for each query 3-word (3-mer)
- E.g. for RKP the following 3-words are similar:  
QKP   KKP   RQP   REP   RRP   RKP

# BLAST step 1: Determining Query Words

- Given:
  - query sequence: **QLNFSAGW**
  - word length  $w = 3$  (Blast default)
  - word score threshold  $T = 8$
- Step 1.1: determine all words of length  $w$  in query sequence

**QLN LNF NFS FSA SAG AGW**



# BLAST step 1: Determining Query Words

- Step 1.2: determine all words that score at least  $T$  when compared to a word in the query sequence:

*words from      query words w/  $T=8$   
sequence*

|     |                                   |
|-----|-----------------------------------|
| QLN | QLN=15, ELN=12, HLN=10, QMD=9,... |
| LNF | LNF=16, LDF=11, FNY=9, LDY=8, ... |
| NFS | NFS=16, NYS=13, AFS=8, DFT=8,...  |
| ... |                                   |
| SAG | none                              |
| ... |                                   |

**Scoring is done using the BLOSUM62 amino acid exchange matrix**

# BLAST step 1: Determining Query Words

- Step 1.2: determine all  $T$  words for QLN

```

Word           QLN  Query
Alignment:    |||
              YYY
Database

```

*words w/  $T=8$  :*

# QLN

QLN  $5+4+6 = 15$

ELN  $2+4+6 = 12$

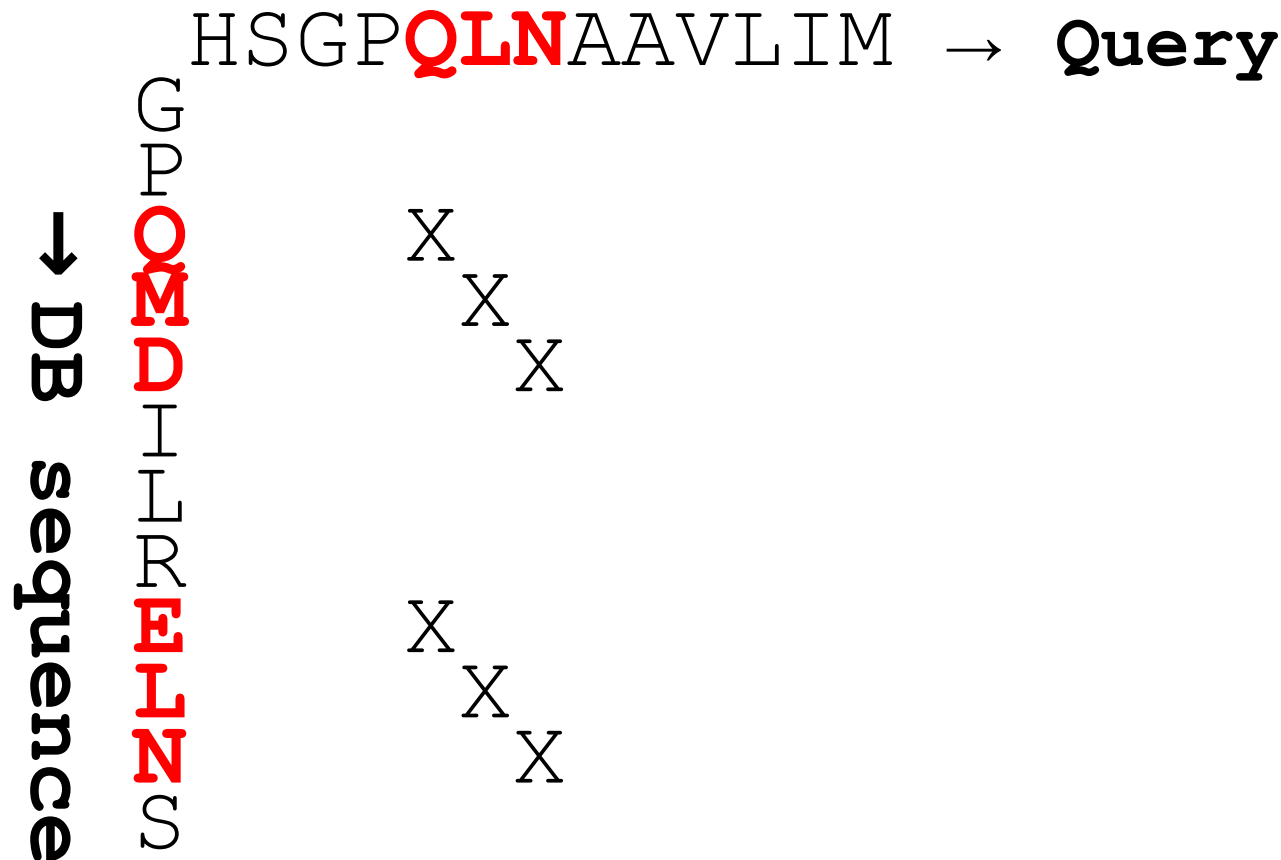
# Algorithms in Sequence Analysis

| A |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |
|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|
| R | -1 | 5  |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |
| N | -2 | 0  | 6  |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |
| D | -2 | -2 | 1  | 6  |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |
| C | 0  | -3 | -3 | -3 | 9  |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |
| Q | -1 | 1  | 0  | 0  | -3 | 5  |    |    |    |    |    |    |    |    |    |    |    |    |    |   |
| E | -1 | 0  | 0  | 2  | -4 | 2  | 5  |    |    |    |    |    |    |    |    |    |    |    |    |   |
| G | 0  | -2 | 0  | -1 | -3 | -2 | -2 | 6  |    |    |    |    |    |    |    |    |    |    |    |   |
| H | -2 | 0  | 1  | -1 | -3 | 0  | 0  | -2 | 8  |    |    |    |    |    |    |    |    |    |    |   |
| I | -1 | -3 | -3 | -3 | -1 | -3 | -3 | -4 | -3 | 4  |    |    |    |    |    |    |    |    |    |   |
| L | -1 | -2 | -3 | -4 | -1 | -2 | -3 | -4 | -3 | 2  | 4  |    |    |    |    |    |    |    |    |   |
| K | -1 | 2  | 0  | -1 | -3 | 1  | 1  | -2 | -1 | -3 | -2 | 5  |    |    |    |    |    |    |    |   |
| M | -1 | -1 | -2 | -3 | -1 | 0  | -2 | -3 | -2 | 1  | 2  | -1 | 5  |    |    |    |    |    |    |   |
| F | -2 | -3 | -3 | -3 | -2 | -3 | -3 | -3 | -1 | 0  | 0  | -3 | 0  | 6  |    |    |    |    |    |   |
| P | -1 | -2 | -2 | -1 | -3 | -1 | -1 | -2 | -2 | -3 | -3 | -1 | -2 | -4 | 7  |    |    |    |    |   |
| S | 1  | -1 | 1  | 0  | -1 | 0  | 0  | 0  | -1 | -2 | -2 | 0  | -1 | -2 | -1 | 4  |    |    |    |   |
| T | 0  | -1 | 0  | -1 | -1 | -1 | -1 | -2 | -2 | -1 | -1 | -1 | -1 | -2 | -1 | 1  | 5  |    |    |   |
| W | -3 | -3 | -4 | -4 | -2 | -2 | -3 | -2 | -2 | -3 | -2 | -3 | -1 | 1  | -4 | -3 | -2 | 11 |    |   |
| Y | -2 | -2 | -2 | -3 | -2 | -1 | -2 | -3 | 2  | -1 | -1 | -2 | -1 | 3  | -3 | -2 | -2 | 2  | 7  |   |
| V | 0  | -3 | -3 | -3 | -1 | -2 | -2 | -3 | -3 | 3  | 1  | -2 | 1  | -1 | -2 | -2 | 0  | -3 | -1 | 4 |
|   | A  | R  | N  | D  | C  | Q  | E  | G  | H  | I  | L  | K  | M  | F  | P  | S  | T  | W  | Y  | V |

**Scoring is done using the BLOSUM62 amino acid exchange matrix**

# BLAST step 1: Determining Query Words

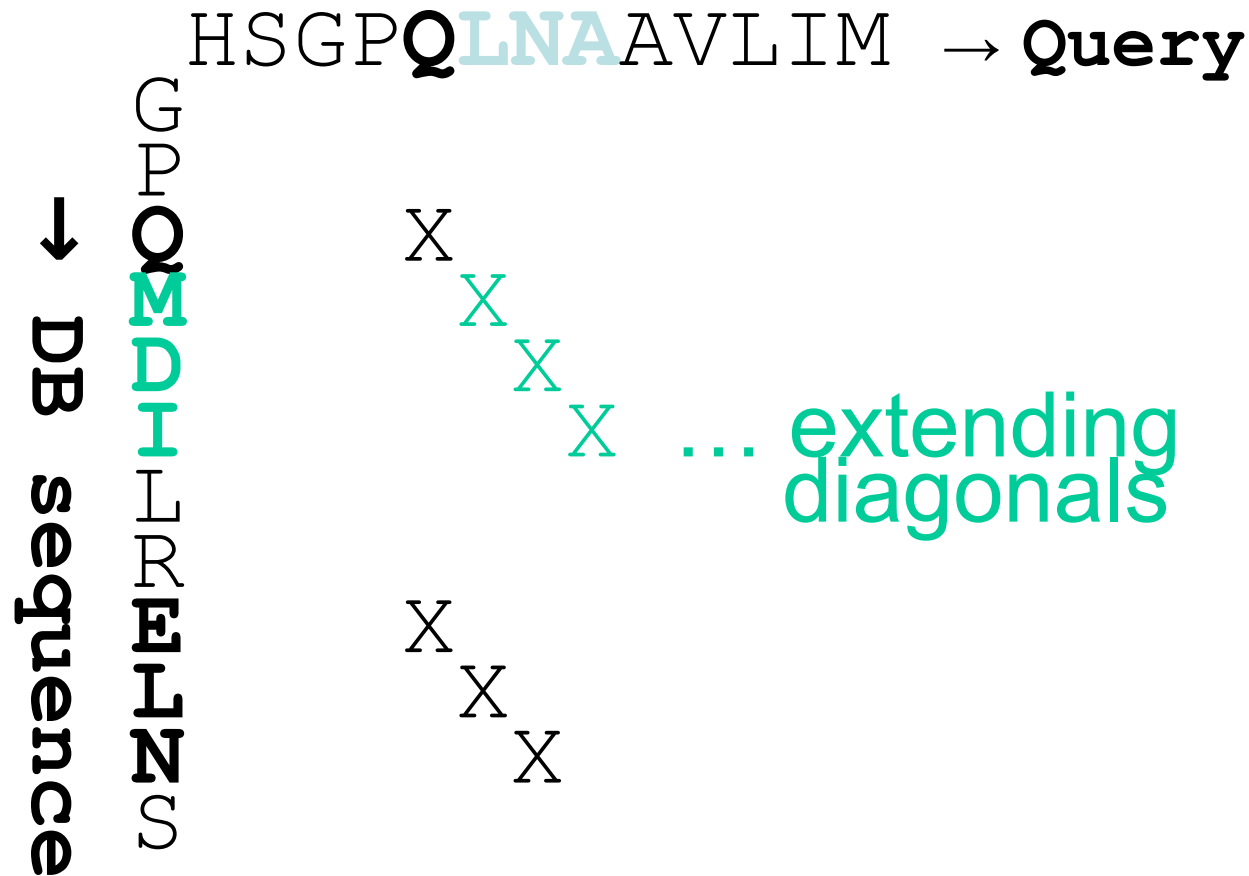
For every neighbor of each k-mer, the naive way is to look all the k-mers in the database and check whether the neighbor matches anything



Without a clever algorithm, one would (for each 3-mer in the query sequence) have to look at every 3-mer in the database sequence and check whether it is in the list of similar 3-mers for that query word. This would lead to  $O(N^2)$  computation steps, where  $N$  is the length of the DB sequence,

Query QLN: QLN=15, ELN=12, HLN=10, QMD=9,...which is too slow..

# BLAST step 1: Determining Query Words



Without a clever algorithm, one would (for each 3-mer in the query sequence) have to look at every 3-mer in the database sequence and check whether it is in the list of similar 3-mers for that query word. This would lead to  $O(N^2)$  computation steps, where  $N$  is the length of the DB sequence, which is too slow..

- 1) Preprocess
- 2) Scan
- 3) Extend

# Step 2: Scanning the Database with DFA (Deterministic Finite-state Automaton)

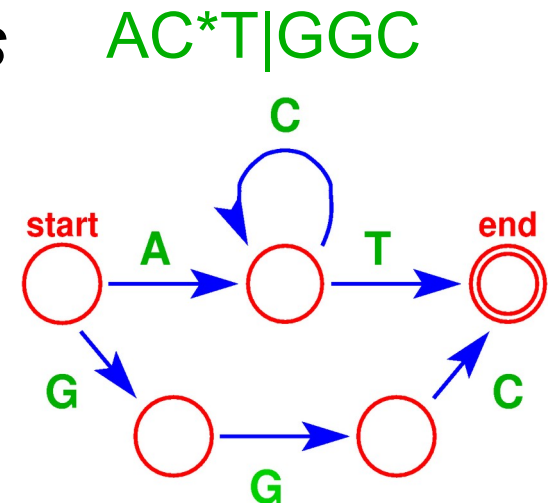
- search database for all occurrences of query words
- can be a massive task
- approach:
  - build a DFA (deterministic finite-state automaton) that recognizes all query words
  - run DB sequences through DFA
  - remember hits

- 1) Preprocess
- 2) Scan
- 3) Extend

# DFA

## Finite state machine

- abstract machine
- constant amount of memory (states)
- used in *computation* and *languages*
- recognizes *regular expressions*
  - `cp dmt*.pdf /home/john`

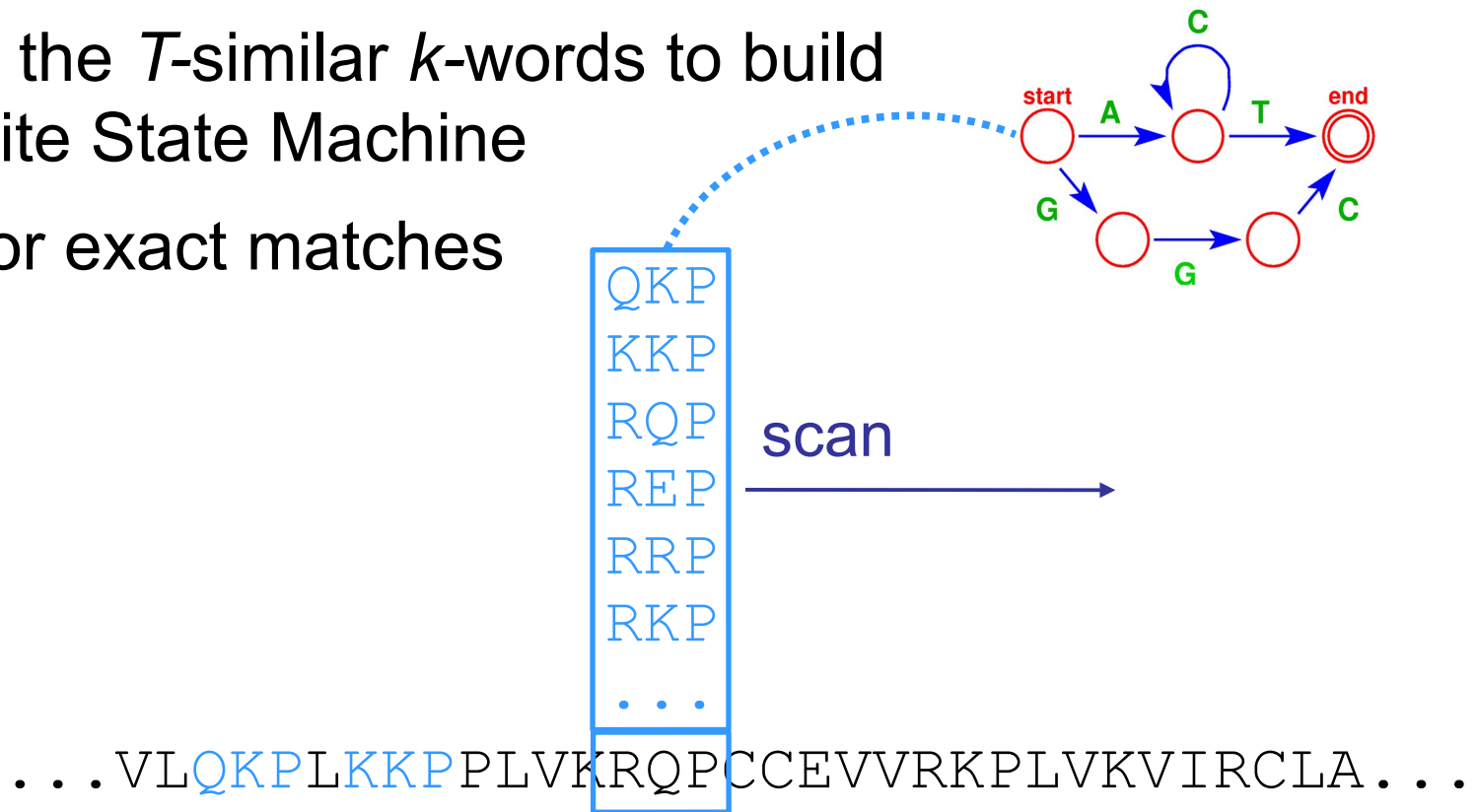


- 1) Preprocess
- 2) Scan
- 3) Extend

# BLAST, Step 2:

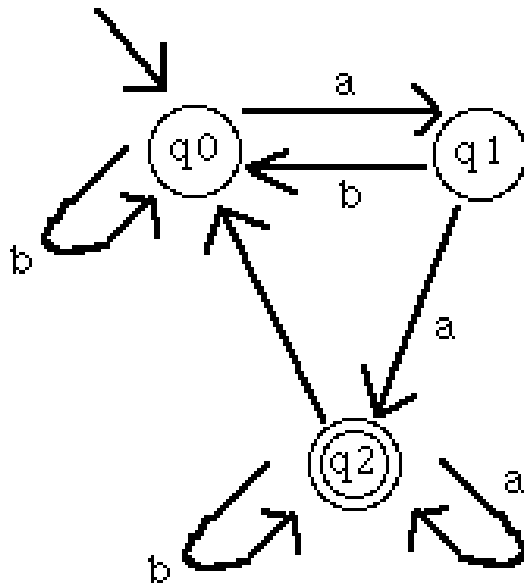
## Find “exact” matches with scanning

- Use all the  $T$ -similar  $k$ -words to build the Finite State Machine
- Scan for exact matches



# Scanning the Database - DFA

- 1) Preprocess
- 2) Scan
- 3) Extend



**Moore paradigm:** the alphabet is (a, b), the states are q0, q1, and q2, the start state is q0 (denoted by the arrow coming from nowhere), the only accepting state is q2 (denoted by the double ring around the state), and the transitions are the arrows. The machine works as follows. Given an input string, we start at the start state, and read in each character one at a time, jumping from state to state as directed by the transitions. When we run out of input, we check to see if we are in an accept state. If we are, then we accept. If not, we reject.

**Moore paradigm: accept/reject states**

**Mealy paradigm: accept/reject transitions**

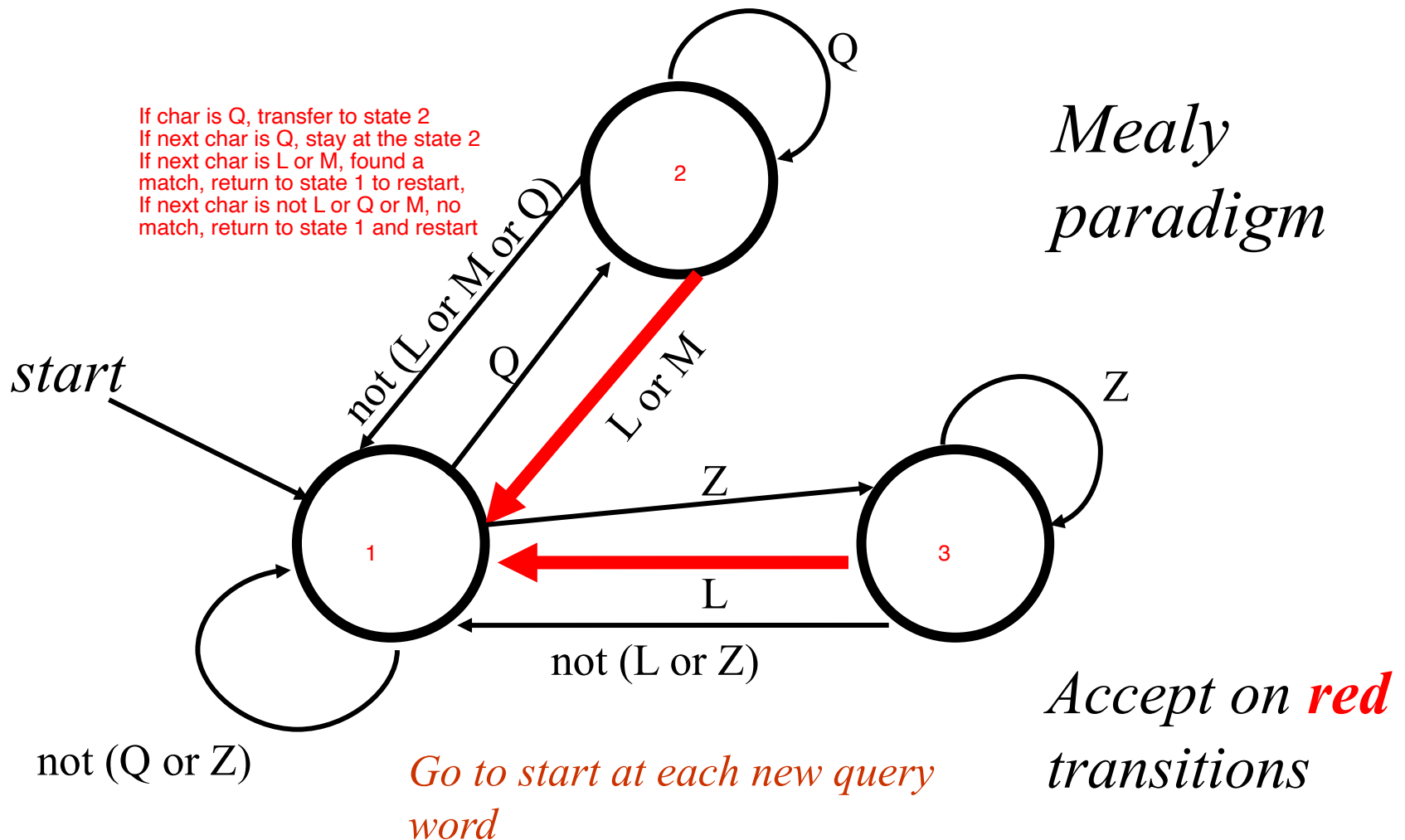
## Example (next 2 slides):

- consider a DFA to recognize the query words: QL, QM, ZL
- All that a DFA does is read strings, and output "accept" or "reject."
- use Mealy paradigm (accept on transitions) to save space and time



# a DFA to recognize the query words: QL, QM, ZL in a fast way

- 1) Preprocess
- 2) Scan
- 3) Extend



# a DFA to recognize the query words

- 1) Preprocess
- 2) Scan
- 3) Extend

- Having preprocessed the query sequence 3-word tables (T-similar words to each of the 3-words in the query sequence) using a Mealy machine and having stored the places in the query sequence where each of the 3-words start (a given 3-word can occur more than once in the sequence), BLAST can now very rapidly fill the alignment search matrix with query-sequence *versus* DB-sequence diagonals (ungapped alignments). This is done for each DB sequence.

- 1) Preprocess
- 2) Scan
- 3) Extend

# BLAST, Step 3: Extending “exact” matches

1. Classical BLAST (not in use anymore): two-way non-gapped extension
2. Current BLAST: two-hit method and extension using DP (Gapped-BLAST)

- 1) Preprocess
- 2) Scan
- 3) Extend

## BLAST, Step 3: Non-gapped extension (old BLAST)

- Having the list of matches (hits) we extend alignment in both directions

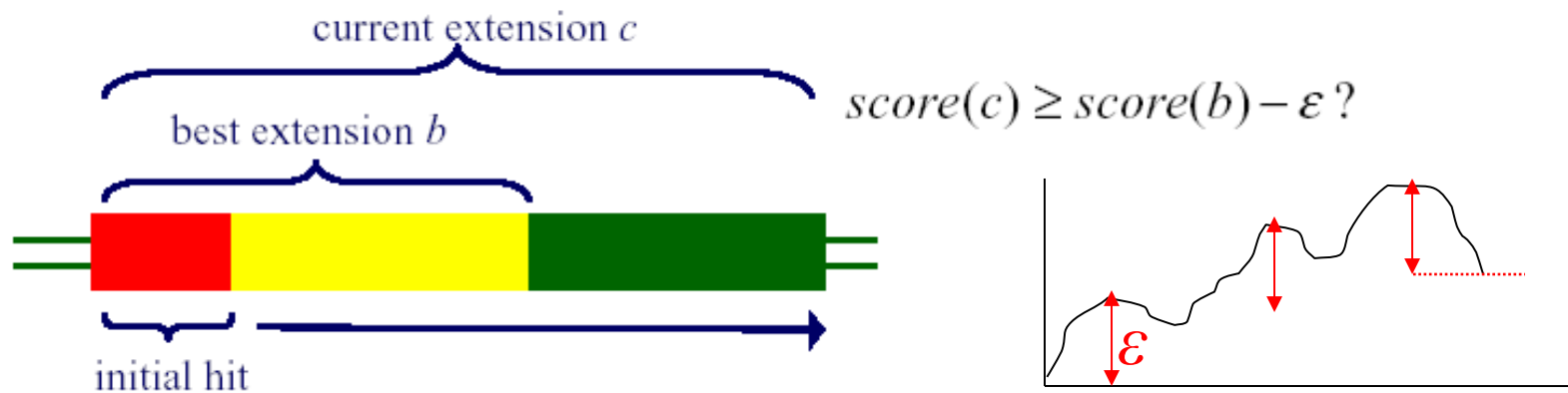
|            |    |   |    |          |          |          |   |    |    |
|------------|----|---|----|----------|----------|----------|---|----|----|
| Query:     | L  | V | N  | <b>R</b> | <b>K</b> | <b>P</b> | V | V  | P  |
| T-similar: |    |   |    | <b>R</b> | <b>R</b> | <b>P</b> |   |    |    |
| Subject:   | G  | V | C  | <b>R</b> | <b>R</b> | <b>P</b> | L | K  | C  |
| Score:     | -3 | 4 | -3 | 5        | 2        | 7        | 1 | -2 | -3 |

- ...till the sum of scores drops below some level X from the best known

# Step 3: Non-gapped extension (old BLAST)

- 1) Preprocess
- 2) Scan
- 3) Extend

- extend hits in both directions without allowing gaps
- terminate extension in one direction when score falls certain distance below best score for shorter extensions



- return segment pairs scoring at least a threshold score  $S$

## Step 3: Current BLAST - Extending hits

- two-hit method
- gapped BLAST

Altschul et al., *Nucleic Acids Research* 1997

# Two-Hit Method - justification

- old extension step typically accounts for 90% of BLAST's execution time
- key idea: do extension only when there are **two non-overlapping hits** on the same diagonal within distance  $A$  of each other ( $A = 40$  a.a.)
- to maintain sensitivity, lower  $T$  parameter
  - more single hits found
  - but only small fraction have associated 2nd hit

# The Two-Hit Method

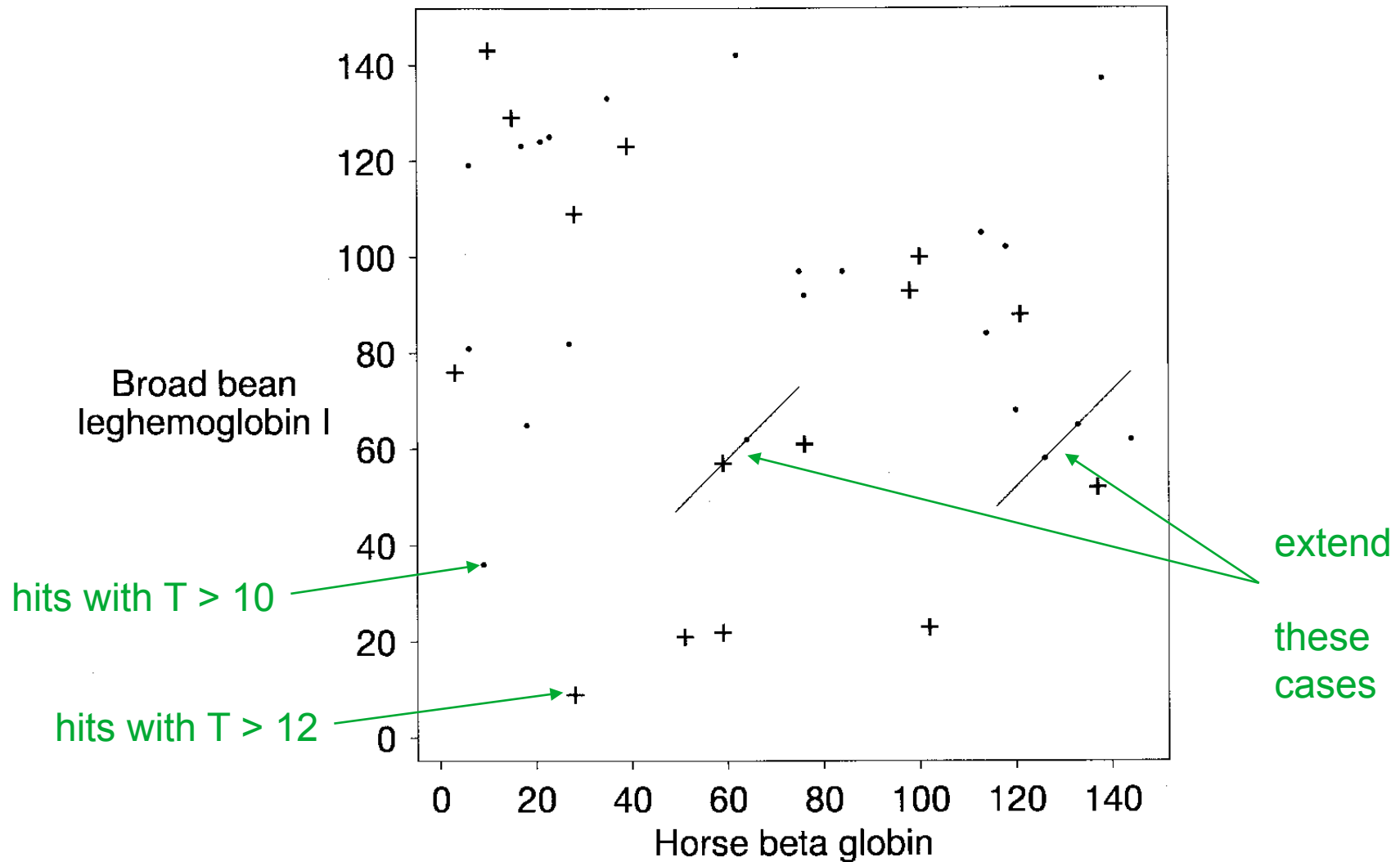
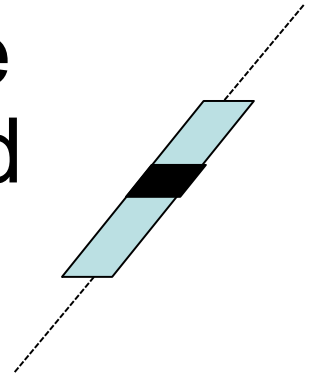


Figure from: Altschul et al. Nucleic Acids Research 25, 1997



# Gapped BLAST

- trigger gapped alignment if two-hit extension has a sufficiently high score
- slide diagonal window to find length-11 segment with highest score; use central pair in this segment as seed
- run DP process both forward & backward from seed
- prune cells when local alignment score falls a certain distance below best score yet



# Gapped BLAST

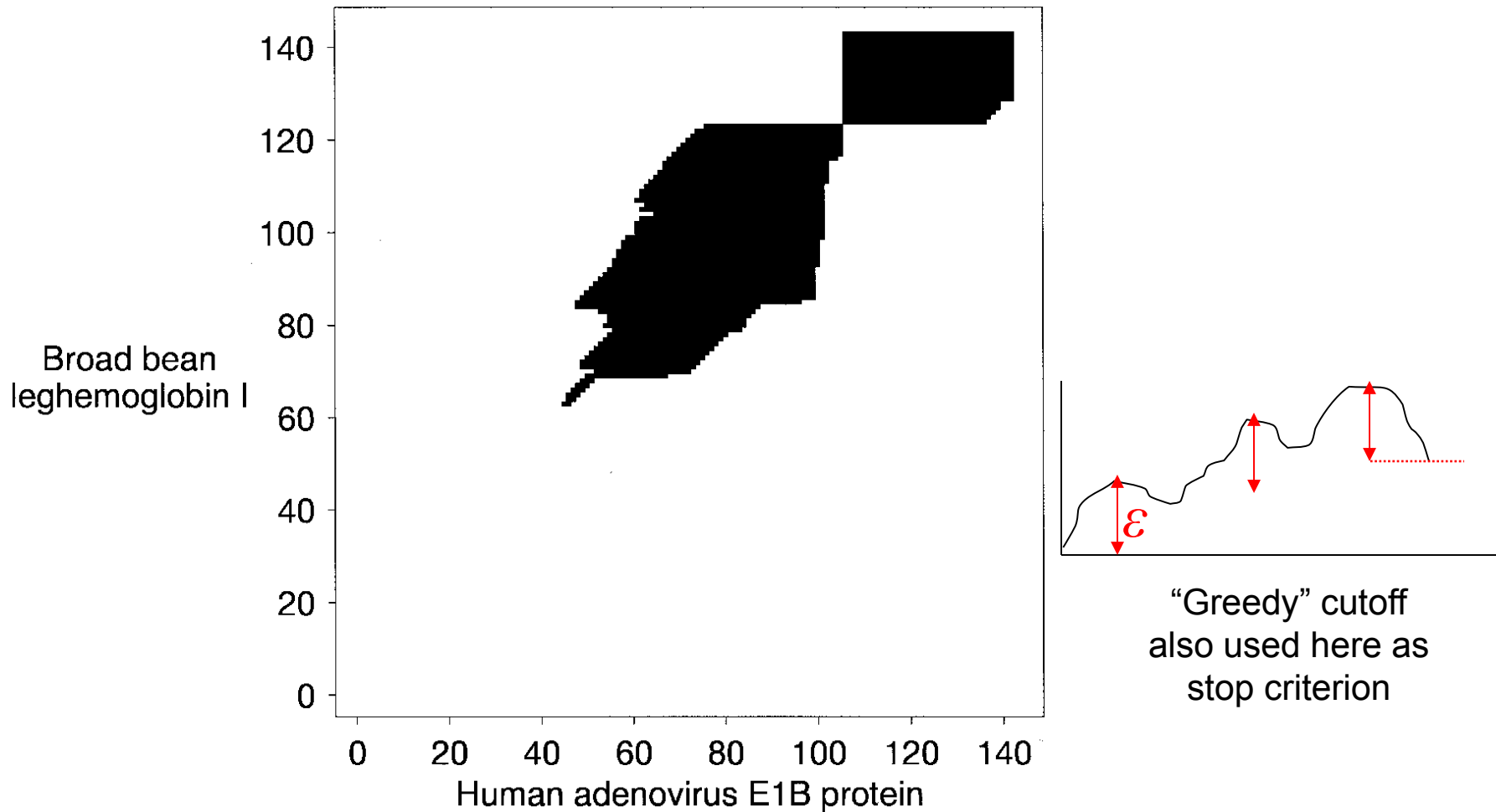


Figure from: Altschul et al. *Nucleic Acids Research* 25, 1997

# Combining the two-hit method and Gapped BLAST

- **Before:**
  - relatively high  $T$  threshold for 3-letter word (hashed) lists
  - two-way hit extension (see earlier slides)
- **Current BLAST:**
  - Lower  $T$ : many more hits (more 3-letter words accepted as match)
  - Relatively few hits (diagonal elements) will be on same matrix diagonal within a given distance  $A$
  - Perform 2-way local Dynamic Programming (gapped BLAST) only on 'two-hits' (preceding bullet)

*The new way is a bit faster on average and gives better (gapped) alignments and better alignment scores!*

# More recent BLAST-related developments

- hashing (indexing) the database
- PSI-BLAST

all are aimed at increasing sensitivity while keeping run-times minimal

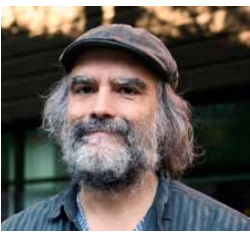
Altschul et al., *Nucleic Acids Research* 1997

# Making things even faster- indexing the complete database (or genome sequence)

- SSAHA – Sequence Search and Alignment by Hashing Algorithms (Ning et al., 2001)
- BLAT – BLAST-like Alignment Tool (Kent, 2002)
- PatternHunter (Ma et al., 2002)
- BLASTZ – alignment of genomic sequences (Schwartz et al., 2003)

# BLAT - BLAST-Like Alignment Tool

- Analyzing vertebrate [genomes](#) requires rapid mRNA/DNA and cross-species protein [alignments](#). **BLAT** (the [BLAST](#)-like alignment tool) was developed by [Jim Kent](#) from UCSC. It is more accurate and 500 times faster than popular existing tools such as BLAST for mRNA/DNA alignments and 50 times faster for protein alignments at sensitivity settings typically used when comparing vertebrate sequences (e.g. BLAST).
- BLAT's speed stems from an index of all nonoverlapping [k-mers](#) in the genome. This index fits inside the [RAM](#) of inexpensive computers, and need only be computed once for each genome assembly. BLAT has several major stages. It uses the index to find regions in the genome likely to be [homologous](#) to the query sequence. It performs an alignment between homologous regions. It stitches together these aligned regions (often [exons](#)) into larger alignments (typically [genes](#)). Finally, BLAT revisits small internal exons possibly missed at the first stage and adjusts large gap boundaries that have canonical splice sites where feasible.
- **From Wikipedia, the free encyclopedia**



For  
reference

# More on Kent

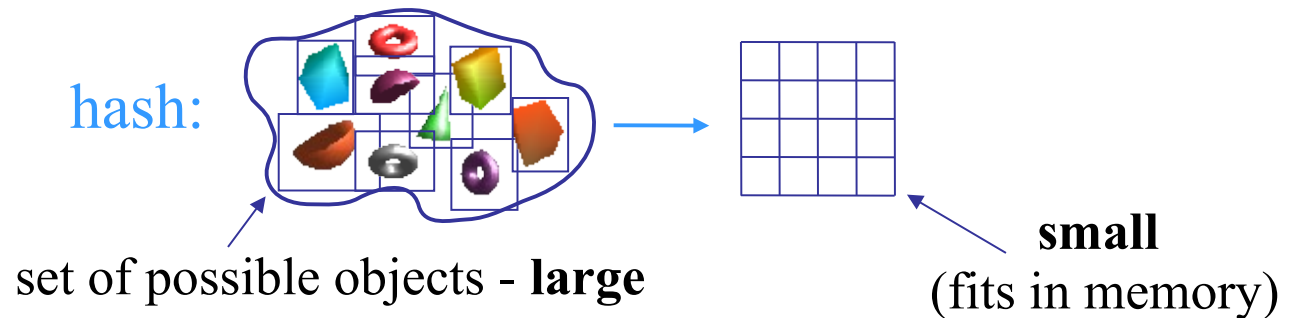
## Involvement with the Human Genome Project

While working on his PhD in Biology at the University of California, Santa Cruz, Kent in May 2000, wrote a program, GigAssembler,<sup>[5]</sup> that allowed the publicly funded Human Genome Project to assemble and publish the human genome sequence. His efforts were motivated out of concern that the data might be made proprietary via patents by Celera Genomics.<sup>[6]</sup> In their close race with Celera, Kent and the UCSC Professor David Haussler quickly built a modest cluster of 50 commodity Personal Computers running the Linux operating system to run the software. In contrast, Celera was using what was thought then to be one of the most powerful civilian supercomputers in the world. Kent's first assembly on the human genome was released on June 22. Celera finished its assembly 3 days later on June 25, and the dual results were announced at the White House on June 26. On July 7, 2000, the Santa Cruz data was made publicly available on the World Wide Web while the research paper describing this publicly funded genome was published in February 2001 special issue of *Nature*,<sup>[7]</sup> in parallel with Celera's results in the journal *Science*.<sup>[8]</sup> In 2002 Tim O'Reilly described Kent's work as "the most significant work of open source development in the past year".

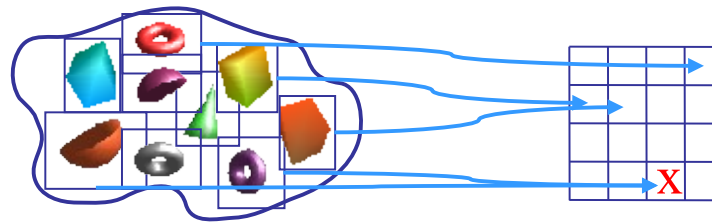
**From Wikipedia, the free encyclopedia**

# Hashing - associative arrays

- Indexing with the object, the
- Hash function:



- Objects should be “well spread”





# Indexing the database: Find "exact" matches with hashing

- 1) Preprocess
- 2) Scan
- 3) Extend

- Preprocess the database
  - Hash the database with k-words
  - For each k-word store in which sequences it appears


k-word: RKP → Hashed DB:

|      |                                  |
|------|----------------------------------|
| QKP: | HUgn0151194, Gene14, IG0, ...    |
| KKP: | haemoglobin, Gene134, IG_30, ... |
| RQP: | HSPHOSR1, GeneA22...             |
| RKP: | galactosyltransferase, IG_1...   |
| REP: | haemoglobin, Gene134, IG_30, ... |
| RRP: | Z17368, Creatine kinase, ...     |
| ...  |                                  |

# Indexing the database:

## Find “exact” matches with hashing

- The database is **preprocessed only once!** (independent from the query)
- In **a constant time** we can get the sequences with a certain *k-word*

k-word: RKP 

**Hashed DB:**  
QKP: HUgn0151194, Gene14, IG0, ...  
KKP: haemoglobin, Gene134, IG\_30, ...  
RQP: HSPHOSR1, GeneA22...  
RKP: galactosyltransferase, IG\_1...  
REP: haemoglobin, Gene134, IG\_30, ...  
RRP: Z17368, Creatine kinase, ...  
...

# BLAST flavours

- `blastp`: protein query, protein db
- `blastn`: DNA query, DNA db
- `blastx`: DNA query, protein db
  - in all reading frames. Used to find potential translation products of an unknown nucleotide sequence.
- `tblastn`: protein query, DNA db
  - database dynamically translated in all reading frames.
- `tblastx`: DNA query, DNA db
  - all translations of query against all translations of db (compare at protein level)

# PSI-BLAST

- Position-Specific Iterated BLAST
- A *profile* (called PSSM by BLAST – *Position Specific Scoring Matrix*) is derived from the result of the first search (using a single query sequence)
- Database is searched against the profile (instead of a sequence) in subsequent rounds
- Up to 3-10 iterations are recommended

# PSI-BLAST steps in words

1. Query sequences are first scanned for the presence of so-called *low-complexity regions* (Wooton and Federhen, 1996), *i.e.* regions with a biased composition likely to lead to spurious hits are excluded from alignment.
2. The program then initially operates on a single query sequence by performing a gapped BLAST search
3. Next, the program takes significant local alignments (hits) found, constructs a multiple alignment (master-slave alignment) and abstracts a position-specific scoring matrix (PSSM) from this alignment.
4. The database is rescanned in a subsequent round, now using the PSSM, to find more homologous sequences. Iteration continues until user decides to stop or the search has converged

# Profile

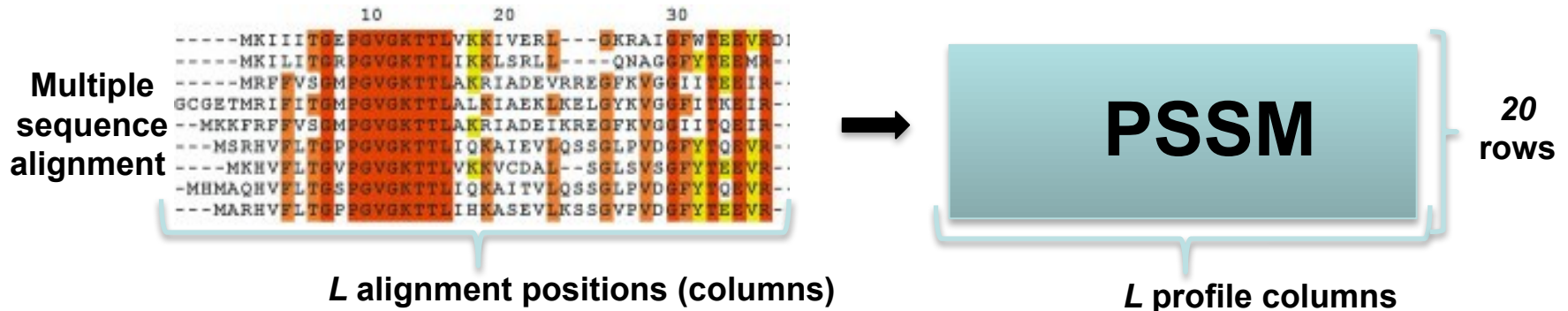
- a **Profile** is a generalized form of sequence (better search capability)
- probabilities instead of a letter

|  |
|--|
|  |
|  |
|  |
|  |
|  |
|  |

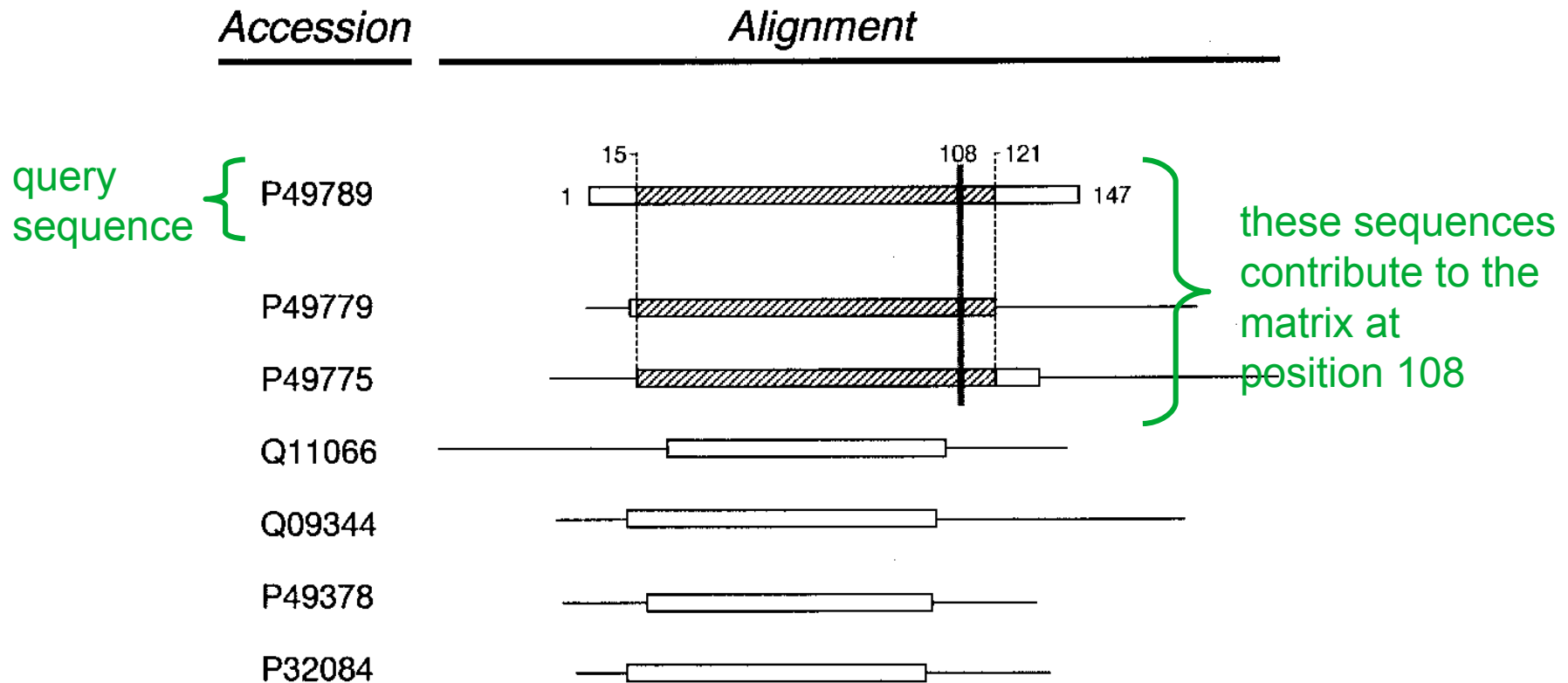
|   |     |     |     |     |     |
|---|-----|-----|-----|-----|-----|
| A | 0.5 | 0.3 | 0.2 | ... | 0   |
| C | 0   | 0.1 | 0.0 | ... | 0.5 |
| D | 0   | 0   | 0.1 | ... | 0.2 |
| . | .   | .   | .   | ... | .   |
| . | .   | .   | .   | ... | .   |
| W | 0   | 0.3 | 0.4 | ... | 0.1 |
| Y | 0.5 | 0.3 | 0.3 | ... | 0.2 |

# What is a sequence profile matrix?

- A sequence profile is a frequency-based scoring matrix that approximates the likelihood of occurrence of an amino acid at a given (multiple) alignment position
  - The mathematics to convert the a.a. frequencies to probabilities may differ (BLAST uses log conversion)
  - Basically, the scoring matrix has dimension  $L * 20$ , with  $L$  the number of columns (positions) in the multiple alignment (or BLAST alignment)
  - Profiles may have an extra column (21<sup>st</sup> position) to describe position-specific gap penalties.
  - In BLAST a profile is called **Position-Specific Scoring Matrix** (PSSM) and has only 20 columns.



# PSI BLAST: Constructing the Profile Matrix



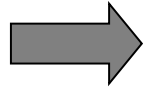
**Figure from: Altschul et al. Nucleic Acids Research 25, 1997**



# PSI-BLAST profile calculation example using frequency normalisation and log conversion

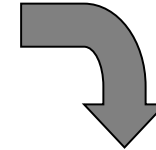
(A)

12345  
S1 GCTCC  
S2 AATCG  
S3 TACGC  
S4 GTGTT  
S5 GTAAA  
S6 CGTCC



|   | 1   | 2   | 3   | 4   | 5   | Overall    |
|---|-----|-----|-----|-----|-----|------------|
| A | .17 | .33 | .17 | .17 | .17 | 6/30 = .20 |
| C | .17 | .17 | .17 | .50 | .50 | 9/30 = .30 |
| G | .50 | .17 | .17 | .17 | .17 | 7/30 = .23 |
| T | .17 | .33 | .50 | .17 | .17 | 8/30 = .27 |

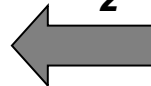
*Normalise by  
dividing by  
overall  
frequencies*



profile

|   | 1     | 2     | 3     | 4     | 5     |
|---|-------|-------|-------|-------|-------|
| A | -0.23 | 0.72  | -0.23 | -0.23 | -0.23 |
| C | -0.81 | -0.81 | -0.81 | 0.74  | 0.74  |
| G | 1.11  | -0.43 | -0.43 | -0.43 | -0.43 |
| T | -0.66 | 0.29  | 0.89  | -0.66 | -0.66 |

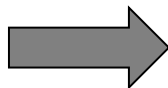
*Convert  
to log to  
base of  
2*



|   | 1    | 2    | 3    | 4    | 5    | Overall    |
|---|------|------|------|------|------|------------|
| A | .85  | 1.65 | .85  | .85  | .85  | 6/30 = .20 |
| C | .57  | .57  | .57  | 1.67 | 1.67 | 9/30 = .30 |
| G | 2.17 | .74  | .74  | .74  | .74  | 7/30 = .23 |
| T | .63  | 1.22 | 1.85 | .63  | .63  | 8/30 = .27 |

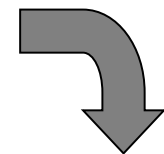
(B)

Match  
GATCA  
to PSSM



*Find  
nucleotides at  
corresponding  
positions*

|   | 1     | 2     | 3     | 4     | 5     |
|---|-------|-------|-------|-------|-------|
| A | -0.23 | 0.72  | -0.23 | -0.23 | -0.23 |
| C | -0.81 | -0.81 | -0.81 | 0.74  | 0.74  |
| G | 1.11  | -0.43 | -0.43 | -0.43 | -0.43 |
| T | -0.66 | 0.29  | 0.89  | -0.66 | -0.66 |



*Sum  
correspondin  
g log odds  
matrix scores*

$$\text{Score} = 1.11 + 0.72 + 0.89 + 0.74 - 0.23 = 3.23$$

# PSI BLAST: Determining profile elements more reliably using pseudo-counts

- the value for a given element of the profile matrix is given by:

$$matrix(i, j) = \log \left( \frac{\Pr(a_i \mid \text{col} = j)}{\Pr(a_i)} \right)$$

*Overall alignment frequency (preceding slide)*

- where the probability of seeing amino acid  $a_i$  in column  $j$  is estimated as:

$$\Pr(a_i \mid \text{col} = j) = \frac{\alpha f_{ij} + \beta g_{ij}}{\alpha + \beta}$$

*Observed frequency*

*Pseudocount (e.g. database frequency)*

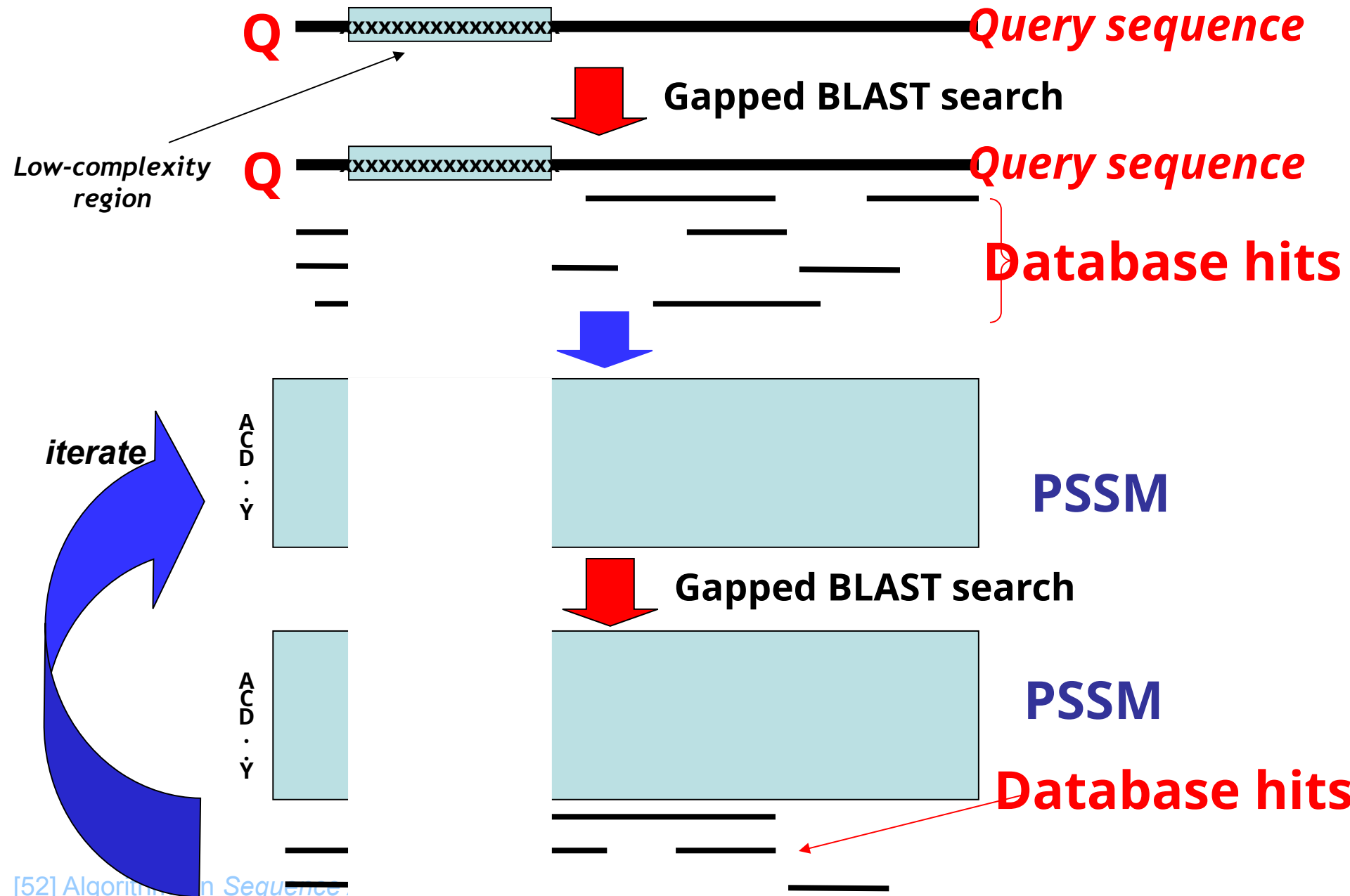
e.g.  $\alpha$  = number of sequences in profile,  $\beta=1$

# PSI BLAST: Determining profile elements more reliably using pseudo-counts

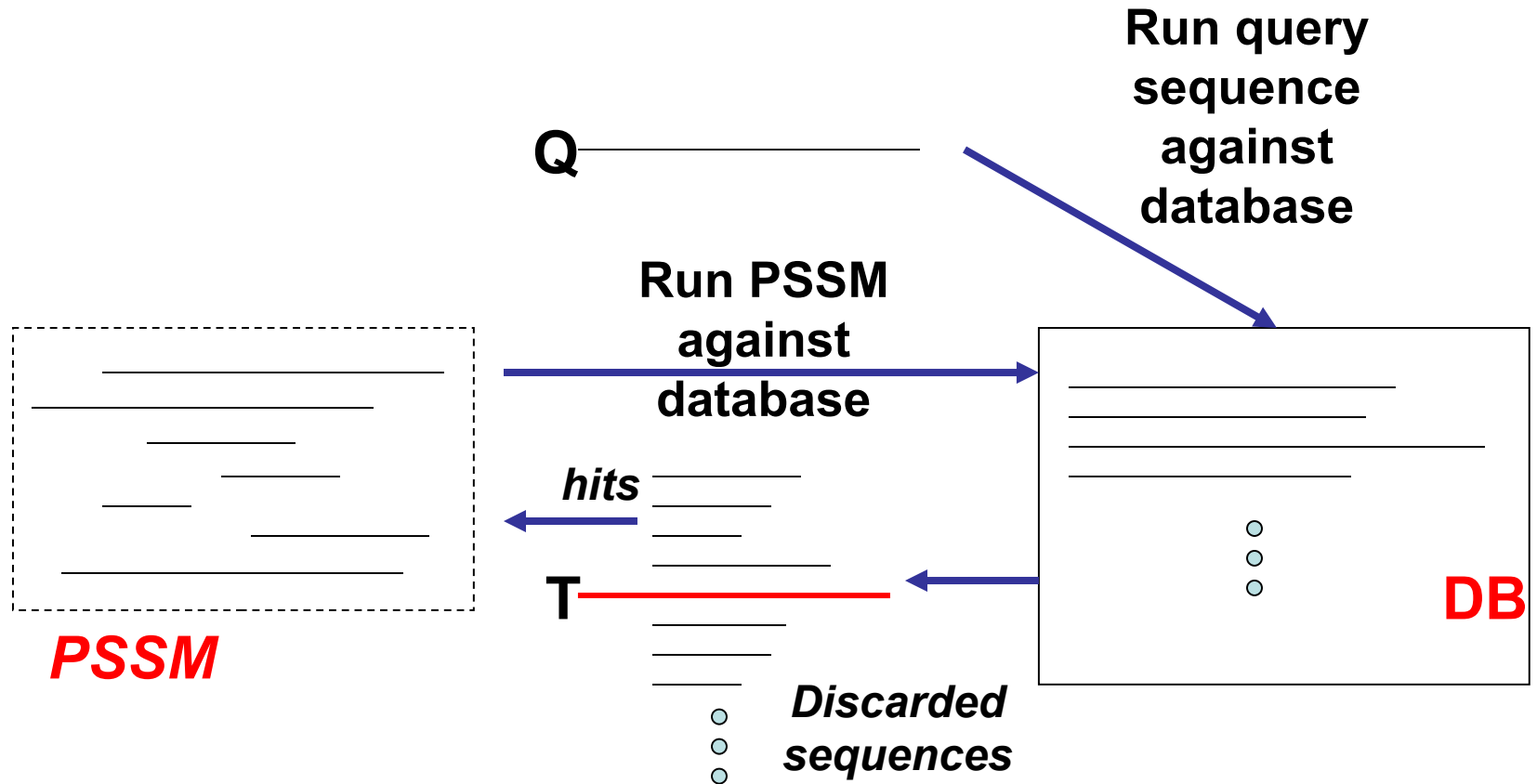
## Pseudo-counts:

- mix observed a.a. frequencies with prior (e.g. database) frequencies
- useful when multiple alignment contains only few sequences so that there is no statistical sample per column yet
- drawback is pulling all frequencies to prior frequencies, which reduces the differences between sequences
- with greater numbers of sequences in the MSA, the profile becomes less dependent on priors

# PSI-BLAST iteration graphic...



# Another PSI-BLAST iteration graphic...

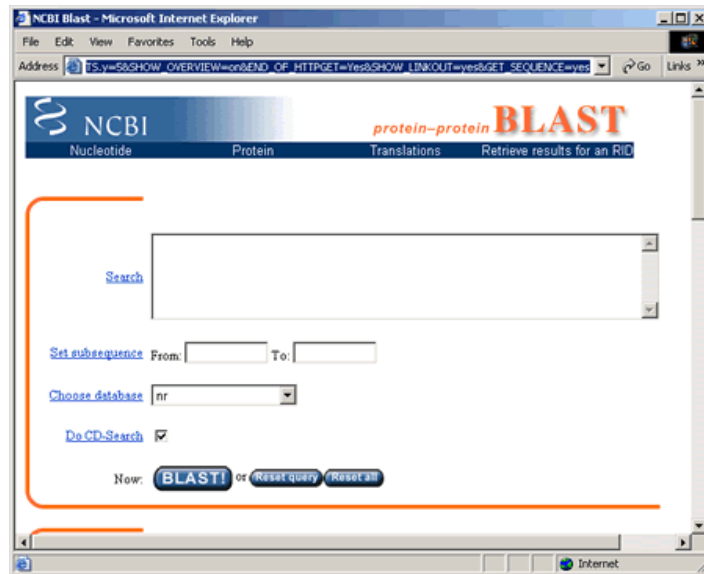


# Low-complexity sequence filtering

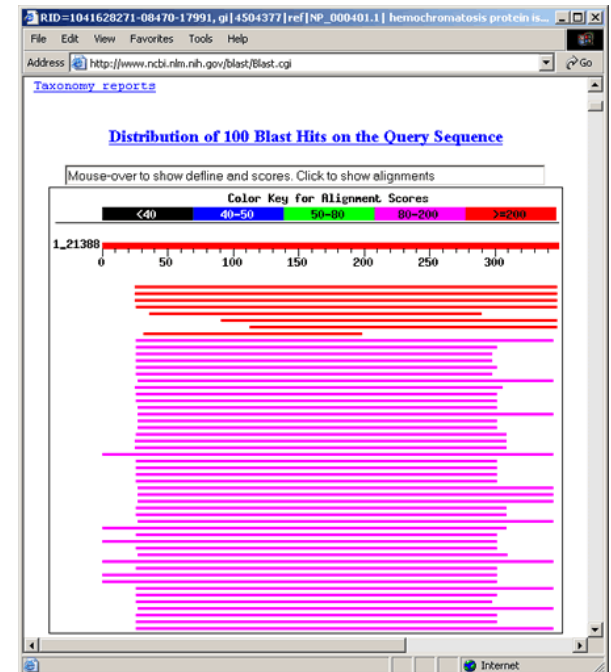
XXXXXXXXXXXXXXXXXXXX **Query sequence**

- For example: AAAAA... or AYLAYLAYL... or AYLLYAALY...
- Low-complexity (sub)sequences have a biased composition and contain less information than high-complexity sequences
- Because of the low information content, they often lead to spurious hits without a biological basis (for example, you can't tell whether a poly-A sequence [AAAAA...] is more similar to a globin, an immunoglobulin or a kinase sequence)
- That is why BLAST filters low-complexity regions in the query sequence out
- See course book *Understanding Bioinformatics* for details

(A)



(B)



(C)

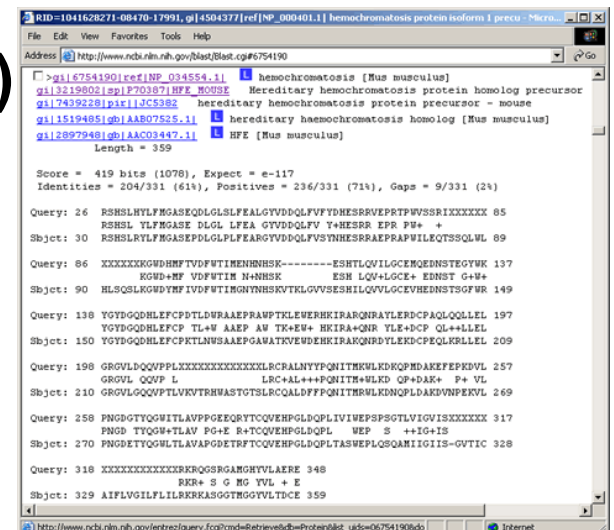
### Related Structures

Sequences producing significant alignments:

|   |                                      |
|---|--------------------------------------|
| <a href="#">gi 6754190 ref NP_034554.1 </a>         | hemochromatosis [Mus musculus] ...   |
| <a href="#">gi 26354116 dbj BAC40688.1 </a>         | unnamed protein product [Mus mu...   |
| <a href="#">gi 12844463 dbj BAB26373.1 </a>         | unnamed protein product [Mus mu...   |
| <a href="#">gi 25742831 ref NP_445753.1 </a>        | hemochromatosis [Rattus norveg...    |
| <a href="#">gi 2624957 gb AAB86597.1 </a>           | hereditary hemochromatosis protei... |
| <a href="#">gi 2072657 emb CAA73197.1 </a>          | HFE (HLA-H) [Mus musculus]           |
| <a href="#">gi 5734363 gb AAD49965.1 AF176534.1</a> | hemochromatosis gene pr...           |
| <a href="#">gi 1930010 gb AAB51504.1 </a>           | hereditary haemochromatosis prote... |
| <a href="#">gi 2225995 emb CAA74333.1 </a>          | MHC class I alpha chain [Rattus ...  |
| <a href="#">gi 2851391 sp P16391 HA12_RAT</a>       | RT1 class I histocompatibilit...     |

| Score<br>(bits) | E<br>Value |
|-----------------|------------|
| 419             | e-117      |
| 419             | e-117      |
| 419             | e-117      |
| 412             | e-115      |
| 366             | e-101      |
| 345             | 7e-95      |
| 303             | 2e-82      |
| 247             | 1e-65      |
| 173             | 4e-43      |
| 171             | 1e-42      |

(D)



# Figure 6

[55] Algorithms in Sequence Analysis

# PSI-BLAST entry page

Protein BLAST: search protein databases using a protein query - Mozilla Firefox

File Edit View History Bookmarks Tools Help

http://www.ncbi.nlm.nih.gov/blast/Blast.cgi?PAGE=Proteins&PROGRAM=blastp&BLAST\_PROGRA... blast

Getting Started Latest Headlines

BLAST Basic Local Alignment Search Tool

Home Recent Results Saved Strategies Help My NCBI [Sign in] [Register]

NCBI/ BLAST/ blastp suite: BLASTP programs search protein databases using a protein query. [more...](#) [Reset page](#) [Bookmark](#)

**Enter Query Sequence**

Enter accession number, gi, or FASTA sequence [Clear](#) Query subrange [From](#) [To](#)

Or, upload file [Browse...](#)

Job Title [Enter a descriptive title for your BLAST search](#)

**Choose Search Set**

Database [Non-redundant protein sequences \(nr\)](#)

Organism [Optional](#) [Enter organism common name, binomial, or tax id. Only 20 top taxa will be shown.](#)

Entrez Query [Optional](#) [Enter an Entrez query to limit search](#)

**Program Selection**

Algorithm

☒ blastp (protein-protein BLAST)

☐ PSI-BLAST (Position-Specific Iterated BLAST)

☐ PHI-BLAST (Pattern Hit Initiated BLAST)

[Choose a BLAST algorithm](#)

**BLAST** Search database nr using Blastp (protein-protein BLAST) ☐ Show results in a new window

Algorithm parameters

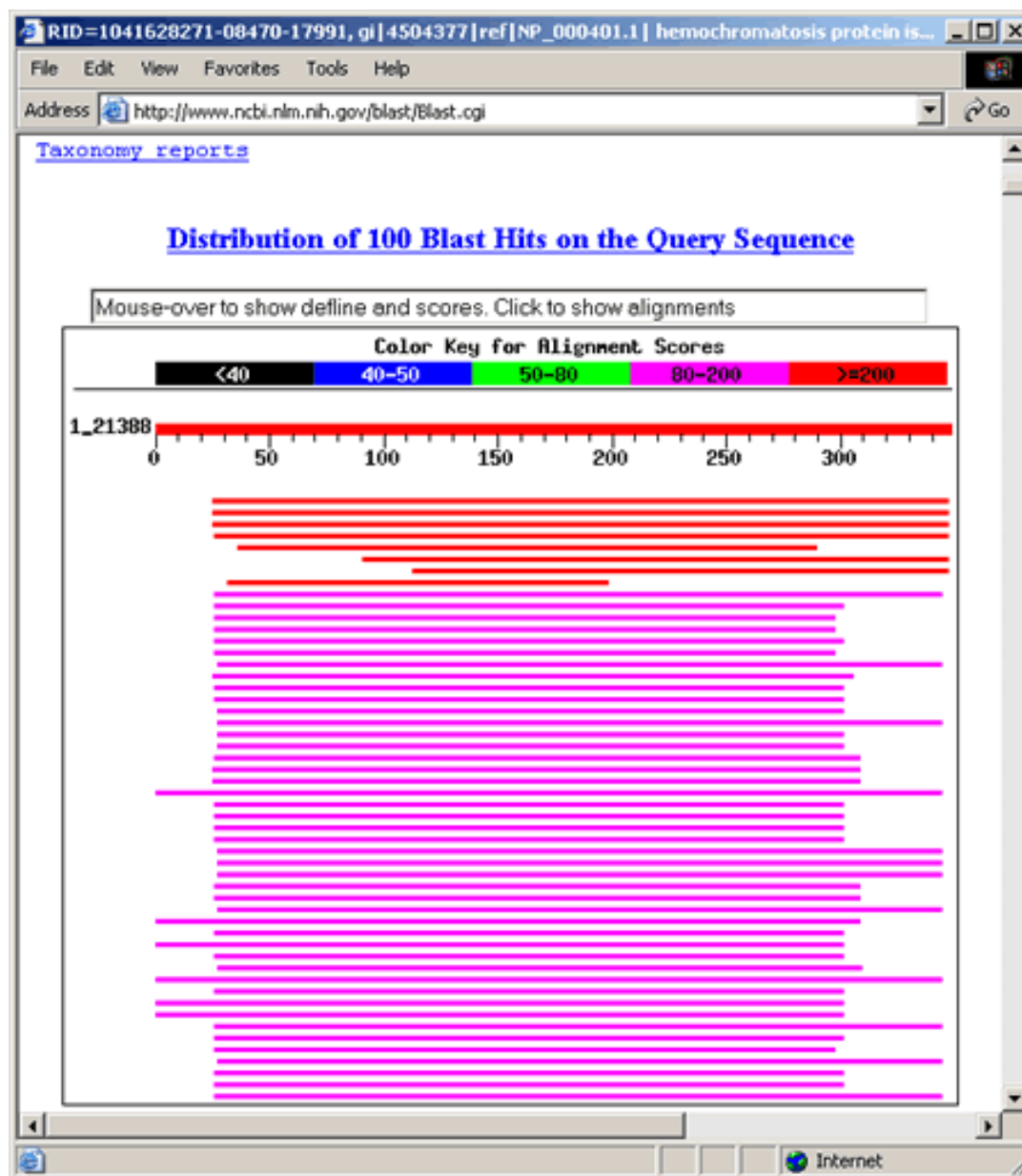
Done

2 Windows Ex... Microsoft Powe... Protein BLAST: ... heringa@flits:/... ref - heringa@fl... NL 0:36

Paste your  
query  
sequence

Choose  
the BLAST  
program  
you want





## Related Structures

Sequences producing significant alignments:

|   |   |                                      | 2                   | 3          |                       |
|---|---|--------------------------------------|---------------------|------------|-----------------------|
|   |   |                                      | Score<br>(bits)     | E<br>Value |                       |
| 1 | <a href="#">gi 6754190 ref NP_034554.1 </a>         | hemochromatosis [Mus musculus] ...   | <a href="#">419</a> | e-117      | <a href="#">L</a> - 4 |
|   | <a href="#">gi 26354116 dbj BAC40688.1 </a>         | unnamed protein product [Mus mu...   | <a href="#">419</a> | e-117      |                       |
|   | <a href="#">gi 12844463 dbj BAB26373.1 </a>         | unnamed protein product [Mus mu...   | <a href="#">419</a> | e-117      | <a href="#">L</a>     |
|   | <a href="#">gi 25742831 ref NP_445753.1 </a>        | hemochromatosis [Rattus norveg...    | <a href="#">412</a> | e-115      | <a href="#">L</a>     |
|   | <a href="#">gi 2624957 gb AAB86597.1 </a>           | hereditary hemochromatosis protei... | <a href="#">366</a> | e-101      | <a href="#">L</a>     |
|   | <a href="#">gi 2072657 emb CAA73197.1 </a>          | HFE (HLA-H) [Mus musculus]           | <a href="#">345</a> | 7e-95      | <a href="#">L</a>     |
|   | <a href="#">gi 5734363 gb AAD49965.1 AF176534.1</a> | hemochromatosis gene pr...           | <a href="#">303</a> | 2e-82      | <a href="#">L</a>     |
|   | <a href="#">gi 1930010 gb AAB51504.1 </a>           | hereditary haemochromatosis prote... | <a href="#">247</a> | 1e-65      | <a href="#">L</a>     |
|   | <a href="#">gi 2225995 emb CAA74333.1 </a>          | MHC class I alpha chain [Rattus ...  | <a href="#">173</a> | 4e-43      | <a href="#">L</a>     |
|   | <a href="#">gi 2851391 sp P16391 HA12 RAT</a>       | RT1 class I histocompatibilit...     | <a href="#">171</a> | 1e-42      | <a href="#">L</a>     |

- 1 - This portion of each description links to the sequence record for a particular hit.
- 2 - Score or bit score is a value calculated from the number of gaps and substitutions associated with each aligned sequence. The higher the score, the more significant the alignment. Each score links to the corresponding pairwise alignment between query sequence and hit sequence (also referred to as subject sequence).
- 3 - E Value (Expect Value) describes the likelihood that a sequence with a similar score will occur in the database by chance. The smaller the E Value, the more significant the alignment. For example, the first alignment has a very low E value of  $e^{-117}$  meaning that a sequence with a similar score is very unlikely to occur simply by chance.
- 4 - These links provide the user with direct access from BLAST results to related entries in other databases. 'L' links to LocusLink records and 'S' links to structure records in NCBI's Molecular Modeling DataBase.

```

RID=1041628271-08470-17991,gi|4504377[ref|NP_000401.1| hemochromatosis protein isoform 1 precu - Micro...
File Edit View Favorites Tools Help
Address http://www.ncbi.nlm.nih.gov/blast/Blast.cgi#6754190
>gi|6754190|ref|NP_034554.1| L hemochromatosis [Mus musculus]
gi|3219802|sp|P70387|HFE_MOUSE Hereditary hemochromatosis protein homolog precursor
gi|7439228|pir|JC5382 hereditary hemochromatosis protein precursor - mouse
gi|1519485|gb|AAB07525.1| L hereditary haemochromatosis homolog [Mus musculus]
gi|2897948|gb|AAC03447.1| L HFE [Mus musculus]
Length = 359

Score = 419 bits (1078), Expect = e-117
Identities = 204/331 (61%), Positives = 236/331 (71%), Gaps = 9/331 (2%)

Query: 26 RSHSLHYLFMGASEQDLGLSLFEALGYVDDQLFVYFDHESRRVEPRTPWVSSRIXXXXXX 85
RSHSL YLFMGASE DLGL LFEA GYVDDQLFV Y+HESRR EPR PW+ +
Sbjct: 30 RSHSLRYLFMGASEPDLGLPLFEARGYVDDQLFVSYNHESRRAEPRAPWILEQTSSQLWL 89

Query: 86 XXXXXXKGMWDHMFVDFWTFIMENHNHNSK-----ESHTLQVILGCEMQEDNSTEGYWK 137
KGMW+MF VDFWTFIM N+NHNSK ESH LQV+LGCE+ EDNST G+W+
Sbjct: 90 HLSQSLKGMWDYMFIVDFWTFINGNYNHNSKVTKLGVVSESHILOVVLGCEVHEDNSTSGFWR 149

Query: 138 YGYDGGQDHLEFCPDTLDWRAAEPRAPWPTKLEWERHKIRARQNRAYLERDCPAQLQOLLEL 197
YGYDGGQDHLEFCP TL+W AAEP AW TK+EW+ HKIRA+QNR YLE+DCP QL++LLEL
Sbjct: 150 YGYDGGQDHLEFCPRTLWNSAAEPGAWATKVEWDEHKIRAKQNRDYLEKDCPEQLKRLEL 209

Query: 198 GRGVLDQQVPPLXXXXXXXXXXXXXLRCLALNYYYPQNIHMKWLKDKQPMDAKEFEPKDV 257
GRGVLD QQVP L LRC+AL+++PQNIH+WLKD QP+DAK+ P+ VL
Sbjct: 210 GRGVLDQQVPPTLVKVRHWASTGTSLRCLALDFFPQNIHMKWLKDNQPLDAKDVNPEKVL 269

Query: 258 PNGDGTYYQGWITLAVPPGEEQRYTCQVEHPGLDQPLIVIEPSPSGTLVIGVISXXXXXX 317
PNGD TYQGW+TLAV PG+E R+TCQVEHPGLDQPL WEP S ++IG+IS
Sbjct: 270 PNGDGTYYQGWITLAVAPGDETRFTCQVEHPGLDQPLTASWEPLQSQAMIIIGIIS-GVTIC 328

Query: 318 XXXXXXXXXXXXKRKRGSGRGAMGHYVLAERE 348
RKR+ S G MG YVL + E
Sbjct: 329 AIFLVGILFLILRKRKASGGTNGGYVLTDC 359

http://www.ncbi.nlm.nih.gov/entrez/query.fcgi?cmd=Retrieve&db=Protein&list_uids=06754190&do Internet

```

**‘X’ residues denote low-complexity sequence fragments that are ignored**

# Recap

- Databases grow exponentially, sequence databases even more so than others (e.g. structural or functional DBs)
- Homology searching: predicting function by sequence database searching using the homology principle
- BLAST
  - Original BLAST (not used anymore)
  - Two-hit method and gapped BLAST
  - Extensions of Blast (indexing the sequence database)
- PSI-BLAST
  - Calculating the PSSM
  - Pseudo-counts
  - Low-complexity subsequences
  - Iteration
- FASTA
  - Base-20 hashing

**BELOW SLIDES ARE FOR  
REFERENCE**

**NOT COVERED IN  
LECTURE**

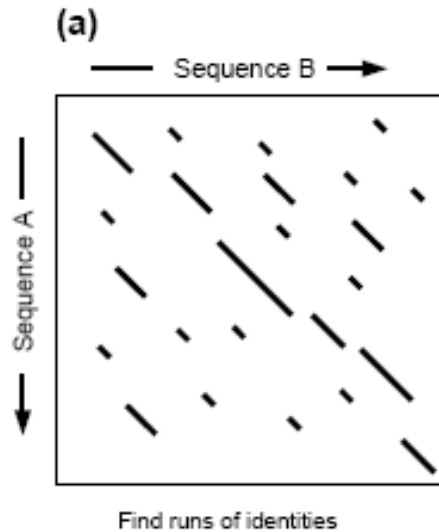
**NOT EXAM MATERIAL**

# A piece of history: FASTA

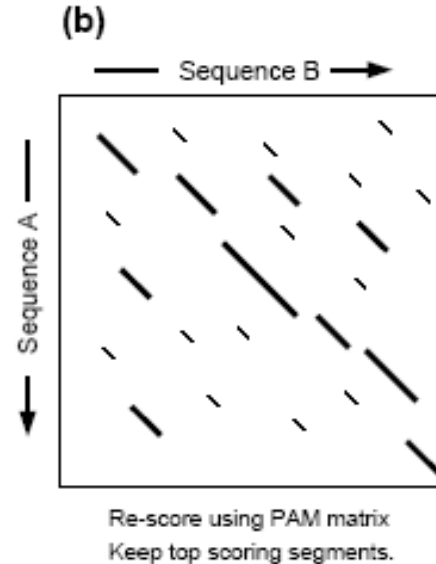
- First homology searching method (FASTP – Lipman & Pearson, 1985)
- Until gapped-BLAST and PSI-BLAST appeared (1997), FASTA has in fact been the better method
  - Unlike the impression created by the BLAST folks (from 1990)
- Compares a given query sequence with a library of sequences and calculates for each pair the highest scoring local alignment
- Similar to BLAST, speed is obtained by delaying application of the dynamic programming technique to the moment where the most similar segments are already identified by faster and less sensitive techniques
- FASTA routine operates in four steps:

## FASTA Algorithm

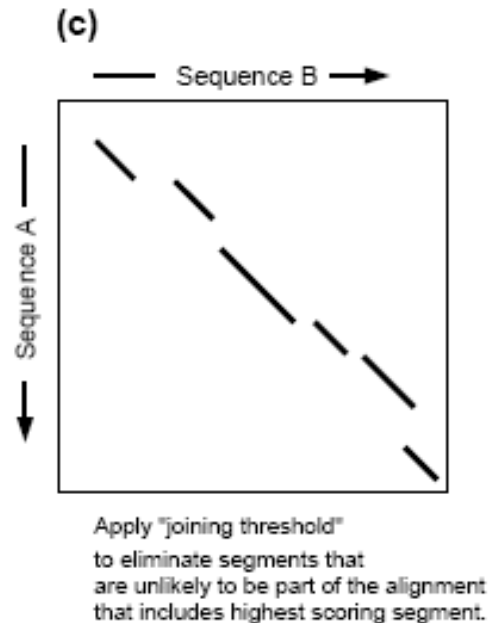
Step 1



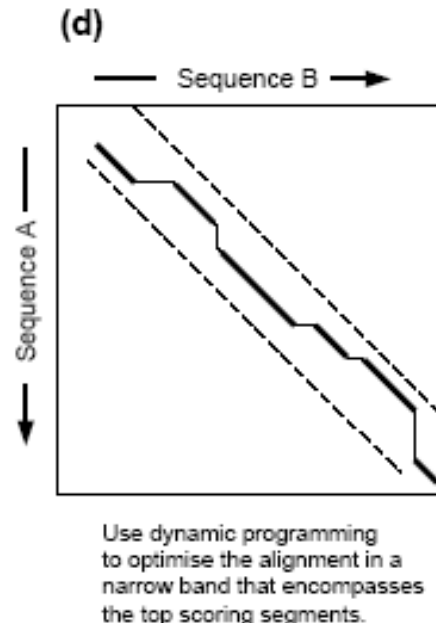
Step 2



Step 3



Step 4



# FASTA

## Operates in four steps:

1. Rapid searches for identical words of a user specified length occurring in query and database sequence(s) (Wilbur and Lipman, 1983, 1984). For each target sequence the 10 regions with highest density of ungapped common words are determined.
2. These 10 regions are rescored using Dayhoff PAM-250 residue exchange matrix (Dayhoff et al., 1983) and the best scoring region of the 10 is reported under *init1* in the FASTA output.
3. Regions scoring higher than a threshold value  $T$  and being sufficiently near each other in the sequence are joined, now allowing gaps. The highest score of these new fragments can be found under *initn* in the FASTA output.  $T$  is set such that only a small fraction of database sequences are retained. These are the only ones that are reported to the user.

**Until here things are quick!**



# FASTA

Operates in four steps (continued):

4. full dynamic programming alignment (Chao *et al.*, 1992) over the final region which is widened by 32 residues at either side, of which the score is written under *opt* in the FASTA output.

**This step is slow –  $O(n^2)$**

# FASTA output example

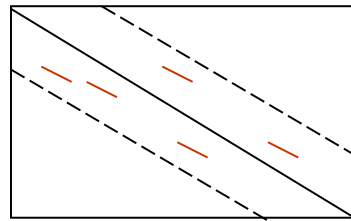
DE METAL RESISTANCE PROTEIN YCF1 (YEAST CADMIUM FACTOR 1) . . .  
SCORES Init1: 161 Initn: 161 Opt: 162 z-score: 229.5 E(): 3.4e-06  
Smith-Waterman score: 162; 35.1% identity in 57 aa overlap

|            |  |     |                             |                                   |     |     |
|------------|--|-----|-----------------------------|-----------------------------------|-----|-----|
|            |  |     |                             | 10                                | 20  | 30  |
| test.seq   |  |     |                             | MQRSPLEKASVVSKLFFSWTRPILRKGYRQRLE |     |     |
|            |  |     |                             | :  : ::   :::  : :: :             |     |     |
| YCFI_YEAST | CASILLLEALPKKPLMPHQHIHQTLTRRKPNPYDSANIFSRITFSWMSGLMKTGYEKYLV |     |                             |                                   |     |     |
|            | 180  | 190 | 200                         | 210                               | 220 | 230 |
|            |  |     | 40                          | 50                                | 60  |     |
|            | test.seq   |     | LSDIYQIPSVDSADNLSEKLEREWDRE |                                   |     |     |
|            |  |     | : : ::   :::  : :: :        |                                   |     |     |
| YCFI_YEAST | EADLYKLPRNFSSEELSQKLEKNWENELKQKSNPSLSWAICRTFGSKMLLAFFKAIHDV  |     |                             |                                   |     |     |
|            | 240  | 250 | 260                         | 270                               | 280 | 290 |

# FASTA how to make step 1 fast

## (1) Rapid identical word searches:

- Searching for  $k$ -tuples of a certain size within a specified bandwidth along search matrix diagonals.



- For not-too-distant sequences ( $> 35\%$  residue identity), little sensitivity is lost while speed is greatly increased.
- Technique employed is known as **hash coding** or **hashing**: a lookup table is constructed for all words in the query sequence, which is then used to compare all encountered words in each database sequence.

# HASHING (continued)

- Preprocessing: a lookup table is constructed for all words in the query sequence, which is then used to compare all encountered words in every database sequence
- **General example of hashing (old school):** the telephone book to find persons' phone numbers (names are ordered)
  - Using a phone book, you do not need to search through all names until you find the person you want
  - In computer speak: find a hash function  $f$  such that  $f(name)$  can be directly assigned to an address in the computer where the telephone number is stored
- Hashing of sequence information is typically based on ***k*-mers** (that are often alpha-numerically ordered)

# Hashing - examples

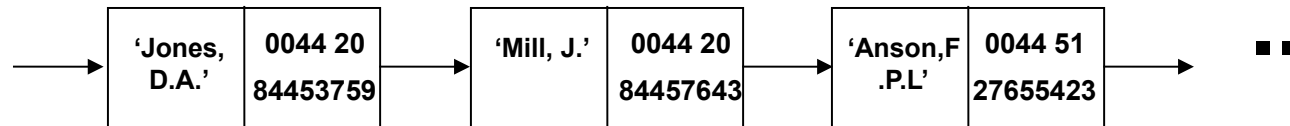
- *T9 Predictive Text* in first-generation mobile phones
  - “hello”:  
4, 4, 3, 3, 5, 5, 5,  
(*pause*) 5, 5, 5, 6, 6, 6
  - “hello” in T9:  
4, 3, 5, 5, 6
  - **Collisions**: 4, 6:  
“*in*”, “*go*”

# Hashing - examples (cont..)

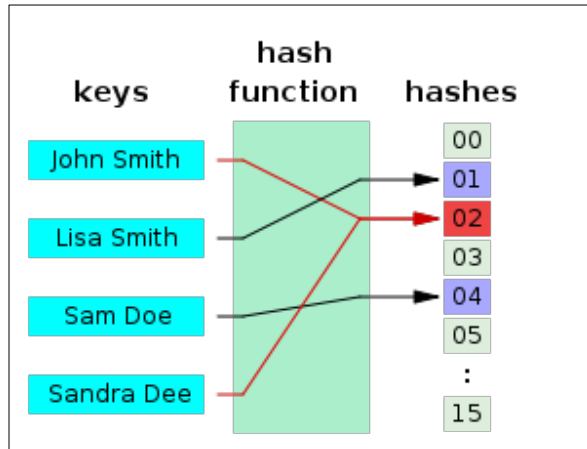
- *Other easier hash function: let  $a=1$ ,  $b=2$ ,  $c=3$ , etc.*
  - “hello” now gets hash address  
 $8+5+12+12+15 = 52$
  - “olleh” will get same address (collision)
  - Each word encountered gets a hash address immediately and can be indexed.
  - *How good is this hash function?*

# HASHING (cont.)

*This takes too long.....*



# HASHING (cont.)



**Name =  
'Jones'**

**$F('Jones')$**

**Hash array  
(table)**

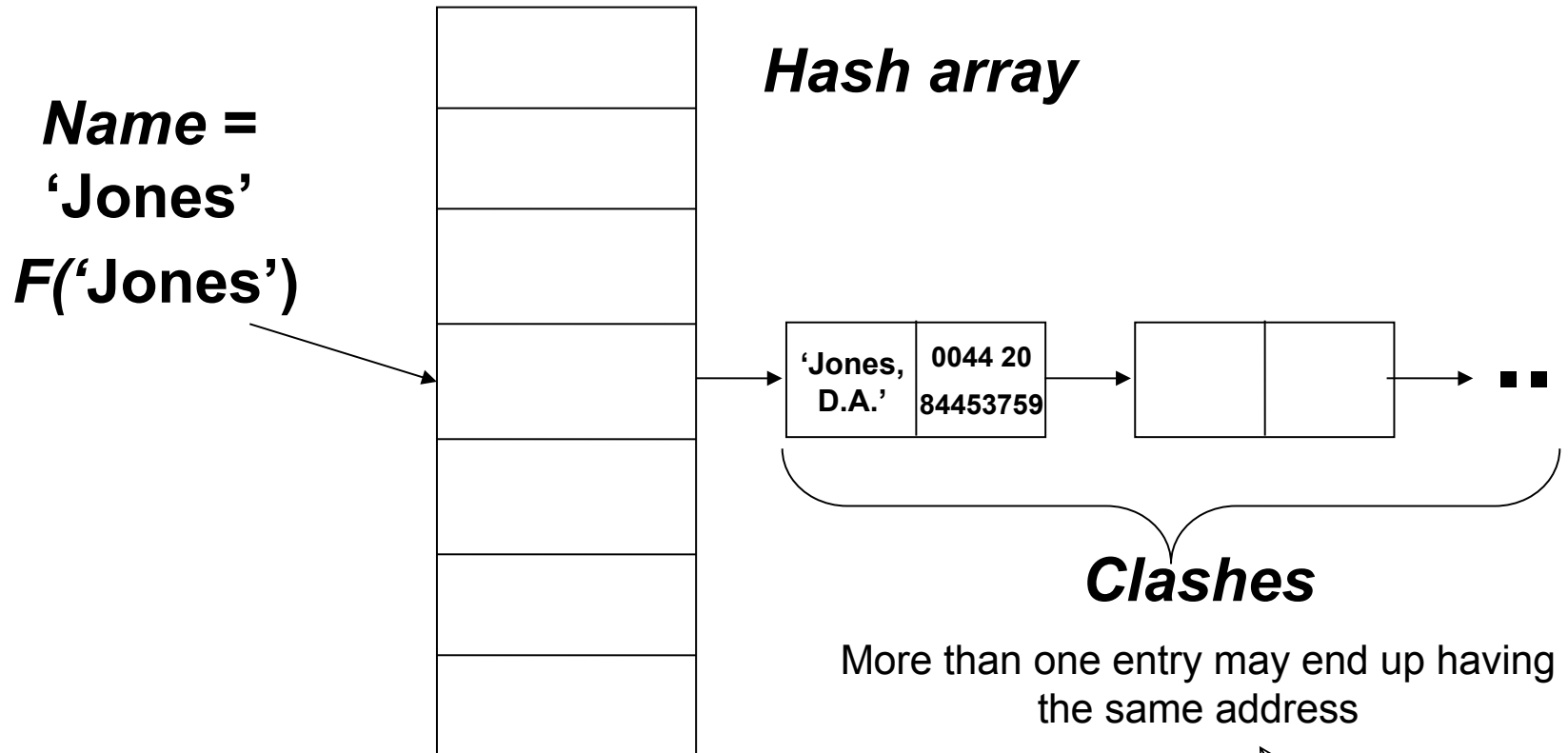
|                     |
|---------------------|
|                     |
|                     |
|                     |
| 0044 20<br>84453759 |
|                     |
|                     |
|                     |

**For sequences:**

- name is *subword* in database sequence
- telephone number is sequence position(s) of subword



# HASHING (cont.)



**Hash function should avoid clashes:**

- clashes take more time
- but need less memory for hash array

**Secondary hash function** will solve searching through clash list

# HASHING (cont.)

Example of hash function:

Take position of letter in alphabet ( $p(a) = 1$ ,  
 $p(b) = 2$ ,  $p(c) = 3, \dots$ )

$$F(\text{'Jones'}) = p(J) + p(o) + p(n) + p(e) + p(s) = 10 + 15 + 14 + 5 + 19 = 63$$

So, 'Jones' goes to slot 63 in Hash array

***What do you think about this function?  
Will there be clashes?***

# HASHING in FASTA

Sequence positions in query are hashed

Query:           ERLFLERLACER .....

DB:               MERIFERLACACTR .....

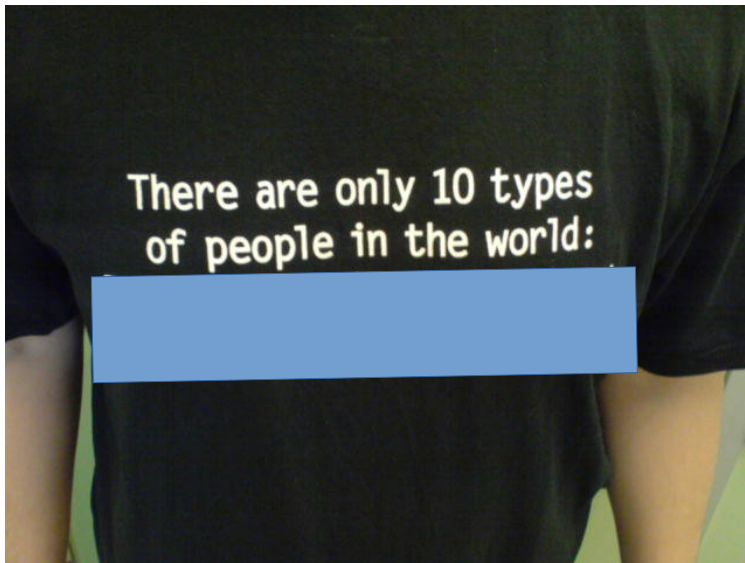
Query hash table:

| <i>Word</i> | <i>Position</i> |
|-------------|-----------------|
| ER          | 1, 5, 10        |
| RL          | 2, 6            |
| LF          | 3               |
| FE          | 4               |
| LA          | 7               |
| AC          | 8               |
| CE          | 9               |
| ....        | ...             |

You only need to go through the DB sequence once: for each word encountered (ER, RL, LF, ..), check the query hash list for the word. If found, you immediately have the query sequence positions of the word. You also know the position you are at in the DB sequence, and so you can fill in the  $m \times n$  matrix with diagonals right away (see earlier slide step 1).

Algorithmic speed therefore is linear with (DB) sequence length or  $O(n)$ . Compare this to finding all word match positions without a hash list (complexity is  $O(m \times n)$ ).

# Number systems



Base-1: binary

0-1

Base-8: octal

0-7

Base-10: decimal 0-9

Base-16: hexadecimal 0-F

Base 20: vigesimal → FASTA

(Decimal)  $503 = 5 \cdot 10^2 + 0 \cdot 10^1 + 3 \cdot 10^0$

(Base-20)  $213 = 2 \cdot 20^2 + 1 \cdot 20^1 + 3 \cdot 20^0 = 823$  (decimal)

# The FASTA implementation

Query:

**ERLFLACER**  
**12345678911**  
**01**

Using the FASTA hash/chaining array setup, one can run along the dipeptides of a database sequence (linear search) and know instantaneously where the identical dipeptides in the query sequence are positioned.

One-let codes: ACDEFGHIKLMNPQRSTVWY  
 10 15 0 5

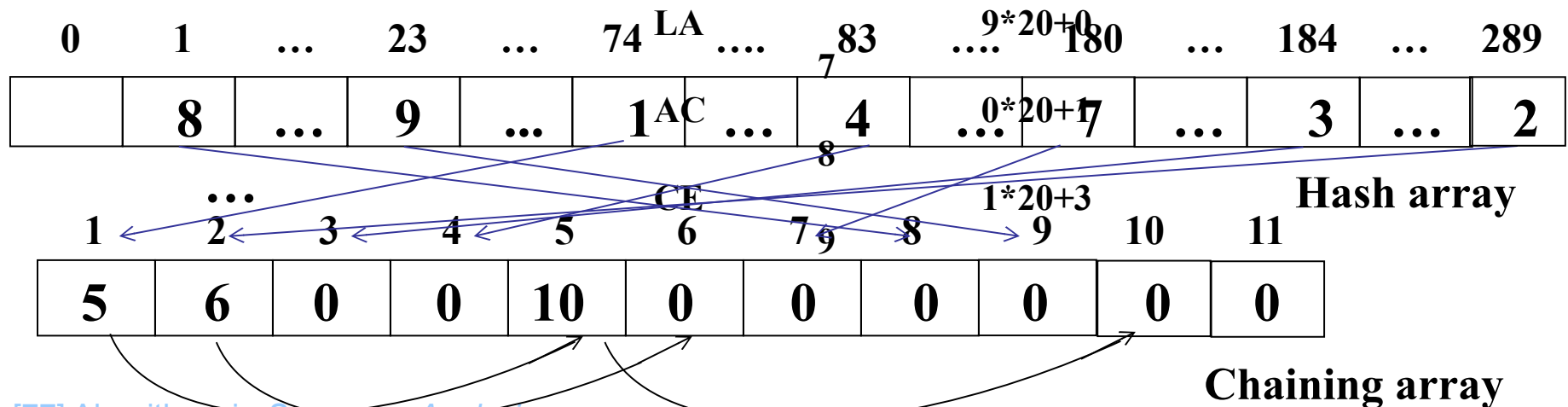
Dipeptides are hashed using vigesimal (base-20) numbering scheme

Query hash table:

| Word | Position | Hash               |
|------|----------|--------------------|
| ER   | 1, 5, 10 | $3 \times 20 + 14$ |
| RL   | 2, 6     | $14 \times 20 + 9$ |
| LF   | 3        | $9 \times 20 + 4$  |
| FE   | 4        | $4 \times 20 + 3$  |

E=3, R=14

$h('ER') = 3 \times 20 + 14 = 74$



# FASTA

- The k-tuple length (step 1) is user-defined and is usually 1 or 2 for protein sequences (i.e. either the positions of each of the individual 20 amino acids or the positions of each of the 400 possible dipeptides are located).
- For nucleic acid sequences, the k-tuple is 5-20 (often 11), and should be longer because short k-tuples are much more common due to the 4 letter alphabet of nucleic acids.
- The larger the k-tuple chosen, the more rapid, but less thorough, the database search.