Problem Set 3

Applied Stats/Quant Methods 1

Due: November 19, 2022

Instructions

- Please show your work! You may lose points by simply writing in the answer. If the problem requires you to execute commands in R, please include the code you used to get your answers. Please also include the .R file that contains your code. If you are not sure if work needs to be shown for a particular problem, please ask.
- Your homework should be submitted electronically on GitHub.
- This problem set is due before 23:59 on Sunday November 19, 2023. No late assignments will be accepted.

In this problem set, you will run several regressions and create an add variable plot (see the lecture slides) in R using the incumbents_subset.csv dataset. Include all of your code.

Question 1

We are interested in knowing how the difference in campaign spending between incumbent and challenger affects the incumbent's vote share.

1. Run a regression where the outcome variable is **voteshare** and the explanatory variable is **difflog**.

Below is the R code:

```
1 ####### Question 1 #######
2
3 ###### (1) ######
5 q1_reg_model <- lm(voteshare ~ difflog , data=inc.sub)
6 summary(q1_reg_model)</pre>
```

Table 1: Abstract of Regression Model in Question 1

	Estimate	Std. Error	t value	$\Pr(> t)$
(Intercept) difflog	0.579031 0.041666		257.19 43.04	<2e-16 *** <2e-16 *

- - -

```
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 0.07867 on 3191 degrees of freedom Multiple R-squared: 0.3673, Adjusted R-squared: 0.3671 F-statistic: 1853 on 1 and 3191 DF, p-value: < 2.2e-16

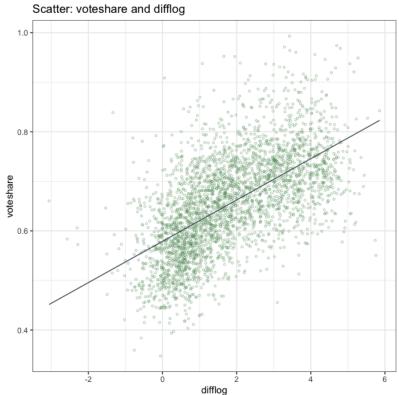
- F test p-value for the entire regression model is 2.2e-16, which is very close to 0, which means we have a very high confidence in rejecting the null hypothesis.. So at least one slope in regression model is not 0.
- F test p-value for the intercept and slope is both 2e-16, which is very close to 0, which means we have a very high confidence in rejecting the null hypothesis.. So the estimate of intercept and slope is not 0.
- The adjusted R-squared is 0.3671, which means that the fit of this model is average.

2. Make a scatterplot of the two variables and add the regression line.

Below is the R code:

```
1 ##### (2) #####
2
3 q1_scatter <- ggplot(inc.sub, aes(x=difflog, y=voteshare)) +
4    geom_point(shape=1, size=0.8, color="#609966", alpha=0.4) +
5    geom_smooth(method="lm", se=FALSE, color="#52616B", size=0.5) +
6    ggtitle("Scatter: voteshare and difflog") +
7    theme_bw()
8 q1_scatter</pre>
```

Figure 1: Scatter - Difflog and Voteshare



• Generally speaking, difflog and voteshare are positively correlated.

3. Save the residuals of the model in a separate object.

In regression model, residuals suggests the differences between the predict values and the true values.

The formulation of residuals is: $e_i = y_i - \hat{y}_i$

In this formulation:

 e_i is residuals, y_i is the reality value, and \hat{y}_i is the value of the regression model.

Below is the R code:

```
1 ##### (3) #####
2
3 q1_residuals <- residuals (q1_reg_model)
4 str (q1_residuals)
5 summary (q1_residuals)</pre>
```

Because regression model in R is a list composed of coefficients, residuals, effects and many other elements.

For coefficients, the first element is the intercept, and the second element is the slope.

Below is the R code:

```
[1] "voteshare = 0.58 + 0.04 * difflog"
```

We are interested in knowing how the difference between incumbent and challenger's spending and the vote share of the presidential candidate of the incumbent's party are related.

1. Run a regression where the outcome variable is **presvote** and the explanatory variable is **difflog**.

Below is the R code:

```
1 ####### Question 2 ########

3 ###### (1) ######

5 q2_reg_model <- lm(presvote ~ difflog, data=inc.sub)

6 summary(q2_reg_model)
```

Table 2: Abstract of Regression Model in Question 2

	Estimate	Std. Error	t value	$\Pr(> t)$
(Intercept) difflog		0.003161 0.001359		<2e-16 *** <2e-16 ***

```
---Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

Residual standard error: 0.1104 on 3191 degrees of freedom Multiple R-squared: 0.08795, Adjusted R-squared: 0.08767 F-statistic: 307.7 on 1 and 3191 DF, p-value: < 2.2e-16

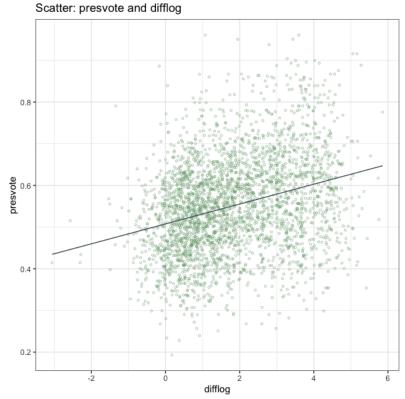
- F test p-value for the entire regression model is 2.2e-16, which is very close to 0, which means we have a very high confidence in rejecting the null hypothesis.. So at least one slope in regression model is not 0.
- F test p-value for the intercept and slope is both 2e-16, which is very close to 0, which means we have a very high confidence in rejecting the null hypothesis.. So the estimate of intercept and slope is not 0.
- The adjusted R-squared is 0.08767, which means that the fit of this model is very bad.

2. Make a scatterplot of the two variables and add the regression line.

Below is the R code:

```
1 ##### (2) #####
2
3 q2_scatter <- ggplot(inc.sub, aes(x=difflog, y=presvote)) +
4    geom_point(shape=1, size=0.8, color="#609966", alpha=0.4) +
5    geom_smooth(method="lm", se=FALSE, color="#52616B", size=0.5) +
6    ggtitle("Scatter: presvote and difflog") +
7    theme_bw()
8 q2_scatter</pre>
```

Figure 2: Scatter - Difflog and Presvote



• Generally speaking, difflog and voteshare are positively correlated.

3. Save the residuals of the model in a separate object.

In regression model, residuals suggests the differences between the predict values and the true values.

The formulation of residuals is: $e_i = y_i - \hat{y}_i$

In this formulation:

 e_i is residuals, y_i is the reality value, and \hat{y}_i is the value of the regression model.

Below is the R code:

```
1 ##### (3) #####
2
3 q2_residuals <- residuals (q2_reg_model)
4 str (q2_residuals)
5 summary (q2_residuals)</pre>
```

```
> str(q2_residuals) Named num [1:3193] 0.00561 0.03758 -0.05313
-0.05299 -0.04584 ...
- attr(*, "names")= chr [1:3193] "1" "2" "3" "4" ...
> summary(q2_residuals) Min. 1st Qu. Median Mean 3rd Qu. Max.
-0.321965 -0.074069 -0.001018 0.000000 0.071507 0.427435
```

Because regression model in R is a list composed of coefficients, residuals, effects and many other elements.

For coefficients, the first element is the intercept, and the second element is the slope.

Below is the R code:

```
[1] "presvote = 0.51 + 0.02 * difflog"
```

We are interested in knowing how the vote share of the presidential candidate of the incumbent's party is associated with the incumbent's electoral success.

1. Run a regression where the outcome variable is **voteshare** and the explanatory variable is **presvote**.

Below is the R code:

```
1 ##### (1) #####
2
3 q3_reg_model <- lm(voteshare ~ presvote, data=inc.sub)
4 summary(q3_reg_model)</pre>
```

Table 3: Abstract of Regression Model in Question 3

	Estimate	Std. Error	t value	$\Pr(> t)$
(Intercept)	0.441330	0.007599	58.08	<2e-16 ***
presvote	0.388018	0.013493	28.76	<2e-16 ***

```
---Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

Residual standard error: 0.08815 on 3191 degrees of freedom Multiple R-squared: 0.2058, Adjusted R-squared: 0.2056 F-statistic: 827 on 1 and 3191 DF, p-value: < 2.2e-16

- F test p-value for the entire regression model is 2.2e-16, which is very close to 0, which means we have a very high confidence in rejecting the null hypothesis. So at least one slope in regression model is not 0.
- F test p-value for the intercept and slope is both 2e-16, which is very close to 0, which means we have a very high confidence in rejecting the null hypothesis. So the estimate of intercept and slope is not 0.
- The adjusted R-squared is 0.08815, which means that the fit of this model is very bad.

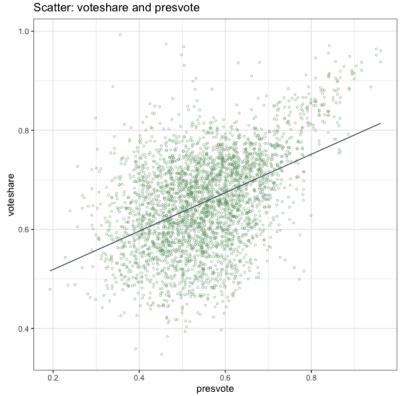
2. Make a scatterplot of the two variables and add the regression line.

Below is the R code:

```
###### (2) #####

q3_scatter <- ggplot(inc.sub, aes(x=presvote, y=voteshare)) +
geom_point(shape=1, size=0.8, color="#609966", alpha=0.4) +
geom_smooth(method="lm", se=FALSE, color="#52616B", size=0.5) +
ggtitle("Scatter: voteshare and presvote") +
theme_bw()
q3_scatter</pre>
```

Figure 3: Scatter - Voteshare and Presvote



• Generally speaking, voteshare and presvote are positively correlated.

Because regression model in R is a list composed of coefficients, residuals, effects and many other elements.

For coefficients, the first element is the intercept, and the second element is the slope.

Below is the R code:

Below is the output in R studio:

[1] "voteshare = 0.44 + 0.39 * presvote"

The residuals from part (a) tell us how much of the variation in **voteshare** is *not* explained by the difference in spending between incumbent and challenger. The residuals in part (b) tell us how much of the variation in **presvote** is *not* explained by the difference in spending between incumbent and challenger in the district.

1. Run a regression where the outcome variable is the residuals from Question 1 and the explanatory variable is the residuals from Question 2.

Below is the R code:

```
1 ####### Question 4 #######
2
3 ###### (1) ######
5 q4_reg_model <- lm(q1_residuals ~ q2_residuals , data=inc.sub)
6 summary(q4_reg_model)</pre>
```

Table 4: Abstract of Regression Model in Question 4

	Estimate	Std. Error	t value	$\Pr(> t)$
(Intercept)	-1.942e-18	1.299e-03	0.00	1
q2residuals	2.569 e-01	1.176e-02	21.84	<2e-16 ***

```
---Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

Residual standard error: 0.0733 on 3191 degrees of freedom Multiple R-squared: 0.13, Adjusted R-squared: 0.1298 F-statistic: 477 on 1 and 3191 DF, p-value: < 2.2e-16

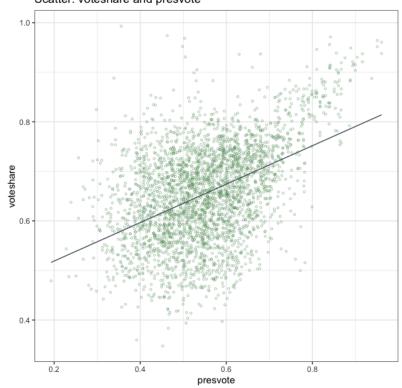
- F test p-value for the entire regression model is 2.2e-16, which is very close to 0, which means we have a very high confidence in rejecting the null hypothesis. So at least one slope in regression model is not 0.
- F test p-value for the intercept and slope is correspondingly 1 and 2e-16, the first one didn't pass the statistics test, which means the intercept is 0. And the second one is very close to 0, which means we have a very high confidence in rejecting the null hypothesis. So the estimate of slope is not 0.
- The adjusted R-squared is 0.1298, which means that the fit of this model is very bad.

2. Make a scatterplot of the two residuals and add the regression line.

Below is the R code:

```
1 ##### (2) #####
2
3 q3_scatter <- ggplot(inc.sub, aes(x=presvote, y=voteshare)) +
4    geom_point(shape=1, size=0.8, color="#609966", alpha=0.4) +
5    geom_smooth(method="lm", se=FALSE, color="#52616B", size=0.5) +
6    ggtitle("Scatter: voteshare and presvote") +
7    theme_bw()
8 q3_scatter</pre>
```

Figure 4: Scatter - q1residuals and q2residuals Scatter: voteshare and presvote



• Generally speaking, q1residuals and q2residuals are positively correlated.

Because regression model in R is a list composed of coefficients, residuals, effects and many other elements.

For coefficients, the first element is the intercept, and the second element is the slope.

Below is the R code:

```
###### (3) #####

q4_cof_vec <- coef(q4_reg_model)

q4_intercept <- q4_cof_vec[1]
q4_slope <- q4_cof_vec[2]

q4_pre_equation <- paste(
    "q1_residuals =", round(q4_intercept, 2), "+", round(q4_slope, 2), "*
    q2_residuals")
q4_pre_equation</pre>
```

```
[1] "q1\_residuals = 0 + 0.26 * q2\_residuals"
```

What if the incumbent's vote share is affected by both the president's popularity and the difference in spending between incumbent and challenger?

1. Run a regression where the outcome variable is the incumbent's voteshare and the explanatory variables are difflog and presvote.

Below is the R code:

```
1 ####### Question 5 #######
2
3 ###### (1) ######
5 q5_reg_model <- lm(voteshare ~ difflog + presvote, data=inc.sub)
6 summary(q5_reg_model)</pre>
```

Table 5: Abstract of Regression Model in Question 5

	Estimate	Std. Error	t value	$\Pr(> t)$
(Intercept)	0.4486442	0.0063297	70.88	<2e-16 ***
difflog	0.0355431	0.0009455	37.59	<2e-16 ***
presvote	0.2568770	0.0117637	21.84	<2e-16 ***

```
---Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

Residual standard error: 0.0739 on 3190 degrees of freedom Multiple R-squared: 0.4496 Adjusted R-squared: 0.4493 F-statistic: 1303 on 2 and 3190 DF, p-value: < 2.2e-16

- F test p-value for the entire regression model is 2.2e-16, which is very close to 0, which means we have a very high confidence in rejecting the null hypothesis. So at least one slope in regression model is not 0.
- F test p-value for the intercept and slope is both 2e-16, which is very close to 0, which means we have a very high confidence in rejecting the null hypothesis. So the estimate of slope and intercept is not 0.
- The adjusted R-squared is 0.4493, which means that the fit of this model is average.

Because regression model in R is a list composed of coefficients, residuals, effects and many other elements.

For coefficients, the first element is the intercept, and the second element is the slope.

Below is the R code:

```
##### (2) #####

q5_cof_vec <- coef(q5_reg_model)

q5_intercept <- q5_cof_vec[1]

q5_slope1 <- q5_cof_vec[2]

q5_slope2 <- q5_cof_vec[3]

q5_pre_equation <- paste(
    "voteshare =", round(q5_intercept, 2),
    "+", round(q5_slope1, 2), "* difflog",
    "+", round(q5_slope2, 2), "* presvote")

q5_pre_equation</pre>
```

Below is the output in R studio:

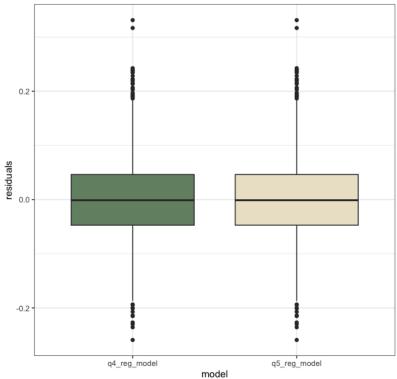
```
[1] "voteshare = 0.45 + 0.04 * difflog + 0.26 * presvote"
```

3. What is it in this output that is identical to the output in Question 4? Why do you think this is the case?

I found that the residuals in question 4's regression model is the same as the one in question 5. We can check that in R code and box plot. Below is the R code:

```
ggtitle("Boxplot: Residuals in Question 4 and 5") +
theme_bw()
q5_boxplot
```

Figure 5: Boxplot - Residuals in Question 4 and 5 Boxplot: Residuals in Question 4 and 5



If two regression model's residuals is the same, we can conclude that:

- The homoskedasticity assumption is met: the residual variances of the two models are similar at different levels of the explanatory variables.
- The model fits the data well: The presence of homoscedasticity may indicate that the model fits the data well because it meets the basic assumptions of linear regression.
- Reliability of model comparisons and interpretations: Model comparisons and interpretation of model results can be made more reliably if the residuals of two models are the same.