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Deductive Verification  
based on Hoare logic

Separation Logic

Prusti

First Words

Key Questions

Mechanism Overview

Evaluation

Conclusion

# Leveraging Rust Types for Modular Specification and Verification

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# What is verification like, anyway?

Verification  $\neq$  Absence of bugs



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## What is verification like, anyway?

**Verification  $\neq$  Absence of bugs**

Program  $\xrightarrow{\textit{satisfies}}$  Property  
or, in verification speak:

Implementation  $\xrightarrow{\textit{satisfies}}$  Specification

# What is verification like, anyway?

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## Properties



- no null pointer dereferences;
- no integer / buffer overflows;
- no data races;
- some property  $P(\text{output}, \text{input})$  holds  
→ *functional specifications*

# What is verification like, anyway?

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## Properties



- no null pointer dereferences;
- no integer / buffer overflows;
- no data races;
- some property  $P(\text{output}, \text{input})$  holds  
→ *functional specifications*



- does what I want;
- no bugs;
- no vulnerabilities

# A binary search function

```
1 method Binfind(a: seq<int>, v: int) returns (rv: int)
2 {
3   rv := -1;
4   var l, r := 0, |a|;
5   if |a| = 0 { return; }
6   while l + 1 < r {
7     var mid := (l + r) / 2;
8     if v = a[mid] { rv := mid; return; }
9     else if v < a[mid] { r := mid; }
10    else { l := mid; }
11  }
12  if a[l] = v { rv := l; return; }
13  rv := -1; return;
14 }
```

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## A binary search function cont.

```

1 method Binfind(a: seq<int>, v: int) returns (rv: int)
2   requires // PRECONDITION: sorted
3      $\forall i, j :: 0 \leq i \leq j < |a| \rightarrow a[i] \leq a[j]$ 
4   ensures // POSTCONDITION: not found
5      $rv = -1 \rightarrow \forall j :: 0 \leq j < |a| \rightarrow a[j] \neq v$ 
6   ensures // POSTCONDITION: found
7      $rv \geq 0 \rightarrow rv < |a| \wedge a[rv] = v$ 
8 {
9   rv := -1;
10  var l, r := 0, |a|;
11  if |a| = 0 { return; }
12  while l + 1 < r {
13    var mid := (l + r) / 2;
14    if v = a[mid] { rv := mid; return; }
15    else if v < a[mid] { r := mid; }
16    else { l := mid; }
17  }
18  if a[l] = v { rv := l; return; }
19  rv := -1; return;
20 }
```

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## A binary search function cont.

```

1 method Binfind(a: seq<int>, v: int) returns (rv: int)
2   // requires and ensures ...
3 {
4   rv := -1;
5   var l, r := 0, |a|;
6   if |a| = 0 { return; }
7   while l + 1 < r
8     // LOOP INVARIANTS
9     invariant 0 ≤ l < r ≤ |a|
10    invariant ∀ i :: 0 ≤ i < l → a[i] < v
11    invariant ∀ i :: r ≤ i < |a| → v < a[i]
12  {
13    var mid := (l + r) / 2;
14    if      v = a[mid] { rv := mid; return; }
15    else if v < a[mid] { r := mid; }
16    else           { l := mid; }
17  }
18  if a[l] = v { rv := l; return; }
19  rv := -1; return;
20 }

```

## A binary search function cont.

```
1 method Binfind(a: seq<int>, v: int) returns (rv: int)
2   // requires and ensures ...
3   {
4     rv := -1;
5     var l, r := 0, |a|;
6     if |a| = 0 { return; }
7     while l + 1 < r
8       // loop invariants
9     {
10      var mid := (l + r) / 2;
11      if v = a[mid] { rv := mid; return; }
12      else if v < a[mid] { r := mid; }
13      else { l := mid; }
14    }
15    if a[l] = v { rv := l; return; }
16    assert l + 1 = r // ASSERTION
17    rv := -1; return;
18  }
```

# The language

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## Elements

- Basic expressions / statements
- Preconditions, postconditions
- Loop invariants
- Assertions
- Propositions : FOF ( $\wedge, \vee, \neg, \forall, \exists$ )

## Characteristics

- Imperative.
- No pointers. No dynamic memory allocation.

Bad for systems programming.

# Verification Mechanism

Encode the conditions into a logical formula. Prove the formula is always true.

```
1 method NonzeroSquare(a: int) returns (rv: int)
2   requires a ≠ 0
3   ensures  rv > 0
4   {
5
6   rv := a * a;
7
8   }
```

# Verification Mechanism cont.

Automatically synthesis Hoare triples  $\{P\} s \{Q\}$ .

$P$  and  $Q$ : propositions.  $s$ : statement.

```
1 method NonzeroSquare(a: int) returns (rv: int)
2   requires a ≠ 0
3   ensures  rv > 0
4   {
5     // { a ≠ 0 ∧ a * a = a * a }
6     rv := a * a;
7     // { a ≠ 0 ∧ rv = a * a }
8   }
```

Hoare triple of assignment:  $\{Q[x \mapsto e]\} x := e \{Q\}$

## Verification Mechanism cont.

Automatically synthesis Hoare triples  $\{P\} s \{Q\}$ .

$P$  and  $Q$ : propositions.  $s$ : statement.

```

1 method NonzeroSquare(a: int) returns (rv: int)
2   requires a ≠ 0
3   ensures  rv > 0
4   {
5     // { a ≠ 0 ∧ a * a = a * a }
6     rv := a * a;
7     // { a ≠ 0 ∧ rv = a * a }
8   }

```

Hoare triple of assignment:  $\{Q[x \mapsto e]\} x := e \{Q\}$

Prove the validity of

$$(a \neq 0 \wedge rv = a \times a) \rightarrow (rv > 0)$$

# Verification Mechanism cont.

Prove the validity of

$$(a \neq 0 \wedge rv = a \times a) \rightarrow (rv > 0)$$

- Automatic: SMT solvers  $\rightarrow$  z3
- Semi-automatic: theorem provers  $\rightarrow$  coq

- Manual:



# Pointers aliasing is bad for verification

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## Problem with Hoare logic

No pointers. No heaps i.e. dynamically allocated memory.

We could extend Hoare logic with pointers in some way ...



# A binary tree example

```
1 method FreeBinTree(a: BinTree*) returns ()
2 {
3   if a = NIL { return; }
4   FreeBinTree(a->lc);
5   FreeBinTree(a->rc);
6   free(a);
7 }
```

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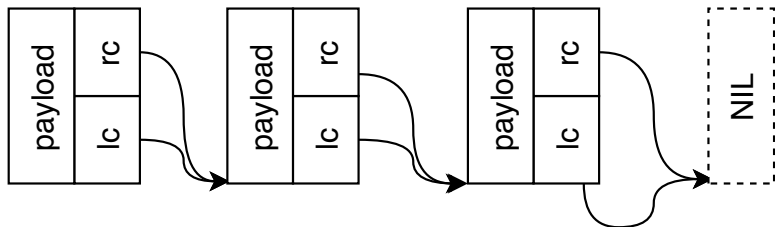
# A binary tree example

```

1 method FreeBinTree(a: BinTree*) returns ()
2 {
3   if a = NIL { return; }
4   FreeBinTree(a->lc);
5   FreeBinTree(a->rc);
6   free(a);
7 }

```

Seems ok. But what if ...



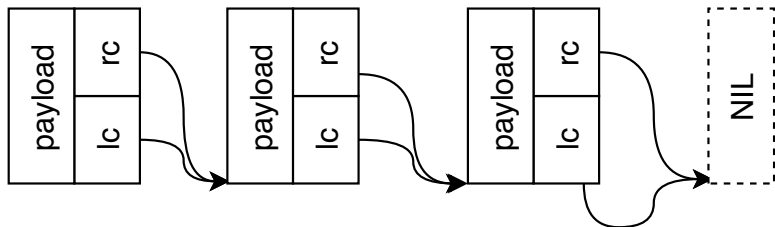
# A binary tree example

```

1 method FreeBinTree(a: BinTree*) returns ()
2 {
3   if a = NIL { return; }
4   FreeBinTree(a->lc);
5   FreeBinTree(a->rc);
6   free(a);
7 }

```

Seems ok. But what if ...



→ Double free!

# A binary tree example cont.

## Add a precondition

```
1 method FreeBinTree(a: BinTree*) returns ()
2   requires IsBinTree(a)
3   {
4     if a = NIL { return; }
5     FreeBinTree(a->lc);
6     FreeBinTree(a->rc);
7     free(a);
8   }
```

## Naively, $\wedge$ (logical and)

```
1 predicate IsBinTree(a: BinTree*)
2   { a = NIL  $\vee$  (IsBinTree(a->lc)  $\wedge$  IsBinTree(a->rc)) }
```

# A binary tree example cont.

## Add a precondition

```
1 method FreeBinTree(a: BinTree*) returns ()
2   requires IsBinTree(a)
3   {
4     if a = NIL { return; }
5     FreeBinTree(a->lc);
6     FreeBinTree(a->rc);
7     free(a);
8   }
```

Separation logic:  $*$  (and, separately)

```
1 predicate IsBinTree(a: BinTree*)
2   { a = NIL  $\vee$  (IsBinTree(a->lc) * IsBinTree(a->rc)) }
```

$a \rightarrow lc$  and  $a \rightarrow rc$  must not alias.

# Separation Logic

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## Key insight

Aliasing needs special attention!

→ Rust's exclusive ownership

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```

1 method Binfind(a: seq<int>, v: int) returns (rv: int)
2   requires forall i, j :: 0 <= i <= j < |a| => a[i] <= a[j]
3   ensures rv == -1 => forall j :: 0 <= j < |a| => a[j] != v
4   ensures rv >= 0 => rv < |a| && a[rv] == v
5 {
6   rv := -1;
7   var l, r := 0, |a|;
8
9   if |a| == 0 { return; }
10
11  while l + 1 < r
12    invariant 0 <= l < r <= |a|
13    invariant forall i :: 0 <= i < l => a[i] < v
14    invariant forall i :: r <= i < |a| => v < a[i]

```

## Status

Still a prototype. ☹️

```

#[ensures="forall k: usize :: (0 <= k && k < arr.len()) ==> arr.lookup(k) == old(arr.lookup(k))"]
#[ensures="elem == old(*elem)"]
#[ensures="result.is_none() ==>
  (forall k: usize :: (0 <= k && k < arr.len()) ==> *elem != arr.lookup(k))"]
#[ensures="result.is_some() ==> {
  0 <= result.peek() && result.peek() < arr.len() &&
  arr.lookup(result.peek()) == *elem"}]
fn binary_search(arr: &mut Vec<u8>, elem: &mut i32) -> usizeOption
{
  let mut size = arr.len();
  let mut base = 0;
  let mut end = base + size;

  let mut result = usizeOption::None;
  let mut continue_loop = size > 0;

  #[invariant="0 <= base"]
  #[invariant="0 <= size"]
  #[invariant="base < 18446744073709551615 - size"]
  #[invariant="base + size <= arr.len()"]
  #[invariant="continue_loop == (size > 0 && result.is_none())"]
  #[invariant="arr.len() == old(arr.len())"]
  #[invariant="*elem == old(*elem)"]
  #[invariant="forall k1: usize, k2: usize :: (0 == k1 && k2 < k2 && k2 < arr.len()) ==>
    arr.lookup(k1) == arr.lookup(k2)"]
  #[invariant="forall k: usize :: (0 <= k && k < arr.len()) ==> arr.lookup(k) == old(arr.lookup(k))"]
  #[invariant="forall k: usize :: (0 <= k && k < base) ==> arr.lookup(k) == *elem"]
  #[invariant="result.is_none() ==>
    (forall k: usize: (base + size <= k && k < arr.len()) ==> *elem < arr.lookup(k))"]
  #[invariant="result.is_some() ==> {
    0 <= result.peek() && result.peek() < arr.len() &&
    arr.lookup(result.peek()) == *elem"}]
  while continue_loop {
    let half = size / 2;
    let mid = base + half;

    let mid_element = arr.borrow[mid];
    let cmp_result = cmp(mid_element, elem);
    base = base + if cmp_result == < { half } else { -half };
    size = size - if cmp_result == < { half } else { half };
  }
}

```



# Closer look

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```
#[requires="forall k1: usize, k2: usize :: (0 <= k1 && k1 < k2 && k2 < arr.len()) ==>
    arr.lookup(k1) <= arr.lookup(k2)"]
// ...
#[ensures="result.is_none() ==>
    (forall k: usize :: (0 <= k && k < arr.len()) ==> *elem != arr.lookup(k)"]
#[ensures="result.is_some() ==> (
    0 <= result.peek() && result.peek() < arr.len() &&
    arr.lookup(result.peek()) == *elem)"]
fn binary_search(arr: &mut VecWrapperI32, elem: &mut i32) -> usize::Option
{
    let mut size = arr.len();
    let mut base = 0;
    let mut end = base + size;

    let mut result = usize::None;
    let mut continue_loop = size > 0;

    #[invariant="0 <= base"]
    #[invariant="0 <= size"]
    #[invariant="base + size <= arr.len()"]
    // ...
    #[invariant="forall k: usize:: (0 <= k && k < base) ==> arr.lookup(k) < *elem"]
    #[invariant="result.is_none() ==>
        (forall k: usize:: (base + size <= k && k < arr.len()) ==> *elem < arr.lookup(k)"]
    // ...
    while continue_loop {
        let half = size / 2;
        let mid = base + half;

        let mid_element = arr.borrow(mid);
        let cmp_result = cmp(mid_element, elem);
        base = match cmp_result {
            Less => {
                mid
            },

```

# Research Question

Deductive verification in Rust.

## Key Questions

- How automatic? → “fully automatic”
- Mechanism overview → program translation
- Infrastructures? → bottom-most: z3
- Why Rust? How about C? → controlled aliasing
- Dealing with libraries? → wrappers

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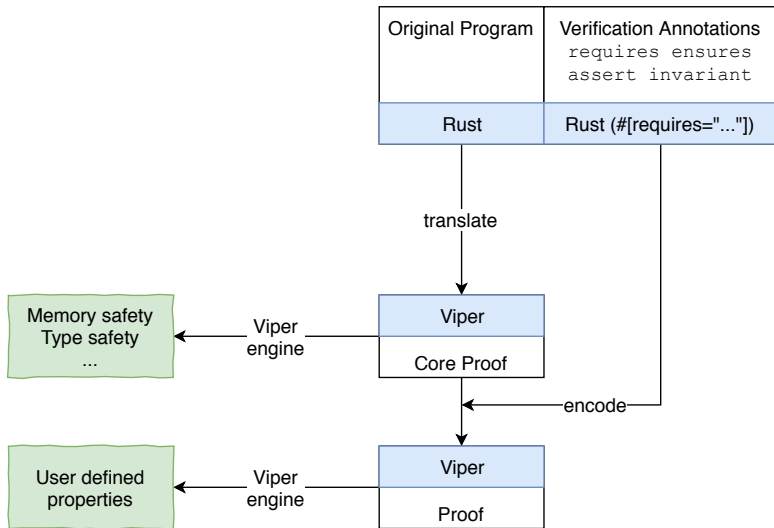
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## Flow graph



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## Verification Language: Viper

- Implicit Dynamic Frames Logic  $\rightarrow$  Separation Logic
- Pointers, heaps!
- Resource capability

## The bottom-most

- Symbolic execution verifier
- z3

# Why Rust?

Reason: what logic do we use for verification?

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# Why Rust?

Reason: what logic do we use for verification? Separation logic:

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# Why Rust?

Reason: what logic do we use for verification? Separation logic: aliasing!

```
struct Node {  
    val: i32,  
    l: Box<Tree>,  
    rc: Box<Tree>  
}
```

Node.lc and Node.rc must not alias.

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- `#[trusted]`
- wrappers

```
62 impl VecWrapperI32 {
63     #[trusted]
64     #[pure]
65     #[ensures="result >= 0"]
66     #[ensures="result < 18446744073709551615"]
67     pub fn len(&self) -> usize {
68         self.v.len()
69     }
70
71     #[trusted]
72     #[ensures="result.len() == 0"]
73     pub fn new() -> Self {
74         VecWrapperI32{ v: Vec::new() }
75     }
76
77     #[trusted]
78     #[pure]
79     #[requires="0 <= index && index < self.len()"]
80     pub fn lookup(&self, index: usize) -> i32 {
81         self.v[index]
82     }

```



# Evaluation questions

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## Core proof

- 500 popular crates
- automatic generation
- verification time:  $90\% < 2 \text{ sec}$

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## Core proof

- 500 popular crates
- automatic generation
- verification time:  $90\% < 2 \text{ sec}$

## Overflow & panic freedom

- filtered, 519 functions
- automatic assertion generation
- error in 467 functions

# Evaluation questions

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### Core proof

- 500 popular crates
- automatic generation
- verification time:  $90\% < 2 \text{ sec}$

### Overflow & panic freedom

- filtered, 519 functions
- automatic assertion generation
- error in 467 functions

### Functional specification

- Hand constructed data, 11 files
- e.g. binary search

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# Main takeaways

- Automatic verification: z3

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# Main takeaways

- Automatic verification: z3
- Throw work to infrastructure

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# Main takeaways

- Automatic verification: z3
- Throw work to infrastructure
- Aliasing with mutability is bad → Rust, SL

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