



Oregon State
University

COLLEGE OF ENGINEERING | School of Electrical Engineering
and Computer Science

CS 161

Introduction to CS I

Lecture 21

- Recursion



Assignment 5 – Treasure Chest

- Define your own struct (type) with at least 4 attributes
- Create a program to store items of that type in a treasure chest and keep track of the total collection value
- User can:
 - Add item
 - Remove item
 - Display item
 - Add an item with random properties
 - <Your choice here>

No live demo
(README.txt instead)

Midterm 2

- Midterm 2: content through **week 7** (but no structs)
- Review questions (and solutions) are on course website
- Bring your questions to class on Wednesday
 - Stuck on pointers? Functions? 2D arrays?
- Review session: Thursday 2/27, 6-7 p.m., **LINC 228**
- Midterm: Friday 2/28, 2-2:50 p.m., **LINC 100**
- Format: true/false, multiple choice, one page short answer
 - Scantron sheet: fill in bubbles with #2 pencil
- Bring to midterm: **student ID and #2 pencil(s)**



Let's calculate factorials

- Mathematical definition

$$0! := 1;$$

$$\begin{aligned} n! &:= n * (n-1) * \dots * 1 \\ &:= n * (n-1)! \end{aligned} \quad \text{if } n > 0$$

Iterative factorial

Iterative definition:

$\text{factorial}(0) := 1;$

$\text{factorial}(n) := n * (n-1) * (n-2) * \dots * 3 * 2 * 1;$

See lec21-factorial-iterative.cpp

```
1. int factorial(int n) {  
2.     int fact;  
3.     if (n==0)  
4.         fact = 1;  
5.     else  
6.         for (fact=n; n > 1; n--)  
7.             fact = fact * (n-1);  
8.     return fact;  
9. }
```

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Computing Factorial Iteratively

```
factorial(4) = 4 * 3  
            = 12 * 2  
            = 24 * 1  
            = 24
```

```
factorial(0) = 1;  
factorial(n) = n*(n-1)*...*2*1;
```

Recursion

- A recursive definition includes a mention of itself
 - "My descendants are my children + all of my children's descendants."
 - "My keys are located in this room or in some other room."
- A recursive function includes [at least one] call to itself
 - Base case: when to stop (simplest case)
 - Recursive step: a general statement that reduces the task (eventually) to a base case

Recursive Factorial

See lec21-factorial-recursive.cpp

Recursive definition:

Base case: $\text{factorial}(0) = 1$;

Recursive step: $\text{factorial}(n) = n * \text{factorial}(n-1)$;

```
1. int factorial(int n) {  
2.     if (n == 0) /* Base case */  
3.         return 1;  
4.     else  
5.         /* recursive call */  
6.         return n * factorial(n - 1);  
7. }
```

Computing Factorial Recursively

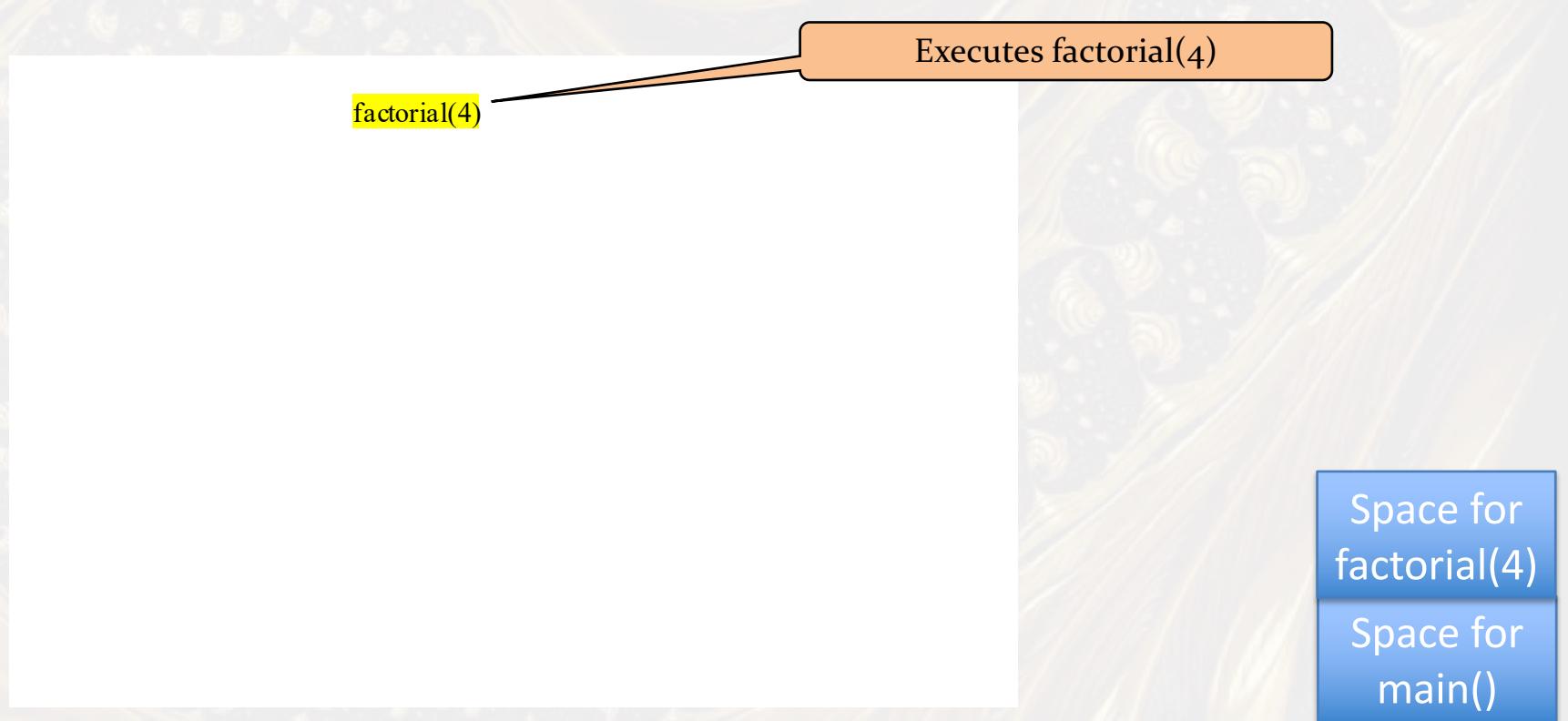
$$\begin{aligned}\text{factorial}(4) &= 4 * \text{factorial}(3) \\ &= 4 * (3 * \text{factorial}(2)) \\ &= 4 * (3 * (2 * \text{factorial}(1))) \\ &= 4 * (3 * (2 * (1 * \text{factorial}(0)))) \\ &= 4 * (3 * (2 * (1 * 1))) \\ &= 4 * (3 * (2 * 1)) \\ &= 4 * (3 * 2) \\ &= 4 * 6 \\ &= 24\end{aligned}$$

```
factorial(0) = 1;  
factorial(n) = n*factorial(n-1);
```

Differences

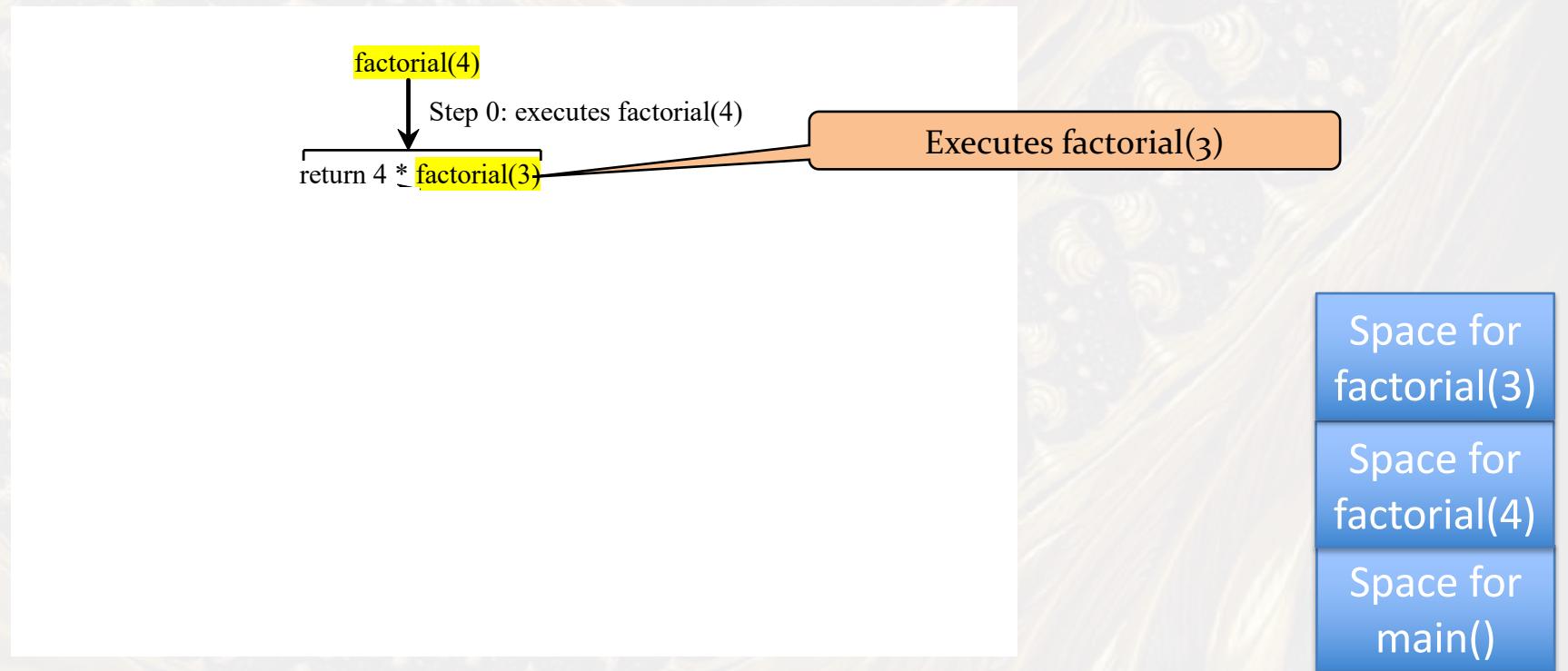
- Pros
 - Readability
- Cons
 - Efficiency
 - Memory

Recursive Factorial

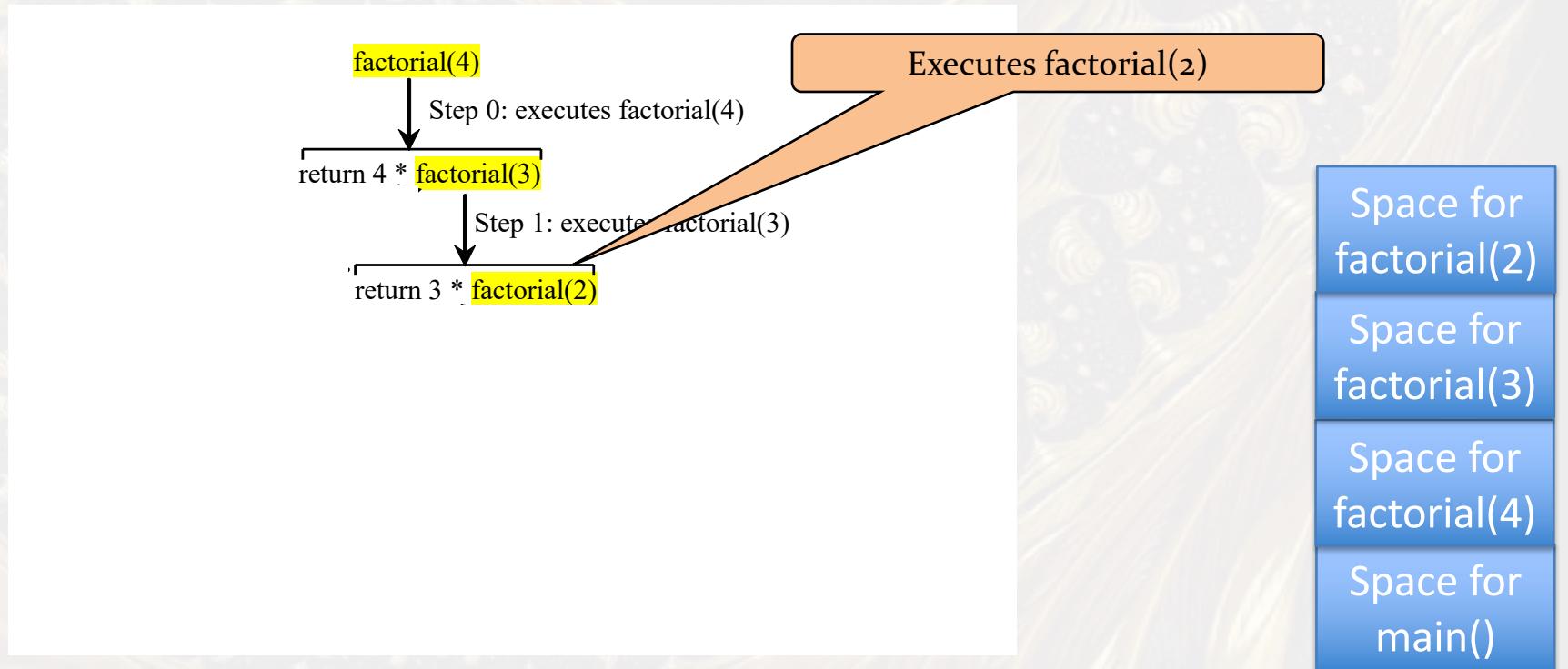


Recursive Factorial

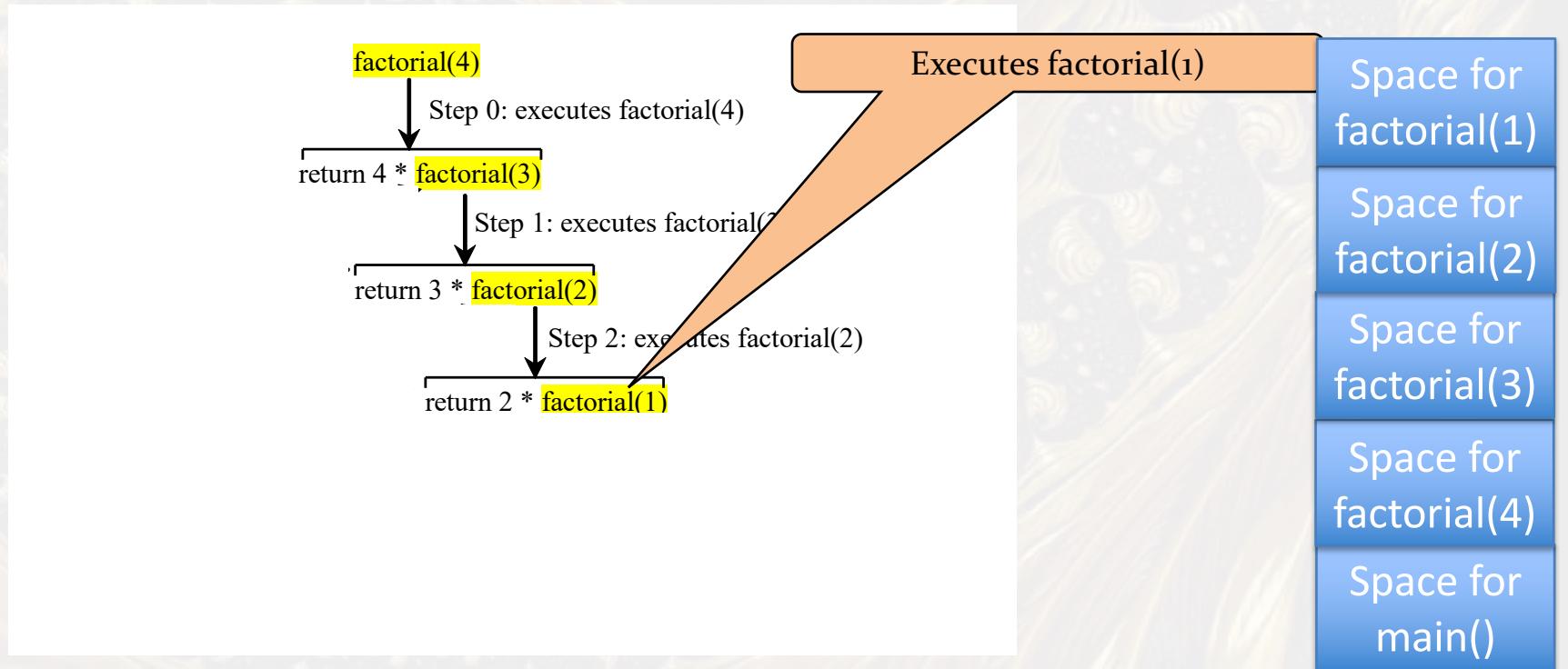
Stack



Recursive Factorial



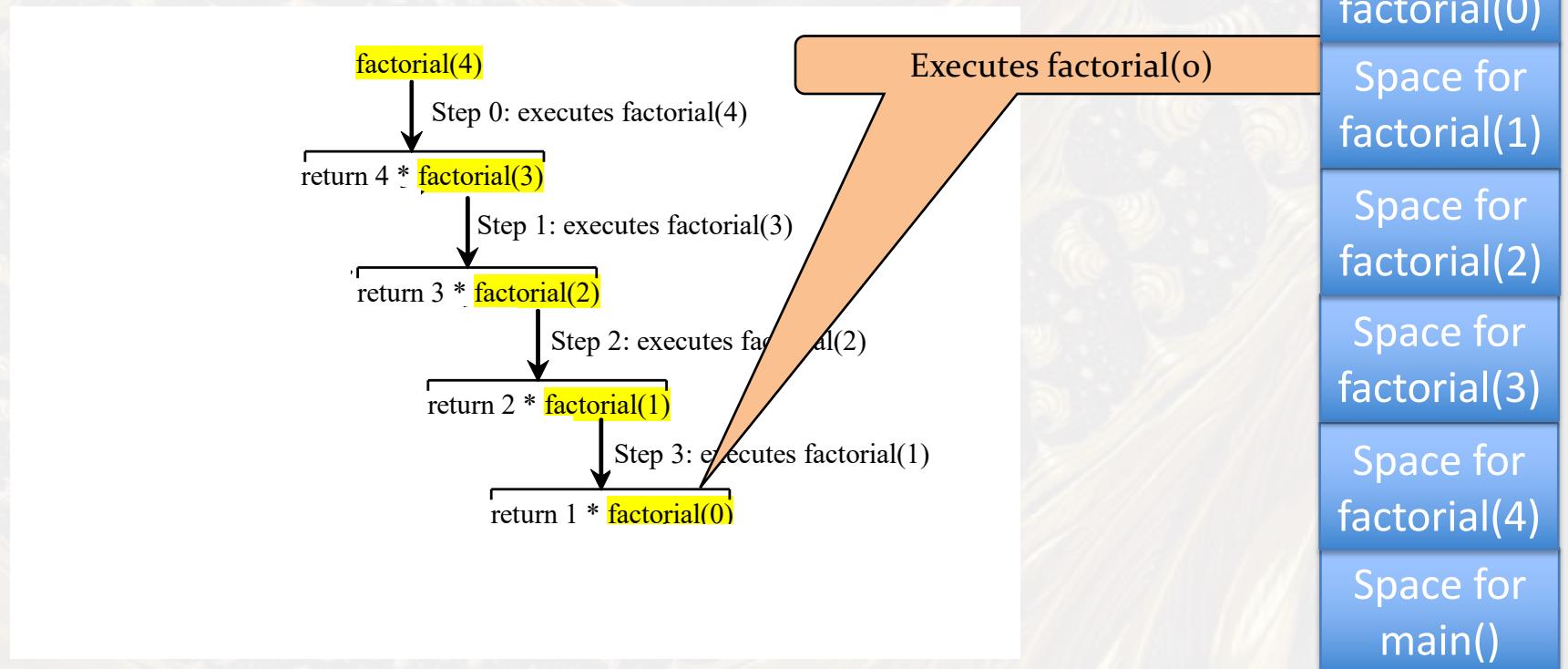
Recursive Factorial





Recursive Factorial

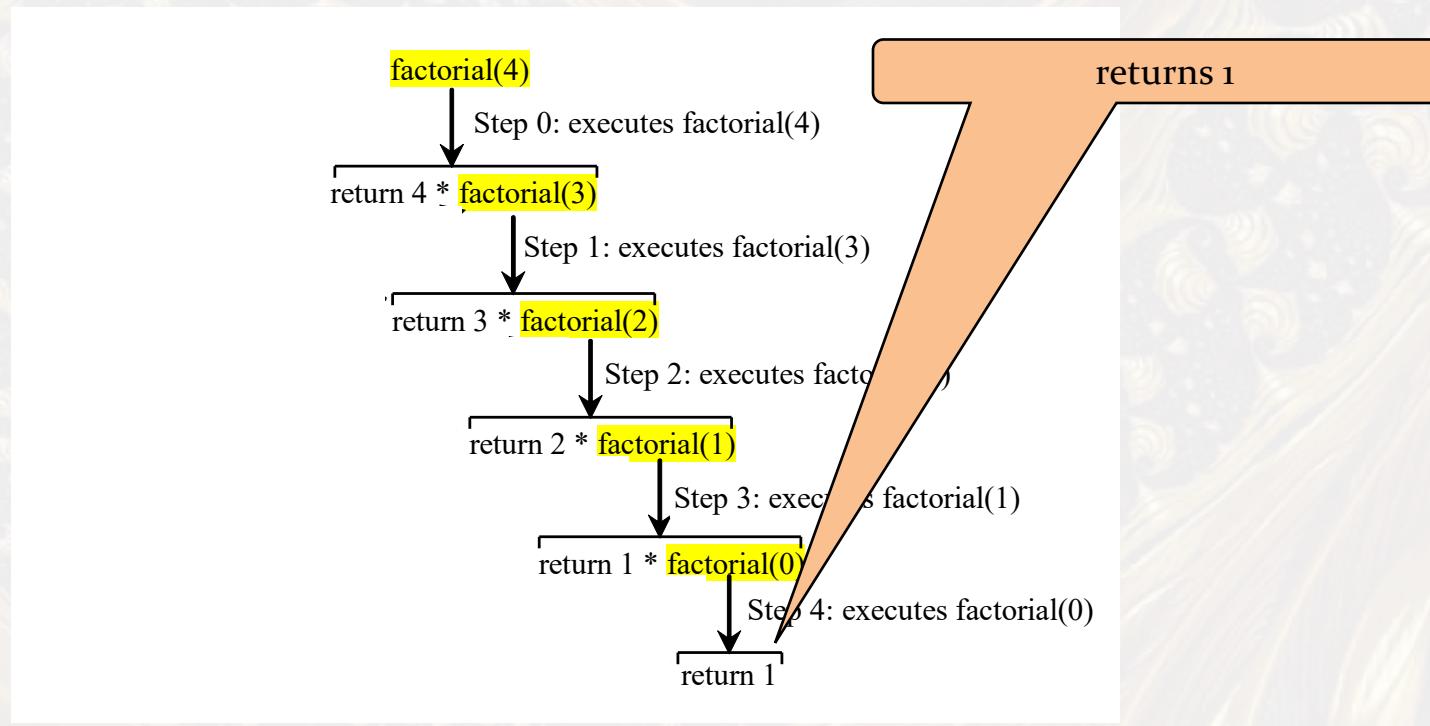
Stack



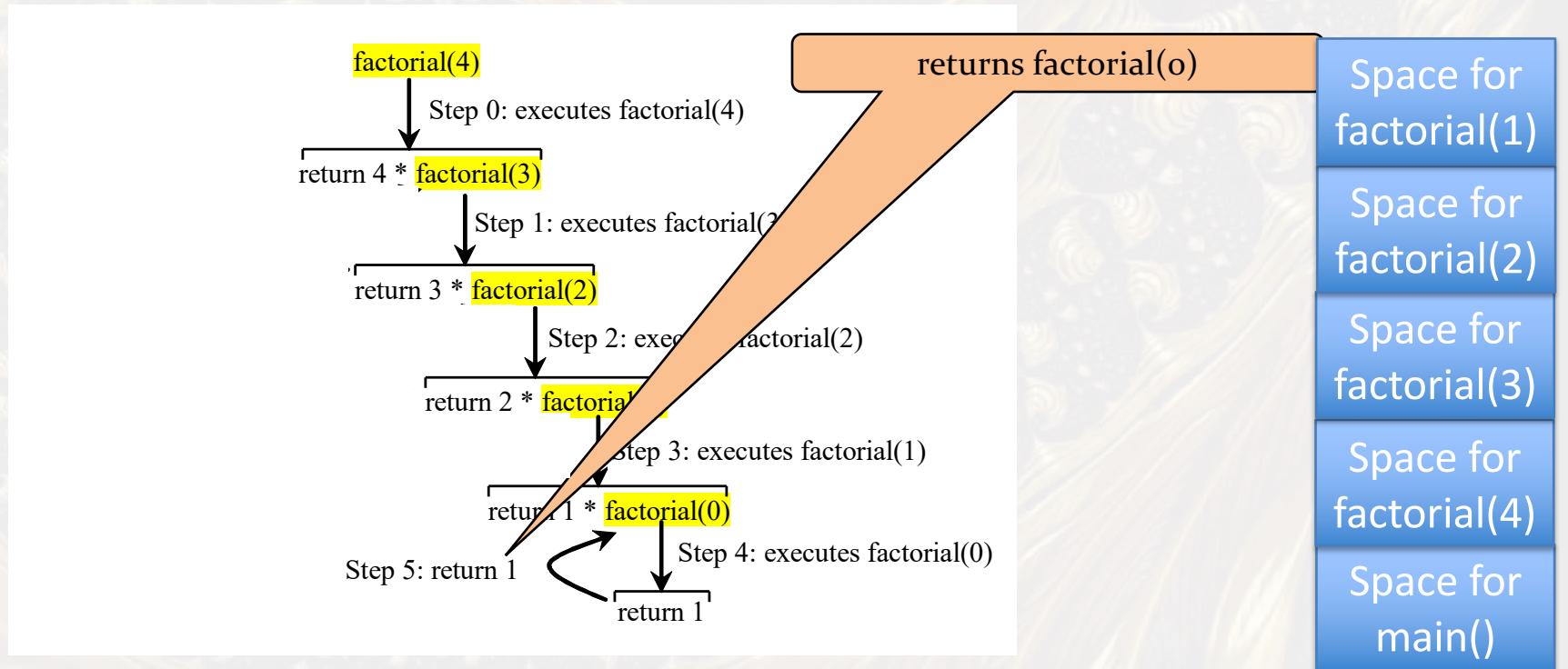


Recursive Factorial

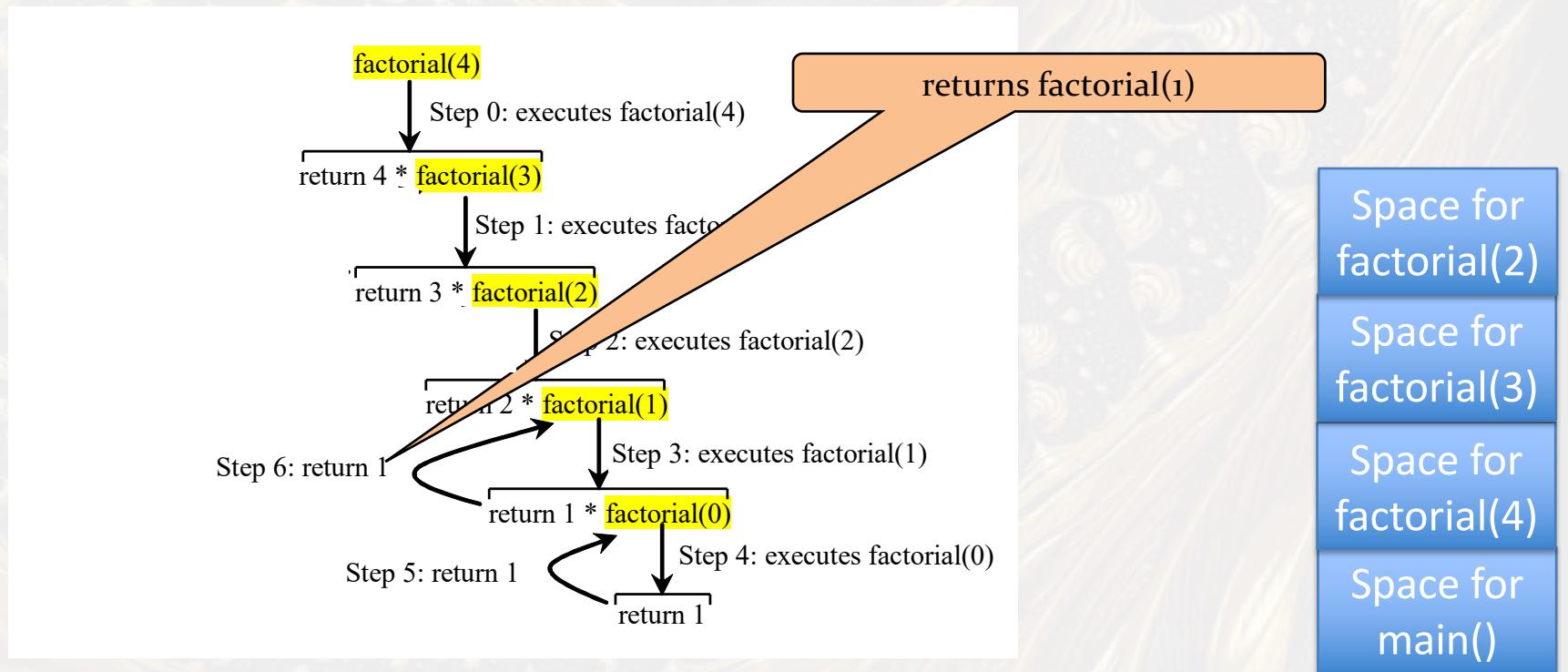
Stack



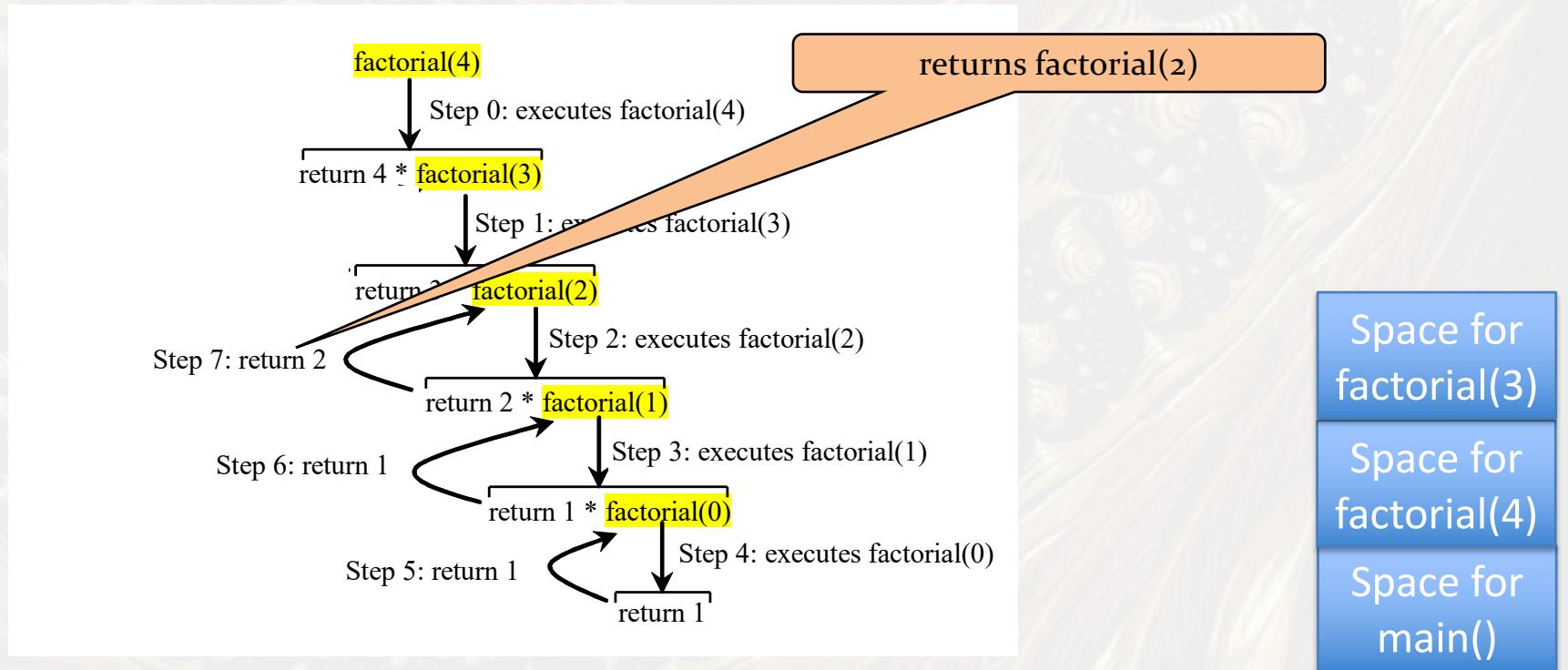
Recursive Factorial



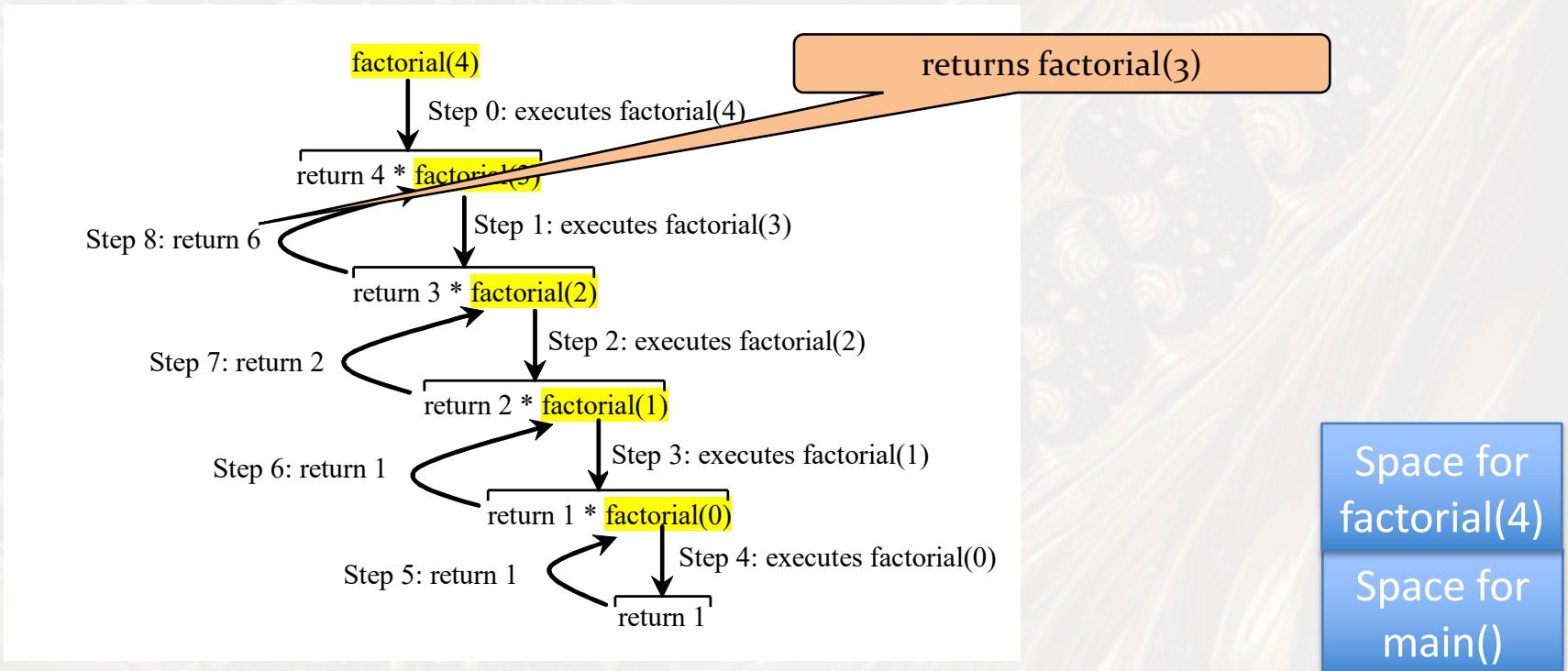
Recursive Factorial



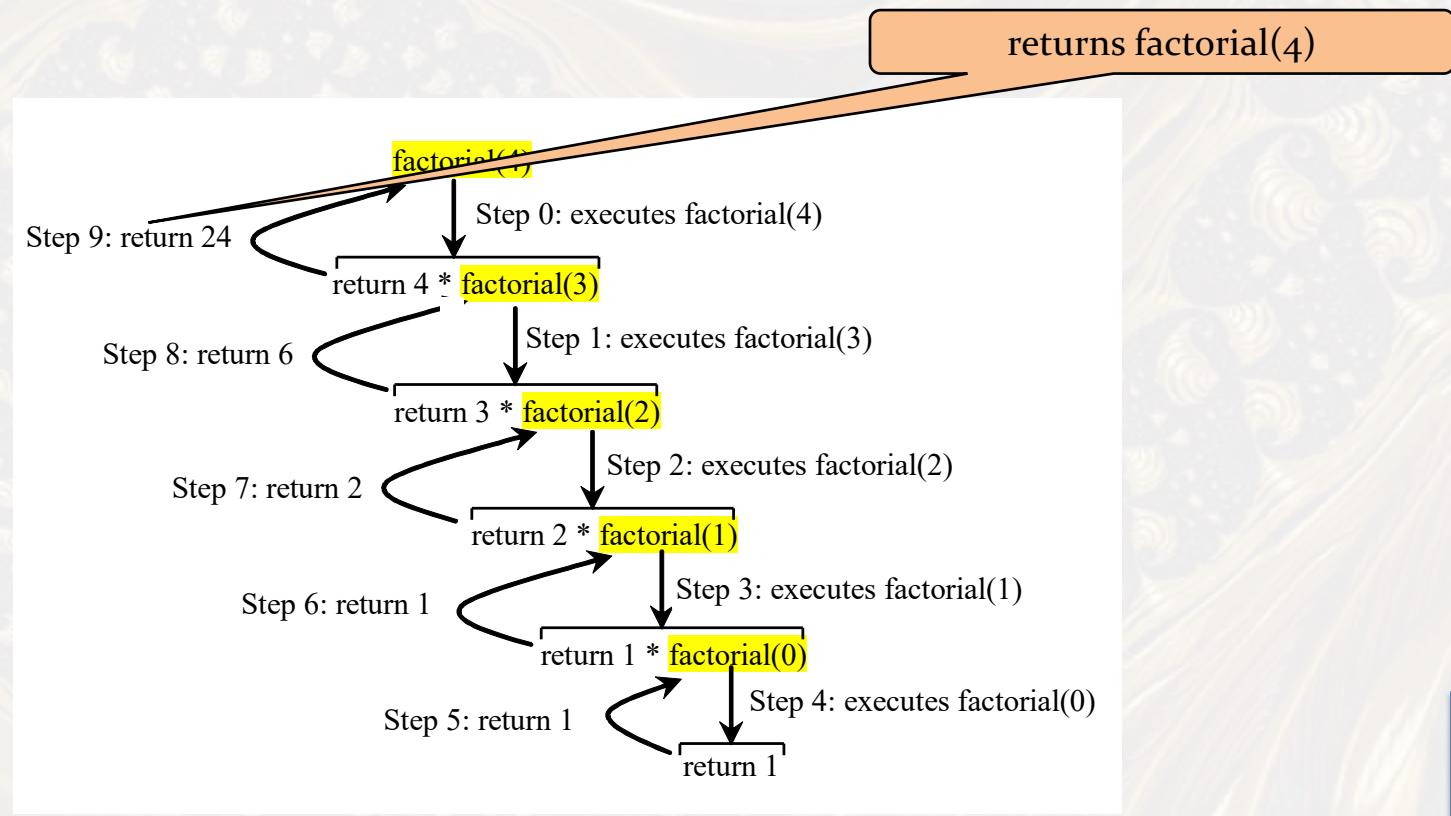
Recursive Factorial



Recursive Factorial



Stack



When is recursion useful?

- Problems that have a "nested" or recursive structure and would be hard to write in an iterative fashion
 - Water in a river is the sum of the water from each tributary
 - Recursion breaks the problem into one small step + "the rest of the solution"



Your turn: descendants

- "My number of descendants is my number of children + the sum of my children's descendants."
 - What is the **base case**?
 - What is the **recursive step**?

Your turn: descendants

- "My number of descendants is my number of children + the sum of my children's descendants."
 - What is the **base case**?
 - No children: #descendants = 0
 - What is the **recursive step**?
 - $\# \text{descendants} = \# \text{children} + \# \text{descendants}(\text{child1}) + \# \text{descendants}(\text{child2}) + \dots$
 - This would be quite difficult to do in an iterative way!

Your turn: exponents

- Compute **base^{exp}** in a recursive function
 - What is the function prototype?
 - What is the **base case**?
 - What is the **recursive step**?

Your turn: exponents

- Compute **base^{exp}** in a recursive function called pwr()
 - What is the function prototype?
 - int pwr(int base, int exp);
 - What is the **base case**?
 - What is the **recursive step**?

Your turn: exponents

- Compute **base^{exp}** in a recursive function called pwr()
 - What is the function prototype?
 - `int pwr(int base, int exp);`
 - What is the **base case**?
 - $\text{exp} = 0$: return 1
 - What is the **recursive step**?
 - $\text{exp} > 0$: return $\text{base} * \text{pwr}(\text{base}, \text{exp}-1)$

Exponent implementation

See lec21-power-recursive.cpp

```
1. int pwr(int base, int exp) {  
2.     if (exp == 0) /* base case */  
3.         return 1;  
4.     else  
5.         /* recursive call */  
6.         return base * pwr(base, exp - 1);  
7. }
```

Gotchas

- Failure to specify base case => stack overflow
- Failure to reach base case => stack overflow
 - Problem doesn't get smaller

```
int myfun(int n) {  
    if (n == 0)  
        return 0;  
    else  
        return myfun(n);  
}
```

What vocabulary did we learn today?

- Recursion
- Base case
- Recursive step

What ideas and skills did we learn today?

- How to design solutions with recursive definitions
- How to translate a recursive definition into a recursive function
- Merits of iteration versus recursion

Week 8 begins!

- Attend lab (laptop required)
- Read Rao lesson 7 (pp. 158-161)
Read Miller lecture 8:
<http://www.doc.ic.ac.uk/~wjk/C++Intro/RobMillerL8.html>
- Start on design for **Assignment 5** (due **Sunday, March 1**)

See you Wednesday (midterm review)!

- Bring your questions about material from weeks 1-7