

Program Structures and Algorithms

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NAME: Xinyi Xu

NUID: 002856992

Code Screenshots:

```
J PriorityQueue.java 5 J QuadPriorityQueue.java 1, U X J Benchmark_Timer.java J BenchmarkHeap.java 3, U
src > main > java > edu > neu > coe > info6205 > pq > J QuadPriorityQueue.java > ...
1 package edu.neu.coe.info6205.pq;
2
3 import java.util.*;
4 import java.util.function.BiPredicate;
5 import java.util.function.Consumer;
6
7 public class QuadPriorityQueue<K> implements Iterable<K> {
8
9     public QuadPriorityQueue(boolean max, Object[] quadHeap, int first, int last, Comparator<K> comparator, boolean floyd) {
10         this.max = max;
11         this.first = first;
12         this.comparator = comparator;
13         this.last = last;
14         this.quadHeap = (K[]) quadHeap;
15         this.floyd = floyd;
16     }
17
18     public QuadPriorityQueue(int n, int first, boolean max, Comparator<K> comparator, boolean floyd) {
19         this(max, new Object[n + first], first, last:0, comparator, floyd);
20     }
21
22     public QuadPriorityQueue(int n, boolean max, Comparator<K> comparator, boolean floyd) {
23         this(n, first:1, max, comparator, floyd);
24     }
25
26     public QuadPriorityQueue(int n, boolean max, Comparator<K> comparator) {
27         this(n, first:1, max, comparator, floyd:false);
28     }
29
30     public QuadPriorityQueue(int n, Comparator<K> comparator) {
31         this(n, first:1, max:true, comparator, floyd:true);
32     }
33
34     public boolean isEmpty() {
35         return last == 0;
36     }
37
38     public int size() {
39         return last;
40     }
41 }
```

```

42 public void give(K key) {
43     if (last == quadHeap.length - first)
44         last--;
45     quadHeap[++last + first - 1] = key;
46     swimUp(last + first - 1);
47 }
48
49 public K take() throws PQException {
50     if (isEmpty()) throw new PQException(msg:"4-ary Heap is empty");
51     if (floyd) return doTake(this::snake);
52     else return doTake(this::sink);
53 }
54
55 K doTake(Consumer<Integer> f) {
56     K result = quadHeap[first];
57     swap(first, last-- + first - 1);
58     f.accept(first);
59     quadHeap[last + first] = null;
60     return result;
61 }
62
63 void sink(int k) {
64     doHeapify(k, (a, b) -> !unordered(a, b));
65 }
66
67 private int doHeapify(int k, BiPredicate<Integer, Integer> p) {
68     int i = k;
69     while (firstChild(i) <= last + first - 1) {
70         int j = firstChild(i);
71         for (int c = 1; c < 4; c++) {
72             if (j + c < last + first - 1 && unordered(j, j + c)) j++;
73         }
74         if (!unordered(k, j)) break;
75         swap(i, j);
76         i = j;
77     }
78     return i;
79 }
--

```

```

81 void snake(int k) {
82     swimUp(doHeapify(k, (a, b) ->!unordered(a, b)));
83 }
84
85 void swimUp(int k) {
86     int i = k;
87     while (i > first && unordered(parent(i), i)) {
88         swap(i, parent(i));
89         i = parent(i);
90     }
91 }
92
93 private void swap(int i, int j) {
94     K tmp = quadHeap[i];
95     quadHeap[i] = quadHeap[j];
96     quadHeap[j] = tmp;
97 }
98
99 boolean unordered(int i, int j) {
100     if (quadHeap[i] == null || quadHeap[j] == null) {
101         return false;
102     }
103     return (comparator.compare(quadHeap[i], quadHeap[j]) > 0) ^ max;
104 }
105
106 private int parent(int k) {
107     return (k + 1 - first) / 4 + first - 1;
108 }
109
110 private int firstChild(int k) {
111     return (k + 1 - first) * 4 + first - 1;
112 }
113
114 private final boolean max;
115 private final int first;
116 private final Comparator<K> comparator;
117 private final K[] quadHeap;
118 private int last;
119 private final boolean floyd;
120
121 public Iterator<K> iterator() {
122     Collection<K> copy = new ArrayList<>(Arrays.asList(Arrays.copyOf(quadHeap, last + first)));
123     Iterator<K> result = copy.iterator();
124     if (first > 0) result.next();
125     return result;
126 }
127 }

```

J PriorityQueue.java 5

J QuadPriorityQueue.java 1, U

J Benchmark_Timer.java

J BenchmarkHeap.java 1, U X

src > main > java > edu > neu > coe > info6205 > util > J BenchmarkHeap.java > BenchmarkHeap > performInsertionsAndRemovalsQuad(i

```
1 package edu.neu.coe.info6205.util;
2
3 import edu.neu.coe.info6205.pq.PriorityQueue;
4 import edu.neu.coe.info6205.pq.QuadPriorityQueue;
5 import edu.neu.coe.info6205.util.Benchmark_Timer;
6
7 import java.util.Random;
8
9 public class BenchmarkHeap {
10
11     private static final int M = 4095;
12     private static final int insertions = 16000;
13     private static final int removals = 4000;
14     private static final Random rand = new Random();
15
16     public static void main(String[] args) {
17         // Benchmark Basic Binary Heap
18         runBenchmark(description:"Basic Binary Heap", () -> {
19             PriorityQueue<Integer> pq = new PriorityQueue<>(M, max:true, Integer::compare);
20             performInsertionsAndRemovals(pq);
21         });
22
23         // Benchmark Binary Heap with Floyd's Trick
24         runBenchmark(description:"Binary Heap with Floyd's Trick", () -> {
25             PriorityQueue<Integer> pq = new PriorityQueue<>(M, max:true, Integer::compare, floyd:true);
26             performInsertionsAndRemovals(pq);
27         });
28
29         // Benchmark 4-ary Heap
30         runBenchmark(description:"4-ary Heap", () -> {
31             QuadPriorityQueue<Integer> pq = new QuadPriorityQueue<>(M, max:true, Integer::compare);
32             performInsertionsAndRemovalsQuad(pq);
33         });
34
35         // Benchmark 4-ary Heap with Floyd's Trick
36         runBenchmark(description:"4-ary Heap with Floyd's Trick", () -> {
37             QuadPriorityQueue<Integer> pq = new QuadPriorityQueue<>(M, max:true, Integer::compare, floyd:true);
38             performInsertionsAndRemovalsQuad(pq);
39         });
40     }
}
```

```

42     private static void runBenchmark(String description, Runnable runnable) {
43         Benchmark_Timer<Void> benchmark = new Benchmark_Timer<>{
44             description,
45             fPre:null,
46             v -> { runnable.run(); },
47             fPost:null
48         };
49         double averageTime = benchmark.runFromSupplier(() -> null, m:10);
50         System.out.println(description + " Average Time: " + averageTime + " ms");
51     }
52
53     private static void performInsertionsAndRemovals(PriorityQueue<Integer> pq) {
54         try {
55             for (int i = 0; i < insertions; i++) {
56                 pq.give(rand.nextInt());
57             }
58             Integer highestPriority = null;
59             for (int i = 0; i < removals; i++) {
60                 Integer removed = pq.take();
61                 if (highestPriority == null || removed > highestPriority) {
62                     highestPriority = removed;
63                 }
64             }
65             System.out.println("Highest Priority Removed: " + highestPriority);
66         } catch (Exception e) {
67             System.err.println("Error in performInsertionsAndRemovals for PriorityQueue: " + e.getMessage());
68         }
69     }
70
71     private static void performInsertionsAndRemovalsQuad(QuadPriorityQueue<Integer> pq) {
72         try {
73             for (int i = 0; i < insertions; i++) {
74                 pq.give(rand.nextInt());
75             }
76             Integer highestPriority = null;
77             for (int i = 0; i < removals; i++) {
78                 Integer removed = pq.take();
79                 if (highestPriority == null || removed > highestPriority) {
80                     highestPriority = removed;
81                 }
82             }
83             System.out.println("Highest Priority Removed: " + highestPriority);
84         } catch (Exception e) {
85             System.err.println("Error in performInsertionsAndRemovalsQuad for QuadPriorityQueue: " + e.getMessage());
86         }
87     }
88 }

```

Unit Test Screenshots:

```

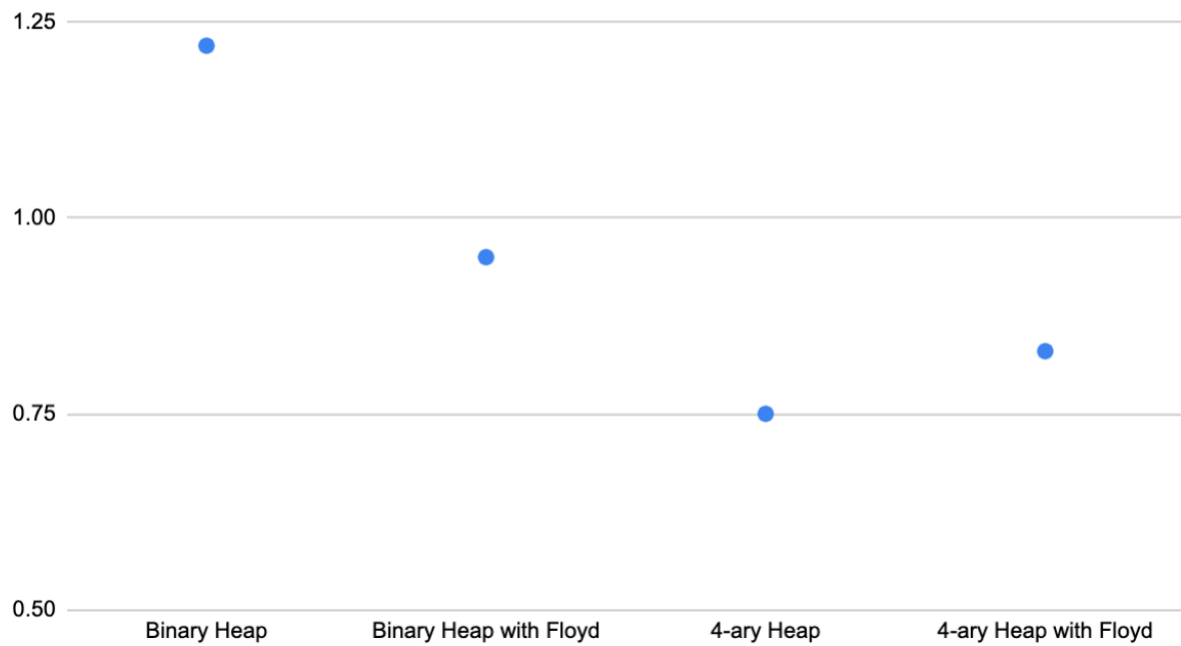
2024-10-21 08:57:26.691 INFO Benchmark_Timer - Begin run: Basic Binary Heap with 10 runs
Highest Priority Removed: 2147098260
Highest Priority Removed: 2147257939
Highest Priority Removed: 2147373520
Highest Priority Removed: 2147369780
Highest Priority Removed: 2147471165
Highest Priority Removed: 2147400740
Highest Priority Removed: 2147460087
Highest Priority Removed: 2147466272
Highest Priority Removed: 2146990502
Highest Priority Removed: 2147422412
Highest Priority Removed: 2147408102
Highest Priority Removed: 2147470205
Basic Binary Heap Average Time: 16.8370786 ms
2024-10-21 08:57:26.927 INFO Benchmark_Timer - Begin run: Binary Heap with Floyd's Trick with 10 runs
Highest Priority Removed: 2146892813
Highest Priority Removed: 2146836268
Highest Priority Removed: 2146685809
Highest Priority Removed: 2146978838
Highest Priority Removed: 2146852699
Highest Priority Removed: 2147418816
Highest Priority Removed: 2147400074
Highest Priority Removed: 2146892847
Highest Priority Removed: 2147431047
Highest Priority Removed: 2147221043
Highest Priority Removed: 2147390346
Highest Priority Removed: 2147070929
Binary Heap with Floyd's Trick Average Time: 8.9305279 ms

2024-10-21 08:57:27.069 INFO Benchmark_Timer - Begin run: 4-ary Heap with 10 runs
Highest Priority Removed: 2146025356
Highest Priority Removed: 2145145678
Highest Priority Removed: 2145992206
Highest Priority Removed: 2146804538
Highest Priority Removed: 2145414918
Highest Priority Removed: 2146785676
Highest Priority Removed: 2146016459
Highest Priority Removed: 2146667981
Highest Priority Removed: 2146930912
Highest Priority Removed: 2144995931
Highest Priority Removed: 2147201582
Highest Priority Removed: 2146432593
4-ary Heap Average Time: 5.6834477 ms
2024-10-21 08:57:27.150 INFO Benchmark_Timer - Begin run: 4-ary Heap with Floyd's Trick with 10 runs
Highest Priority Removed: 2146906826
Highest Priority Removed: 2147094211
Highest Priority Removed: 2145507156
Highest Priority Removed: 2147202357
Highest Priority Removed: 2146428437
Highest Priority Removed: 2145215203
Highest Priority Removed: 2147106877
Highest Priority Removed: 2146417449
Highest Priority Removed: 2145338589
Highest Priority Removed: 2146293590
Highest Priority Removed: 2146056342
Highest Priority Removed: 2146667361
4-ary Heap with Floyd's Trick Average Time: 6.734245 ms

```

Observations:

Log Average Time(ms) when Log M = 3.61



4-ary heap performs better than the binary heap, and the Floyd trick can help improve the performance.