

# AM 207 Project Proposal

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## 1 What is the problem you are addressing?

- Our area of interest is in **Information Retrieval** systems.
- The general project idea is to **identify latent topics** in a corpus of documents.
- Our corpus will be 10 books from Project Gutenberg
- We will use our model to perform inference on a randomly selected page from our corpus to predict which book it originated from.
- We will employ **bayes theorem** and **gibbs sampling** to perform inference

## 2 What has been done already?

Significant progress has been made on this problem by researchers in the field of Information Retrieval

### 2.1 TF-IDF

#### Description

- The text-frequency inverse-document frequency scheme [1] uses a vocabulary of words across all documents, and, for each document in the corpus, a count is formed of the number of occurrences of each word.
- After normalization, the term frequency count is compared to an inverse document frequency count, which measures the number of occurrences of a word in the entire corpus #### Advantages
- Tf-idf reduction can perform basic identification of sets of words that are discriminative for documents in the collection ##### Shortcomings
- Provides a relatively small amount of reduction in description length
- Reveals little in the way of inter or intradocument statistical structure.

### 2.2 LSI

- Latent Semantic Indexing [2] uses a singular value decomposition of the X matrix to identify a linear subspace in the space of tf-idf features that captures most of the variance in the collection.
- This addresses the reduction problem between does not give information on the inter and intra-document structure

### 2.3 pLSI

- The probabilistic Latent Semantic Indexing [3] model attempts to relax the simplifying assumption made in the mixture of unigrams model that each document is generated from only one topic.
- pLSI posits that a document label  $d$  and a word  $w_n$  are conditionally independent given an unobserved topic  $z$ .

$$p(d, w_n) = p(d) \sum_z p(w_n|z)p(z|d)$$

- Each word is generated from a single topic, and different words in a document may be generated from different topics.
  - Each document is represented as a list of mixing proportions for these mixture components and thereby reduced to a probability distribution on a fixed set of topics ##### Shortcomings
- (1) The number of parameters in the model grows linearly with the size of the corpus, which leads to overfitting
  - (2) It is not clear how to assign probability to a document outside of the training set.

## 2.4 LDA

- LDA overcomes both of these problems by treating the topic mixture weights as a k-parameter hidden random variable rather than a large set of individual parameters which are explicitly linked to the training set [4]
- LDA generalizes easily to new documents.
- Furthermore, the parameters in a k-topic LDA model do not grow with the size of the training corpus
- Gibbs sampling can be used to perform learning with LDA [5]

## 2.5 Papers

## 2.6 What are the questions you are trying to answer?

Given an unseen page from a book, can we predict the book title using its topical composition?

## 2.7 What methodology are you planning to use?

- Since LDA seems to be more robust than TF-IDF, pLSI and LSI in topic modeling, we plan to use this technique.
- In LDA, documents are represented as random mixtures over latent topics, where each topic is characterized by a distribution over words.
- We assume that there are a fixed universe of topics that produce words in a corpus.
- The figure below illustrates this model.

LDA assumes the following generative process for each document  $w$  in a corpus  $C$ :

- Choose  $N \sim \text{poisson}(\xi)$ .
- Choose  $\theta \sim \text{Dir}(\alpha)$ .
- For each of the  $N$  words  $w_n$ :
  - Choose a topic  $z_n \sim \text{Mult}(\theta)$ .
  - Choose a word  $w_n$  from  $p(w_n|z_n, \beta)$ , a multinomial probability conditioned on the topic  $z_n$ .

Given the parameters  $\alpha$  and  $\beta$ , the joint distribution of a topic mixture  $\theta$ , a set of  $N$  topics  $z$ , and a set of  $N$  words  $w$  is given by:

$$p(\theta, z, w, \alpha, \beta) = p(\theta|\alpha) \prod_{n=1}^N p(z_n|\theta) p(w_n|z_n, \beta),$$

1. We use Gibbs sampling to sample from the conditionals of the posterior of Latent Dirichlet Allocation.
2. We perform inference on a new, unseen document to predict the topics that it references.

### 3 What data do you have available?

1. Frankenstein - <https://www.gutenberg.org/cache/epub/84/pg84.txt>
2. The Adventures of Sherlock Holmes - <https://www.gutenberg.org/cache/epub/1661/pg1661.txt>
3. A tale of two cities - <https://www.gutenberg.org/cache/epub/98/pg98.txt>
4. Moby Dick - <https://www.gutenberg.org/cache/epub/2701/pg2701.txt>
5. Beowulf - <https://www.gutenberg.org/cache/epub/16328/pg16328.txt>
6. Dracula - <https://www.gutenberg.org/cache/epub/345/pg345.txt>
7. The Adventures of Huckleberry Finn - <https://www.gutenberg.org/cache/epub/76/pg76.txt>
8. Ulysses - <https://www.gutenberg.org/cache/epub/4300/pg4300.txt>
9. The Republic - <https://www.gutenberg.org/cache/epub/1497/pg1497.txt>
10. The Divine Comedy - <https://www.gutenberg.org/cache/epub/8800/pg8800.txt>

### References

- [1] G. Salton and M. McGill, editors. Introduction to Modern Information Retrieval. McGraw-Hill, 1983.
- [2] S. Deerwester, S. Dumais, T. Landauer, G. Furnas, and R. Harshman. Indexing by latent semantic analysis. *Journal of the American Society of Information Science*, 41(6):391–407, 1990.
- [3] T. Hofmann. Probabilistic latent semantic indexing. *Proceedings of the Twenty-Second Annual International SIGIR Conference*, 1999.
- [4] Blei, David M and Ng, Andrew Y and Jordan, Michael I, Latent dirichlet allocation. *The Journal of machine Learning research*, (3):993–1022, 2003
- [5] Darling, W. M. A Theoretical and Practical Implementation Tutorial on Topic Modeling and Gibbs Sampling. In *Proceedings of the 49th Annual Meeting of the Association for Computational Linguistics: Human Language Technologies*, (Portland, Oregon, USA, 2011).